

Longitudinal Data Analysis using Mplus and R

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Personal website

Personal website

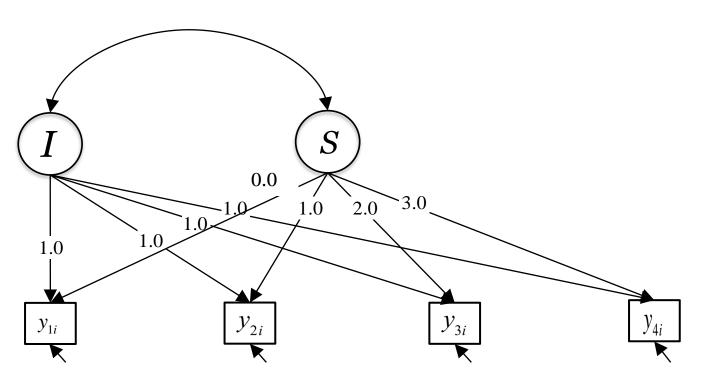
Plan for today

- Objectives of longitudinal research
- Role of time scores/factor loadings in LGCM
- Growth Curve Models
 - No growth, linear and quadratic LGCM
 - Spline/Piecewise/Multiphase LGCM
 - Adding time-invariant and time-varying (dynamical) predictors, and (distal) outcomes
 - Multi-group LGCM and invariance testing
 - Multi (Parallel) process LGCM

- 1. Identification of intraindividual (within-person) changes (and stability)
 - Is there change over time on average?
 - ✓ Growth models can address various linear and nonlinear patterns of intraindividual change
- 2. Analysis of causes (determinants) of intraindividual change
 - What factors/mechanisms time-varying/dynamical predictors drive change?
 - ✓ Inclusion of time-varying (dynamical) predictors in growth models
- Identification of interindividual differences (or similarity) in intraindividual change
 - Do different individuals change in different ways?
 - ✓ Growth models are structured to address interindividual differences in the growth factors
- 4. Analysis of causes (determinants) of interindividual differences in intraindividual change
 - What factors explain between-person differences in change
 - ✓ Inclusion of time-invariant covariates in growth models, multigroup LGCM, Growth mixture models
- Interrelationships in change
 - Does change in one variable related (precede, covary and/or follow) to change in another variable?
 - Correlating slopes of X and Y could provide evidence that one variable is changing in the same people as another variable correlated changes! Or common changes!
 - ✓ Multi (parallel & sequentially contingent) process LGCM

- Identification of interindividual differences (or similarity) in intraindividual change 3.
 - Do different individuals change in different ways?
 - Differences between groups of persons in the way people change
- Analysis of causes (determinants) of interindividual differences in intraindividual change 4.
 - What factors explain between-person differences in change?
 - Inclusion of time-invariant covariates in growth models, multigroup LGCM, Growth mixture models

- Interrelationships in change 5.
 - Does change in one variable relate (precede, covary and/or follow) to change in another variable?
 - Correlating slopes of X and Y could provide evidence that one variable is changing in the same people as another variable correlated changes! Or common changes!
 - ✓ Multi (parallel & sequentially contingent) process LGCM

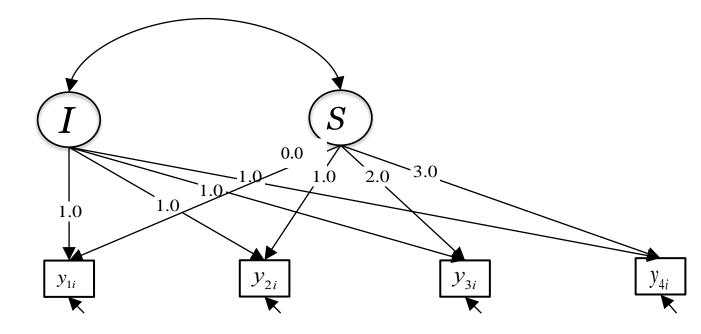


Role of time scores

- Time of observation as factor loading
- Time scores determine
 - 1. Form/shape of growth process
 - 2. Centering point of growth process
 - 3. Scaling of growth factors

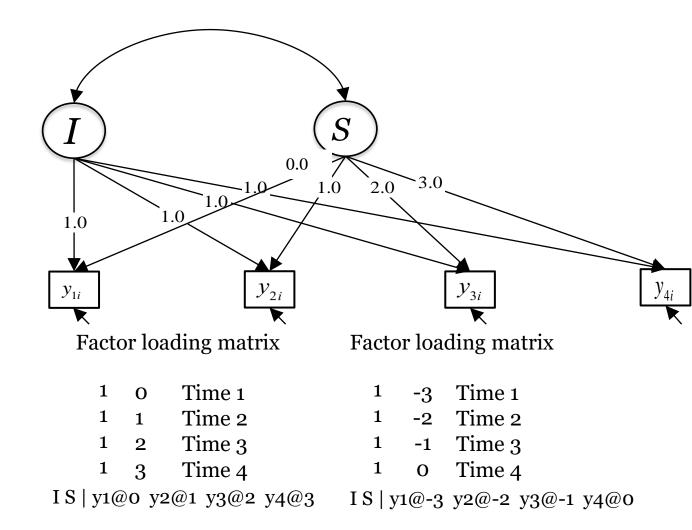
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Role of time scores

- Time of observation as factor loading
- Time scores determine
 - 1. Form/shape of growth process
 - 2. Centering point of growth process
 - 3. Scaling of growth factors



Factor loading matrix											
1 1 1 1	0 1 2 3	Time 1 Time 2 Time 3 Time 4									

```
IS | y1@0 y2@1 y3@2 y4@3 y5@4
```

IS | y1@0 y2@1 y3@3 y4@4 y5@6 [No observations on Months 3 & 6, time scores specified to match observed time points]

IS | y1@-5 y2@-4 y3@-3 y4@-2 y5@-1 y6@0 [End of observation defined as centering point; intercept status; predicted level of y at end of obs.]

Free time score/Unspecified LGCM/Model estimated time score = empirically determines shape of outcome growth

- IS | y1@0 y2* y3* y4@1
- Freely estimated parameters represent the proportion of predicted overall change that occurred up to a specific point in time eg Time 2, for y2*
- The Slope growth factor represents the total amount of change from the first to the last timepoint

IS | v1@0 v2@6 v3@12 v4@18 v5@24 Either one is correct, same model fit indices

Factor loading matrix	Factor loading matrix								
1 0 Time 1 1 1 Time 2 1 2 Time 3 1 3 Time 4	1 1 1 1	0 1 2 3 4	Month 1 Month 6 Month 12 Month 18 Month 24						
$S \mid v_1 @ 0 v_2 @ 1 v_2 @ 2 v_4 @ 2$									

IS | y1@0 y2@1 y3@2 y4@3)

```
I S | y1@0 y2@1 y3@2 y4@3 y5@4
I S | y1@0 y2@6 y3@12 y4@18 y5@24
```

Either one is correct, same model fit indices

IS | y1@0 y2@1 y3@3 y4@4 y5@6 [No observations on Months 3 & 6, time scores specified to match observed time points]

IS | y1@-5 y2@-4 y3@-3 y4@-2 y5@-1 y6@0 [End of observation defined as centering point; intercept status; predicted level of y at end of obs.]

Free time score/Unspecified LGCM/Model estimated time score = empirically determines shape of outcome growth IS | y1@0 y2@1 y3* y4* y5*

- IS | y1@0 y2* y3* y4@1
- Freely estimated parameters represent the proportion of predicted overall change that occurred up to a specific point in time eg Time 2, for y2'
- The Slope growth factor represents the total amount of change from the first to the last timepoint

Factor loading matrix

Factor loading matrix		Factor loading matrix		(unequal time interval)							
1 1 1 1	0 1 2 3	Time 1 Time 2 Time 3 Time 4	1 1 1 1	0 1 2 3 4	Month 1 Month 6 Month 12 Month 18 Month 24	1 1 1 1 1	0 1 2 3 4	Month 1 Month 2 Month 3 Month 4 Month 5 Month 6			
I S y10	@o y2	2@1 y3@2 y4@3)				1	6	Month 7			

15 | y1@0 y2@1 y3@2 y4@3

```
I S | y1@0 y2@1 y3@2 y4@3 y5@4
I S | y1@0 y2@6 y3@12 y4@18 y5@24
```

Either one is correct, same model fit indices

IS | y1@0 y2@1 y3@3 y4@4 y5@6 [No observations on Months 3 & 6, time scores specified to match observed time points]

IS | y1@-5 y2@-4 y3@-3 y4@-2 y5@-1 y6@0 [End of observation defined as centering point; intercept status; predicted level of y at end of obs.]

Free time score/Unspecified LGCM/Model estimated time score = empirically determines shape of outcome growth IS | y1@0 y2@1 y3* y4* y5*

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Factor loading matrix

Factor loading matrix	Factor loading matrix		(unequal time interval)			Factor loading matrix			
1 0 Time 1 1 1 Time 2 1 2 Time 3 1 3 Time 4	1 1 1 1	0 1 2 3 4	Month 1 Month 6 Month 12 Month 18 Month 24	1 1 1 1 1 1	0 1 2 3 4 5	Month 1 Month 2 Month 3 Month 4 Month 5 Month 6 Month 7	1 1 1 1 1	-5 -4 -3 -2 -1 0	Month 1 Month 2 Month 3 Month 4 Month 5 Month 6
IS y1@0 y2@1 y3@2 y4@3)				-	U	MOHUI /			

```
I S | y1@0 y2@1 y3@2 y4@3 y5@4
I S | y1@0 y2@6 y3@12 y4@18 y5@24
```

Either one is correct, same model fit indices

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- Freely estimated parameters represent the proportion of predicted overall change that occurred up to a specific point in time eg Time 2, for y2'
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Easter leading matrix

Factor loading matrix	Factor loading matrix		(unequal time interval)			Factor loading matrix			
1 0 Time 1 1 1 Time 2 1 2 Time 3 1 3 Time 4	1 1 1 1	0 1 2 3 4	Month 1 Month 6 Month 12 Month 18 Month 24	1 1 1 1 1	0 1 2 3 4 5	Month 1 Month 2 Month 3 Month 4 Month 5 Month 6 Month 7	1 1 1 1 1	-5 -4 -3 -2 -1 0	Month 1 Month 2 Month 3 Month 4 Month 5 Month 6
IS y1@0 y2@1 y3@2 y4@3)				1	O	Month 7			

```
I S | y1@0 y2@1 y3@2 y4@3 y5@4
I S | y1@0 y2@6 y3@12 y4@18 y5@24
```

Either one is correct, same model fit indices

IS | y1@0 y2@1 y3@3 y4@4 y5@6 [No observations on Months 3 & 6, time scores specified to match observed time points]

IS | y1@-5 y2@-4 y3@-3 y4@-2 y5@-1 y6@0 [End of observation defined as centering point; intercept status; predicted level of y at end of obs.]

