Prácticas MD

Francisco Javier Mercader Martínez

Actividad 1. Realizar las siguientes operaciones con Python:

a)
$$(2^4 + 3)^2$$
 b) $\frac{2 + 4^4}{1 + \frac{2}{4 \cdot 3^3}}$ c) $\left(\frac{4 + 3}{2} + 5^3\right)^6$
d) $1 + 2\frac{7}{2^4 + 5}$ e) $(2 + 3^2 + 5^3)^{\frac{1}{3}}$ f) $\left(1 + 2^3 \frac{5}{2^4 + 1}\right)^{\frac{1}{2}}$

```
[1]: print(f"a) {(2**4+3)**2}")
    print(f"b) {(2+4**4)/(1+(2/(4*3**3)))}")
    print(f"c) {((4+4**3)/2+5**2)**6}")
    print(f"d) {1+2*(7/(2**4+5))}")
    print(f"e) {(2+3**2+5**3)**(1/3)}")
    print(f"f) {(1+2**3*(5/(2**4+1)))**(1/2)}")
```

- a) 361
- b) 253.30909090909088
- c) 42180533641.0
- d) 1.66666666666665
- e) 5.14256318131647
- f) 1.8311038136792213

Actividad 2. Obtener el resto y el cociente de las siguientes divisiones enteras:

- a) 45 entre 3 b) 111 entre 67
- c) 99 entre 54 d) 103964 entre 78

```
[2]: print(f"a)\n Cociente:{45//3} \n Resto:{45%3}")
    print(f"b)\n Cociente:{111//67} \n Resto:{111%67}")
    print(f"c)\n Cociente:{99//54} \n Resto:{99%54}")
    print(f"d)\n Cociente:{103964//78} \n Resto:{103964%78}")
```

a)
Cociente:15
Resto:0
b)
Cociente:1
Resto:44
c)

```
Cociente:1
Resto:45
d)
Cociente:1332
Resto:68
```

Actividad 3. Dadas las listas A de los 10 primeros números naturales pares y B de los 5 primeros múltiplos de 3, hacer las siguientes operaciones:

- 1. Hacer la unión de A y B. LLamar C a esta nueva lista.
- 2. Eliminar los elementos repetidos de C eliminando el elemento repetido que aparece en primer lugar.
- 3. Añadir a la lista resultante los números 5 y 7 al final de la lista.
- 4. Eliminar los elementos repetidos de C eliminando el elemento repetido que aparece en último lugar.
- 5. Eliminar los elementos repetidos de C eliminando el elemento repetido que aparece en último lugar.
- 6. Crear una nueva lista D con los elementos pares de C, sin escribir el número en cuestión, sino seleccionándolo de la lista C.

```
[3]: # Apartado 1
     A = []
     B=[]
     for i in range(10):
         A.append(i+1)
     for j in range(5):
         B.append((j+1)*3)
     C = A + B
     print(f"A={A}")
     print(f"B={B}")
     print(f"C={C}")
     # Apartado 2
     for n in C:
         while(C.count(n) > 1):
             C.remove(n)
     print(C)
     # Apartado 3
     C.append(5)
     C.append(7)
     print(C)
```

```
# Apartado 4
lista = [3,4,5]

C = lista + C
print(C)

# Apartado 5
for i in range(len(C) - 1, 0, -1):
    if C[i] in C[:i]:
        C.pop(i)
print(C)

# Apartado 6
D = []
for i in C:
    if i%2==0:
        D.append(i)
print(D)
```

```
A=[1, 2, 3, 4, 5, 6, 7, 8, 9, 10]

B=[3, 6, 9, 12, 15]

C=[1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 3, 6, 9, 12, 15]

[1, 2, 4, 5, 7, 8, 10, 3, 6, 9, 12, 15]

[1, 2, 4, 5, 7, 8, 10, 3, 6, 9, 12, 15, 5, 7]

[3, 4, 5, 1, 2, 4, 5, 7, 8, 10, 3, 6, 9, 12, 15, 5, 7]

[3, 4, 5, 1, 2, 7, 8, 10, 6, 9, 12, 15]

[4, 2, 8, 10, 6, 12]
```

