Intro To Regression

James Woods

This is something like a notebook. You can work with data and text at the same time. Things chunks are for code

```
print("I am in a chunk.")
## [1] "I am in a chunk."
```

By default they echo the code and then produce the result.

You can turn off the echo and just see the result.

[1] "No Echo"

Assignment and Access

1. Lets start with a few R conventions. Lets start with scalars. '<-' is the assignment operator in R. '=' also works but '==' is used for comparisons.

```
1 + 1

## [1] 2

A <- 2 + 3

A + 2

## [1] 7

A <- A+2

B <- A + 4

A + B

## [1] 18

C = A + B

C

## [1] 18

A == B
```

[1] FALSE

Note that when you save values to variables you can see them in the Environment tab.

Play with this in the chunk below and run to see what happens.

```
ThisIsAVariable <-10
this_is_a_variable <-23
```

2. R has many ways of representing values

```
A <- "Shale"

## [1] "Shale"

C <- c("Tom", "Dick", "Harry")

C
```

```
## [1] "Tom"
                  "Dick"
                            "Harry"
C[[1]]
## [1] "Tom"
C[1]
## [1] "Tom"
1:1000
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D <- 1:10
D
             2 3 4 5
                           6 7
                                8
                                    9 10
    [1] 1
as.character(D)
    [1] "1" "2"
                    "3"
                          "4"
                               "5" "6" "7" "8"
                                                      "9" "10"
as.factor(D)
    [1] 1 2 3 4 5 6 7
                                8
## Levels: 1 2 3 4 5 6 7 8 9 10
summary(D)
                                                    Max.
##
      Min. 1st Qu.
                      Median
                                  Mean 3rd Qu.
##
      1.00
               3.25
                         5.50
                                  5.50
                                           7.75
                                                   10.00
summary(as.character(D))
##
      Length
                   Class
                               Mode
           10 character character
summary(as.factor(D))
```

```
2 3 4 5 6 7 8 9 10
1 1 1 1 1 1
            1
              1 1
```

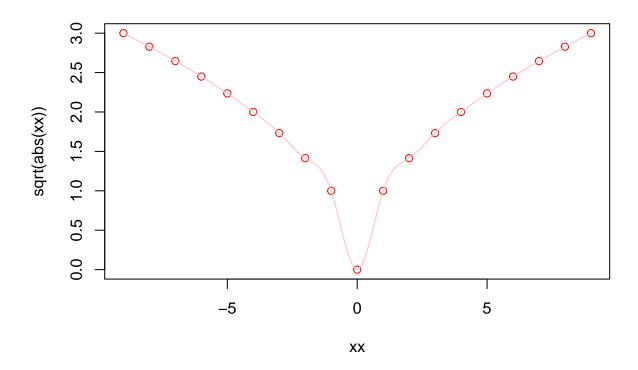
There are many others, "list" being the most important not shown.

3. There are also functions. Most, but not all, work on many things at once.

```
sqrt(D)
    [1] 1.000000 1.414214 1.732051 2.000000 2.236068 2.449490 2.645751
##
   [8] 2.828427 3.000000 3.162278
#sqrt(A)
sqrt(D[6])
## [1] 2.44949
sqrt(D[1:3])
## [1] 1.000000 1.414214 1.732051
  4. If you need help, use the help pane or ask for help. Everything has a help file and many functions come
     with examples of how to use.
help(sqrt)
```

```
## starting httpd help server ... done
example(sqrt)
##
```

```
## sqrt> require(stats) # for spline
## sqrt> require(graphics)
##
## sqrt> xx <- -9:9
## sqrt> plot(xx, sqrt(abs(xx)), col = "red")
```



```
##
## sqrt> lines(spline(xx, sqrt(abs(xx)), n=101), col = "pink")
```

4. You can work with vectors and matrix but you will most frequently deal with dataframes, which is a matrix with extra attributes. Dataframes are objects that have variables inside them. You can access those variables with specific functions or with a '\$'.

```
X <- runif(20, 2, 40)
MyData <- as.data.frame(X)
MyData$Y <- 100 - 2 * MyData$X + rnorm(20, mean = 0, sd = 1)

names(MyData)
## [1] "X" "Y"

names(MyData) <- c("Price", "Quantity")
names(MyData)
## [1] "Price" "Quantity"

summary(MyData)
## Price Quantity</pre>
```

5. You can get at columns and rows in other ways.

```
MyData[1:2]
```

```
##
         Price Quantity
     12.398847 76.16359
## 1
## 2
     26.563382 47.88302
## 3 35.863552 28.48715
## 4 14.144763 71.81721
## 5 17.721183 64.54552
## 6
     13.138583 73.57231
## 7 26.887124 46.59248
## 8 12.764642 73.31685
## 9
      8.801452 83.61818
## 10 18.611558 62.13668
## 11 10.937182 80.20880
## 12 26.261519 47.97472
## 13 25.230284 50.63122
## 14 18.714767 62.38143
## 15 20.348490 58.97369
## 16 15.220098 69.60273
## 17 19.543000 60.02417
## 18 19.856604 62.40889
## 19 5.001052 89.66214
## 20 8.750835 84.02796
```

