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Header

```
typedef uint8_t u8;
typedef uint16_t u16;
typedef uint32_t u32;
typedef uint64_t u64;

typedef int8_t i8;
typedef int16_t i16;
typedef int32_t i32;
typedef int64_t i64;

typedef float f32;
typedef double f64;
typedef long double f80;

#define pb push_back
#define pf push_front
#define snd second
```

Mathematics

Number theory

Given a, b, finds $g = \gcd(a, b)$ and u, v such that ua + vb = g $\mathit{Time} : \mathcal{O}(\log ab)$

```
#include "../header.h"

array<i64, 3> extended_euclid(i64 a, i64 b) {
   if (b == 0)
     return {a, 1, 0};
   auto [g, x, y] = extended_euclid(b, a % b);
   return {g, y, x - y * (a / b)};
}
```

Finds $x^{-1} \mod m$ in $\mathcal{O}(\log m)$.

```
9  optional<i64> inv(i64 x, i64 m) {
10    auto [g, y, _] = extended_euclid(x, m);
11    if (g != 1)
12     return {};
13    return (y >= 0 ? y % m : m - (-y) % m);
14  }
```

Modular integers

Implements operations over the integers under a modulus. *Time*: $\mathcal{O}(1)$ for +, - and *. *Time*: $\mathcal{O}(\log \mod)$ for / (only if mod is prime)

```
#include "../header.h"
3 template<int mod = MOD> struct mint {
     i64 x;
5
     mint inv() { // only prime mod
6
       mint i = 1, b = x;
8
       for (int e = mod - 2; e; e >>= 1) {
9
      if (e & 1) i *= b;
10
         b *= b;
       }
12
       return i;
     }
14
     mint operator+(mint o) {
      return (x + o.x) % mod;
16
17
18
     mint operator+=(mint o) {
       (x += o.x) \% = mod;
20
       return *this;
     mint operator-(mint o) {
       return (x - o.x + mod) % mod;
24
     mint operator -= (mint o) {
       (x += mod - o.x) \% = mod;
       return *this;
28
    }
29
     mint operator*(mint o) {
30
       return x * o.x % mod;
    }
     mint& operator*=(mint o) {
      (x *= o.x) %= mod;
34
       return *this;
35
36
     mint operator/(mint o) { // only prime mod
37
       return x * o.inv().x % mod;
```

```
38     }
39     mint& operator/=(mint o) { // only prime mod
40         (x *= o.inv().x) %= mod;
41         return *this;
42     }
43     mint(i64 x) : x(x % mod) { }
44     mint() : x(0) { }
45     };
```

Combinatorics

Computes $b^0, ..., b^{\text{maxn}}$ modulo mod. *Time*: $\mathcal{O}(\text{maxn})$.

```
#include "../header.h"
#include "../math/modular_int.cpp"

template<i64 mod = MOD>
vector<mint<mod>> get_pows(i64 b, int maxn) {
vector<mint<mod>> pows(maxn + 1, 1);
for (int i = 1; i <= maxn; i++)
    pows[i] = pows[i - 1] * b;
return pows;
}</pre>
```

Computes $0!, ..., \max!$ and $(0!)^{-1}, ..., (\max!)$ modulo mod. *Time*: $\mathcal{O}(\max)$.

```
11  array<vector<mint<mod>> , 2> get_fact(int maxn) {
12    vector<mint<mod>> f(maxn + 1, 1), i(maxn + 1);
13
14    for (int j = 1; j <= maxn; j++)
15        f[j] = f[j - 1] * j;
16    i[maxn] = f[maxn].inv();
17    for (int j = maxn - 1; j >= 0; j--)
18        i[j] = i[j + 1] * (j + 1);
19    return {f, i};
20 }
```

Computes $\binom{n}{\mathrm{ks}_0,\dots}$. The last element of ks can be omitted and it will be assumed to be $n-\sum \mathrm{ks}_i$. Time: $\mathcal{O}(1)$.

```
21  template<i64 mod = MOD>
22  mint<mod> multinom(i64 n, vector<i64> ks) {
23   mint ans = fact[n];
24  for (auto k: ks) {
25   if (k < 0)
26   return 0;</pre>
```

