

stat consulting

#Quasi-independence

```
datagss <- data.frame(
  Now = c("NortheastN", "MidwestN", "SouthN", "WestN",
          "NortheastN", "MidwestN", "SouthN", "WestN",
          "NortheastN", "MidwestN", "SouthN", "WestN",
          "NortheastN", "MidwestN", "SouthN", "WestN"),
  Age16 = rep( c("Northeast16", "Midwest16", "South16", "West16"), each=4),
  Count = c(394,17,81,38,8,596,74,59,29,32,769,35,10,24,35,417)
)
fit1<-glm(Count ~ Now + Age16,family=poisson,data=datagss)
summary(fit1)
```

Call:

```
glm(formula = Count ~ Now + Age16, family = poisson, data = datagss)
```

Coefficients:

	Estimate	Std. Error	z value	Pr(> z)
(Intercept)	5.23821	0.04970	105.407	< 2e-16 ***
NowNortheastN	-0.41674	0.06133	-6.795	1.09e-11 ***
NowSouthN	0.36011	0.05037	7.149	8.76e-13 ***
NowWestN	-0.19769	0.05759	-3.433	0.000597 ***
Age16Northeast16	-0.32971	0.05695	-5.789	7.07e-09 ***
Age16South16	0.16014	0.05013	3.195	0.001400 **
Age16West16	-0.41638	0.05843	-7.126	1.03e-12 ***

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

(Dispersion parameter for poisson family taken to be 1)

Null deviance: 4236.9 on 15 degrees of freedom
 Residual deviance: 3871.7 on 9 degrees of freedom
 AIC: 3981

Number of Fisher Scoring iterations: 6

```
datagss_quasi <- data.frame(
  Now = c("NortheastN", "MidwestN", "SouthN", "WestN",
          "NortheastN", "MidwestN", "SouthN", "WestN",
          "NortheastN", "MidwestN", "SouthN", "WestN",
          "NortheastN", "MidwestN", "SouthN", "WestN"),
  Age16 = rep( c("Northeast16", "Midwest16", "South16", "West16"), each=4),
  Count = c( 394,17,81,38,8,596,74,59,29,32,769,35,10,24,35,417),
  diag_index = c(1,0,0,0,0,2,0,0,0,0,3,0,0,0,0,4) )
fit2 <- glm(Count ~ factor(Now) + factor(Age16) + factor(diag_index), family=poisson, data=datagss_quasi)
summary(fit2)
```

Call:

```
glm(formula = Count ~ factor(Now) + factor(Age16) + factor(diag_index),
     family = poisson, data = datagss_quasi)
```

Coefficients:

	Estimate	Std. Error	z value	Pr(> z)
(Intercept)	3.38251	0.16019	21.115	< 2e-16 ***
factor(Now)NortheastN	-0.48251	0.19270	-2.504	0.01228 *
factor(Now)SouthN	0.97109	0.15062	6.447	1.14e-10 ***
factor(Now)WestN	0.42567	0.15172	2.806	0.00502 **
factor(Age16)Northeast16	-0.11300	0.12406	-0.911	0.36237
factor(Age16)South16	0.03512	0.14716	0.239	0.81137
factor(Age16)West16	-0.59721	0.15254	-3.915	9.04e-05 ***
factor(diag_index)1	3.18935	0.18796	16.968	< 2e-16 ***
factor(diag_index)2	3.00773	0.16535	18.191	< 2e-16 ***
factor(diag_index)3	2.25637	0.15333	14.716	< 2e-16 ***
factor(diag_index)4	2.82212	0.17038	16.563	< 2e-16 ***

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

(Dispersion parameter for poisson family taken to be 1)

Null deviance: 4236.927 on 15 degrees of freedom
 Residual deviance: 29.803 on 5 degrees of freedom

AIC: 147.09

Number of Fisher Scoring iterations: 4

#bradley-Terry

```
Tennis <- read.table("http://www.stat.ufl.edu/~aa/cat/data/Tennis.dat",header=TRUE)
Tennis
```

	Djokovic	Federer	Murray	Nadal	Wawrinka	nij	nji
1	1	-1	0	0	0	9	6
2	1	0	-1	0	0	14	3
3	1	0	0	-1	0	9	2
4	1	0	0	0	-1	4	3
5	0	1	-1	0	0	5	0
6	0	1	0	-1	0	5	1
7	0	1	0	0	-1	7	2
8	0	0	1	-1	0	2	4
9	0	0	1	0	-1	2	2
10	0	0	0	1	-1	4	3