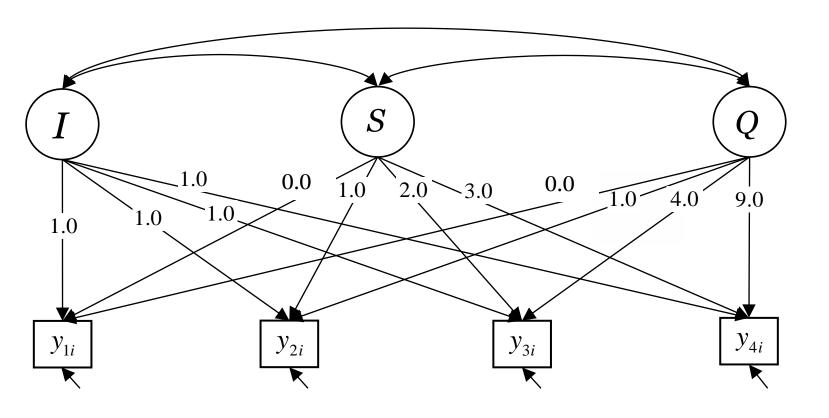
Free time score/Unspecified LGCM/Model estimated time score = empirically determines shape of outcome growth IS | y1@0 y2@1 y3* y4* y5*

Latent basis model/Unstructured growth model

IS | y1@0 y2* y3* y4@1

- Freely estimated parameters represent the proportion of predicted overall change that occurred up to a specific point in time eg Time 2, for y2*
- The Slope growth factor represents the total amount of change from the first to the last timepoints

Non-linear change (e.g., quadratic)



Factor loading matrix

Time 1 Time 2 Time 3 2 Time 4 3

(ISQ| y1@0 y2@1 y3@2 y4@3)

Dataset

Variable Names	Time 1 (2015)	Time 2 (2016)	Time 3 (2018)	Time 4 (2019)	Time 5 (2021)
Id	personid				
Female	female				
Parental drug use	pdu1				
Adverse childhood environment	ace1				
Worry	worry1				
Loneliness	lone1	lone2	lone3	lone4	lone5
Anxiety symptoms	anx1	anx2	anx3	anx4	anx5
Depression symptoms	dep1	dep2	dep3	dep4	dep5
Hostility	host1	host2	host3	host4	host5
Peer conflict					percon5
Peer conflict					percon5b
Substance use					subs5
Substance use					subs5b
Difficulty sleeping					sleep5
Difficulty sleeping					sleep5b

Things to do before fitting growth models to longitudinal data

1. Examine univariate and bivariat

Code

	vars	n	mean	sd	median	trimmed	mad	min	max	range	sl
lone1	1	398	1.46	0.46	1.32	1.38	0.34	1	3.75	2.75	1.
lone2	2	395	1.47	0.52	1.31	1.38	0.31	1	5.00	4.00	2.
lone3	3	390	1.53	0.52	1.36	1.44	0.37	1	3.78	2.78	1.
						1.25					
lone5	5	409	1.32	0.39	1.20	1.24	0.25	1	3.43	2.43	2.

The means and standard deviations show a simple pattern with increases in the feeling of loneliness from T1 through to T3 and begins to decline afterwards though to T5 coupled with increases in variation and then a decline after T3.

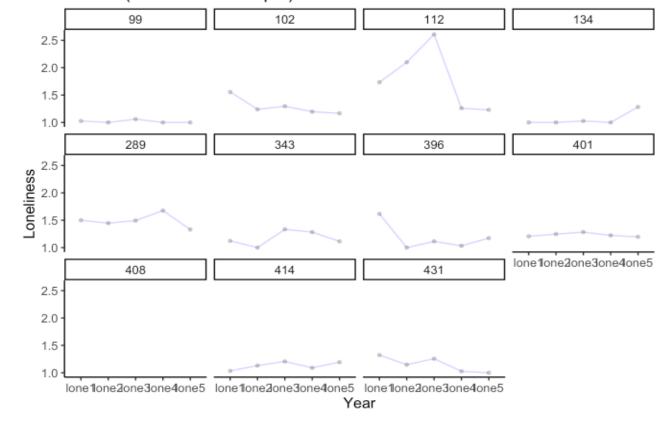
5. Examine separate individual longitudinal plots

▶ Code

Warning: Removed 5 rows containing missing values (`geom_line()`).

Warning: Removed 5 rows containing missing values (`geom_point()`).

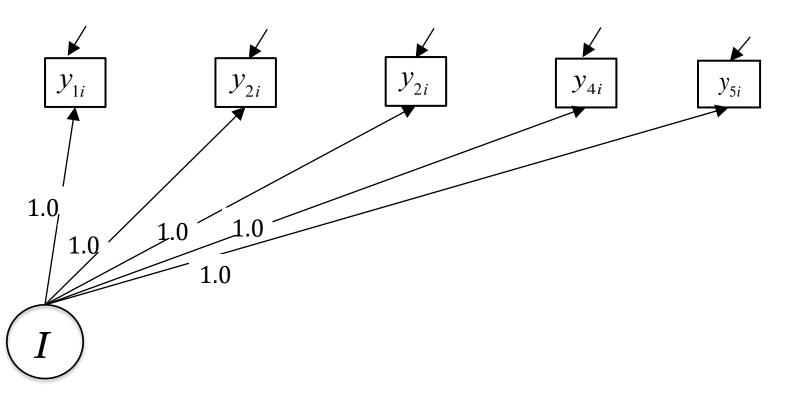
N = 11 (2.5% of the sample)



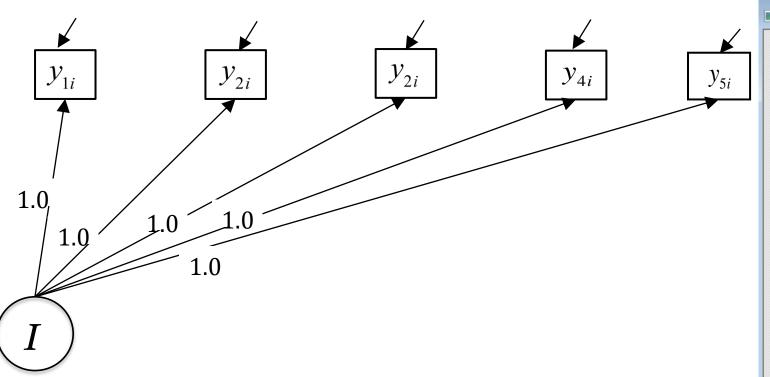
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 - ✓ Growth models can address various linear and nonlinear patterns of intraindividual change
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 - Does change in one variable relate (precede, covary and/or follow) to change in another variable?
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 - ✓ Multi (parallel & sequentially contingent) process LGCM

- What does the overall trajectory of loneliness look like?
 - Is there change over time on average?
 - What growth function characterizes change over time/shape of growth?

No growth/Intercept only model



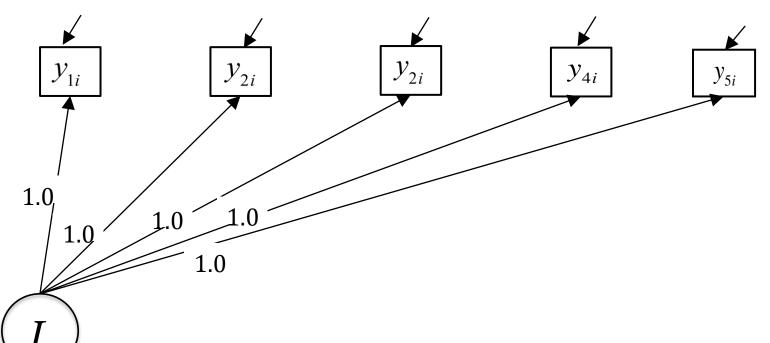
No growth/Intercept only model



```
# 001_No growth model
nogrowth <- ' i =~ 1*lone1 + 1*lone2 + 1*lone3 + 1*lone4 + 1*lone5'
fit_nogrowth <- growth(nogrowth, data = data)
summary(fit_nogrowth, fit.measures = TRUE)</pre>
```

```
001_No_change_No_growth_Intercept_only_model
 TITLE: 001 No change No growth Intercept only model
 DATA:
 FILE IS data.dat;
 LISTWISE = ON;
 VARIABLE:
 NAMES ARE
 id female pdul acel worryl
 lonel lone2 lone3 lone4 lone5
 anx1 anx2 anx3 anx4 anx5
 dep1 dep2 dep3 dep4 dep5
 host1 host2 host3 host4 host5
 percon5 percon5b subs5 subs5b sleep5 sleep5b;
 USEVARIABLES ARE
         lone1 lone2 lone3 lone4 lone5;
 MISSING ARE ALL (-999);
 ANALYSIS:
     ESTIMATOR = ML;
 MODEL:
     Illone1@1 lone2@1 lone3@1 lone4@1 lone5@1;
      !I|lone1-lone5@1;
 OUTPUT:
      SAMPSTAT;
```

No growth/Intercept only model



RESULTS

Model fit:

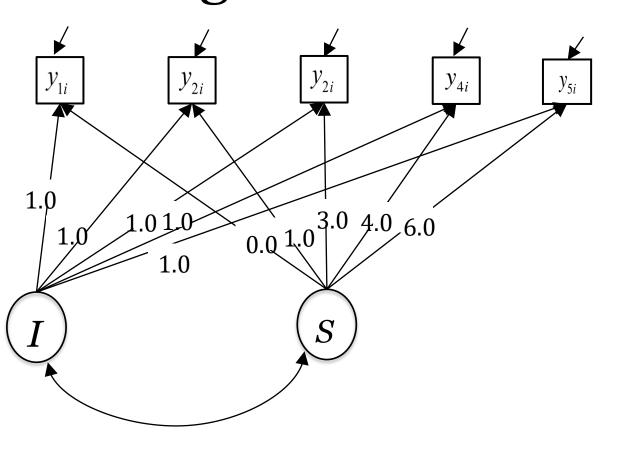
 $(\chi^2 = 186.433, df = 13; p < .001; RMSEA = .204, [90\% CI = 0.179, 0.230]; CFI = .607; TLI = .698)$

Parameter estimates:

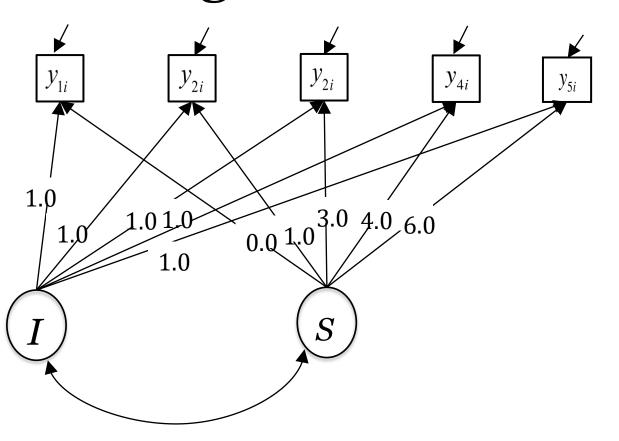
Intercept: 1.398***
Intercept variance: 0.075***

Residual variance: 0.092 - 1.167, all***

Linear growth

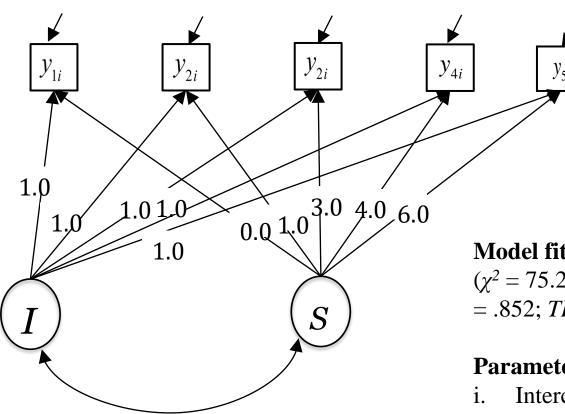


Linear growth



```
002_Linear_growht_curve_model
 FITLE: 002 Linear growht curve model
 DATA:
 FILE IS data.dat;
 LISTWISE = ON;
 VARIABLE:
 NAMES ARE
 id female pdul acel worryl
 lone1 lone2 lone3 lone4 lone5
 anx1 anx2 anx3 anx4 anx5
 dep1 dep2 dep3 dep4 dep5
 host1 host2 host3 host4 host5
 percon5 percon5b subs5 subs5b sleep5 sleep5b;
 USEVARIABLES ARE
        lone1 lone2 lone3 lone4 lone5:
 MISSING ARE ALL (-999);
 ANALYSIS:
     ESTIMATOR = ML;
 MODEL:
     I Sllone100 lone201 lone303 lone404 lone506;
 OUTPUT:
     SAMPSTAT;
 PLOT:
     TYPE = PLOT3;
     SERIES = lone1 - lone5(S);
```

Linear growth



RESULTS

Model fit:

 $(\chi^2 = 75.244, df = 10; p < .001; RMSEA = .143, [90\% CI = 0.113, 0.174]; CFI$ = .852; TLI = .852)

