Heat Equation

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Heat Equation

Our Oodo

OpenCL CLIDA

OpenGL-CUDA interoperability

Heat Equation

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Our Code

Performances

OpenGL-CUDA interoperability

Heat Equation

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OpenGL-CUDA interoperability

We consider heat propagation in a medium (e.g. a solid) far away from any state transition and we define:

 ϵ : internal energy density

c: specific heat

ho: mass density

T: temperature

By virtue of the first thermodinamic principle $(\Delta U = \Delta Q - L = \Delta Q)$:

$$d\left[\int_{\Omega} c\rho T \, dV\right] = \left[-\int_{\partial\Omega} \vec{J} \cdot \vec{n} \, dS\right] dt \tag{1}$$

$$d\left[\int_{\Omega} c\rho T \, dV\right] = \left[-\int_{\partial\Omega} \vec{J} \cdot \vec{n} \, dS\right] dt$$

Newton-Fourier Law, heat spreads and temperature becomes uniform throughout the medium:

$$\vec{J} = -k\vec{\nabla}T\tag{2}$$

By substituting equation (2) in (1) and applying the *divergence theorem* one gets the **heat equation**:

$$\frac{\partial T}{\partial t} - \frac{k}{c\rho} \Delta T = 0 \tag{3}$$

OpenGL-CLIDA

- $\frac{\partial T}{\partial t} \frac{k}{c\rho} \Delta T = f(\vec{x}, t)$
- First order in time
- Second order in space
- ▶ If we consider a heating system, we must add $f(\vec{x}, t)$

$$\frac{\partial T}{\partial t} - \frac{k}{c\rho} \Delta T = f(\vec{x}, t)$$

Discretize space and time: foreward difference for time, central difference for space:

$$T_{i,j}^{n+1} = T_{i,j}^{n} + \eta \left[T_{i+1,j}^{n} + T_{i-1,j}^{n} + T_{i,j+1}^{n} + T_{i,j-1}^{n} - 4T_{i,j}^{n} \right]$$
 (4)

where n is the time index, i,j are x-index and y-index, $\eta = \frac{k\Delta t}{c\rho(\Delta x)^2}$.

General Structure

sim2d.cu

integrator.h integrator.cu

gl_helper.cu gl_helper.h Heat Equation

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```
Set: number of block, number of threads, other parameters.
```

integrator.cu

```
Heat Equation
```

```
__global__
void stepSimulation2D(float *T, float *K, float *dT,
                        unsigned n_loop, uchar4 *tex,
                        char copy_tex)
device
void loadSharedMemory2D(const UsefulConstants consts,
                        float *T)
device
void integrate2D(const UsefulConstants consts, float *T,
                        float *K, float *dT)
```

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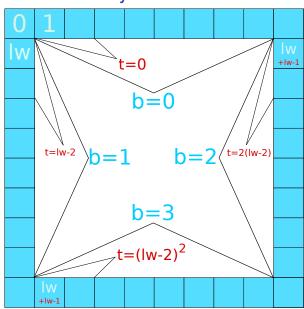
```
Heat Equation
loadSharedMemory2D
```

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```
for (i = 0; i < n_loop; ++i) {</pre>
        local_T[lid_1d + i] = T[gid_1d + i];
        //d_operation[gid_1d+i] = 255;
__syncthreads();
```

loadSharedMemory2D



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integrate2D

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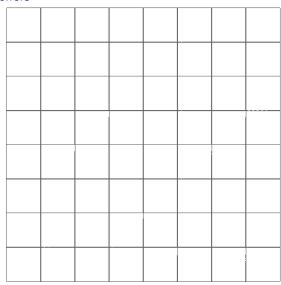
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Shared Memory

Random errors



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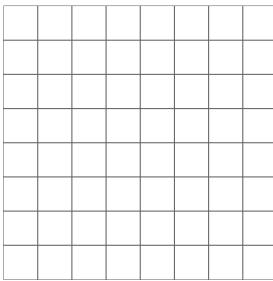
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Shared Memory

Synchronized threads



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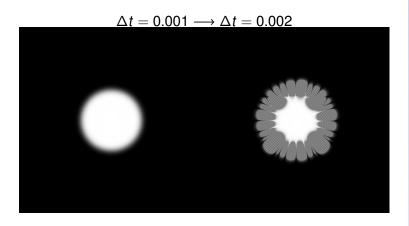
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Performances

Stability



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Heat Equation

Our Code

Performances

Performances GPU

Heat Equation

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Performances

OpenGL-CUDA nteroperability

descrizione della gpu usata (numero blocchi e thread eccecc)

Execution time vs blocks number

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Execution time vs loops number

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Execution time GPU vs CPU

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Different GPUs

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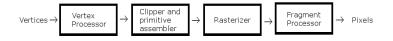
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Performances

OpenGL is a graphics API (similar in scope to Direct3D) that allows to use the graphics card to draw 2D and 3D vector graphics.

- 1992 OpenGL is first released
- 2004 OpenGL 2.0 is released. Adds support for programmable pipeline (shaders).
- 2010 OpenGL 4.0 is released. Adds support for geometry shader (tesselation).



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```
glColor3f(1.0f, 0.0f, 0.0f);
glBegin(GL_QUADS);
    glVertex2f(-0.25f, 0.25f);
    glVertex2f(-0.5f, -0.25f);
    glVertex2f(0.5f, -0.25f);
    glVertex2f(0.25f, 0.25f);
glVertex2f(0.25f, 0.25f);
```

Moreover the API had to support many features, for example textures coordinates, lighting, shadows, coordinate transformation and perspective matrices.

This results in a complex API and lack of flexibility.

Modern approach

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arguments).

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simplify the API interface (avoid function with too many OpenGL-CUDA interoperability

```
// Tell OpenGL which array contains the data
glBindBuffer(GL_ARRAY_BUFFER, vbo);
// Specify how the data for position can be accessed
glVertexAttribPointer(0, size, GL_FLOAT, GL_FALSE, 0, 0);
// Enable the attribute
glEnableVertexAttribArray(0); // location = 0
// Draw
glDrawArrays(type, 0, vertex_num);
```

Since the rendering of the 3D scene is a very complex task. OpenGL uses the concept of state machine to

OpenGL VBOs

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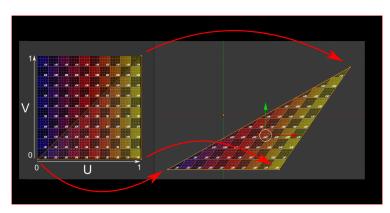
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OpenGL-CUDA interoperability

VBO (Vertex Buffer Object) - is an array of data in the GPU memory for storing vertices.

OpenGL Textures

Texture - is an image that is mapped to vertices.



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