Actividad 4. Dada la función f(x) = 3.95x(1-x) y $x_0 = 0.5$, obtener los 100 primeros elementos de la recursión

$$x_{n+1} = f(x_n).$$

```
[4]: import numpy as np

def f(x):
    return (3.95*x*(1-x))

x4 = np.zeros(100)

x4[0] = 0.5
for i in range(1,100):
    x4[i] = f(x4[i-1])

for j in range(len(x4)):
    print(f"x_{j} = {x4[j]}")
```

- $x_0 = 0.5$
- $x_1 = 0.9875$
- x 2 = 0.04875781249999983
- $x_3 = 0.183202928469848$
- $x_4 = 0.591076481106183$
- $x_5 = 0.9547350446277946$
- $x_6 = 0.17070335479006285$
- $x_7 = 0.5591766918412491$
- $x_8 = 0.9736675706137671$
- $x_9 = 0.10127417856796533$
- $x_10 = 0.35951999132722934$
- x 11 = 0.9095482002950283
- $x_12 = 0.3249675729586585$
- $x_13 = 0.8664864154618691$
- $x_14 = 0.4569664437635456$
- $x_15 = 0.9801850464986934$
- $x_16 = 0.07671816842023815$
- x 17 = 0.2797883396652044
- $x_18 = 0.7959519573777409$
- $x_19 = 0.6415291337509211$
- $x_20 = 0.9083795419838698$
- $x_21 = 0.3287432912717266$
- x 22 = 0.8716510018764594
- $x_23 = 0.44190835457668476$
- $x_24 = 0.9741701748914467$
- x 25 = 0.09939244871148847
- x 26 = 0.35357867990995934
- $x_27 = 0.9028151482412049$
- x 28 = 0.3465728275722937
- $x_29 = 0.8945174059053136$
- x 30 = 0.3727062649290811
- x 31 = 0.9234954047961941
- x 32 = 0.27907398636020553
- $x_33 = 0.7947072011640559$
- $x_34 = 0.6444332790490923$
- $x_35 = 0.9050991602173518$
- $x_36 = 0.3392839480452255$
- $x_37 = 0.8854728850440775$
- $x_38 = 0.4005720868383919$
- $x_39 = 0.9484506558330944$
- $x_40 = 0.1931234366673267$
- $x_41 = 0.6155157607646546$
- $x_42 = 0.9347916306091042$
- $x_43 = 0.24077713991149136$
- $x_44 = 0.7220738597897574$
- $x_45 = 0.7926986431524128$
- $x_46 = 0.6490936419721093$
- x 47 = 0.8996957893977955

- x 48 = 0.3564609399538088
- $x_49 = 0.906116326052171$
- x 50 = 0.33602464236985274
- $x_51 = 0.8812927242557581$
- x 52 = 0.41323264079700855
- $x_53 = 0.9577621302389092$
- $x_54 = 0.15979263687058687$
- x 55 = 0.5303228527864999
- $x_56 = 0.9838680721656087$
- $x_57 = 0.06269317051801239$
- $x_58 = 0.23211281070922665$
- x 59 = 0.7040339925648631
- $x_60 = 0.8230620130182635$
- x 61 = 0.5752421961911199
- x 62 = 0.9651375170537312
- $x_63 = 0.13290600640490524$
- $x_64 = 0.4552058994722979$
- x 65 = 0.979574279803761
- $x_66 = 0.07903361509528065$
- $x_67 = 0.2875098459819941$
- $x_68 = 0.8091493410593463$
- $x_69 = 0.6099854054441592$
- $x_70 = 0.9397176818276715$
- $x_71 = 0.22376102313798982$
- $x_72 = 0.6860835092658077$
- x 73 = 0.8507230639383221
- x74 = 0.5016236630657768
- $x_75 = 0.987489586687083$
- x 76 = 0.0487979163430452
- $x_77 = 0.18334588482930833$
- x 78 = 0.5914341768145921
- x 79 = 0.9544771756754398
- $x_80 = 0.17162946232079807$
- $x_81 = 0.5615825204378737$
- $x_82 = 0.9725199930472495$
- $x_83 = 0.10556318187397795$
- $x_84 = 0.37295740620114665$
- $x_85 = 0.9237477084753952$
- $x_86 = 0.2782296242693133$
- $x_87 = 0.7932307067706668$
- $x_88 = 0.6478622227967622$
- x 89 = 0.9011402141249226
- $x_90 = 0.3518917880166544$
- x 91 = 0.9008526322952307
- x 92 = 0.35280281036883904
- $x_93 = 0.9019153000905179$
- $x_94 = 0.3494331616349383$
- x 95 = 0.8979520273797601

```
x_96 = 0.3619550264221378

x_97 = 0.9122271618160548

x_98 = 0.3162716298912667

x_99 = 0.854163349767894
```