Parameter estimates:

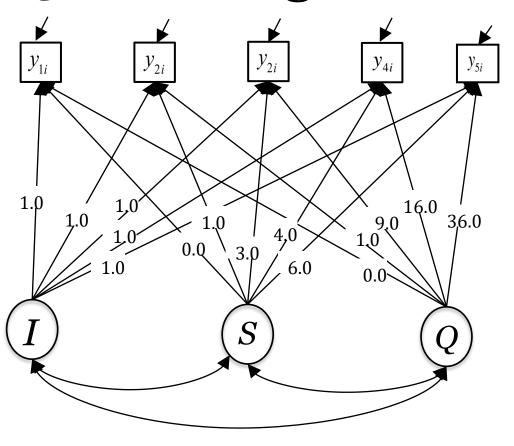
1.466*** Intercept: ii. Slope: -0.025***

(Co) Variances:

0.139*** Intercept: 0.003*** Slope: ii. -0.015*** Intercept WITH Slope:

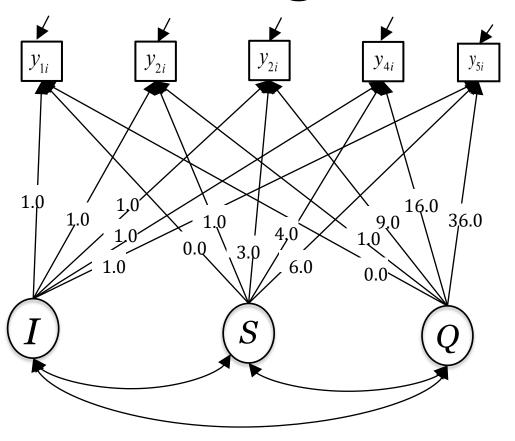
Unconditional Linear LGCM

Quadratic growth



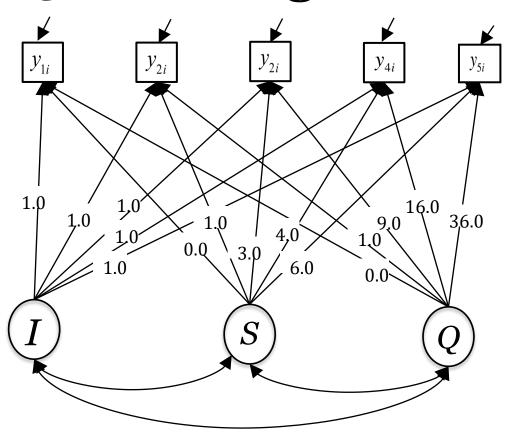
Unconditional Quadratic LGCM

Quadratic growth



```
003_Quadratic_growht_curve_model
 TITLE: 003 Quadratic growht curve model
 DATA:
 FILE IS data.dat;
 LISTWISE = ON;
 VARIABLE:
 NAMES ARE
 id female pdul acel worryl
 lone1 lone2 lone3 lone4 lone5
 anx1 anx2 anx3 anx4 anx5
 dep1 dep2 dep3 dep4 dep5
 host1 host2 host3 host4 host5
 percon5 percon5b subs5 subs5b sleep5 sleep5b;
 USEVARIABLES ARE
        lone1 lone2 lone3 lone4 lone5;
 MISSING ARE ALL (-999);
 ANALYSIS:
     ESTIMATOR = ML;
 MODEL:
     I S Ollone100 lone201 lone303 lone404 lone506;
 OUTPUT:
     SAMPSTAT;
 PLOT:
     TYPE = PLOT3;
     SERIES = lone1 - lone5(S);
```

Quadratic growth



Unconditional Quadratic LGCM

RESULTS

Model fit:

 $(\chi^2 = 46.671, df = 6; p < .001; RMSEA = .145, [90\% CI = 0.108, 0.185]; CFI = .908; TLI = .846)$

Parameter estimates:

i. Intercept: 1.466***

ii. Slope: 0.017

iii. Quadratic: -0.007**

(Co) Variances:

i. Intercept: 0.148***

ii. Slope: 0.003**

iii. Quadratic: 0.000

iv. Intercept WITH Slope: -0.020*

v. Intercept WITH Quadratic 0.000

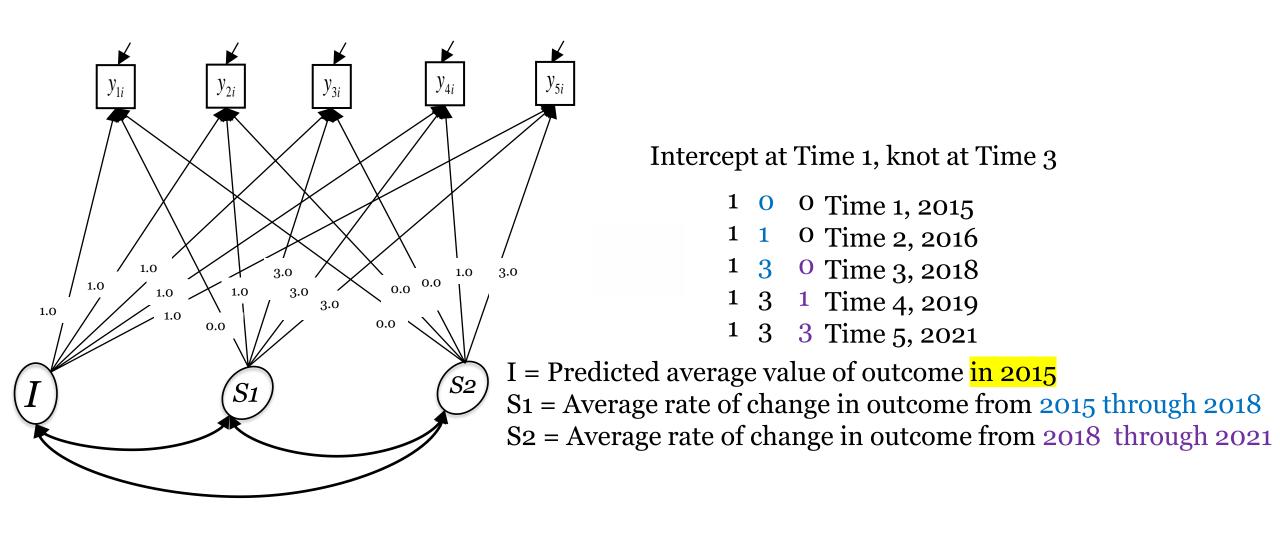
vi. Slope WITH Quadratic -0.002

Spline/Piecewise/Multiphase/Slope-segmented LGCM

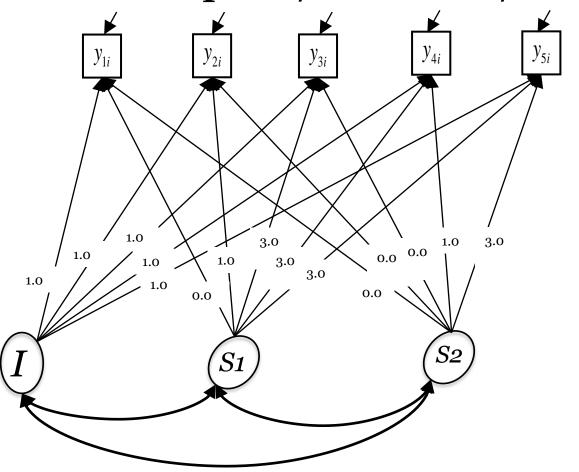
- When theoretical reasons suggest to separate time/development into discrete phases
 - Trajectory of loneliness before divorce and after divorce
 - Trajectory of depression before and after intervention
 - Pre-crawling and post-crawling in children
 - Childhood and adolescence

- Different phases of development are captured by more than one slope growth factor
 - Knots or transition points show where one phase is ending, and another phase is beginning

Bilinear Spline/Piecewise/Multiphase LGCM - 1



Bilinear Spline/Piecewise/Multiphase LGCM - 1



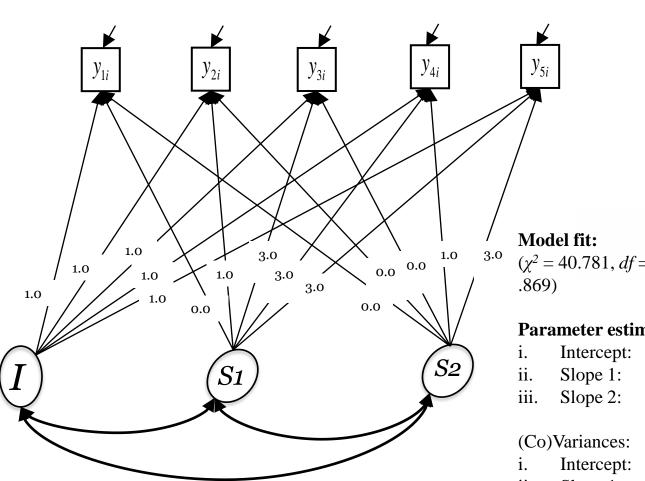
Intercept at Time 1, knot at Time 3

I = Predicted average value of outcome in 2015
 S1 = Average rate of change in outcome from 2015 through 2018
 S2 = Average rate of change in outcome from 2018 through 2021

```
■ 004_1_Bilinear_spline_growht_curve_model
 TITLE: 004 Bilinear spline growht curve model
 DATA:
 FILE IS data.dat;
 LISTWISE = ON;
 VARIABLE:
 NAMES ARE
 id female pdul acel worryl
 lone1 lone2 lone3 lone4 lone5
 anx1 anx2 anx3 anx4 anx5
 dep1 dep2 dep3 dep4 dep5
 host1 host2 host3 host4 host5
 percon5 percon5b subs5 subs5b sleep5 sleep5b;
 USEVARIABLES ARE
        lone1 lone2 lone3 lone4 lone5;
 MISSING ARE ALL (-999);
 ANALYSIS:
     ESTIMATOR = ML;
 MODEL:
     I S1|lone1@0 lone2@1 lone3@3 lone4@3 lone5@3;!Slope 1
     I S2|lone1@0 lone2@0 lone3@0 lone4@1 lone5@3;!Slope 2
 OUTPUT:
                                 Frederick Anyan, PhD - NTNU
      SAMPSTAT;
```

Bilinear Spline/Piecewise/Multiphase LGCM - 1

Intercept at Time 1, knot at Time 3



1	0	O	Time 1, 2015
1	1	Ο	Time 2, 2016
1	3	O	Time 3, 2018
1	3	1	Time 4, 2019
1	3	3	Time 5, 2021

