

Assignment 3 – Solutions: Part 2 (STAR — High School Graduation)

Applied Quantitative Methods II, UC3M

1. Data preparation

a) Load and create factor variables:

```
library(dplyr)
library(broom)
library(ggplot2)
library(modelsummary)
library(marginaleffects)

star = read.csv("https://raw.githubusercontent.com/franvillamil/AQM2/refs/heads/master/datasets/star/star.csv")

star$classtype = factor(star$classtype,
  levels = 1:3,
  labels = c("Small", "Regular", "Regular+Aide"))

star$race = factor(star$race,
  levels = 1:6,
  labels = c("White", "Black", "Asian", "Hispanic",
    "Native American", "Other"))
```

b) Create binary small indicator:

```
star$small = ifelse(star$classtype == "Small", 1, 0)
```

c) Drop observations with missing hsgrad:

```
df = star %>% filter(!is.na(hsgrad))
nrow(df)
```

```
## [1] 3047
```

d) Graduation rate overall and by class type:

```
mean(df$hsgrad)
```

```
## [1] 0.8332786
```

```
df %>%
  group_by(classtype) %>%
  summarise(grad_rate = mean(hsgrad), n = n())
```

```
## # A tibble: 3 x 3
##   classtype   grad_rate     n
##   <fct>       <dbl> <int>
## 1 Small         0.836   902
## 2 Regular       0.825  1081
## 3 Regular+Aide  0.839  1064
```

Students in small classes have a slightly higher graduation rate than those in regular or regular+aide classes.

2. LPM and logit

a) LPM:

```
lpm1 = lm(hsgrad ~ small, data = df)
tidy(lpm1)
```

```
## # A tibble: 2 x 5
##   term          estimate std.error statistic p.value
##   <chr>         <dbl>    <dbl>    <dbl>   <dbl>
## 1 (Intercept)  0.832     0.00805   103.     0
## 2 small        0.00375   0.0148     0.254   0.800
```

b) Logit:

```
logit1 = glm(hsgrad ~ small, family = binomial, data = df)
tidy(logit1)
```

```
## # A tibble: 2 x 5
##   term          estimate std.error statistic  p.value
##   <chr>         <dbl>    <dbl>    <dbl>   <dbl>
## 1 (Intercept)  1.60     0.0578    27.7  4.92e-169
## 2 small        0.0271   0.107     0.254  8.00e- 1
```

c) The LPM coefficient on `small` is the estimated difference in graduation probability between small and non-small classes. Because this is experimental data, it has a causal interpretation.

d) AME from logit:

```
avg_slopes(logit1)
```

```
##
##   Term          Contrast Estimate Std. Error    z Pr(>|z|)    S  2.5 % 97.5 %
## small mean(1) - mean(0)  0.00375    0.0147  0.255    0.799 0.3 -0.0251 0.0326
##
## Columns: term, contrast, estimate, std.error, statistic, p.value, s.value, conf.low, conf.high, predict
## Type: response
```

The AME is very close to the LPM coefficient, as expected when the outcome probability is moderate (around 0.8).

3. Adding controls

a) Controlled models:

```
lpm2 = lm(hsgrad ~ small + race + yearssmall, data = df)
logit2 = glm(hsgrad ~ small + race + yearssmall,
             family = binomial, data = df)
```

b) Compare bivariate and controlled coefficients on small:

```
tidy(lpm1) %>% filter(term == "small") %>% select(term, estimate)
```

```
## # A tibble: 1 x 2
##   term estimate
##   <chr>      <dbl>
## 1 small  0.00375
```

```
tidy(lpm2) %>% filter(term == "small") %>% select(term, estimate)
```

```
## # A tibble: 1 x 2
##   term estimate
##   <chr>      <dbl>
## 1 small -0.0756
```

The coefficient on small changes little when controls are added. This is consistent with successful randomization: because treatment was randomly assigned, covariates are balanced across groups and do not confound the treatment effect.