Actividad 5. Dada la recursión de la actividad 4, obtener los 100 primeros elementos pares, es decir, los de la sucesión $x_0, x_2, x_4, x_6, \dots$

```
[5]: import numpy as np
     def f(x):
         return (3.95*x*(1-x))
     x = np.zeros(200)
     x[0] = 0.5
     print(f''x_0 = \{x[0]\}'')
     for i in range(1,200):
         x[i] = f(x[i-1])
         if i % 2 == 0:
             print(f"x_{i} = \{x[i]\}")
    x_0 = 0.5
    x_2 = 0.04875781249999983
    x_4 = 0.591076481106183
    x_6 = 0.17070335479006285
    x_8 = 0.9736675706137671
    x_10 = 0.35951999132722934
    x 12 = 0.3249675729586585
    x_14 = 0.4569664437635456
    x 16 = 0.07671816842023815
    x 18 = 0.7959519573777409
    x_20 = 0.9083795419838698
    x_22 = 0.8716510018764594
    x_24 = 0.9741701748914467
    x_26 = 0.35357867990995934
    x_28 = 0.3465728275722937
    x_30 = 0.3727062649290811
    x_32 = 0.27907398636020553
    x_34 = 0.6444332790490923
    x_36 = 0.3392839480452255
    x_38 = 0.4005720868383919
    x_40 = 0.1931234366673267
    x 42 = 0.9347916306091042
    x_44 = 0.7220738597897574
    x 46 = 0.6490936419721093
    x_48 = 0.3564609399538088
    x_50 = 0.33602464236985274
```

- x 52 = 0.41323264079700855
- $x_54 = 0.15979263687058687$
- x 56 = 0.9838680721656087
- $x_58 = 0.23211281070922665$
- $x_60 = 0.8230620130182635$
- $x_62 = 0.9651375170537312$
- $x_64 = 0.4552058994722979$
- $x_66 = 0.07903361509528065$
- $x_68 = 0.8091493410593463$
- $x_70 = 0.9397176818276715$
- $x_72 = 0.6860835092658077$
- x74 = 0.5016236630657768
- $x_76 = 0.0487979163430452$
- X_10 0.0401313100400402
- $x_78 = 0.5914341768145921$
- $x_80 = 0.17162946232079807$
- $x_82 = 0.9725199930472495$
- $x_84 = 0.37295740620114665$
- x 86 = 0.2782296242693133
- $x_88 = 0.6478622227967622$
- $x_90 = 0.3518917880166544$
- $x_92 = 0.35280281036883904$
- $x_94 = 0.3494331616349383$
- $x_96 = 0.3619550264221378$
- $x_98 = 0.3162716298912667$
- $x_100 = 0.49204487064067837$
- $x_102 = 0.049720270839305$
- x 104 = 0.5996076384403604
- $x_106 = 0.19362394377429912$
- x 108 = 0.933679416980738
- x 110 = 0.7298297760941513
- $x_1112 = 0.6803493626260131$
- x 114 = 0.47835559976717507
- $x_116 = 0.055871010026073496$
- $x_118 = 0.6515378020282968$
- $x_120 = 0.36559235540186297$
- $x_122 = 0.30346333026396255$
- $x_124 = 0.5444105542351017$
- $x_126 = 0.07852152477740656$
- $x_128 = 0.8062773110444152$
- $x_130 = 0.9334588325364238$
- $x_132 = 0.731351998615936$
- x 134 = 0.6864277291644301
- $x_136 = 0.503025992862475$
- x 138 = 0.048897102036946666
- x 140 = 0.5923180078073083
- $x_142 = 0.1739310704686262$
- x 144 = 0.969485605681602
- x 146 = 0.40763631372603204

```
x 148 = 0.17405053589544103
x_150 = 0.9693210830054336
x_152 = 0.4094815187419775
x_154 = 0.1692648491204359
x_156 = 0.9753652930346579
x_158 = 0.33931313756757653
x_160 = 0.400459233166295
x_162 = 0.19343762952952226
x_164 = 0.9340945839444051
x_166 = 0.7269504199189561
x_168 = 0.6687980636722092
x_170 = 0.4321690151352626
x_172 = 0.11744620476504807
x 174 = 0.9550968333930211
x_176 = 0.555787592747178
x_178 = 0.09550584959890672
x_180 = 0.8879145764780896
x_182 = 0.942371928051122
x_184 = 0.6655637317008795
x_186 = 0.4194436669022315
x_188 = 0.14488091524723745
x_190 = 0.9870534288252106
x_192 = 0.18931941723260337
x_194 = 0.9429195984312224
x_196 = 0.661229916218985
x_198 = 0.4025603833594322
```