I = Predicted average value of outcome in 2015

S1 = Average rate of change in outcome from 2015 through 2018

S2 = Average rate of change in outcome from 2018 through 2021

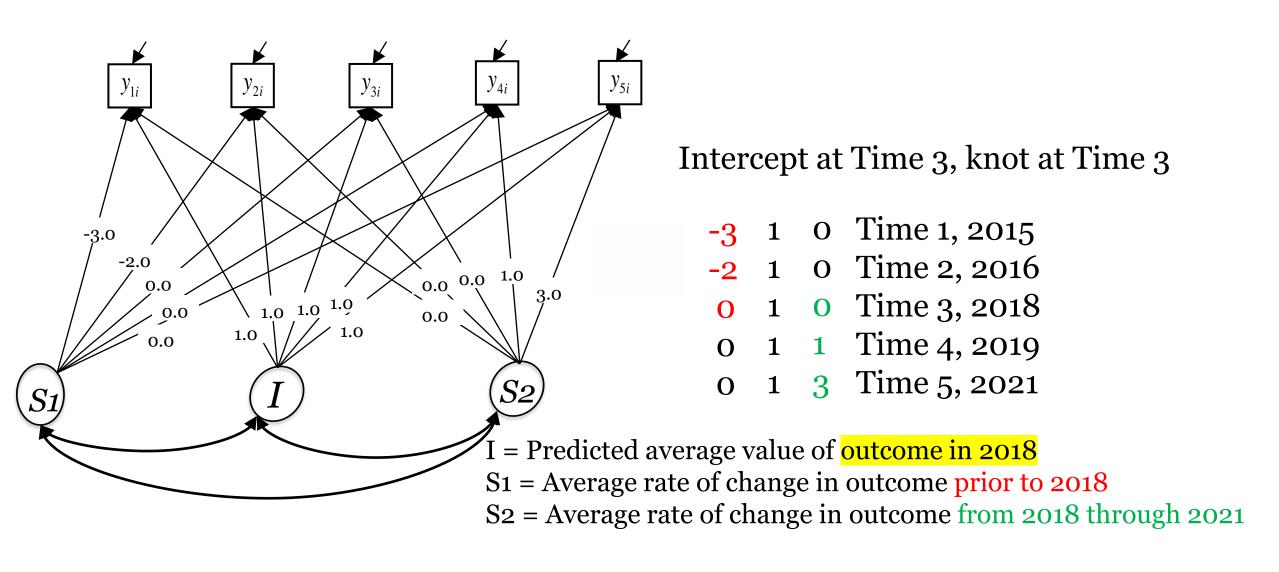
RESULTS

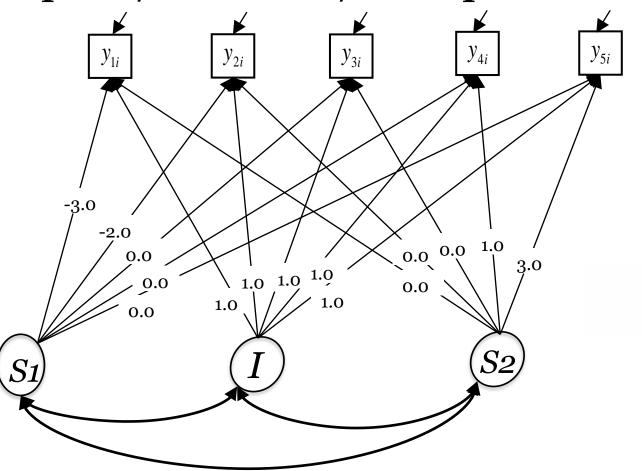
 $(\gamma^2 = 40.781, df = 6; p < .001; RMSEA = .134, [90\% CI = 0.097, 0.175]; CFI = .921; TLI = .921; TLI$

Parameter estimates:

i.	Intercept:	1.444***
ii.	Slope 1:	0.007
iii.	Slope 2:	-0.059***

i.	Intercept:	0.140***
ii.	Slope 1:	0.001**
iii.	Slope 2:	0.002
iv.	Intercept WITH Slope 1:	-0.015**
v.	Intercept WITH Slope 2	-0.019**





```
# 004_2_Bilinear/Spline growth curve model - 2
bilinear_2 <- ' i =~ 1*lone1 + 1*lone2 + 1*lone3 + 1*lone4 + 1*lone5

s1 =~ -3*lone1 + -2*lone2 + 0*lone3 + 0*lone4 + 0*lone5

s2 =~ 0*lone1 + 0*lone2 + 0*lone3 + 1*lone4 + 3*lone5'

fit_bilinear_2 <- growth(bilinear_2, data = data)

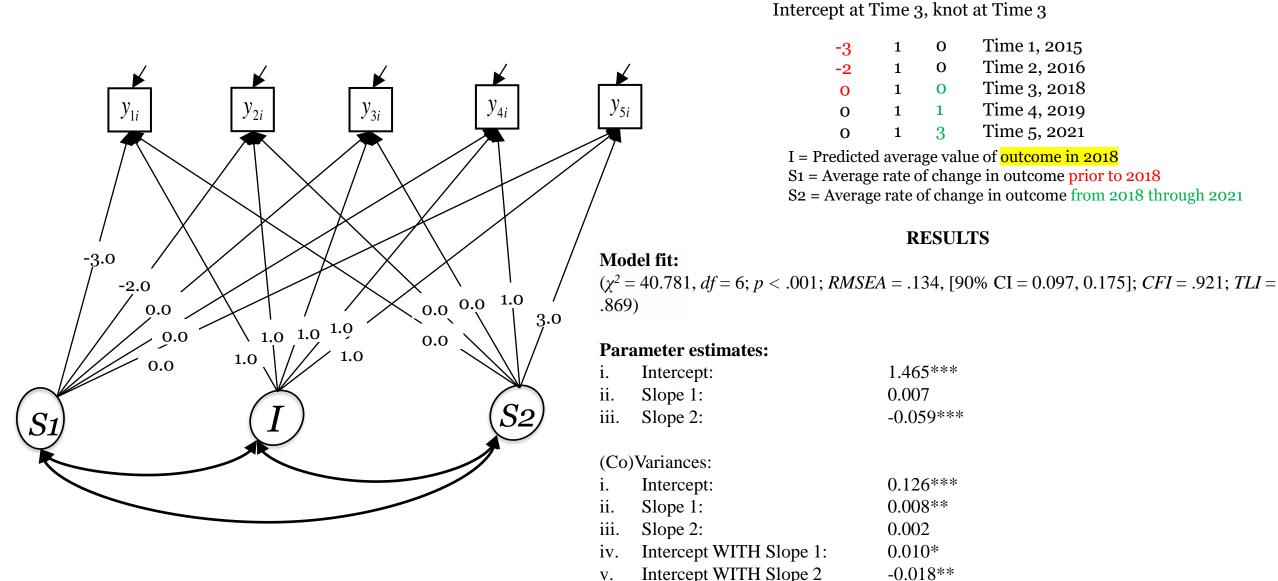
summary(fit_bilinear_2, fit.measures = TRUE)
```

```
Intercept at Time 3, knot at Time 3

I = Predicted average value of outcome in 2018
```

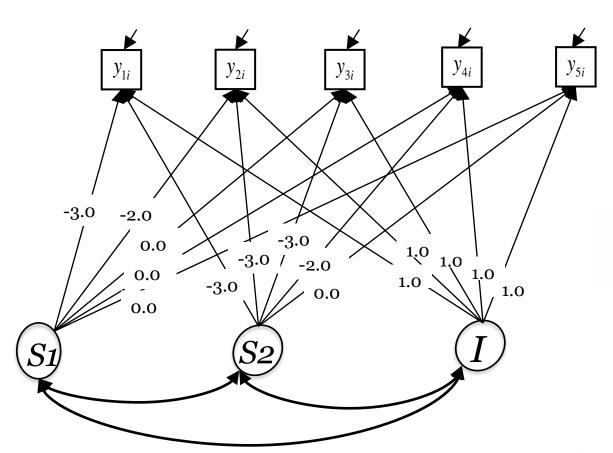
S1 = Average rate of change in outcome prior to 2018 S2 = Average rate of change in outcome from 2018 through 2021

```
004_2_Bilinear_spline_growht_curve_model_2
 TITLE: 002 Bilinear spline growht curve model
 DATA:
 FILE IS data.dat;
 LISTWISE = ON;
 VARIABLE:
 NAMES ARE
 id female pdul acel worryl
 lone1 lone2 lone3 lone4 lone5
 anx1 anx2 anx3 anx4 anx5
 dep1 dep2 dep3 dep4 dep5
 host1 host2 host3 host4 host5
 percon5 percon5b subs5 subs5b sleep5 sleep5b;
 USEVARIABLES ARE
         lone1 lone2 lone3 lone4 lone5;
 MISSING ARE ALL (-999);
 ANALYSIS:
     ESTIMATOR = ML;
 MODEL:
     I S1|lone1@-3 lone2@-2 lone3@0 lone4@0 lone5@0;!Slope 1
     I S2|lone1@0 lone2@0 lone3@0 lone4@1 lone5@3;!Slope 2
 OUTPUT:
                                Frederick Anyan, PhD - NTNU
      SAMPSTAT;
```



Slope 1 WITH Slope 2

0.000



Intercept at Time 5, knot at Time 3

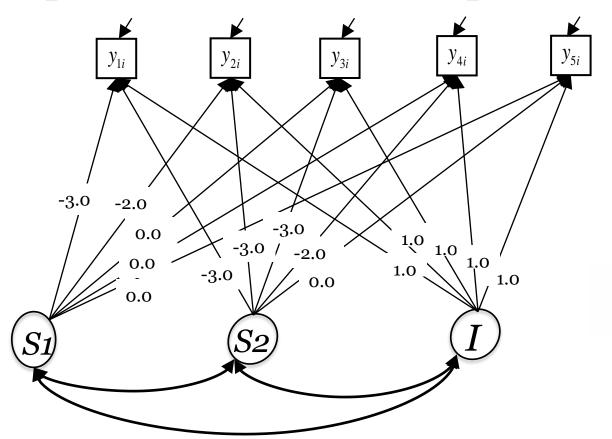
- Time 1, 2015
- Time 2, 2016
- 1 Time 3, 2018
- -2 1 Time 4, 2019
- Time 5, 2021

I = Predicted average value of outcome at end of observation in 2021

S1 = Average rate of change in outcome prior to 2018

S2 = Average rate of change in between 2018 to 2021

Spline/Piecewise/Multiphase LGCM - 3

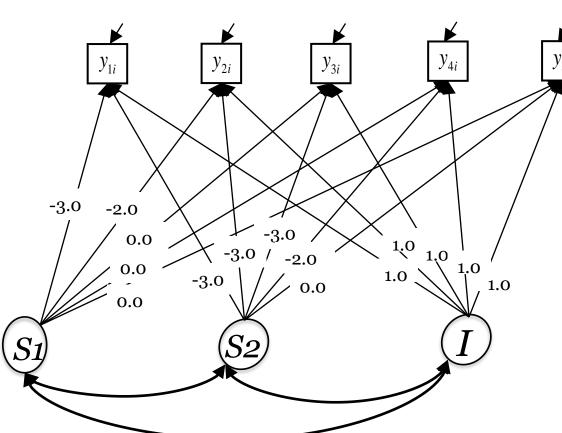


Intercept at Time 5, knot at Time 3

I = Predicted average value of outcome at end of observation in 2021 S1 = Average rate of change in outcome prior to 2018 S2 = Average rate of change in outcome from 2018 through 2021

```
004_3_Bilinear_spline_growht_curve_model_3
TITLE: 002 Bilinear spline growht curve model
DATA:
FILE IS data.dat;
LISTWISE = ON;
VARIABLE:
NAMES ARE
id female pdul acel worryl
lone1 lone2 lone3 lone4 lone5
anx1 anx2 anx3 anx4 anx5
dep1 dep2 dep3 dep4 dep5
host1 host2 host3 host4 host5
percon5 percon5b subs5 subs5b sleep5 sleep5b;
USEVARIABLES ARE
       lone1 lone2 lone3 lone4 lone5;
MISSING ARE ALL (-999);
ANALYSIS:
    ESTIMATOR = ML;
MODEL:
    I S1|lone1@-3 lone2@-3 lone3@-3 lone4@-2 lone5@0;!Slope 1
    I S2|lone1@-3 lone2@-2 lone3@0 lone4@0 lone5@0;!Slope 2
OUTPUT:
                              Frederick Anyan, PhD - NTNU
     SAMPSTAT;
```

Spline/Piecewise/Multiphase LGCM - 3



Intercept at Time 5, knot at Time 3

-3	-3	1	Time 1, 2015
-2	-3	1	Time 2, 2016
O	-3	1	Time 3, 2018
0	-2	1	Time 4, 2019
0	0	1	Time 5, 2021

I = Predicted average value of outcome at end of observation in 2021

S1 = Average rate of change in outcome prior to 2018

S2 = Average rate of change in outcome from 2018 through 2021

RESULTS

Model fit:

 $(\chi^2 = 40.781, df = 6; p < .001; RMSEA = .134, [90\% CI = 0.097, 0.175]; CFI =$.921; TLI = .869)