Computes the n-th catalan number. *Time*: $\mathcal{O}(1)$

Counts the possible completions of a bracket sequence where only n ' (' and m ') ' are left to be placed. Time: $\mathcal{O}(1)$

Permutations

Implements swaps in a permutation mantaining the inverse. Time: $\mathcal{O}(N)$ construction and $\mathcal{O}(1)$ query.

```
struct Perm {
     int n;
     vector<int> perm, pos of; // perm and inverse
     void swap(int i, int j) { // perm_i <-> perm_j
       ::swap(perm[i], perm[j]);
       ::swap(pos_of[perm[i]], pos_of[perm[j]]);
8
9
     void invert() { ::swap(perm, pos of); }
10
12
     Perm(int n) : n(n) {
13
       iota(perm.begin(), perm.end(), 0);
14
       iota(pos of.begin(), pos of.end(), 0);
15
     }
16
     Perm(const vector<int> &p) :
```

Dihedral group

Implements operations over D_n in $\mathcal{O}(1)$.

```
#include "../header.h"
   struct Dihedral {
     i64 n. rot:
     bool flip;
6
     Dihedral inv() const {
       if (flip) return *this;
       return {n, (n - rot) % n, false};
10
     }
     Dihedral operator*(Dihedral o) const {
13
      if (flip) {
14
         o.flip ^= true;
         o.rot = (n - o.rot) % n;
16
       o.rot = (o.rot + rot) % n;
18
       return o;
19
     }
20
     Dihedral(i64 n, i64 rot, bool flip) :
       n(n), rot(rot), flip(flip) { }
     Dihedral(i64 n) : Dihedral(n, 0, false) { }
24 };
```

String algorithms

Z-function

Builds the Z function of a string. Time: $\mathcal{O}(N)$ where N is the length of the string.

```
template<typename T>
temp
```

```
for(int i = 1; i < n; i++) {
    if (i < r) z[i] = min(r - i, z[i - l]);
    while (
        i + z[i] < n && s[z[i]] == s[i + z[i]]
        ) z[i]++;
    if(i + z[i] > r) l = i, r = i + z[i];
}
return z;
}
```

Aho-Corasick

Builds the Aho-Corasick automaton.

Time: $\mathcal{O}(N)$ where N is the total length of the strings. *Memory*: $\mathcal{O}(\Sigma N)$ where Σ is the size of the alphabet.

```
template<int K = 26> class AhoCorasick {
      struct Node {
        Node* tr[K];
                           // transitions
        Node* suff:
                           // dictionary suffix
        vector<Node*> adj; // incoming dict suffixes
        Node() : suff(nullptr) {
          fill(tr, tr + K, nullptr);
8
9
       }
10
     };
12
      Node* root;
      vector<Node*> dict;
14
      Node* insert(const string &s) {
16
        Node* curr = root;
        for (auto c: s) {
18
          if (!curr->tr[c - 'a'])
19
            curr->tr[c - 'a'] = new Node;
20
          curr = curr->tr[c - 'a'];
       }
23
        return curr;
24
25
26
      void get suffixes() {
        queue<Node*> q;
28
29
        for (int i = 0; i < K; i++) {
30
          if (root->tr[i]) {
31
            root->tr[i]->suff = root;
32
            root->adj.push back(root->tr[i]);
            q.push(root->tr[i]);
33
34
          } else {
35
            root->tr[i] = root;
36
```

```
37
       }
38
       while (!q.empty()) {
39
         Node* curr = q.front(); q.pop();
40
41
         for (int i = 0; i < K; i++) {
42
           if (curr->tr[i]) {
43
             curr->tr[i]->suff = curr->suff->tr[i];
44
             curr->tr[i]->suff->adj
45
               .push_back(curr->tr[i]);
46
             q.push(curr->tr[i]);
47
           } else {
48
             curr->tr[i] = curr->suff->tr[i];
49
50
           }
51
52
       }
     }
54
55
   public:
56
     AhoCorasick(const vector<string> &words) {
57
58
       root = new Node;
       for (auto &word: words) {
59
         dict.push_back(insert(word));
60
61
       }
       get_suffixes();
62
63 }
64 };
```