Actividad 6. Dada la recursión de la actividad 4, obtener los 100 primeros elementos múltiplos de 4, es decir, los de la sucesión x_0, x_4, x_8, x_{12}

```
[6]: import numpy as np

def f(x):
    return (3.95*x*(1-x))

x = np.zeros(400)

x[0] = 0.5
print(f"x_0 = {x[0]}")

for i in range(1,400):
    x[i] = f(x[i-1])
    if i % 4 == 0:
        print(f"x_{i} = {x[i]}")
```

```
x_0 = 0.5

x_4 = 0.591076481106183

x_8 = 0.9736675706137671

x_12 = 0.3249675729586585
```

- x 16 = 0.07671816842023815
- $x_20 = 0.9083795419838698$
- x 24 = 0.9741701748914467
- $x_28 = 0.3465728275722937$
- x 32 = 0.27907398636020553
- $x_36 = 0.3392839480452255$
- $x_40 = 0.1931234366673267$
- $x_44 = 0.7220738597897574$
- $x_48 = 0.3564609399538088$
- $x_52 = 0.41323264079700855$
- $x_56 = 0.9838680721656087$
- $x_60 = 0.8230620130182635$
- $x_64 = 0.4552058994722979$
- x 68 = 0.8091493410593463
- x72 = 0.6860835092658077
- x 76 = 0.0487979163430452
- $x_80 = 0.17162946232079807$
- x 84 = 0.37295740620114665
- $x_88 = 0.6478622227967622$
- $x_92 = 0.35280281036883904$
- $x_96 = 0.3619550264221378$
- $x_100 = 0.49204487064067837$
- $x_104 = 0.5996076384403604$
- $x_108 = 0.933679416980738$
- $x_112 = 0.6803493626260131$
- $x_116 = 0.055871010026073496$
- x 120 = 0.36559235540186297
- $x_124 = 0.5444105542351017$
- $x_128 = 0.8062773110444152$
- $x_132 = 0.731351998615936$
- $x_136 = 0.503025992862475$
- $x_140 = 0.5923180078073083$
- $x_144 = 0.969485605681602$
- $x_148 = 0.17405053589544103$
- $x_152 = 0.4094815187419775$
- $x_156 = 0.9753652930346579$
- $x_160 = 0.400459233166295$
- $x_164 = 0.9340945839444051$
- $x_168 = 0.6687980636722092$
- $x_172 = 0.11744620476504807$
- $x_176 = 0.555787592747178$
- x 180 = 0.8879145764780896
- $x_184 = 0.6655637317008795$
- x 188 = 0.14488091524723745
- x 192 = 0.18931941723260337
- x 196 = 0.661229916218985
- $x_200 = 0.18763634616776279$
- $x_204 = 0.6334801720948651$

