#### **Heat Equation**

Francesco Pasa Enrico Panontin

Heat Equation

Our Code

Performances

OpenGL-CUDA interoperability

# Heat Equation

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We consider heat propagation in a medium (e.g. a solid) far away from any state transition and we define:

 $\epsilon$ : internal energy density

c: specific heat

ho: mass density

T: temperature

By virtue of the first thermodinamic principle  $(\Delta U = \Delta Q - L = \Delta Q)$ :

$$d\left[\int_{\Omega} c\rho T \, dV\right] = \left[-\int_{\partial\Omega} \vec{J} \cdot \vec{n} \, dS\right] dt \tag{1}$$

$$d\left[\int_{\Omega} c\rho T \, dV\right] = \left[-\int_{\partial\Omega} \vec{J} \cdot \vec{n} \, dS\right] dt$$

*Newton-Fourier Law*, heat spreads and temperature becomes uniform throughout the medium:

$$\vec{J} = -k\vec{\nabla}T\tag{2}$$

By substituting equation (2) in (1) and applying the *divergence theorem* one gets the **heat equation**:

$$\frac{\partial T}{\partial t} - \frac{k}{c\rho} \Delta T = 0 \tag{3}$$

- $\frac{\partial T}{\partial t} \frac{k}{c\rho} \Delta T = f(\vec{x}, t)$
- First order in time
- Second order in space
- ▶ If we consider a heating system, we must add  $f(\vec{x}, t)$

$$\frac{\partial T}{\partial t} - \frac{k}{c\rho} \Delta T = f(\vec{x}, t)$$

Discretize space and time: foreward difference for time, central difference for space:

$$T_{i,j}^{n+1} = T_{i,j}^{n} + \eta \left[ T_{i+1,j}^{n} + T_{i-1,j}^{n} + T_{i,j+1}^{n} + T_{i,j-1}^{n} - 4T_{i,j}^{n} \right]$$
 (4)

where n is the time index, i,j are x-index and y-index,  $\eta = \frac{k\Delta t}{c\rho(\Delta x)^2}$ .

## **General Structure**

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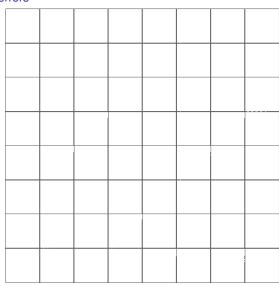
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# **Shared Memory**

#### Random errors



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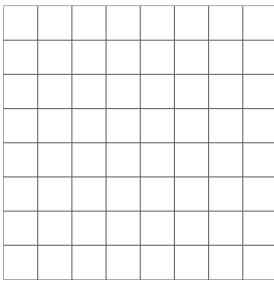
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# **Shared Memory**

Synchronized threads



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# Performances GPU

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descrizione della gpu usata (numero blocchi e thread eccecc)

Execution time vs blocks number

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Execution time vs loops number

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Execution time GPU vs CPU

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Different GPUs

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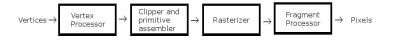
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OpenGL is a graphics API (similar in scope to Direct3D) that allows to use the graphics card to draw 2D and 3D vector graphics.

- 1992 OpenGL is first released
- 2004 OpenGL 2.0 is released. Adds support for programmable pipeline (shaders).
- 2010 OpenGL 4.0 is released. Adds support for geometry shader (tesselation).



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```
glColor3f(1.0f, 0.0f, 0.0f);
glBegin(GL_QUADS);
    glVertex2f(-0.25f, 0.25f);
    glVertex2f(-0.5f, -0.25f);
    glVertex2f(0.5f, -0.25f);
    glVertex2f(0.25f, 0.25f);
glVertex2f(0.25f, 0.25f);
```

Moreover the API had to support many features, for example textures coordinates, lighting, shadows, coordinate transformation and perspective matrices.

This results in a complex API and lack of flexibility.

# Modern approach

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```
Since the rendering of the 3D scene is a very complex task, OpenGL uses the concept of state machine to simplify the API interface (avoid function with too many arguments).
```

```
// Tell OpenGL which array contains the data
glBindBuffer(GL_ARRAY_BUFFER, vbo);
// Specify how the data for position can be accessed
glVertexAttribPointer(0, size, GL_FLOAT, GL_FALSE, 0, 0);
// Enable the attribute
glEnableVertexAttribArray(0); // location = 0
// Draw
glDrawArrays(type, 0, vertex_num);
```

# OpenGL VBOs

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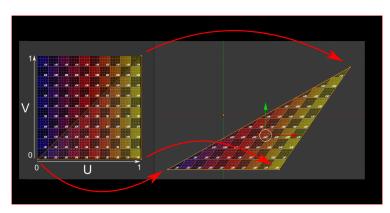
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VBO (Vertex Buffer Object) - is an array of data in the GPU memory for storing vertices.

# **OpenGL Textures**

Texture - is an image that is mapped to vertices.



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