Parameter estimates:

i.	Intercept:	1.288***
ii.	Slope 1:	-0.059***
iii.	Slope 2:	0.007

(Co) Variances:

i.	Intercept:	0.036
ii.	Slope 1:	0.002
iii.	Slope 2:	0.008**
iv.	Intercept WITH Slope 1:	-0.012
v.	Intercept WITH Slope 2	0.011**
vi.	Slope 1 WITH Slope 2	0.000

Model comparisons and selection

Model		Compared with	χ^2	df	RMSEA	CFI	TLI
M 1	No growth		186.443	13	.204[0.179, 0.230]	.607	.698
M2	Linear growth	M1	75.244	10	.143[0.113, 0.174]	.852	.852
M3	Quadratic growth	M2	46.671	6	.145[0.108, 0.185]	.908	.846
M4	Bilinear spline growth	NON-NESTED!	40.781	6	.134[0.097, 0.175]	.921	.869

Model Comparison

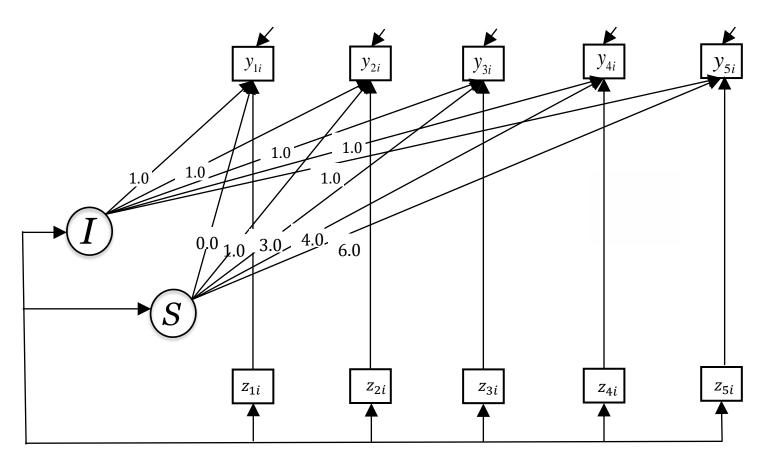
	Model M1 No growth	Model M2 Linear growth	Model M3 Quadratic growth	Model M4 Bilinear spline
Parameters	7	10	14	
-2LL	1629.268	1518.080	1489.508	
AIC	1643.269	1538.080	1517.507	1511.809
BIC	1669.669	1575.796	1570.308	1564.418
Δ parameters	-	3	4	
Δ -2LL	-	111.19***	28.573***	

- Do not compare nested models whose fit indices do not reach acceptable, e.g. M1 and M2
- Bilinear is a non-nested model with M1-M3
 - So use AIC and BIC

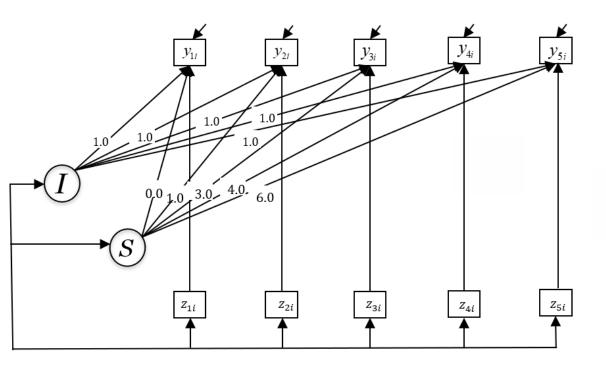
Objectives of longitudinal research

- Analysis of causes (determinants) of intraindividual change 2.
 - What factors/mechanisms time-varying/dynamical predictors drive change?
 - Inclusion of time-varying (dynamical) predictors in growth models

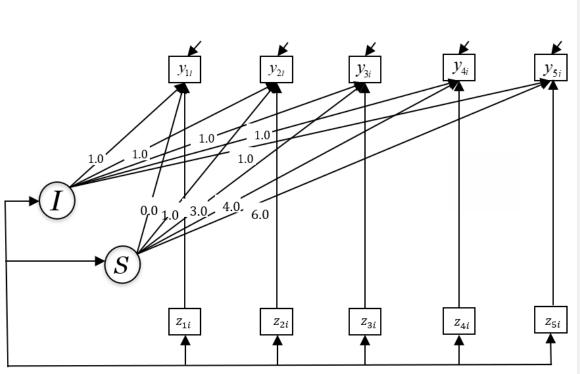
- What dynamics or factors drive within-person changes?
 - Does hostility affect the trajectory of loneliness?
 - Loneliness is more elevated than usual when someone is more hostile than usual?



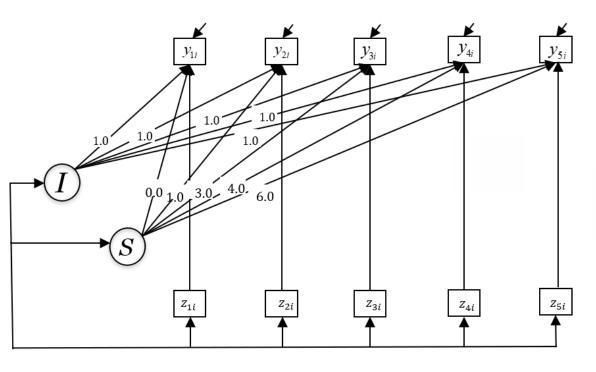
- TVC is exogenous to the developmental process
- The effect of TVC is a within-person effect which influences an individual's change trajectory
 - Flexibility in SEM allows correlating TVC with I and S – growth factors.
 - Convergence problems
 - Fix covariance between TVC with I and S to zero



```
005_Linear_growht_curve_model_with_time_varying_covariate
 FITLE: 005 Linear growht curve model with time varying covariate
 DATA:
 FILE IS data.dat;
 LISTWISE = ON;
 VARIABLE:
 NAMES ARE
 id female pdul acel worryl
 lone1 lone2 lone3 lone4 lone5
 anx1 anx2 anx3 anx4 anx5
 dep1 dep2 dep3 dep4 dep5
 host1 host2 host3 host4 host5
 percon5 percon5b subs5 subs5b sleep5 sleep5b;
 USEVARIABLES ARE
        lone1 lone2 lone3 lone4 lone5
        host1 host2 host3 host4 host5;
 MISSING ARE ALL (-999);
 ANALYSIS:
     ESTIMATOR = ML;
 MODEL:
     I S|lone100 lone201 lone303 lone404 lone506; Growth for loneliness
     !Regress loneliness on time-varying covariate
     lone1 ON host1;!By adding labels to the parameter estimates
     lone2 ON host2; you can test whether TVC effects are constant over time
     lone3 ON host3;
     lone4 ON host4;
     lone5 ON host5;
     !However, if you already assume constant effect of TVC over time
     !and do not want to test, you can use this model specification
     !lone1 ON host1(a); !By adding the same label (a) to the parameter estimates
     !lone2 ON host2(a);!you constrain the effects to be constant across time
     !lone3 ON host3(a);
     !lone4 ON host4(a);
     !lone5 ON host5(a);
     !Fix TVC covariance with intercept and slope to zero
     I S WITH host1-host5@0;
 OUTPUT:
     SAMPSTAT;
```



```
# 005_Linear growth curve model with time-varying covariates
    timevarvingcov \leftarrow ' i =~ 1*lone1 + 1*lone2 + 1*lone3 + 1*lone4 + 1*lone5
89
                         s = 0*lone1 + 1*lone2 + 3*lone3 + 4*lone4 + 6*lone5
    # Time-varying covariates
    lone1 ~ host1
                                #lone1 ~ eq*host1
                                #lone2 ~ eq*host2
    lone2 ~ host2
    lone3 ~ host3
                                #lone3 ~ eq*host3
    lone4 ~ host4
                               #lone4 ~ eq*host4
                                #lone5 ~ eq*host5
     lone5 ~ host5
     #Estimate the means of the TVC
    host1 ~ 1
    host2 ~ 1
    host3 ~ 1
    host4 ~ 1
    host5 ~ 1
103
    #Estimate covariance between TVC
105 host1 ~~ host2 + host3 + host4 + host5
106 host2 \( \simes \text{host3} + \text{host4} + \text{host5} \)
    host3 ~~ host4 + host5
    host4 ~~ host5'
109
110 fit_timevaryingcov <- growth(timevaryingcov, data = data)
111 summary(fit_timevaryingcov, fit.measures = TRUE)
```



RESULTS

Model fit:

 $(\chi^2 = 103.191, df = 30; p < .001; RMSEA = .087, [90\% CI = 0.069, 0.106]; CFI =$.972; *TLI* = .967)

Parameter estimates:

0.414*** Intercept: Slope 1: -0.010

TVC

Hostility: 0.719 - 0.737

(Co) Variances:

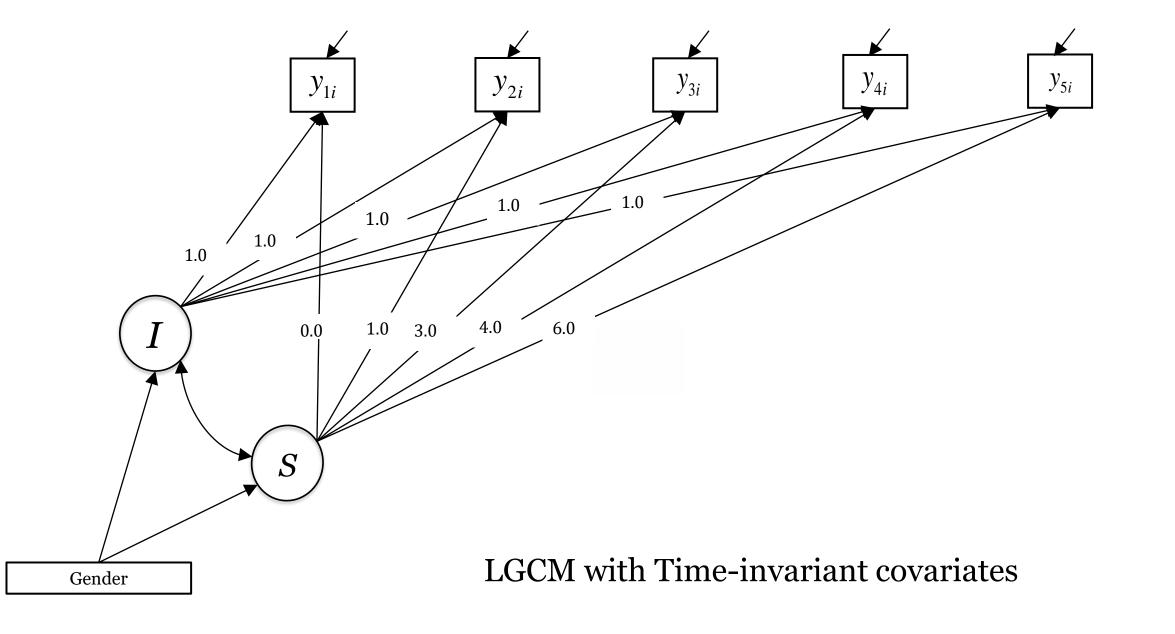
Intercept: 0.028*** ii. 0.001*** Slope 1: Intercept WITH Slope: -0.003***

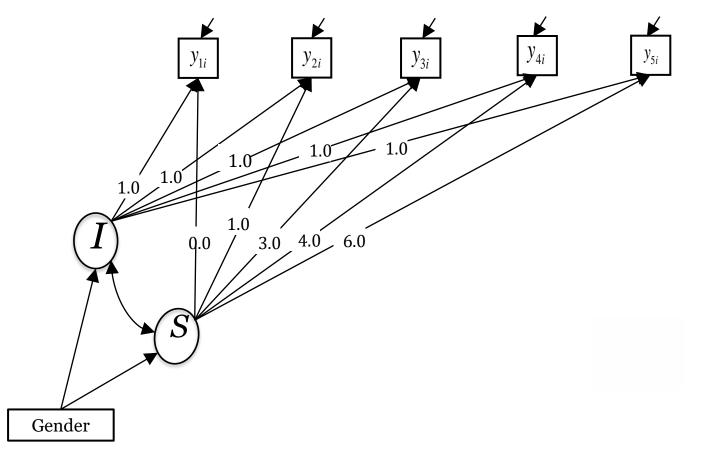
TVC WITH TVC: 0.036 - 0.161***

Objectives of longitudinal research

- Identification of interindividual differences (or similarity) in intraindividual change 3.
 - Do different individuals change in different ways?
 - Differences between groups of persons in the way people change
- Analysis of causes (determinants) of interindividual differences in intraindividual change 4.
 - What factors explain between-person differences in change?
 - Inclusion of time-invariant covariates in growth models, multigroup LGCM, Growth mixture models

- Do girls have different intercept and slope of the feeling of loneliness from boys?
 - Does gender influence between-person differences in the trajectory of loneliness?

