

Exam II

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There are benefits of hiring a firm specializing in nonparametric statistics. Nonparametric methods require minimal assumptions about the distribution of the population. (Higgins p7) With a traditional t-test a few assumptions must be made. The data must be made up of independent observations, it must be normally distributed, and the variances of the populations must be the same. We can safely assume the first, but we must run more tests in order to check the distribution and variance.

You have requested our services in examining two problems. The first task is to analyze the differences between states regarding test scores. The second task is to determine if the *We Come to You* instructors time spent ultimately makes a difference on test scores. We will begin with a broad overview of the data analyzing summary statistics and a few initial plots.

Looking at the summary statistics for the state testing data it seems like most are roughly the same, except for the test scores for state 4. State 4 test results appear to be nearly 10 lower than other states. It is worth noting that there are many observations missing from the data set, so we do not have population means. The boxplot of the state testing data is a visual representation of the same summary statistics. Again, we can see that one box is much different from the others. We also want to do an initial check for normality. Figure 3 contains both a Q-Q plot and a histogram. It is clear that this data is not normally distributed. For the Q-Q plot we want to see a straight line with the points lying atop the line. There are many points toward the bottom that are not on the line. For the histogram normal data would show a bell-shaped curve, but in this case it is heavily left-skewed.

	Our State	State 1	State 2	State 3	State 4	State 5	Combined
Min.	83.08	83.16	83.37	83.48	74.62	83.41	74.62
1 <sup>st</sup> Quart.	83.90	83.52	84.72	83.79	75.07	83.71	83.38
Median	84.70	84.81	84.88	84.79	76.06	84.33	84.07
Mean	84.78	84.69	85.09	84.90	75.99	84.61	83.20
3 <sup>rd</sup> Quart.	86.00	85.69	86.09	85.91	76.35	85.18	85.61
Max.	86.24	86.91	86.72	86.99	78.46	86.88	86.99
NA's	1	0	3	1	0	1	6