MyData[1]

```
##
          Price
## 1 12.398847
## 2 26.563382
## 3 35.863552
## 4 14.144763
## 5 17.721183
## 6 13.138583
## 7
     26.887124
## 8 12.764642
## 9
       8.801452
## 10 18.611558
## 11 10.937182
## 12 26.261519
## 13 25.230284
## 14 18.714767
## 15 20.348490
## 16 15.220098
## 17 19.543000
## 18 19.856604
## 19 5.001052
## 20 8.750835
```

MyData[1:3,]

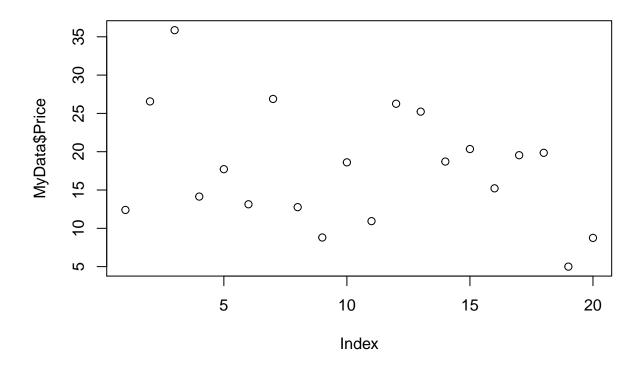
```
##
        Price Quantity
## 1 12.39885 76.16359
## 2 26.56338 47.88302
## 3 35.86355 28.48715
```

```
MyData[1:3,"Price"]
## [1] 12.39885 26.56338 35.86355
MyData["Price"]
##
          Price
## 1 12.398847
     26.563382
## 2
## 3 35.863552
## 4 14.144763
## 5 17.721183
## 6 13.138583
## 7 26.887124
## 8 12.764642
## 9
      8.801452
## 10 18.611558
## 11 10.937182
## 12 26.261519
## 13 25.230284
## 14 18.714767
## 15 20.348490
## 16 15.220098
## 17 19.543000
## 18 19.856604
## 19 5.001052
## 20 8.750835
MyData[c(1,5,8),]
##
       Price Quantity
## 1 12.39885 76.16359
## 5 17.72118 64.54552
## 8 12.76464 73.31685
```

Pictures

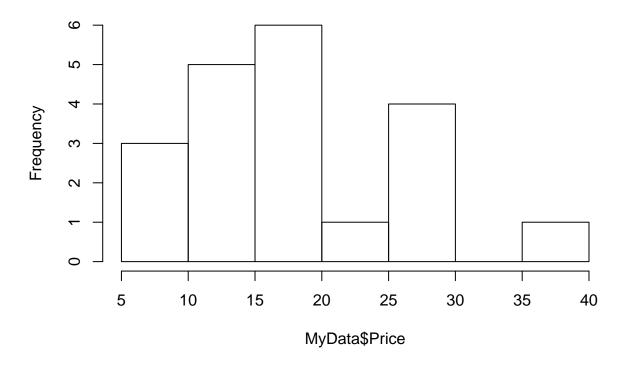
Now lets make pictures.

plot(MyData\$Price)



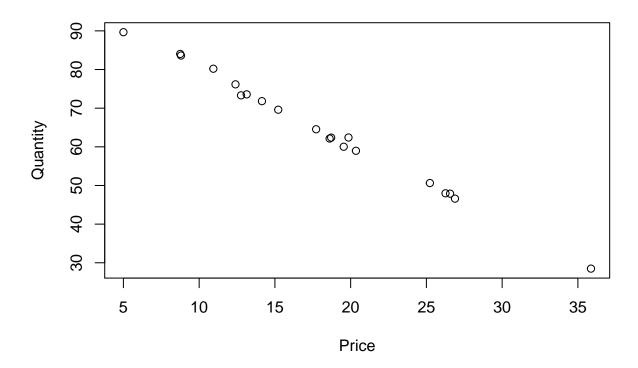
If you don't want to see the code and just the result, make sure to add echo=false to the chunk. Here is a Histogram without the code.