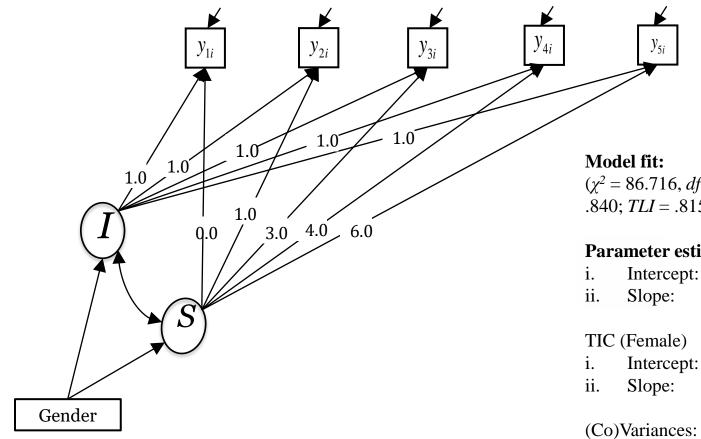




LGCM with Time-invariant covariates

```
114 # 006_Linear growth curve model with time invariant covariates
115 timeinvar <- ' i =~ 1*lone1 + 1*lone2 + 1*lone3 + 1*lone4 + 1*lone5
116
                    s = 0*lone1 + 1*lone2 + 3*lone3 + 4*lone4 + 6*lone5
117
     # Time invariant covariates
    i ∼ female
    s ~ female'
121 fit_timeinvar <- growth(timeinvar, data = data)
    summary(fit_timeinvar, fit.measures = TRUE)
```

```
006_Linear_growht_curve_model_with_time_invariant_covariates
 TITLE: 006 Linear growht curve model with time invariant covariate
 DATA:
 FILE IS data.dat;
 LISTWISE = ON;
 VARIABLE:
 NAMES ARE
 id female pdul acel worryl
 lone1 lone2 lone3 lone4 lone5
 anx1 anx2 anx3 anx4 anx5
 dep1 dep2 dep3 dep4 dep5
 host1 host2 host3 host4 host5
 percon5 percon5b subs5 subs5b sleep5 sleep5b;
 USEVARIABLES ARE
        lone1 lone2 lone3 lone4 lone5 female;
 MISSING ARE ALL (-999);
 ANALYSIS:
     ESTIMATOR = ML;
 MODEL:
     I S|lone1@0 lone2@1 lone3@3 lone4@4 lone5@6;
     !Regress growth factors on the time-invariant covariate
     I S ON female;
 OUTPUT:
      SAMPSTAT;
```



LGCM with Time-invariant covariates

RESULTS

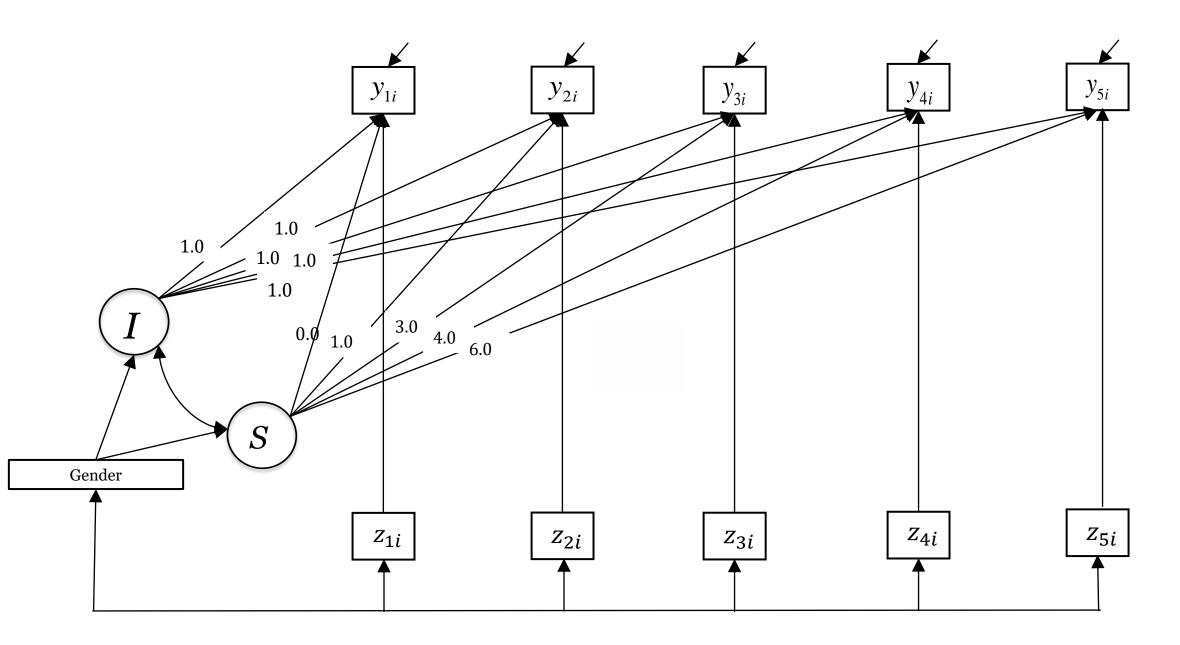
 $(\chi^2 = 86.716, df = 13; p < .001; RMSEA = .133, [90\% CI = 0.107, 0.160]; CFI = 0.107, 0.160]$.840; TLI = .815)

Parameter estimates:

i.	Intercept:	1.526***
ii.	Slope:	-0.029***

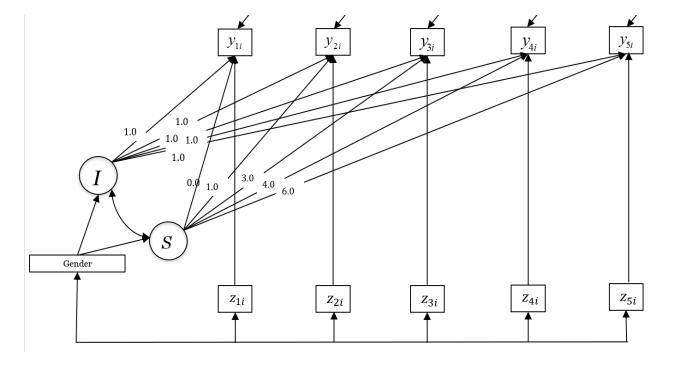
i.	Intercept:	-0.132**
ii.	Slope:	0.007

i.	Intercept:	0.134***
ii.	Slope:	0.003***
iii.	Intercept WITH Slope:	-0.015***



LGCM with Time-invariant and time-varying covariates

LGCM with Time-invariant and time-varying covariates



```
007_Linear_growht_curve_model_with_time-invariant and time-varying covariates
 FITLE: 007 Linear growht curve model with time-invariant and time-v
 DATA:
 FILE IS data.dat;
 LISTWISE = ON;
 VARIABLE:
 NAMES ARE
 id female pdul acel worryl
 lone1 lone2 lone3 lone4 lone5
 anx1 anx2 anx3 anx4 anx5
 dep1 dep2 dep3 dep4 dep5
 host1 host2 host3 host4 host5
 percon5 percon5b subs5 subs5b sleep5 sleep5b;
 USEVARIABLES ARE
        lone1 lone2 lone3 lone4 lone5
        host1 host2 host3 host4 host5
        female;
 MISSING ARE ALL (-999);
 ANALYSIS:
     ESTIMATOR = ML;
 MODEL:
     I S|lone100 lone201 lone303 lone404 lone506;
     !Regress growth factors on time-invariant covariates
     I S ON female;
     !Regress loneliness on TVC
     lone1 ON host1(a);!Constrain TVC effect to be equal across time
     lone2 ON host2(a);
     lone3 ON host3(a);
     lone4 ON host4(a);
     lone5 ON host5(a);
     !Fix TVC covariance with intercept and slope to zero
     I S WITH host1-host5@0;
     !Estimate the covaraince between covariates
     female WITH host1-host5;
 OUTPUT:
                                       Frederick Anyan, PhD - NTNU
     SAMPSTAT;
```

LGCM with Time-invariant and time-varying covariates

```
y_{1i} y_{2i} y_{3i} y_{4i} y_{5i}

1.0
1.0
1.0
1.0
1.0
21i z_{2i} z_{3i} z_{4i} z_{5i}
```

```
125 # 007_Linear growth curve model with time invariant and time-varying covariates
126 timeinvartimevar <- ' i =\sim 1*lone1 + 1*lone2 + 1*lone3 + 1*lone4 + 1*lone5
127
                          s = 0*lone1 + 1*lone2 + 3*lone3 + 4*lone4 + 6*lone5
    # Time-varying covariates held equal
128
    lone1 ~ eq*host1
    lone2 ~ eq*host2
    lone3 ~ eq*host3
132 lone4 ~ eq*host4
133
    lone5 ~ eq*host5
134
     # Time invariant covariates
136 i ∼ female
137 s ∼ female
138
    #Estimate the means of TVC and TIC
140 host1 ~ 1
141 host2 ~ 1
142 host3 ~ 1
    host4 ~ 1
    host5 ~ 1
145 female ~ 1
146
147
    #Estimate covariances between TIC with TVC
    female ~~ host1 + host2 + host3 + host4 + host5
    host1 ~~ host2 + host3 + host4 + host5
    host2 ~~ host3 + host4 + host5
152 host3 ~~ host4 + host5
    host4 ~~ host5
154
155 #Fix covariances between TVC and growth factors to zero
156 i ~~ 0*host1
157 i ~~ 0*host2
158 i ~~ 0*host3
159 i ~~ 0*host4
160 i ~~ 0*host5
161
162 s ~~ 0*host1
163 s ~~ 0*host2
164 s ~~ 0*host3
165 s ~~ 0*host4
166 s ~~ 0*host5
167
168 fit_timeinvar_timevar <- growth(timeinvartimevar, data = data)</pre>
169 summary(fit_timeinvar_timevar, fit.measures = TRUE)
```

\mathcal{Y}_{4i} SGender z_{1i} z_{2i} z_{3i} Z_{4i}

RESULTS

Model fit:

 $(\chi^2 = 106.720, df = 37; p < .001; RMSEA = .077, [90\% CI = 0.060, 0.094]; CFI = .0000, 0.0000, 0.0000, 0.0000, 0.0000, 0.00000, 0.00000, 0.00000, 0.0000, 0.0000, 0.0000, 0.0000, 0.00000, 0.0000, 0.0000, 0.0000, 0.00000, 0.0000,$.973; *TLI* = .971)

Parameter estimates:

Intercept: 0.456*** ii. -0.009** Slope:

TIC (Female)