Figure 1. Table of summary statistics for state testing data

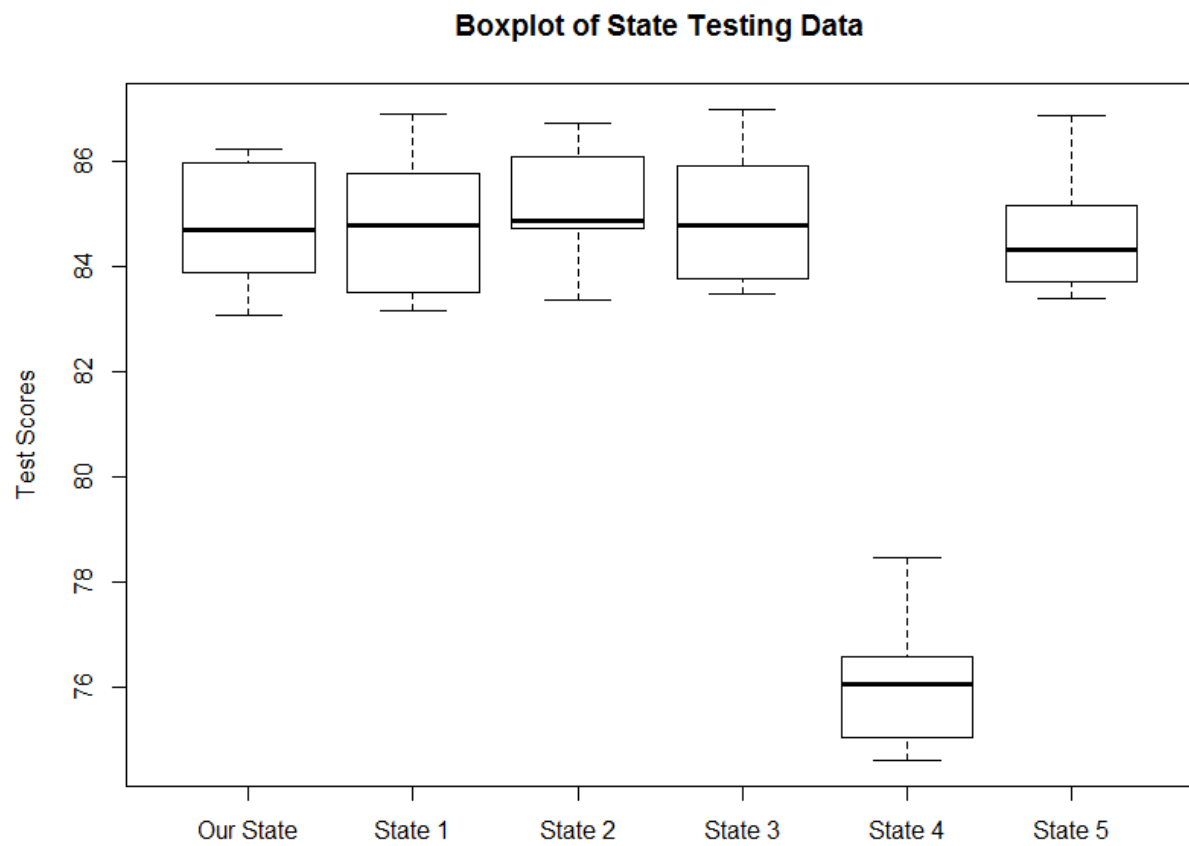


Figure 2. Boxplot of state testing data

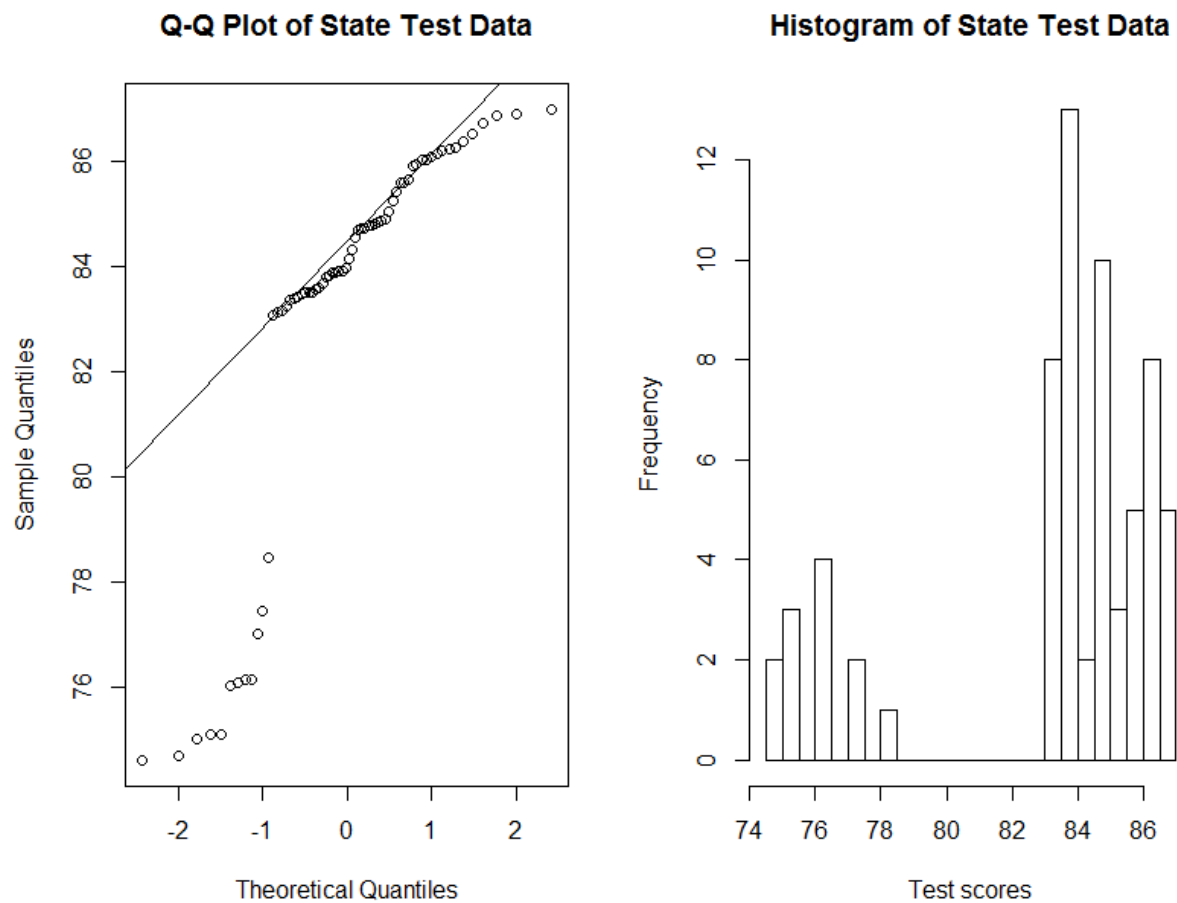


Figure 3. State Q-Q plot & Histogram

We will also look at the summary statistics for the time data. The scores in Figure 4 seem very similar. Interestingly the under 30 minute scores appear to be the best of the bunch. The boxplot looks more consistent than the previous boxplot. There are no major outliers and all scores are within a few points. The Q-Q plot does not quite look like a normal distribution since the tails do not fall on the line. The histogram makes the distribution seem like more of a uniform distribution.

	< 30 min	60 min	90 min	120 min	180 min	Combined
Min.	81.00	80.05	80.24	80.15	80.37	80.05
1 <sup>st</sup> Quart.	82.34	80.79	81.58	80.80	81.80	81.15
Median	82.93	81.45	82.19	81.00	82.51	82.15
Mean	82.82	81.76	82.16	81.50	82.32	82.11
3 <sup>rd</sup> Quart.	83.59	82.92	82.77	82.38	83.03	83.06
Max.	83.98	83.84	83.89	83.29	83.71	83.98

Figure 4. Table of summary statistics for Internal Research - WCTY Time Data.