Histogram of MyData\$Price



Show the relationship between two variables with "plot" or more than two with "pairs".

plot(Quantity ~ Price, data= MyData)



Regression with Pictures

5. A regression line can be thought of as just putting a line through a cloud of data in a well defined way. Remember the data we created? Here is what the regression gives you. You may want to make some notes on how to write formulas for regression in this file.

```
FirstRegression<- lm(Quantity ~ Price, data=MyData)
summary(FirstRegression)</pre>
```

```
##
## Call:
  lm(formula = Quantity ~ Price, data = MyData)
##
##
##
  Residuals:
##
       Min
                1Q Median
                                3Q
                                       Max
##
  -1.5526 -0.5960 -0.1865
                            0.6884
                                    1.7533
##
##
   Coefficients:
##
                Estimate Std. Error t value Pr(>|t|)
## (Intercept) 100.45269
                            0.55300
                                       181.7
                                               <2e-16 ***
## Price
                -2.00422
                            0.02863
                                       -70.0
                                               <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
```

```
## Residual standard error: 0.9486 on 18 degrees of freedom
## Multiple R-squared: 0.9963, Adjusted R-squared: 0.9961
## F-statistic: 4901 on 1 and 18 DF, p-value: < 2.2e-16</pre>
```

Note that the estimates are the parameter, or very close to the parameters we used to create the data. Note also that the residual standard errors are the same as what we used to create the data. Nice when you know what is true.

Some other things you should note:

- MORE NOTES FOR YOU TO ADD

You should probably make a lot of notes in this document so you can remember what we are talking about. Just add things. By the way, you can do equations too, $\frac{1}{2}x$ or even

$$\lim_{x \to +\infty} \frac{3x^2 + 7x^3}{x^2 + 5x^4} = 3$$

If you take 400 level math classes, your homework will be in latex like this.

Regression can also show you things that are not true. You always have to assume a functional form and if you get that functional form wrong you get garbage. Sometimes the garbage makes some kind of sense and sometimes it leads you to believe that you have to make some kind of statistical fix. Students that have taken econometrics will be aware of autocorrelation, heterskedasticity and endogenaity as common problems. Having the wrong functional form will often present as one of these problems.

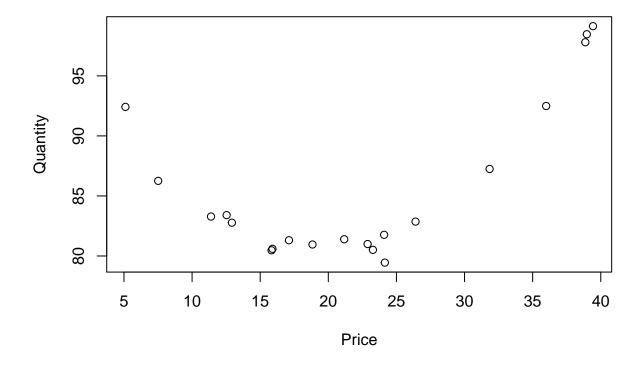
Lets wake new data and show how getting the regression model wrong can cause problems.

```
MyData2 <- data.frame(Price = runif(20, 2, 40))
MyData2$Quantity <- 100 - 2 * MyData2$Price + .05 * MyData2$Price^2 + rnorm(20, mean =0, sd = 1)
summary(MyData2)</pre>
```

```
##
        Price
                          Quantity
##
    Min.
           : 5.107
                      Min.
                              :79.45
##
    1st Qu.:15.106
                      1st Qu.:80.99
    Median :22.027
                      Median :82.82
##
    Mean
            :22.212
                      Mean
                              :85.68
##
    3rd Qu.:27.763
                      3rd Qu.:88.54
##
    Max.
            :39.428
                      Max.
                              :99.14
```

Not a line

```
plot(Quantity ~ Price, data = MyData2)
```

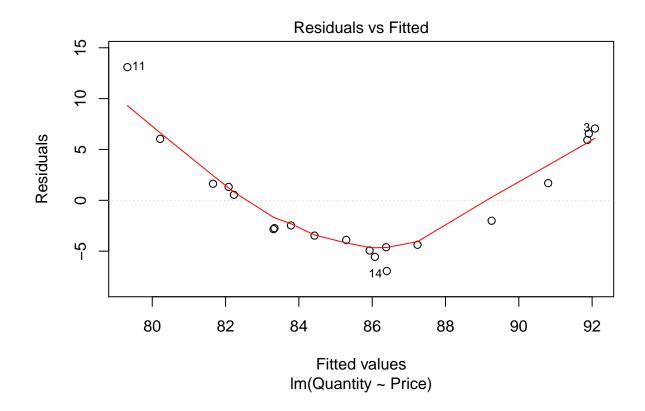


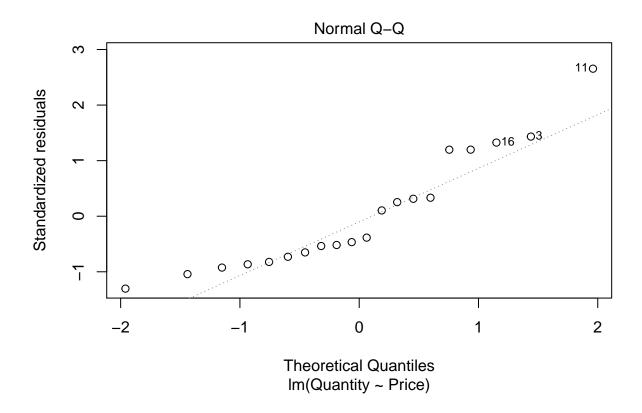
Give me a line anyway.