-0.131** Intercept: ii. Slope: 0.008

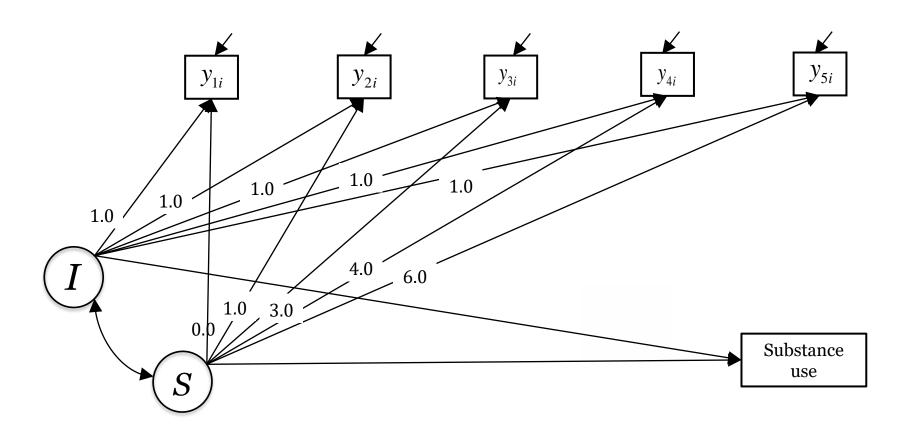
TVC

.731*** Host

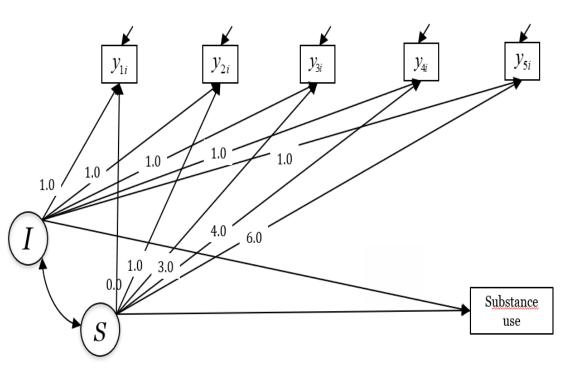
(Co) Variances:

0.023*** Intercept: ii. 0.001*** Slope: iii. Intercept WITH Slope: -0.002***

TVC WITH TVC: 0.037 - 0.161***



LGCM growth factors predicting distal outcome

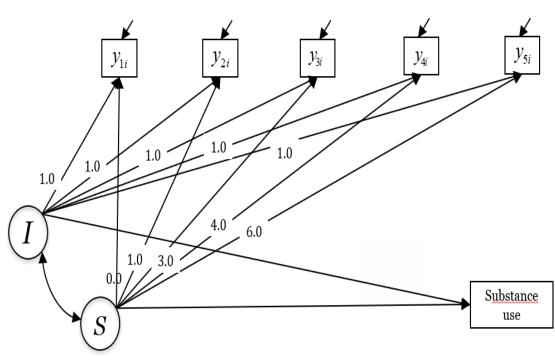


LGCM growth factors predicting distal outcome

182 summary(fit_distal, fit.measures = TRUE)

```
172 # 008_Linear growth curve model with growth factors predicting distal outcome
173 distal <- ' i =~ 1*lone1 + 1*lone2 + 1*lone3 + 1*lone4 + 1*lone5
                s = 0*lone1 + 1*lone2 + 3*lone3 + 4*lone4 + 6*lone5
174
175
    # Time invariant covariates
177
    subs5 \sim i + s
178
179 #Estimate the intercept of subs
180 subs5 ~ 1'
181 fit_distal <- growth(distal, data = data)
```

```
- D X
■ 008_Linear_growht_curve_model_with_growth_factors_predicting_distal_outcome
 TITLE: 008 Linear growht curve model with growth factors predicting distal out
 DATA:
 FILE IS data.dat;
 LISTWISE = ON;
 VARIABLE:
 NAMES ARE
 id female pdul acel worryl
  lonel lone2 lone3 lone4 lone5
 anx1 anx2 anx3 anx4 anx5
 dep1 dep2 dep3 dep4 dep5
 host1 host2 host3 host4 host5
 percon5 percon5b subs5 subs5b sleep5 sleep5b;
 USEVARIABLES ARE
         lone1 lone2 lone3 lone4 lone5 subs5;
 MISSING ARE ALL (-999);
 ANALYSIS:
     ESTIMATOR = ML;
 MODEL:
     I S|lone1@0 lone2@1 lone3@3 lone4@4 lone5@6;
     !Regress distal outcome on growth factors and time-invariant predictors
     subs5 ON I S;
 OUTPUT:
     SAMPSTAT;
```



LGCM growth factors predicting distal outcome

RESULTS

Model fit:

 $(\chi^2 = 74.672, df = 13; p < .001; RMSEA = .128, [90\% CI = 0.101, 0.157]; CFI = .128$.854; *TLI* = .832)

Parameter estimates:

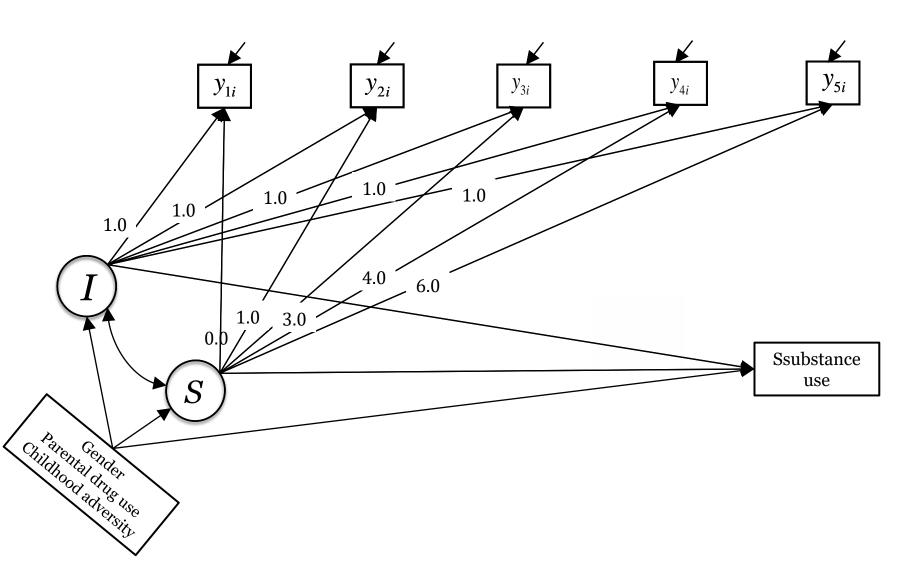
i.	Intercept:	1.466***
ii.	Slope:	-0.023***

Distal outcome (substance use)

i.	Intercept:	0.896*
ii.	Slope:	5.889

(Co)Variances:

i.	Intercept:	0.142***
ii.	Slope:	0.003***
iii.	Intercept WITH Slope:	-0.015***



LGCM with Time-invariant covariates and distal outcome

Multigroup LGCM

- How is it different from using time-invariant covariate model?
 - Time-invariant covariate (TIC) models examine the difference in the average growth trajectory
 - TIC models do not examine aspects of the growth model related to
 - Group differences in the
 - Average trajectory and invariance testing
 - Variability and covariability of growth trajectories
 - iii. Unexplained within-person variability
- Multigroup LGCM models can examine differences in any aspect of growth trajectory for known, measured or predefined groups
 - Growth mixture models are used for unknown or unmeasured groups that may exist as subpopulations in the data

Multigroup LGCM

- What factors account for between-person differences in the trajectory of loneliness between boys and girls?
 - Do boys and girls *significantly* differ in their trajectories of loneliness?
 - What is the extent of differences in the average trajectory of boys and girls?
 - What is the extent of variability around the individual trajectories of boys and girls?

Model comparisons

Model Comparison for the Multiple-Group LGCM

	Model M1 Invariance model	Model M2 Means model	Model M3 Means and covariances model	Model M4 Means, covariances and residual variances model
Parameters				
-2LL				
Δ parameters				
Δ -2LL				

Sequence of testing

- M1: Constrain all parameters (growth factor means, growth factor variances and covariances, and residual variances) to be identical across groups
- M2: Freely estimate growth factor means across groups, while keeping constraints on the growth factor variances and covariance, and residual variances
- M3: Freely estimate growth factor means, growth factor variances and covariances, while keeping the constraints on the residual variances
- M4: Freely estimate growth factor means, growth factor variances and covariances, and residual variances across the groups

Questions to answer

- M1 vs. M2: Tests whether the groups differ in their average trajectory
- M2 vs. M3: Tests the extent of between-person differences in the trajectories of groups
- M₃ vs. M₄: Tests the extent of within-person variability around individual trajectories
 - If all models fit equally well (i.e., no significant results from the LRT) then choose the model with the smallest number of parameters, M1 most parsimonious model as it is the most constrained/reduced form

• M1: Constrain all parameters (growth factor means, growth factor variances and covariances, and residual variances) to be identical across groups

```
009_1_Multigroup_LGCM_M1_Invariance_model
 MODEL:
     I S|lone1@0 lone2@1 lone3@3 lone4@4 lone5@6;
     !Estimate means of growth factors and label them
     [I] (INT);
     [S] (SLP);
     !Estimate variances of growth factors
     I(INT V);
     S(SLP_V);
     !Estimate covariance of growth factors
     I WITH S(IS COV);
     !Estimate residual variance and constrain them equal
     lone1-lone5 (RES);
 !Sequentially testing models means specific parameters are o
 !For those parameters, we will begin by constraining them to
 !Those parameters are (MEANS OF GROWTH FACTORS, CO/VARIANCES
 !In subsequent models, we will freely estimate those paramet
 MODEL MALES:
     !Growth factor means for males
     [I] (INT); !The INT label will make the males' intercept q
     [S] (SLP);!The labelling for all the parameters will make
     !Growth factor variances for males
     I(INT V);
     S(SLP V);
     !Growth factor covariance for males
     I WITH S(IS COV);
     !Residual variances for males
     lone1-lone5 (RES);
 MODEL FEMALES:
     !Gorwth factor means for females
     [I](INT); !The INT label will make the females' intercept
     [S] (SLP);
     !Growth factor variances for females
     I(INT V);
     S(SLP V);
     !Growth factor covariance for females
     I WITH S(IS COV);
     !Residual variances for females
     lone1-lone5 (RES);
 OUTPUT:
     SAMPSTAT;
```

```
189 # 009_1_Multigroup LGCM M1 Invariance model
190 multigroupM1 <- ' i =~ 1*lone1 + 1*lone2 + 1*lone3 + 1*lone4 + 1*lone5
                      s = 0*lone1 + 1*lone2 + 3*lone3 + 4*lone4 + 6*lone5
191
192 #Growth factor means constrained equal
193 i \sim c(int, int)*1
194 s \sim c(slp, slp)*1
195
196 #Growth factor variances held equal
197 i ∼ c(vint, vint)*i
198 s \sim c(vslp, vslp)*s
199
200 #Growth factor covariances held equal
201 i \sim c(cvf, cvf)*s
202
203 #Residual variances of observed items held equal
204 lone1 ~~ c(res, res)*lone1
205 lone2 ~~ c(res, res)*lone2
206 lone3 ~~ c(res, res)*lone3
207 lone4 ~~ c(res, res)*lone4
208 lone5 ~~ c(res, res)*lone5
209
210 fit_multigroupM1 <- growth(multigroupM1, data = data, group = "female")
211 summary(fit_multigroupM1, fit.measures = TRUE)
212
```