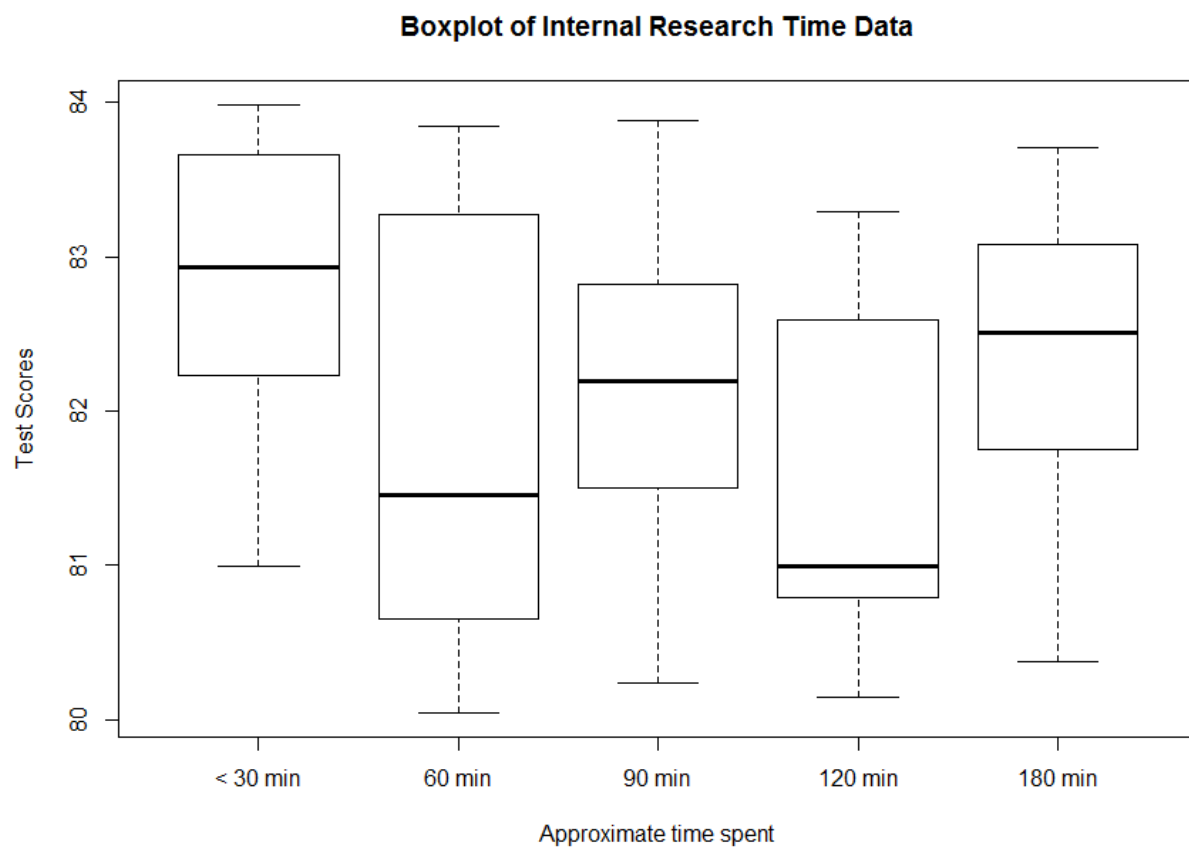
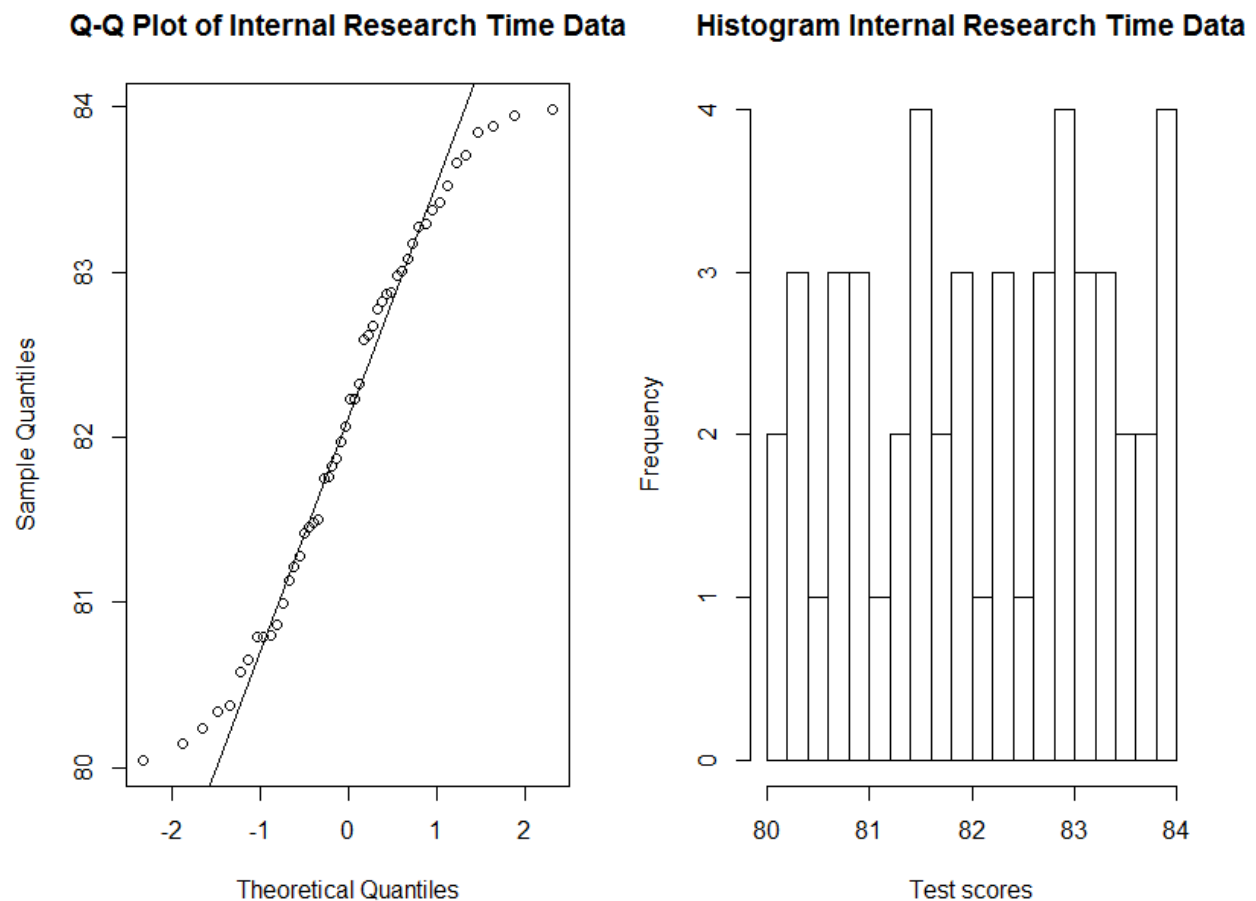


