## 1 Impact of $d, g, \theta, \mu$ on Cross Correlation of Quantities

## 1.1 Cross correlation within a market side

Figure 1 shows the effect of the sum of the indirect network effects d and g (INE) and the substitution parameter  $\mu$  (which is equal to  $\theta$ ) on the correlation of quantites  $q_i, q_j$  on market side a. A high degree of homogeneity causes the negative correlation to increase, which is consistent with what we expected from theory. Homogeneous products cause higher degree of competition which leads to a higher negative correlation of quantities (see also Figure 7). What is new is the effect of INE on the correlation: The higher the absolute amount of INE, the higher the negative correlation.

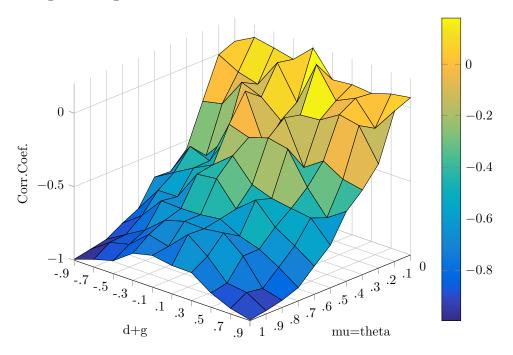


Figure 1: Cross Correlations QQ

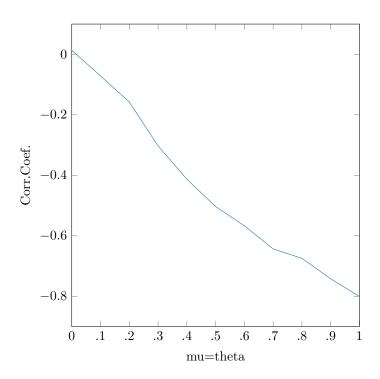


Figure 2: Cross Correlations QQ for d=g=0  $\,$ 

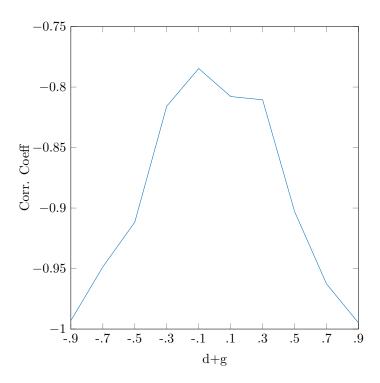


Figure 3: Cross Correlations QQ for  $\mu=1$ 

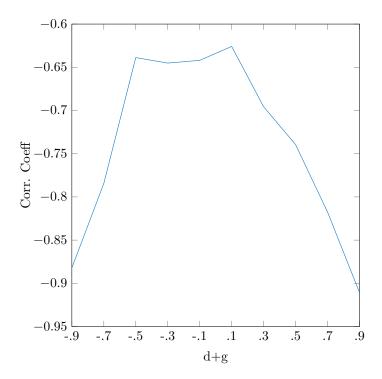


Figure 4: Cross Correlations QQ for  $\mu=0.7$ 

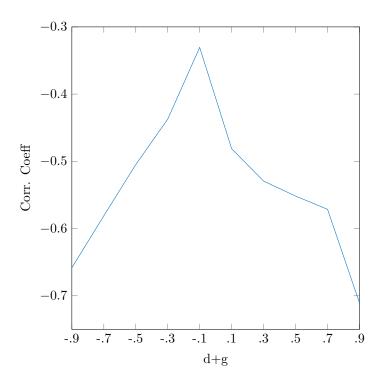


Figure 5: Cross Correlations QQ for  $\mu=0.5$ 

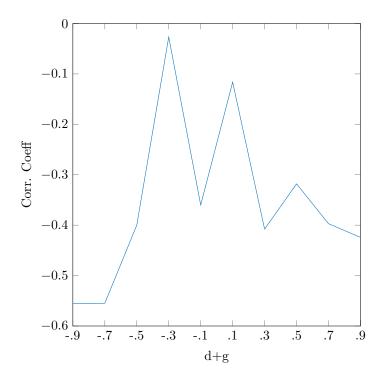


Figure 6: Cross Correlations QQ for  $\mu=0.3$ 

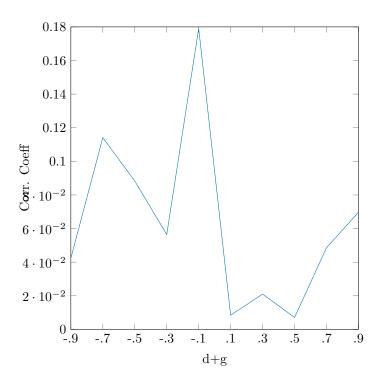


Figure 7: Cross Correlations QQ for  $\mu=0$ 

## 1.2 Crosscorrelation between market sides

Figure 8 shows the correlation between the quantities  $q_i$  and  $s_i$  of platform i on market side a and b. The substitution parameters  $\mu$  and  $\theta$  nearly have no impact on the correlation (see also Figure 9 <sup>1</sup>), while the sum of the INE has an important effect on the correlation. Different to Figure 1, we can see a difference between the sign of the sum of INE: If the sum has a negative sing, correlation gets negative. A quantity increase on one market side - say b - causes a decrease on market side a. One can think of a real world example as a TV-Program. If the negative impact (g) of advertisement (side b) on viewers (side a) is much larger than the positive effect of viewers on advertiser (d) so that d+g<0, negative correlations of quantities might be possible.

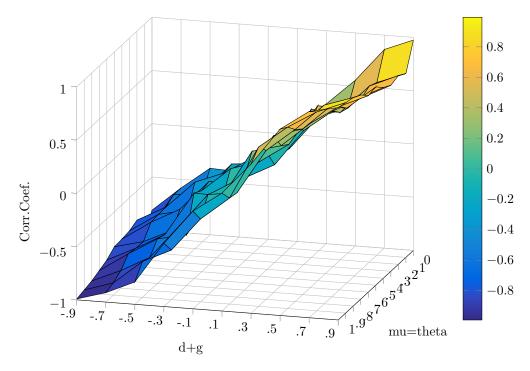


Figure 8: Cross Correlations QS

 $<sup>^1</sup>$ A change in the substitution parameters does not seem to have any impact on the cross correlation coefficient. The variation of the cross correlation goes from -0.04 to 0.04.

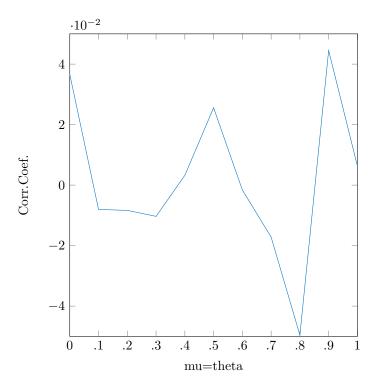


Figure 9: Cross Correlations QS for d=g=0  $\,$