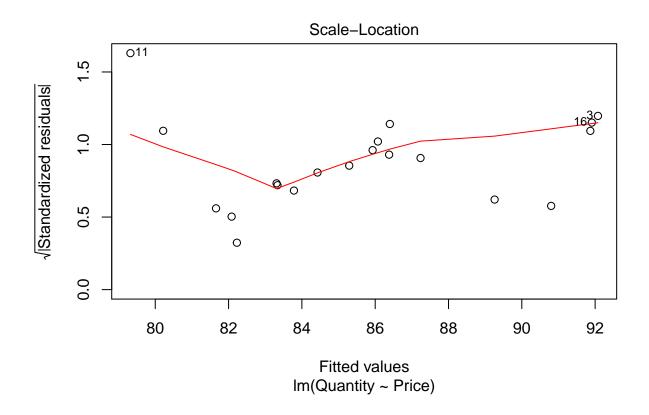
```
NotALine<- lm(Quantity ~ Price, data=MyData2)
summary(NotALine)
##</pre>
```

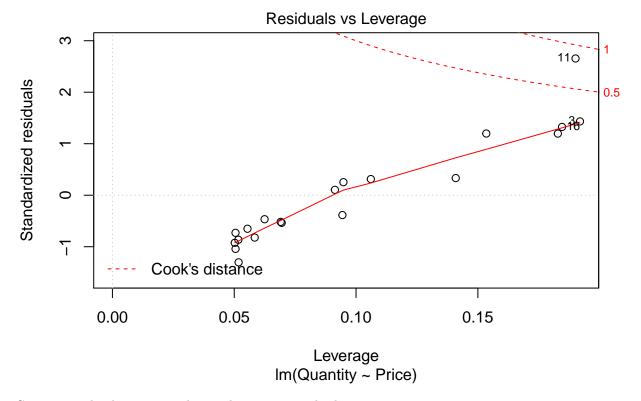
```
lm(formula = Quantity ~ Price, data = MyData2)
##
##
## Residuals:
##
     Min
             1Q Median
                           3Q
                                 Max
  -6.952 -4.016 -2.241 2.750 13.094
##
##
## Coefficients:
##
              Estimate Std. Error t value Pr(>|t|)
                                    26.41 7.57e-16 ***
## (Intercept) 77.4245
                           2.9316
                                     3.10 0.00619 **
## Price
                0.3716
                           0.1199
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 5.48 on 18 degrees of freedom
## Multiple R-squared: 0.348, Adjusted R-squared: 0.3118
## F-statistic: 9.607 on 1 and 18 DF, p-value: 0.006185
```