Figure 5. Boxplot of state testing data



*Figure 6. Internal Research Histogram and Q-Q plot*

The first tests we must run are to compare the scale and variance of the distributions. This must be done since the other tests have certain assumptions that must be met in order to be able to use them. Since we do not know the means we cannot use the Siegel-Tukey or Ansari-Bradley tests to check for variance. In this case we will use an RMD test in order to determine whether the groups have equal variances. As mentioned in the introduction nonparametric is useful when we are not analyzing a normal distribution. Since we have gathered that neither distribution is close to normal we know that a nonparametric test is required to achieve an accurate result.

After checking variances we can begin to run k-sample permutation tests. The Kruskal-Wallis permutation test will be used. First we will rank the data from the smallest to largest scores. Using our original data we can find a test statistic and average rank for each different treatment. The data will then be sampled to try many possible combinations performing the same test. At the end we can compare each permutation to our original test statistic and find a p-value. The null hypothesis for this test is that each treatment is the same, while the alternative is that at least one treatment is different. We must also use an adjustment since there are multiple samples in order to account for type 1 error. The adjustment to be used is the Bonferroni adjustment, which is one of the more conservative adjustments.

RMD Tests for equal variances					
	State1	State2	State3	State4	State5
Ourstate	0.23	0.01	0.95	0.51	0.05

Figure 7. Check various sets for equal variance.

	Ranks	Sample Size	Mean Rank
Our State	47, 58, 33, 37, 27, 34, 14, 54, 13, 59, 53	11	39
State 1	22, 55, 45, 65, 21, 15, 40, 59, 16, 52, 28, 42	12	38.33
State 2	44, 43, 46, 56, 24, 17, 62, 38, 63	9	43.67
State 3	25, 26, 41, 20, 29, 31, 60, 66, 48, 57, 51	11	41.27
State 4	8.5, 2, 7, 1, 12, 10, 8.5, 4, 5, 6, 11, 3	12	6.5
State 5	18, 23, 30, 32, 61, 35, 50, 64, 19, 36, 39	11	37

Figure 8. KS test for state data

We ran a Kruskal-Wallis permutation test on each data set. The p-value for the state test data was 1.573e-05. Using the Bonferroni adjustment we would need a p-value of 0.003333333 in order to reject the null hypothesis. For the internal data we found a p-value of 0.1092, while we would need a p-value of 0.005 in order to reject the null hypothesis.

To interpret the results from these tests we decide whether or not we were able to reject the null hypothesis ( $H_0$ =all treatments are equal). For the state data we rejected the null

hypothesis since the p-value was less than 0.00333333. In this case we can conclude that at least one of the treatments is not equal to the other treatments. The test does not tell us which one, however, from the previous graphs it would appear state 4 did not perform as well as the others. For the internal data we are unable to reject the null hypothesis. We can conclude that each treatment is equal to each other.

In conclusion we can say that your assumption is correct in that there is a difference between states. Judging from the summary statistics and the permutation test results we can say that at least one other state is not performing the same as the others. Your state seems to be performing as well as the other 4 states. Regarding possible discrepancies in the *We Come to You* training program we can't say that there is a difference between the groups. It does not appear to make a difference how much time the instructors spent with clients; all test results are similar.

Code is attached.

Software: R, RStudio

Works Cited:

Higgins, James J. *Introduction to Modern Nonparametric Statistics*. Belmont: Brooks/Cole Cengage Learning. 2004.