- $x_208 = 0.5576887664660336$
- $x_212 = 0.9002669401320579$
- $x_216 = 0.889658396228557$
- $x_220 = 0.7008861420609539$
- $x_224 = 0.10685923426372336$
- $x_228 = 0.7690558227342181$
- $x_232 = 0.9707878977981979$
- $x_236 = 0.21513151585969176$
- $x_240 = 0.9652302833330871$
- $x_244 = 0.08037386921642775$
- $x_248 = 0.9542731845105783$
- x 252 = 0.10905860832617482
- $x_256 = 0.7264508196060054$
- X_230 = 0.7204300130000034
- $x_260 = 0.42424487344492495$ $x_264 = 0.9806839884871316$
- x 268 = 0.6672195577407398
- $x_272 = 0.1303299103894285$
- $\times 276 = 0.3231593329224524$
- $x_280 = 0.06813402697257925$
- X_200 = 0.00013402091231923
- $x_284 = 0.7290107163276519$
- $x_288 = 0.46514116018195406$
- $x_292 = 0.7355399628983461$
- $x_296 = 0.5711425472062732$
- $x_300 = 0.9679115908713581$
- $x_304 = 0.13206647659900914$
- $x_308 = 0.2986186052891005$
- $x_312 = 0.11065598467542272$
- $x_316 = 0.6945602833238884$
- $x_320 = 0.06869093504798097$
- $x_324 = 0.7433170209744371$
- $x_328 = 0.6944477064640189$
- $x_332 = 0.06818935966399586$
- $x_336 = 0.7304462438816353$
- $x_340 = 0.48833169879300115$
- $x_344 = 0.6092880012968456$
- $x_348 = 0.8574012778210138$
- $x_352 = 0.19888274418689014$
- $x_356 = 0.8066416672212617$
- $x_360 = 0.7257221207451932$
- $x_364 = 0.41274593939786913$
- $x_368 = 0.9830492280209023$
- $x_372 = 0.7851067509627749$
- $x_376 = 0.9639622809861216$ $x_380 = 0.06461979343242154$
- \times 384 = 0.6321731710048271
- x 388 = 0.5763105657203039
- $x_392 = 0.9817946656532536$
- $x_396 = 0.7236780891275244$

Actividad 7. Dada la función f(x) = 3.95x(1-x) y $x_0 = 0.5$, $x_1 = 0.25$, obtener los 100 primeros elementos de la recursión

$$x_{n+1} = 0.25 \cdot x_{n-1} + 0.75 \cdot f(x_n)$$

```
[7]: import numpy as np

def f(x):
    return (3.95*x*(1-x))

x7 = np.zeros(100)

x7[0] = 0.5
    x7[1] = 0.25

for i in range(2,100):
        x7[i] = 0.25 * x7[i-2] + 0.75*f(x7[i-1])

for j in range(len(x7)):
    print(f"x_{j} = {x7[j]}")
```

```
x_1 = 0.25
```