How to tell you were wrong thinking it was a line. Make a pictures



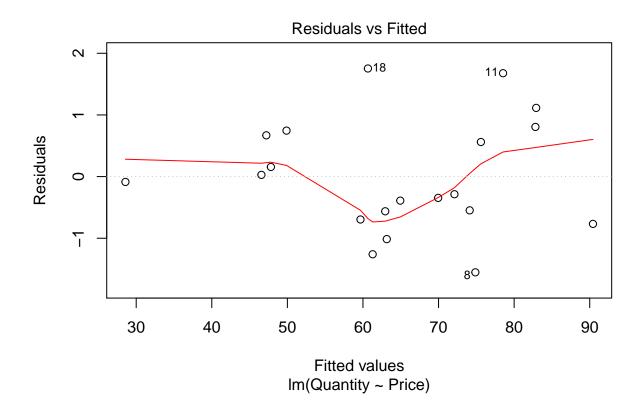


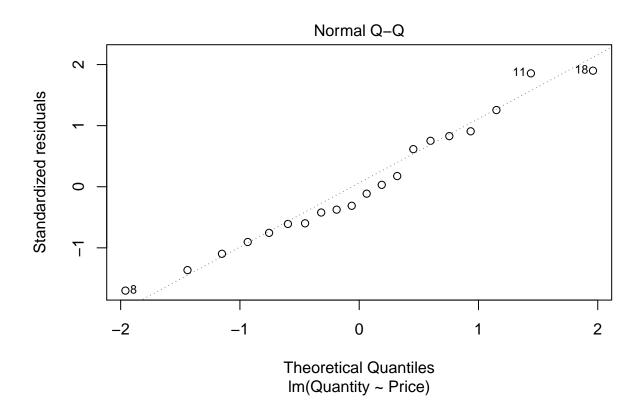


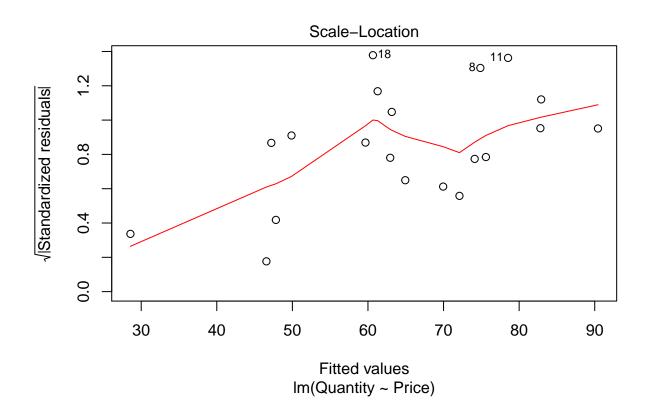


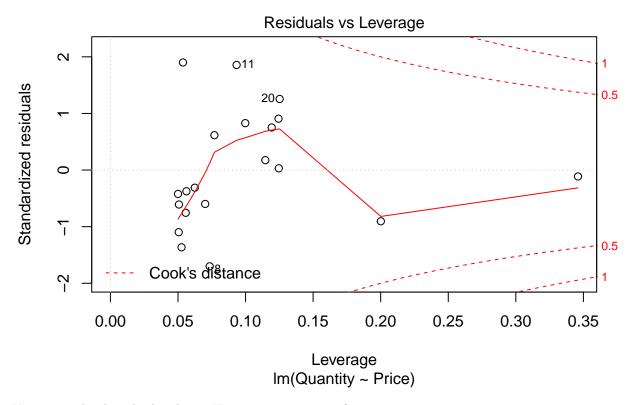
Compare with when it was a line and you estimated a line

plot(FirstRegression)



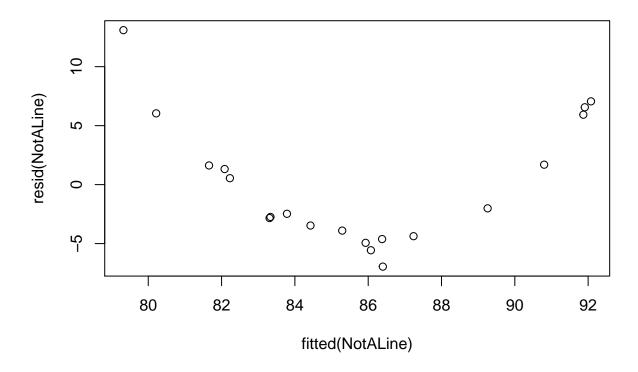






You can make these by hand too. Here are two accessor functions.

plot(resid(NotALine)~fitted(NotALine))



Dummy Variables

Not every variable is real valued, some are true false or categorical like night and day. R deals with categorical variables, called factors, very well and has fewer of the problems you see in other languages.

Lets make new fake data with dummy variables. I will reuse the first artificial dataset that was truly linear.

```
MyData$Time <- as.factor(ifelse(runif(20) < .5, "Day", "Night"))

MyData$Quantity[MyData$Time == "Day"] <- MyData$Quantity[MyData$Time == "Day"] + 12</pre>
```

I just made it so that if it is Day the quantity is 12 higher.

```
WTime <- lm(Quantity ~ Price + Time, data=MyData)
summary(WTime)</pre>
```

```
##
## Call:
## lm(formula = Quantity ~ Price + Time, data = MyData)
##
## Residuals:
## Min    1Q Median   3Q Max
## -1.5244 -0.6323 -0.1873   0.7215   1.7173
##
## Coefficients:
```

```
##
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) 112.49584
                           0.63562 176.99 < 2e-16 ***
                           0.02953
                                   -67.87 < 2e-16 ***
## Price
               -2.00458
                                   -27.43 1.62e-15 ***
## TimeNight
              -12.06681
                           0.43983
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.9754 on 17 degrees of freedom
## Multiple R-squared: 0.9967, Adjusted R-squared: 0.9963
## F-statistic: 2547 on 2 and 17 DF, p-value: < 2.2e-16
```

See something odd. Interpreting this can be tricky. Best take some notes.

You can also make it so that the reaction to price is different depending on if it is night or day.

```
WTimeInteract <- lm(Quantity ~ Price*Time, data=MyData)
summary(WTimeInteract)</pre>
```

```
##
## Call:
## lm(formula = Quantity ~ Price * Time, data = MyData)
##
## Residuals:
##
      Min
                1Q Median
                                3Q
                                       Max
## -1.4779 -0.6286 -0.1197 0.6299
                                   1.7696
##
## Coefficients:
##
                   Estimate Std. Error t value Pr(>|t|)
                               0.78080 144.218 < 2e-16 ***
## (Intercept)
                   112.60528
## Price
                   -2.01050
                               0.03815 -52.696 < 2e-16 ***
                               1.20680 -10.237 1.98e-08 ***
## TimeNight
                   -12.35372
## Price:TimeNight
                     0.01617
                                0.06307
                                          0.256
                                                   0.801
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1.003 on 16 degrees of freedom
## Multiple R-squared: 0.9967, Adjusted R-squared: 0.9961
## F-statistic: 1605 on 3 and 16 DF, p-value: < 2.2e-16
```

You will need a lot of notes on this. Interpreting interactive effects is tricky.

