

Decision Boundary

In order to get our discrete 0 or 1 classification, we can translate the output of the hypothesis function as follows:

$$h_{ heta}(x) \geq 0.5
ightarrow y = 1 \ h_{ heta}(x) < 0.5
ightarrow y = 0$$

The way our logistic function g behaves is that when its input is greater than or equal to zero, its output is greater than or equal to 0.5:

$$g(z) \ge 0.5$$
 when $z \ge 0$

Remember.

$$egin{aligned} z=0,e^0&=1\Rightarrow g(z)=1/2\ z o\infty,e^{-\infty}&\to0\Rightarrow g(z)=1\ z o-\infty,e^{\infty}&\to\infty\Rightarrow g(z)=0 \end{aligned}$$

So if our input to g is $\theta^T X$, then that means:

$$h_{ heta}(x) = g(heta^T x) \geq 0.5 \ when \ heta^T x \geq 0$$

From these statements we can now say:

$$egin{aligned} heta^T x &\geq 0 \Rightarrow y = 1 \ heta^T x &< 0 \Rightarrow y = 0 \end{aligned}$$

The **decision boundary** is the line that separates the area where y = 0 and where y = 1. It is created by our hypothesis function.

Example:



$$heta = egin{bmatrix} 5 \ -1 \ 0 \end{bmatrix} \ y = 1 \ if \ 5 + (-1)x_1 + 0x_2 \geq 0 \ 5 - x_1 \geq 0 \ -x_1 \geq -5 \end{bmatrix}$$