 $x_2 = 0.6804687500000001$

 $x_3 = 0.7066394271850587$

 $x_4 = 0.7842438733804189$

 $x_5 = 0.6779309148666401$

 $x_6 = 0.8428949648417141$

 $x_7 = 0.5617859938595264$

 $x_8 = 0.9400393706876955$

 $x_9 = 0.3074288544900332$

 $x_10 = 0.8657745411509747$

 $x_11 = 0.4211263318206727$

 $x_12 = 0.9386387582740082$

 $x_13 = 0.27590985068443286$

 $x_14 = 0.8265186193209428$

 $x_15 = 0.49375727670996594$

 $x_16 = 0.9471392014827857$

 $x_17 = 0.27176142762585154$

 $x_18 = 0.8230847443345053$

 $x_19 = 0.49932849154219844$

 $x_20 = 0.946394850222435$

 $x_21 = 0.2751245995566608$

 $x_22 = 0.8274132108466229$

 $x_23 = 0.4918278958773633$

 $x_24 = 0.9472804572274992$

 $x_25 = 0.2709047944945801$

 $x_26 = 0.821959447744622$

- $x_27 = 0.5012647113722799$
- $x_28 = 0.946110123432647$
- x 29 = 0.2763614852393863
- $x_30 = 0.8289855069533245$
- x 31 = 0.4890796598457889
- $x_32 = 0.9475180872696707$
- $x_33 = 0.2695878161021899$
- $x_34 = 0.8202260648950639$
- $x_35 = 0.5042331835849462$
- $x_36 = 0.9456284286880968$
- $x_37 = 0.2783761326482333$
- x 38 = 0.8315225841289121
- $x_39 = 0.4846188826915552$
- $\times 40 = 0.9478047814271218$
- $x_41 = 0.2677121959509991$
- $x_42 = 0.8177267345236808$
- $x_43 = 0.5084878509131706$
- $x_44 = 0.9448432544270399$ $x_45 = 0.28151110673841884$
- $x_46 = 0.8354137765386983$
- $x_47 = 0.4777144122646974$
- $x_48 = 0.9480071261508275$ $x_49 = 0.2654490872609761$
- -
- $x_50 = 0.8146474194375809$
- $x_51 = 0.5136908885850094$
- $x_52 = 0.9437315625847882$
- $x_53 = 0.2857382869807117$ $x_54 = 0.8405551987107909$
- x 55 = 0.46847521076467463
- x 56 = 0.9478196306313151
- x 57 = 0.2636368787640699
- x 58 = 0.8120723646071705
- x 59 = 0.5180188309646669
- $x_60 = 0.942681231778893$
- $x_61 = 0.28957843906968084$
- $x_62 = 0.8451240042805803$
- $x_63 = 0.460154521462834$
- $x_64 = 0.9472025519215725$
- $x_65 = 0.26319289262190193$
- $x_66 = 0.8112957298949761$
- $x_67 = 0.5193420674823445$
- x 68 = 0.9423406150843128
- $x_69 = 0.29080230335182544$
- x 70 = 0.846560262782982
- x 71 = 0.4575174292075856
- $x_72 = 0.9469184380631406$
- x 73 = 0.26328618984503466
- x 74 = 0.8113555793084702

```
x75 = 0.5192549932904637
x_76 = 0.9423655338310183
x_77 = 0.2907152242148706
x_78 = 0.8464585357330376
x_79 = 0.45770451199371165
x_80 = 0.9469399930776525
x_81 = 0.2632758816646311
x_82 = 0.8113465102220021
x_83 = 0.5192691464874282
x_84 = 0.942361651286677
x_85 = 0.2907289386794704
x_86 = 0.8464745706444899
x_87 = 0.45767502391388976
x 88 = 0.946936609494079
x_89 = 0.26327746974426125
x 90 = 0.8113478917438828
x_91 = 0.5192669949694847
x_92 = 0.9423622422915766
x_93 = 0.29072685177937274
x_94 = 0.8464721307706078
x_95 = 0.457679510895195
x_96 = 0.9469371246908698
x_97 = 0.26327722719648283
x_98 = 0.8113476803500026
x_99 = 0.5192673242983633
```

0.27246097755087745

Actividad 8. Dados los elementos obtenidos en las actividades 4 y 7, obtener una lista que resulte de multiplicar los elementos de las dos lista dos a dos.

```
[8]: x = []
     for i in range(len(x4)):
         x.append(x4[1] * x7[i])
         print(x[i])
    0.49375
    0.246875
    0.6719628906250001
    0.6978064343452455
    0.7744408249631637
    0.6694567784308072
    0.8323587777811927
    0.5547636689362824
    0.9282888785540994
    0.30358599380890783
    0.8549523593865876
    0.4158622526729143
    0.9269057737955831
```

- 0.8161871365794311
- 0.4875853107510914
- 0.935299961464251
- 0.2683644097805284
- 0.812796185030324
- 0.493086885397921
- 0.9345649145946546
- 0.2716855420622025
- 0.8170705457110401
- 0.4856800471788963
- 0.9354394515121555
- 0.2675184845633979
- 0.8116849546478143
- 0.4949989024801264
- 0.9342837468897389
- 0.27290696667389397
- 0.818623188116408
- 0.48296616409771653
- 0.9356741111787998
- 0.26621796840091255
- 0.8099732390838756
- 0.49793026879013436
- 0.9338080733294957
- 0.2748964309901304
- 0.8211285518273007
- 0.4785611466579108
- 0.9359572216592827
- 0.2643657935016116
- 0.8075051503421349
- 0.502131752776756
- 0.9330327137467019
- 0.2779922179041886
- 0.8249711043319646
- 0.4717429821113887
- 0.9361570370739422
- 0.26213097367021393
- 0.8044643266946112
- 0.5072697524776969
- 0.9319349180524784
- 0.2821665583934528
- 0.830048258726906
- 0.4626192706301162
- 0.9359718852484238
- 0.260341417779519
- 0.8019214600495809
- 0.5115435955776086
- 0.9308977163816569
- 0.28595870858130984

- 0.8345599542270731
- 0.4544025899445486
- 0.9353625200225529
- 0.25990298146412816
- 0.8011545332712889
- 0.5128502916388151
- 0.930561357395759
- 0.28716727455992763
- 0.8359782594981948
- 0.4517984613424908
- 0.9350819575873514
- 0.2599951124719717
- 0.8012136345671144
- 0.5127643058743329
- 0.9305859646581306
- 0.28708128391218474
- 0.8358778040363747
- 0.4519832055937903
- 0.9351032431641819
- 0.25998493314382326
-
- 0.8012046788442271
- 0.5127782821563354
- 0.9305821306455936 0.28709482694597704
- 0.8358936385114338
- 0.4519540861149662
- 0.935099901875403
- 0.259986501372458
- 0.8012060430970843
- 0.5127761575323662
- 0.9305827142629319
- 0.2870927661321306
- 0.8358912291359752
- 0.4519585170090051
- 0.9351004106322339
- 0.2599862618565268
- 0.8012058343456276
- 0.5127764827446338

Actividad 9. Definir las funciones siguientes.