Useful facts

Residuals:

You can get elasticites directly out of a regression model if both quantity and price are logged. In every other case you have to calculate elasticities by hand and they are different at every point.

```
ElastForm <- lm(log(Quantity) ~ log(Price) + Time, data=MyData)
summary(ElastForm)

##
## Call:
## lm(formula = log(Quantity) ~ log(Price) + Time, data = MyData)
##</pre>
```

```
##
                       Median
                  1Q
## -0.22717 -0.02676 0.02481 0.05043 0.11269
##
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) 5.55542
                           0.13179
                                   42.153 < 2e-16 ***
## log(Price)
              -0.45458
                           0.04603
                                    -9.876 1.86e-08 ***
## TimeNight
               -0.11947
                           0.04250
                                    -2.811
                                               0.012 *
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.09456 on 17 degrees of freedom
## Multiple R-squared: 0.8618, Adjusted R-squared: 0.8455
                   53 on 2 and 17 DF, p-value: 4.948e-08
## F-statistic:
I did it, but is it right?
If only the right hand side variable is logged, you interpret the parameter as the effect of a percent change.
PercentForm <- lm(Quantity ~ log(Price) + Time, data=MyData)</pre>
summary(PercentForm)
##
## Call:
## lm(formula = Quantity ~ log(Price) + Time, data = MyData)
## Residuals:
##
       Min
                1Q
                    Median
                                30
                                       Max
## -10.145 -1.291
                     1.315
                             2.282
                                     5.455
##
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
                             6.073 26.649 2.63e-15 ***
## (Intercept)
               161.832
                -31.078
                             2.121 -14.654 4.48e-11 ***
## log(Price)
## TimeNight
                 -9.395
                             1.958 -4.797 0.000168 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 4.357 on 17 degrees of freedom
## Multiple R-squared: 0.9336, Adjusted R-squared: 0.9258
## F-statistic: 119.6 on 2 and 17 DF, p-value: 9.688e-11
```

Common statistical problems

This is the basics. You now know enough to be insanely overconfident. Don't destroy the world.

Beyond getting the specification wrong, which you usually support with several similar models that show similar results, there are common statistical problems that you learn about in econometrics

- Autocorrelation, which makes your regression look better than it actually is.
- Heteroskadasticity, which makes it worse.
- Endogenaity, which biases your parameters in unknown directions.
- Errors in variables (RHS), which bias parameters towards zero.
- ...

Don't get cocky.

What we are going to do next is read in some real data that looks like either supply or demand but will be neither. Why, because supply and demand determine price and quantity simultaneously, that means that something either price or quantity is endogenous. At this point, you are at about 1910 as far as standard econometric practice.

Real Data

- I will walk you through a few steps on reading in the data. The biggest hurdle to doing stats on the data is reading it in. There is actually an R library for working with EIA data directly, EIAdata, but we will use the more general tools to read files.
- Download into R data on coal prices and quantities. Again, the assignment operator in R is the "<-" symbol.

```
Coal <- read.csv("https://www.eia.gov/totalenergy/data/browser/csv.cfm?tbl=T06.01")
```

There are many ways of loading data into R (http://www.r-tutor.com/r-introduction/data-frame/data-import). Some work some of the time. In most cases Comma Separated Values (CSV) is the safest format to work with.

• Take a look at the summary of the data

summary(Coal)

```
##
                         MMYYYY
                                                  Value
         MSN
                                                               Column_Order
##
    CLEXPUS: 604
                    Min.
                            :194913
                                       Not Available: 244
                                                              Min.
                                                                     :1.00
##
    CLIMPUS: 604
                    1st Qu.:198211
                                       2
                                                         3
                                                              1st Qu.:2.75
##
    CLLUPUS: 604
                    Median: 199406
                                       3
                                                         3
                                                              Median:4.50
    CLNIPUS: 604
                                                         3
##
                    Mean
                            :199352
                                       834.633
                                                              Mean
                                                                     :4.50
                                                     :
                    3rd Qu.:200535
                                       -4657
                                                              3rd Qu.:6.25
##
    CLPRPUS: 604
                                                         2
    CLSCPUS: 604
                                                         2
##
                            :201708
                                                              Max.
                                                                     :8.00
                    Max.
                                       114
##
    (Other):1208
                                       (Other)
                                                     :4575
##
                               Description
                                                                 Unit
                                              Thousand Short Tons: 4832
##
    Coal Consumption
                                      : 604
##
    Coal Exports
                                      : 604
##
   Coal Imports
                                      : 604
##
    Coal Losses and Unaccounted for: 604
    Coal Net Imports
                                      : 604
##
    Coal Production
                                      : 604
##
    (Other)
                                      :1208
```

You will notice that for some variables they give counts, e.g., MSN, and for others you get numerical summaries, e.g., Column_Order. The difference has to do with the data types (http://www.statmethods.net/input/datatypes.html).