c) Interpret yearssmall from the logit:

```
tidy(logit2)
```

```
## # A tibble: 7 x 5
##   term          estimate std.error statistic  p.value
##   <chr>          <dbl>    <dbl>    <dbl>    <dbl>
## 1 (Intercept)    1.83     0.0712   25.6  4.97e-145
## 2 small         -0.562    0.189   -2.98  2.91e- 3
## 3 raceBlack      -0.834    0.102   -8.20  2.32e- 16
## 4 raceAsian      -0.192    1.10    -0.175 8.61e- 1
## 5 raceNative American 11.7    535.     0.0219 9.83e- 1
## 6 raceOther       11.9    377.     0.0316 9.75e- 1
## 7 yearssmall      0.210    0.0572   3.66  2.48e- 4
```

```
avg_slopes(logit2, variables = "yearssmall")
```

```
##
##      Term      Contrast Estimate Std. Error    z Pr(>|z|)    S  2.5 % 97.5 %
## yearssmall mean(dY/dX)  0.0283    0.0077  3.67  <0.001 12.0 0.0132 0.0434
##
## Columns: term, contrast, estimate, std.error, statistic, p.value, s.value, conf.low, conf.high, predict
## Type: response
```

The coefficient on yearssmall captures the cumulative effect of each additional year in a small class on the probability of graduating. The AME converts the log-odds coefficient to a probability scale.

4. Predicted probabilities

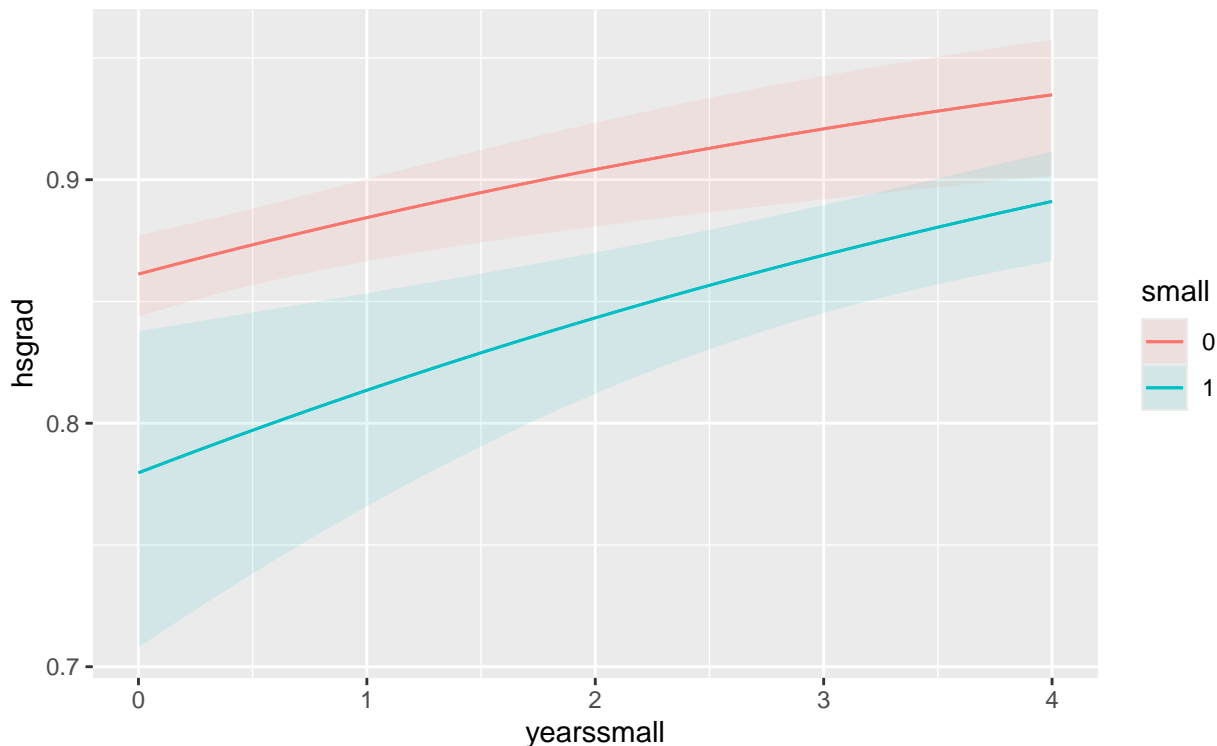
a) Predicted probabilities for specific profiles:

```
predictions(logit2,
  newdata = datagrid(
    small = c(1, 0),
    race = c("White", "Black"),
    yearssmall = c(3, 0)))
```

```
##
##   small  race yearssmall Estimate Pr(>|z|)      S 2.5 % 97.5 %
##     1 White         3    0.869   <0.001 266.0 0.845  0.890
##     1 White         0    0.780   <0.001  34.0 0.708  0.838
##     1 Black         3    0.742   <0.001  68.6 0.698  0.782
##     1 Black         0    0.606   0.0312   5.0 0.510  0.694
##     0 White         3    0.921   <0.001 145.8 0.892  0.943
##     0 White         0    0.861   <0.001 479.4 0.844  0.877
##     0 Black         3    0.835   <0.001  60.7 0.780  0.878
##     0 Black         0    0.729   <0.001  98.6 0.695  0.762
##
## Columns: rowid, estimate, p.value, s.value, conf.low, conf.high, small, race, yearssmall, hsgrad
## Type:   invlink(link)
```