Definit has functiones significances.
$$f_1(x) = 3x^2 + x - 1 \qquad f_2(x) = \frac{2x+1}{x^2+1}$$

$$f_3(x) = \begin{cases} 2x & \text{si } x \le 0 \\ x^2 & \text{si } x > 0 \end{cases} \qquad f_4(x) = \begin{cases} \frac{2x}{x+1} & \text{si } 0 < x \le -2 \\ x^2+3 & \text{si } x > -2 \end{cases}$$

$$f_5(x) = \begin{cases} 2x & \text{si } x \le 0 \\ x^2 & \text{si } 0 < x < 2 \end{cases} \qquad f_6(x) = \begin{cases} \frac{2x+1}{x^2+1} & \text{si } x \le -1 \\ x^2 & \text{si } 0 < x < 2 \\ 0 & \text{si } x \ge 3 \end{cases}$$

```
[9]: def f1(x):
        return 3 * x**2 + x - 1
     # Definición de f2(x) = (2x + 1) / (x^2 + 1)
     def f2(x):
         return (2 * x + 1) / (x**2 + 1)
     def f3(x):
        if x \ll 0:
            return 2 * x
         else:
            return x**2
     def f4(x):
        if 0 < x <= -2:
            return (2 * x) / (x + 1)
         else:
            return x**2 + 3
     def f5(x):
         if x \ll 0:
            return 2 * x
         elif 0 < x < 2:
            return x**2
         else:
             return x**3 + 1
     def f6(x):
         if x <= -1:
            return (2 * x + 1) / (x**2)
         elif 0 < x < 2:
             return x**2
         else:
```

```
return 0
```

Actividad 12. Dados los conjuntos:

 $A = \{1, 2, 3, 4, 5\},\$ $B = \{2, 4, 6, 8, 10, 12\}$

у

$$C = \{1, 9, 4, 3, 2, 5, 11\},\$$

obtener:

- $\begin{array}{ll} a) \ A \cap B \cup C & b) \ B \backslash C \cup A \\ c) \ (B \backslash C) \cup A & d) \ (A \cup C) \triangle B \\ e) \ A \cap (C \triangle B) & f) \ (A \triangle B) \cup (B \backslash C) \end{array}$
- [10]: A = {1,2,3,4,5}
 B = {2,4,6,8,10,12}
 C = {1,9,4,3,2,5,11}

 print(f"a) {A & B | C}")
 print(f"b) {B C | A}")
 print(f"c) {(B C) | A}")
 print(f"d) {(A | C) ^ B}")
 print(f"e) {A & (C ^ B)}")
 print(f"f) {(A ^ B) | (B C)}")
 - a) {1, 2, 3, 4, 5, 9, 11}
 - b) {1, 2, 3, 4, 5, 6, 8, 10, 12}
 - c) {1, 2, 3, 4, 5, 6, 8, 10, 12}
 - d) {1, 3, 5, 6, 8, 9, 10, 11, 12}
 - e) {1, 3, 5}
 - f) {1, 3, 5, 6, 8, 10, 12}

Actividad 13. Crear un módulo llamado fun1var.py con las funciones definidas en la actividad 9.

```
[11]: from fun1var import *
```

Actividad 17. Demostrar que las proposiciones $\neg(p \land q)$ y $\neg p \lor \neg q$ son lógicamente equivalentes.

```
[12]: from sympy import symbols, And, Not, Or

p, q=symbols('p q')

Not(And(p, q)).equals(Or(Not(p), Not(q)))
```

[12]: True

Actividad 18. Demostrar que el argumento $\{p \to q, \neg p\}$ implica $\neg q$.

```
[13]: from sympy import symbols, And, Not, Or, Implies

p, q=symbols('p q')
```

```
print(Implies(And(Implies(p, q), Not(p)), Not(q)).subs({p:True, q:True}))
print(Implies(And(Implies(p, q), Not(p)), Not(q)).subs({p:True, q:False}))
print(Implies(And(Implies(p, q), Not(p)), Not(q)).subs({p:False, q:True}))
print(Implies(And(Implies(p, q), Not(p)), Not(q)).subs({p:False, q:False}))
```