Tennis

	Djokovic	Federer	Murray	Nadal	Wawrinka	nij	nji
1	1	-1	0	0	0	9	6
2	1	0	-1	0	0	14	3
3	1	0	0	-1	0	9	2
4	1	0	0	0	-1	4	3
5	0	1	-1	0	0	5	0
6	0	1	0	-1	0	5	1
7	0	1	0	0	-1	7	2
8	0	0	1	-1	0	2	4
9	0	0	1	0	-1	2	2
10	0	0	0	1	-1	4	3

```
data <- data.frame(
  Winner = c("Djokovic", "Federer", "Murray", "Nadal", "Wawrinka"),
  Djokovic = c(NA, 6, 3, 2, 3),
  Federer = c(9, NA, 0, 1, 2),
  Murray = c(14, 5, NA, 4, 2),
  Nadal = c(9, 5, 2, NA, 3),
  Wawrinka = c(0, 0, 0, 0, NA))
```

```
Wawrinka = c(4, 7, 2, 4, NA)
)
table_result <- as.matrix(data[, -1])
rownames(table_result) <- data$Winner
table_result
```

	Djokovic	Federer	Murray	Nadal	Wawrinka
Djokovic	NA	9	14	9	4
Federer	6	NA	5	5	7
Murray	3	0	NA	2	2
Nadal	2	1	4	NA	4
Wawrinka	3	2	2	3	NA

```
library(knitr)
kable(table_result, format = "markdown", col.names = c("Djokovic", "Federer", "Murray", "Nadal", "Wawrinka"),
caption = "Tennis Match Wins (Loser in Columns, Winner in Rows)")
```

Table 1: Tennis Match Wins (Loser in Columns, Winner in Rows)

	Djokovic	Federer	Murray	Nadal	Wawrinka
Djokovic	NA	9	14	9	4
Federer	6	NA	5	5	7
Murray	3	0	NA	2	2
Nadal	2	1	4	NA	4
Wawrinka	3	2	2	3	NA

```
fit <- glm(nij/(nij+nji) ~ -1 + Djokovic + Federer + Murray + Nadal + Wawrinka, family=binomial)
summary(fit)
```

Call:

```
glm(formula = nij/(nij + nji) ~ -1 + Djokovic + Federer + Murray +
    Nadal + Wawrinka, family = binomial, data = Tennis, weights = nij +
    nji)
```

Coefficients: (1 not defined because of singularities)

	Estimate	Std. Error	z value	Pr(> z)
Djokovic	1.17612	0.49952	2.354	0.0185 *
Federer	1.13578	0.51095	2.223	0.0262 *

Murray	-0.56852	0.56833	-1.000	0.3172
Nadal	-0.06185	0.51487	-0.120	0.9044
Wawrinka	NA	NA	NA	NA

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

(Dispersion parameter for binomial family taken to be 1)

Null deviance: 26.8960 on 10 degrees of freedom
 Residual deviance: 4.3958 on 6 degrees of freedom
 AIC: 34.041

Number of Fisher Scoring iterations: 4

```
library(BradleyTerry2)
Head2Head<-countsToBinomial(table_result)
names(Head2Head)[3:4]<-c("Win", "Lose")
model<-BTm(cbind(Win, Lose), player1, player2, formula=~player, id="player", refcat="Wawrinka")
summary(model)
```

Call:

```
BTm(outcome = cbind(Win, Lose), player1 = player1, player2 = player2,
     formula = ~player, id = "player", refcat = "Wawrinka", data = Head2Head)
```

Coefficients:

	Estimate	Std. Error	z value	Pr(> z)
playerDjokovic	1.17612	0.49952	2.354	0.0185 *
playerFederer	1.13578	0.51095	2.223	0.0262 *
playerMurray	-0.56852	0.56833	-1.000	0.3172
playerNadal	-0.06185	0.51487	-0.120	0.9044

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

(Dispersion parameter for binomial family taken to be 1)

Null deviance: 26.8960 on 10 degrees of freedom
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 AIC: 34.041

Number of Fisher Scoring iterations: 4

```
BTabilities(model)
```

	ability	s.e.
Djokovic	1.17612172	0.4995230
Federer	1.13578408	0.5109457
Murray	-0.56851913	0.5683333
Nadal	-0.06185141	0.5148698
Wawrinka	0.00000000	0.0000000

```
modal2<-update(model, refcat="Nadal")  
BTabilities(modal2)
```

	ability	s.e.
Djokovic	1.23797313	0.4736563
Federer	1.19763549	0.5162229
Murray	-0.50666771	0.5367784
Nadal	0.00000000	0.0000000
Wawrinka	0.06185141	0.5148698