b) Plot across yearssmall by small:

```
p1 = plot_predictions(logit2, condition = c("yearssmall", "small"))
p1
```



```
ggsave("pred_prob_yearssmall.png", p1, width = 6, height = 4)
```

5. Interactions

a) Interaction model:

```
logit3 = glm(hsgrad ~ small * race + yearssmall,
             family = binomial, data = df)
```

b) Marginal effect of small by race:

```
avg_slopes(logit3, variables = "small", by = "race")
```

```
##
##   Term                Contrast      race   Estimate Std. Error      z
## small mean(1) - mean(0) White      -0.076464381    0.029265 -2.612799
## small mean(1) - mean(0) Black      -0.102992190    0.047833 -2.153167
## small mean(1) - mean(0) Asian       0.222953892    0.197711  1.127673
## small mean(1) - mean(0) Native American -0.000001064    0.000570 -0.001868
## small mean(1) - mean(0) Other      -0.000000273    0.000987 -0.000277
## Pr(>|z|)   S    2.5 %   97.5 %
## 0.00898 6.8 -0.13382 -0.01911
## 0.03131 5.0 -0.19674 -0.00924
## 0.25946 1.9 -0.16455  0.61046
## 0.99851 0.0 -0.00112  0.00112
## 0.99978 0.0 -0.00193  0.00193
##
## Columns: term, contrast, race, estimate, std.error, statistic, p.value, s.value, conf.low, conf.high, p
## Type: response
```

c) The small class effect differs somewhat across racial groups. Some groups show a larger benefit from small classes, though confidence intervals are wide for groups with fewer observations (Asian, Hispanic, Native American). The interaction results suggest that the benefits of small classes may not be uniform across all student populations.

6. Presenting results and discussion

a) Comparison table:

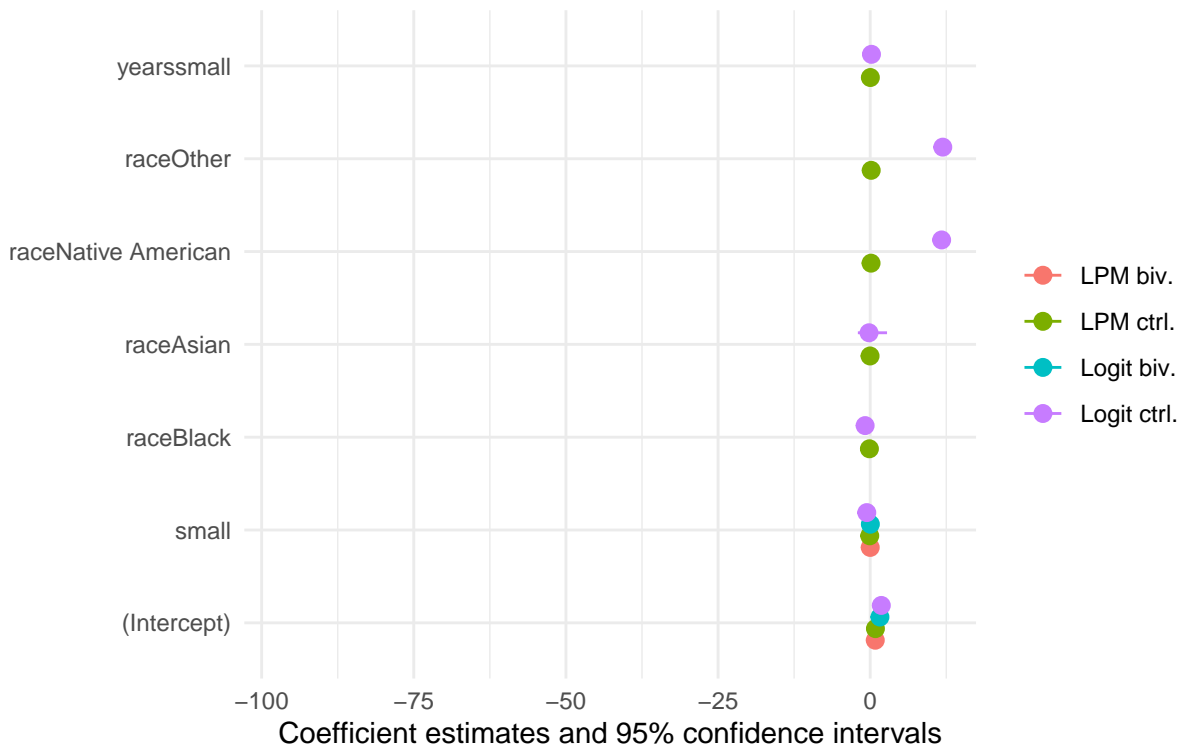
```
modelsummary(
  list("LPM biv." = lpm1, "LPM ctrl." = lpm2,
       "Logit biv." = logit1, "Logit ctrl." = logit2),
  vcov = list("robust", "robust", NULL, NULL),
  output = "markdown")
```

b) Coefficient plot:

```
p2 = modelplot(
  list("LPM biv." = lpm1, "LPM ctrl." = lpm2,
       "Logit biv." = logit1, "Logit ctrl." = logit2),
```

	LPM biv.	LPM ctrl.	Logit biv.	Logit ctrl.
(Intercept)	0.832 (0.008)	0.860 (0.009)	1.601 (0.058)	1.826 (0.071)
small	0.004 (0.015)	-0.076 (0.026)	0.027 (0.107)	-0.562 (0.189)
raceBlack		-0.127 (0.015)		-0.834 (0.102)
raceAsian		-0.024 (0.150)		-0.192 (1.100)
raceNative American		0.140 (0.368)		11.741 (535.411)
raceOther		0.165 (0.260)		11.926 (377.410)
yearssmall		0.027 (0.007)		0.210 (0.057)
Num.Obs.	3047	3047	3047	3047
R2	0.000	0.028		
R2 Adj.	-0.000	0.026		
AIC	2638.7	2563.0	2750.2	2679.4
BIC	2656.8	2611.2	2762.2	2721.5
Log.Lik.	-1316.361	-1273.489	-1373.096	-1332.681
F	0.065		0.064	13.460
RMSE	0.37	0.37	0.37	0.37
Std.Errors	HC3	HC3		

```
vcov = list("robust", "robust", NULL, NULL))
p2
```



```
ggsave("coefplot_star.png", p2, width = 6, height = 4)
```

c) The STAR data provide experimental evidence that small class sizes have a positive effect on high school graduation. The estimated effect is modest but consistent across specifications. The LPM and logit results are very similar, both in magnitude and significance, which is expected when the outcome probability is not extreme. This similarity confirms that functional form assumptions make little practical difference here. The experimental design gives this evidence more credibility than observational studies, where class size correlates with school resources, neighborhood characteristics, and student composition. Random assignment eliminates these confounders by design, allowing a causal interpretation of the treatment effect. The stability of the small-class coefficient when controls are added further supports successful randomization.