True True False

True

Actividad 19. Determinar la validez del argumento $\{p \to q, \neg p\}$ implica $\neg p$.

```
[14]: from sympy import symbols, And, Not, Or, Implies

import sympy as sy

p, q=symbols('p q')

print(Implies(And(Implies(p, q), Not(p)), Not(p)).subs({p:True, q:True}))
print(Implies(And(Implies(p, q), Not(p)), Not(p)).subs({p:True, q:False}))
print(Implies(And(Implies(p, q), Not(p)), Not(p)).subs({p:False, q:True}))
print(Implies(And(Implies(p, q), Not(p)), Not(p)).subs({p:False, q:False}))
print()
print()
print(sy.simplify_logic(Implies(And(Implies(p, q), Not(p)), Not(p))))
```

True True

True

True

True

Actividad 20. Demostrar que el argumento $\{p \to \neg q, r \lor q, r\}$ implica $\neg p$

```
print(Implies(And(Implies(p, Not(q)), Or(r,q)), r), Not(p)).subs({p:False, q:
        →True, r:False}))
       print(Implies(And(Implies(p, Not(q)), Or(r,q)), r), Not(p)).subs({p:True, q:
       \hookrightarrowFalse, r:False\}))
       print(Implies(And(And(Implies(p, Not(q)), Or(r,q)), r), Not(p)).subs({p:False, q:
        \rightarrowFalse, r:False\}))
      True
      False
      True
      True
      True
      True
      True
      True
      Actividad 21. Demostrar que (p \lor q \land \neg r) \land (p \land q) es equivalente a p \land q.
[16]: from sympy import simplify_logic, And, Or, Not, Implies, Equivalent, symbols
       p, q, r = symbols('p q r')
       And(And(Or(p, q), Not(r)), And(p, q)).equals(And(p, q))
[16]: False
      Actividad 22. Demostrar que (p \lor q \land \neg r) \land (p \lor q) es equivalente a p \lor (q \land \neg r).
[17]: from sympy import simplify_logic, And, Or, Not, Implies, Equivalent, symbols
       p, q, r = symbols('p q r')
       And(And(Or(p, q), Not(r)), Or(p, q)).equals(Or(p, And(q, Not(r))))
[17]: False
      Actividad 23. Demostrar que (p \lor q \land \neg r) \lor (p \lor q) es equivalente a p \lor q.
[18]: from sympy import simplify_logic, And, Or, Not, Implies, Equivalent, symbols
       p, q, r = symbols('p q r')
       Or(And(Or(p, q), Not(r)), Or(p, q)).equals(Or(p, q))
[18]: False
      Actividad 24. Simplificar los siguientes conjuntos.
                                                         b) (A^c \cap B^c \cup C) \triangle (C \cup A)
                       a) (A \cap B \cup C^c) \cap (C \cup A)
                       c) (A \cap B \cup C^c) \cap ((C \cup A) \setminus B) d) (A \cap B \cup C^c) \cap (C \cup A^c)
                       e) (A \cap B \cup C^c) \cup (C \cup A)^c
                                                         (A \cap B)^c \cap (C \cup A)^c \setminus (C \cup B)
```

Nota: Se debe usar que $A \backslash B = A \cap B^c$ y $A \triangle B = (A \backslash B) \cup (B \backslash A)$

```
[19]: from sympy import simplify_logic, symbols
A, B, C = symbols("A B C")

print(f"a) {simplify_logic((A & B | ~C) & (C | A))}")
print(f"b) {simplify_logic((~A & ~B | C) & ~(C | ~A)) | ((C | A) & ~(A & ~B | L) & ~(C)))}")
print(f"c) {simplify_logic((A & B | ~C) & ((C | A) & ~B))}")
print(f"d) {simplify_logic((A & B | ~C) & (C | ~A))}")
print(f"e) {simplify_logic((A & B | ~C) | ~(C | A))}")
print(f"f) {simplify_logic((A & B | ~C) | ~(C | A))}")

a) A & (B | ~C)
b) A & ~C
c) A & ~B & ~C
d) (A | ~C) & (B | ~C) & (C | ~A)
e) ~C | (A & B)
f) ~A & ~B & ~C
```