## bradley-Terry

Tennis <- read.table("http://www.stat.ufl.edu/~aa/cat/data/Tennis.dat",header=TRUE)
Tennis</pre>

```
Djokovic Federer Murray Nadal Wawrinka nij nji
1
           1
                   -1
                                   0
                                                       6
2
           1
                    0
                           -1
                                   0
                                              0
                                                 14
                                                       3
3
           1
                    0
                            0
                                  -1
                                              0
                                                  9
                                                       2
4
           1
                    0
                            0
                                   0
                                            -1
                                                       3
5
           0
                    1
                           -1
                                   0
                                              0
                                                       0
6
           0
                            0
                    1
                                  -1
                                              0
                                                       1
7
           0
                    1
                                  0
                                            -1
                                                       2
           0
                    0
8
                            1
                                  -1
                                             0
9
           0
                    0
                            1
                                   0
                                            -1
                                                  2
                                                       2
10
           0
                    0
                            0
                                   1
                                                       3
                                            -1
```

#### Tennis

```
Djokovic Federer Murray Nadal Wawrinka nij nji
1
           1
                   -1
                            0
                                   0
                                             0
                                                  9
                                                      6
           1
                    0
                                   0
                                                 14
                                                      3
2
                           -1
                                             0
3
           1
                    0
                            0
                                  -1
                                             0
                                                      2
4
           1
                    0
                            0
                                  0
                                                      3
                                            -1
5
           0
                    1
                           -1
                                   0
                                             0
                                                      0
6
           0
                    1
                            0
                                  -1
                                             0
                                                  5
                                                      1
7
           0
                    1
                            0
                                 0
                                                      2
                                            -1
8
           0
                    0
                                  -1
                                             0
                                                      4
           0
                    0
                            1
                                  0
                                                  2
                                                      2
9
                                            -1
10
           0
                    0
                                   1
                                            -1
                                                      3
```

```
data <- data.frame(
  Winner = c("Djokovic", "Federer", "Murray", "Nadal", "Wawrinka"),
  Djokovic = c(NA, 6, 3, 2, 3),
  Federer = c(9, NA, 0, 1, 2),
  Murray = c(14, 5, NA, 4, 2),
  Nadal = c(9, 5, 2, NA, 3),
  Wawrinka = c(4, 7, 2, 4, NA)
)
table_result <- as.matrix(data[,-1])
rownames(table_result) <- data$Winner
table_result</pre>
```

	Djokovic	Federer	Murray	Nadal	Wawrinka
Djokovic	NA	9	14	9	4
Federer	6	NA	5	5	7
Murray	3	0	NA	2	2
Nadal	2	1	4	NA	4
Wawrinka	3	2	2	3	NA

Table 1: Tennis Match Wins (Loser in Columns, Winner in Rows)

	Djokovic	Federer	Murray	Nadal	Wawrinka
Djokovic	NA	9	14	9	4
Federer	6	NA	5	5	7
Murray	3	0	NA	2	2
Nadal	2	1	4	NA	4
Wawrinka	3	2	2	3	NA

```
fit <- glm(nij/(nij+nji) ~ -1 + Djokovic + Federer + Murray + Nadal + Wawrinka, family=binom summary(fit)
```

```
Call:
```

```
glm(formula = nij/(nij + nji) ~ -1 + Djokovic + Federer + Murray +
   Nadal + Wawrinka, family = binomial, data = Tennis, weights = nij +
```

```
nji)
```

```
Coefficients: (1 not defined because of singularities)
        Estimate Std. Error z value Pr(>|z|)
Djokovic 1.17612 0.49952 2.354 0.0185 *
        1.13578
                   0.51095 2.223 0.0262 *
Federer
Murray -0.56852 0.56833 -1.000 0.3172
        -0.06185 0.51487 -0.120 0.9044
Nadal
Wawrinka
              NA
                         NA
                                NΑ
                                         NA
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
(Dispersion parameter for binomial family taken to be 1)
    Null deviance: 26.8960 on 10 degrees of freedom
Residual deviance: 4.3958 on 6 degrees of freedom
AIC: 34.041
Number of Fisher Scoring iterations: 4
library(BradleyTerry2)
Head2Head<-countsToBinomial(table_result)</pre>
names(Head2Head)[3:4]<-c("Win", "Lose")</pre>
model <-BTm(cbind(Win, Lose), player1, player2, formula=~player, id="player", refcat="Wawrinks
summary(model)
Call:
BTm(outcome = cbind(Win, Lose), player1 = player1, player2 = player2,
    formula = ~player, id = "player", refcat = "Wawrinka", data = Head2Head)
Coefficients:
              Estimate Std. Error z value Pr(>|z|)
playerDjokovic 1.17612 0.49952 2.354 0.0185 *
                          0.51095
playerFederer 1.13578
                                   2.223 0.0262 *
playerMurray -0.56852
                          0.56833 -1.000 0.3172
playerNadal
              -0.06185
                          0.51487 -0.120 0.9044
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
(Dispersion parameter for binomial family taken to be 1)
```

Null deviance: 26.8960 on 10 degrees of freedom Residual deviance: 4.3958 on 6 degrees of freedom

AIC: 34.041

Number of Fisher Scoring iterations: 4

#### BTabilities(model)

ability s.e.
Djokovic 1.17612172 0.4995230
Federer 1.13578408 0.5109457
Murray -0.56851913 0.5683333
Nadal -0.06185141 0.5148698
Wawrinka 0.00000000 0.0000000

# model2<-update(model, refcat="Nadal") BTabilities(model2)</pre>

ability s.e.
Djokovic 1.23797313 0.4736563
Federer 1.19763549 0.5162229
Murray -0.50666771 0.5367784
Nadal 0.00000000 0.0000000
Wawrinka 0.06185141 0.5148698

```
library("qvcalc")
tennis.qv <- qvcalc(BTabilities(model))
plot(tennis.qv,levelNames = c("Djo","Fed","M","N","w"))</pre>
```

### Intervals based on quasi standard errors