- Since we are trying to make a simple supply model, i.e., trying to explain coal production, lets select just the production part of the data set and also get only the annual production values. This is a little primer on changing data types and taking part of data.
- Load the dplyr package. This is the normal way to load libraries of functions that you need.

```
library(dplyr)
```

```
##
## Attaching package: 'dplyr'
```

```
## The following objects are masked from 'package:stats':
##
## filter, lag
## The following objects are masked from 'package:base':
##
## intersect, setdiff, setequal, union
```

• Select only the Coal Production Figures and save it as CoalProduction. There is a cheat sheet for dplyr built into R. Look under the help menu.

```
CoalProduction <- Coal %>% filter(MSN == "CLPRPUS")
```

• Note that you have monthly data but that the annual data is shown as month 13. Grab all of the observations with month not equal to 13.

```
library(stringr)

CoalProduction <- CoalProduction %>% filter(str_sub(as.character(YYYYMM),5) != "13")
```

• At this point you will have noticed that we don't need all the columns so lets keep just the ones we need and then give the two columns we saved new names.

```
CoalProduction <- CoalProduction %>% select(YYYYMM, Value)

names(CoalProduction) <- c("RawMonth", "ProductionKShortTon")
summary(CoalProduction)</pre>
```

```
##
       RawMonth
                      ProductionKShortTon
##
    Min.
           :197301
                      100000.27 : 1
##
    1st Qu.:198403
                      100427.638:
   Median:199505
                      100627.455:
##
  Mean
           :199490
                      100653.897:
##
    3rd Qu.:200606
                      101144.833:
##
   Max.
           :201708
                      101490.13:
##
                      (Other)
                                :530
```

• Notice that the ProductionKShortTon variable shows a count rather than a numerical summary. This means that R thinks it is a factor rather than a number. Lets fix that. It requires to first convert the factor, which is an integer, to the real value as a character and then convert that to numeric.

```
CoalProduction$ProductionKShortTon <- as.numeric(as.character(CoalProduction$ProductionKShortTon))</pre>
```

Play around with this doing one function at a time to see what each does and what each does alone.

• Next lets create a column for the year and make it a numeric value.

```
CoalProduction <- CoalProduction %>% mutate(Year = as.numeric(str_sub(as.character(RawMonth),0,4))) %
summary(CoalProduction)
```

```
##
       RawMonth
                      ProductionKShortTon
                                                               Month
                                                Year
##
   Min.
           :197301
                             : 23664
                                           Min.
                                                  :1973
                                                           Min.
                                                                  : 1.00
   1st Qu.:198403
                      1st Qu.: 69745
                                                           1st Qu.: 3.00
##
                                           1st Qu.:1984
## Median :199505
                      Median: 82459
                                           Median:1995
                                                           Median: 6.00
                             : 79100
                                                                  : 6.47
## Mean
           :199490
                      Mean
                                           Mean
                                                   :1995
                                                           Mean
    3rd Qu.:200606
                      3rd Qu.: 90530
                                           3rd Qu.:2006
                                                           3rd Qu.: 9.00
## Max.
           :201708
                             :104390
                                           Max.
                                                  :2017
                                                           Max.
                                                                  :12.00
                      Max.
```

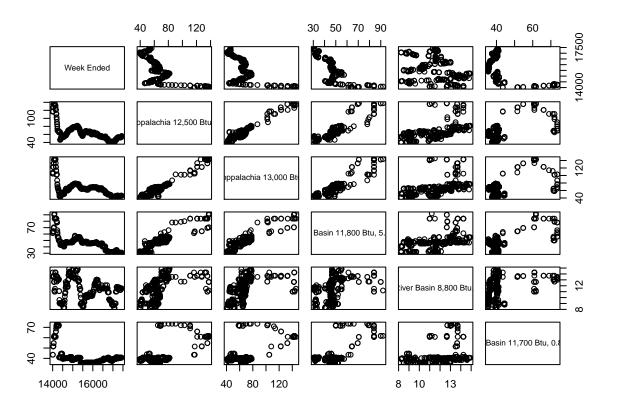
• Now grab some price data. We are going to use Quandl (https://www.quandl.com/), which has a bunch of data on energy and a lot of other things (https://www.quandl.com/collections/markets/coal). Make sure you have the Quandl library installed. If you don't install.packages("Quandl") should do it.

library(Quandl)

• Lets make a picture

```
## Loading required package: xts
## Loading required package: zoo
##
## Attaching package: 'zoo'
## The following objects are masked from 'package:base':
##
##
       as.Date, as.Date.numeric
##
## Attaching package: 'xts'
## The following objects are masked from 'package:dplyr':
##
##
       first, last
Prices <- Quandl("EIA/COAL")</pre>
summary(Prices)
##
      Week Ended
                         Central Appalachia 12,500 Btu, 1.2 SO2
   Min.
           :2008-05-06
                         Min.
                                : 39.55
   1st Qu.:2010-09-20
                         1st Qu.: 52.75
##
                         Median: 60.90
##
  Median :2013-01-11
                                 : 63.96
##
  Mean
           :2013-01-19
                         Mean
## 3rd Qu.:2015-05-23
                         3rd Qu.: 68.99
## Max.
           :2017-09-29
                         Max.
                                 :137.50
##
   Northern Apppalachia 13,000 Btu, <3.0 SO2
##
  Min.
           : 40.75
   1st Qu.: 51.50
##
##
   Median: 63.70
##
  Mean
           : 64.43
##
   3rd Qu.: 68.65
## Max.
           :145.50
   Illinois Basin 11,800 Btu, 5.0 SO2 Powder River Basin 8,800 Btu, 0.8 SO2
##
##
  Min.
           :30.70
                                        Min.
                                               : 8.25
   1st Qu.:40.32
                                        1st Qu.:10.13
##
  Median :46.00
                                        Median :11.55
## Mean
           :45.72
                                        Mean
                                               :11.38
##
  3rd Qu.:47.90
                                        3rd Qu.:12.86
## Max.
           :92.00
                                        Max.
                                               :14.90
## Uinta Basin 11,700 Btu, 0.8 S02
## Min.
           :35.50
##
  1st Qu.:36.73
## Median :39.45
## Mean
           :41.03
##
   3rd Qu.:40.55
## Max.
           :73.50
```

library(ggplot2) plot(Prices)



- Story time on the picture. What do you see? What stories come to mind?
- As before we will convert the year to a numeric value.

library(lubridate)

```
##
## Attaching package: 'lubridate'
## The following object is masked from 'package:base':
##
## date
# Prices$Year <- as.numeric(str_sub(Prices$Year,0,4))
Prices <- Prices %>% mutate(Month = month(`Week Ended`) ) %>% mutate(Year = year (`Week Ended`))
```

• Now we are going to get monthly averages

```
Prices <- Prices %>% group_by(Month, Year) %>% summarise_all(mean)
```

For illustrative purposes lets let stick with one price and then merge the price and volume data.

```
Prices <- Prices %>% select(Year, Month, Price = `Central Appalachia 12,500 Btu, 1.2 SO2` )
```

• Merge the two data frames

```
summary(CoalProduction)
      RawMonth
                   ProductionKShortTon
##
                                           Year
                                                        Month
                   Min. : 23664
##
                                                   Min. : 1.00
  Min. :197301
                                  Min.
                                            :1973
  1st Qu.:198403
                   1st Qu.: 69745
                                      1st Qu.:1984
                                                    1st Qu.: 3.00
## Median :199505
                   Median : 82459
                                      Median:1995
                                                    Median: 6.00
## Mean :199490
                   Mean : 79100
                                      Mean :1995
                                                    Mean : 6.47
## 3rd Qu.:200606
                   3rd Qu.: 90530
                                      3rd Qu.:2006
                                                    3rd Qu.: 9.00
## Max.
         :201708
                   Max.
                         :104390
                                      Max.
                                            :2017
                                                    Max. :12.00
summary(Prices)
##
        Year
                     Month
                                     Price
## Min.
                 Min. : 1.000
          :2008
                                 Min. : 40.50
## 1st Qu.:2010
                 1st Qu.: 4.000
                                 1st Qu.: 52.83
                 Median : 7.000
                                 Median : 61.24
## Median :2013
                 Mean : 6.522
                                 Mean : 64.08
## Mean
         :2013
                 3rd Qu.: 9.000
## 3rd Qu.:2015
                                 3rd Qu.: 69.10
## Max.
          :2017
                 Max. :12.000
                                 Max.
                                       :137.50
CoalMarket <- inner_join(Prices, CoalProduction, by =c("Year", "Month"))</pre>
summary(CoalMarket)
        Year
                                                  RawMonth
                     Month
                                   Price
## Min.
        :2008
                 Min. : 1.0
                               Min. : 40.50
                                                      :200805
                                               Min.
   1st Qu.:2010
                 1st Qu.: 4.0
                               1st Qu.: 52.81
                                               1st Qu.:201009
##
## Median :2012
                 Median: 6.5
                              Median : 61.37
                                               Median :201257
                 Mean : 6.5
                               Mean : 64.17
## Mean :2012
                                               Mean :201257
## 3rd Qu.:2015
                 3rd Qu.: 9.0
                               3rd Qu.: 69.33
                                               3rd Qu.:201504
                              Max. :137.50
## Max.
         :2017
                 Max. :12.0
                                               Max. :201708
## ProductionKShortTon
## Min. : 48115
## 1st Qu.: 76273
## Median: 84543
## Mean : 82097
## 3rd Qu.: 90310
## Max. :104390
Lets look at the data.
```

pairs(~ Year+ Price + ProductionKShortTon, data = CoalMarket)