• M2: Freely estimate growth factor means across groups, while keeping constraints on the growth factor variances and covariance, and residual

```
009_2_Multigroup_LGCM_M2_Growth_factor_means
         lone1 lone2 lone3 lone4 lone5;
 GROUPING = FEMALE (0 = MALES 1 = FEMALES);
 MISSING ARE ALL (-999);
 ANALYSIS:
     ESTIMATOR = ML;
 MODEL:
     I S|lone1@0 lone2@1 lone3@3 lone4@4 lone5@6;
      [I] (INT);
      [S] (SLP);
     I(INT V);
     S(SLP V);
     I WITH S(IS COV);
     lone1-lone5 (RES);
 MODEL MALES:
      [I] (INT M); !Free growth factor means by using
      [S] (SLP M);
     I(INT V);
     S(SLP V);
     I WITH S(IS COV);
     lone1-lone5 (RES);
 MODEL FEMALES:
      [I] (INT F);!Different labels are used to freel
      [S] (SLP F);
     I(INT V);
     S(SLP V);
     I WITH S(IS COV);
     lone1-lone5(RES);
```

```
214 # 009_2_Multigroup LGCM M2 Free factor means
    multigroupM2 < ' i = 1*lone1 + 1*lone2 + 1*lone3 + 1*lone4 + 1*lone5
                       s = 0*lone1 + 1*lone2 + 3*lone3 + 4*lone4 + 6*lone5
216
    #Growth factor means freely estimated
217
218 i \sim c(intm, intf)*1
    s \sim c(slpm, slpf)*1
220
221
    #Growth factor variances held equal
222 i ~~ c(vint, vint)*i
223 s \sim c(vslp, vslp)*s
224
225 #Growth factor covariances held equal
226
    i \sim c(cvf, cvf)*s
227
228 #Residual variances of observed items held equal
   lone1 ~~ c(res, res)*lone1
229
    lone2 ~~ c(res, res)*lone2
    lone3 ~~ c(res, res)*lone3
    lone4 ~~ c(res, res)*lone4
    lone5 ~~ c(res, res)*lone5
234
    |fit_multigroupM2 <- growth(multigroupM2, data = data, group = "female")</pre>
235
    summary(fit_multigroupM2, fit.measures = TRUE)
```

OUTPUT:

SAMPSTAT;

• M3: Freely estimate growth factor means, growth factor variances and covariances, while keeping the constraints on the residual variances

```
GROUPING = FEMALE (0 = MALES 1 = FEMALES);
MISSING ARE ALL (-999);
                                                                   239 # 009_3_Multigroup LGCM M3 Free factor means and co/variances
ANALYSIS:
                                                                   240 multigroupM3 <- ' i =~ 1*lone1 + 1*lone2 + 1*lone3 + 1*lone4 + 1*lone5
   ESTIMATOR = ML;
                                                                                            s = 0*lone1 + 1*lone2 + 3*lone3 + 4*lone4 + 6*lone5
                                                                   241
MODEL:
                                                                   242 #Growth factor means freely estimated
   I S|lone1@0 lone2@1 lone3@3 lone4@4 lone5@6;
                                                                   243 i \sim c(intm, intf)*1
                                                                        s \sim c(slpm, slpf)*1
   [I] (INT);
   [S] (SLP);
                                                                   245
                                                                   246 #Growth factor variances freely estimated
   I(INT V);
                                                                   247 i ∼ c(vinm, vinf)*i
   S(SLP V);
                                                                        s ~~ c(vslm, vslf)*s
                                                                   249
   I WITH S(IS COV);
                                                                   250 #Growth factor covariances freely estimated
   lone1-lone5(RES);
                                                                   251 i ~~ c(covm, covf)*s
                                                                   252
MODEL MALES:
                                                                        #Residual variances of observed items held equal
    [I S];!First: Growth factor means are freely estimated
                                                                   254 lone1 ~~ c(res, res)*lone1
   I S;!Second: Growth factor variances are freely estimated
                                                                   255 lone2 ~~ c(res, res)*lone2
   I WITH S;! Second: Growth factor covariances are freely estimated
                                                                       lone3 ~~ c(res, res)*lone3
                                                                   257 lone4 ~~ c(res, res)*lone4
   lone1-lone5(RES);
                                                                        lone5 ~~ c(res, res)*lone5
                                                                   258
                                                                   259
MODEL FEMALES:
                                                                       fit_multigroupM3 <- growth(multigroupM3, data = data, group = "female")</pre>
    [I S];!First: Growth factor means are freely estimated
   I S;!Second: Growth factor variances are freely estimated
                                                                        summary(fit_multigroupM3, fit.measures = TRUE)
   I WITH S;! Second: Growth factor covariances are freely estimated
   lone1-lone5(RES);
```

64

! 0 = INT M - INT F;

SAMPSTAT;

OUTPUT:

• M4: Freely estimate growth factor means, growth factor variances and covariances, and residual variances across the groups

```
GROUPING = FEMALE (0 = MALES 1 = FEMALES);
MISSING ARE ALL (-999);
ANALYSIS:
                                                                     264 # 009_4_Multigroup LGCM M4 Free factor means and co/variances
   ESTIMATOR = ML;
                                                                          multigroupM4 \leftarrow ' i \Rightarrow 1*lone1 + 1*lone2 + 1*lone3 + 1*lone4 + 1*lone5
                                                                                              s = 0*lone1 + 1*lone2 + 3*lone3 + 4*lone4 + 6*lone5
                                                                     266
MODEL:
    I Sllone100 lone201 lone303 lone404 lone506;
                                                                     267 #Growth factor means freely estimated
                                                                     268 i \sim c(intm, intf)*1
    [I](INT);
                                                                          s \sim c(slpm, slpf)*1
    [S] (SLP);
                                                                     270
   I(INT V);
                                                                     271 #Growth factor variances freely estimated
   S(SLP V);
                                                                     272 i ~~ c(vinm, vinf)*i
                                                                          s ~~ c(vslm, vslf)*s
   I WITH S(IS COV);
                                                                     274
   lone1-lone5(RES);
                                                                          #Growth factor covariances freely estimated
                                                                         i \sim c(covm, covf)*s
MODEL MALES:
    [I S] (INT M SLP M);!First: Growth factor means are freely estimated
                                                                     277
   I S;!Second: Growth factor variances are freely estimated
                                                                          #Residual variances of observed items freely estimated
                                                                     279 lone1 ~~ c(rsm1, rsf1)*lone1
   I WITH S;! Second: Growth factor covariances are freely estimated
                                                                     280 lone2 ~~ c(rsm2, rsf2)*lone2
   lone1-lone5;!Third, residual variances freely estimated
                                                                     281 lone3 ~~ c(rsm3, rsf3)*lone3
                                                                         lone4 ~~ c(rsm4, rsf4)*lone4
MODEL FEMALES:
    [I S] (INT F SLP F); !First: Growth factor means are freely estimated
                                                                          lone5 ~~ c(rsm5, rsf5)*lone5
                                                                     283
   I S;!Second: Growth factor variances are freely estimated
                                                                     284
                                                                          |fit_multigroupM4 <- growth(multigroupM4, data = data, group = "female")</pre>
   I WITH S;! Second: Growth factor covariances are freely estimated
                                                                     286 summary(fit_multigroupM4, fit.measures = TRUE)
   lone1-lone5;!Third: residual variances freely estimated
!MODEL TEST:
```

- M1: Constrain all parameters (growth factor means, growth factor variances and covariances, and residual variances) to be identical across groups
- M2: Freely estimate growth factor means across groups, while keeping constraints on the growth factor variances and covariance, and residual variances
- M3: Freely estimate growth factor means, growth factor variances and covariances, while keeping the constraints on the residual variances
- M4: Freely estimate growth factor means, growth factor variances and covariances, and residual variances across the groups

Questions to answer

- M1 vs. M2: Tests whether the groups differ in their average trajectory
- M2 vs. M3: Tests the extent of between-person differences in the trajectories of groups
- M3 vs. M4: Tests the extent of within-person variability around individual trajectories
 - If all models fit equally well (i.e., no significant results from the LRT) then choose the model with the smallest number of parameters, M1 most parsimonious model as it is the most constrained/reduced form

```
#The `anova` function in `lavaan` computes the LRT for nested models.

compare_groups <- anova(fit_multigroupM1, fit_multigroupM2, fit_multigroupM3, fit_multigroupM4)

compare_groups
```

```
# Test of parameter constraints
constint = 'intm - intf == 0'
lavTestWald(fit_multigroupM4, constraints = constint)
constslp = 'slpm - slpf ==0'
lavTestWald(fit_multigroupM4, constraints = constslp)
```

Multigroup LGCM

Models	Invariance Model		Means model		Means and Co/variances		Means, Co/variances and residual variances	
	GROUP 1	GROUP 2	GROUP 1	GROUP 2	GROUP 1	GROUP 2	GROUP 1	GROUP 2
Model fit								
χ²(df)	2017.477(34)***		196.543(32)***		186.447(29)***		178.403(28)***	
RMSEA	.179 [0.156, 0.202]		.179 [0.156, 0.204]		.184 [0.159, 0.210]		.183 [0.158, 0.209]	
CFI	.609		.629		.645		.661	
TLI	.770		.768		.755		.758	
Parameter estimates								
Intercept	1.484***	1.484***	1.550***	1.401***	1.550***	1.401***	1.550***	1.401***
Slope	-0.026***	-0.026***	-0.031***	-0.020**	-0.031***	-0.020**	-0.031***	-0.020**
(Co)Variances								
Intercept	0.135***	0.135***	0.130***	0.130***	0.170***	0.079***	0.163***	0.087***
Slope	0.001*	0.001*	0.001*	0.001*	0.002**	0.000	0.001	0.003
Intercept WITH Slope	-0.011***	-0.011	-0.010***	-0.010***	-0.015***	-0.004	-0.014***	-0.006*
Residual variance	0.109***	0.109***	0.109***	0.109***	0.109***	0.109***	0.121***	0.093***

Model comparisons

Model Comparison for the Multiple-Group LGCM

	Model M1 Invariance model	Model M2 Means model	Model M3 Means and covariances model	Model M4 Means, covariances and residual variances model
Parameters	6	8	11	12
-2LL	1553.446	1542.510	1532.416	1448.148
Δ parameters	-	2	3	1
Δ-2LL	-	10.936**	10.094*	8.046**

Questions to answer

- M1 vs. M2: Tests whether the groups differ in their average trajectory
- M2 vs. M3: Tests the extent of between-person differences in the trajectories of groups
- M3 vs. M4: Tests the extent of within-person variability around individual trajectories

Males and females differ in their average growth trajectories of loneliness, the extent of between-person differences in those trajectories and the extent of variability around their individual trajectories

Objectives of longitudinal research

- Interrelationships in change 5.
 - Does change in one variable relate (precede, covary and/or follow) to change in another variable?
 - Correlating slopes of X and Y could provide evidence that one variable is changing in the same people as another variable correlated changes! Or common changes!
 - ✓ Multi (parallel & sequentially contingent) process LGCM

Multi Process LGCM

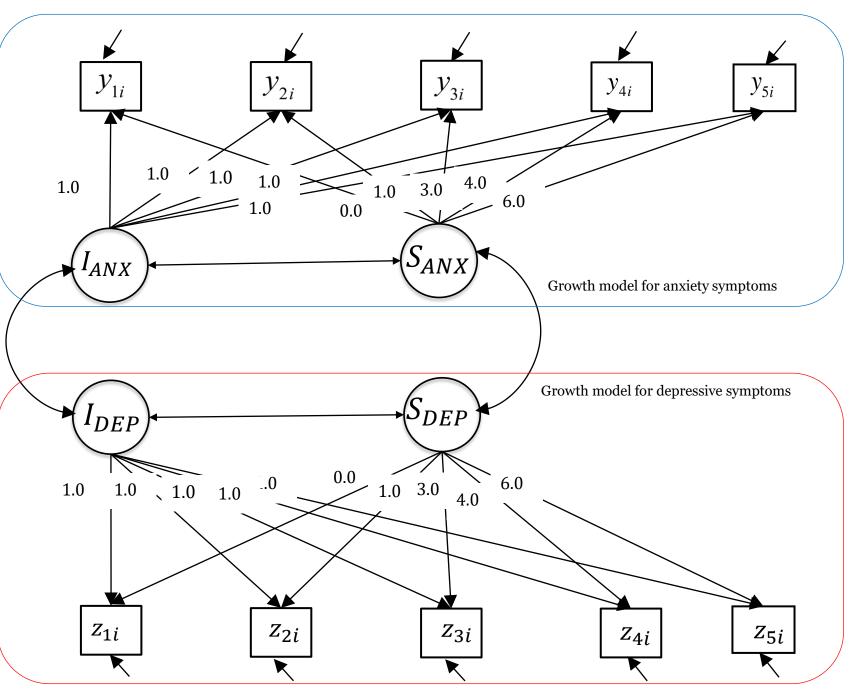
Simultaneously model multiple outcomes

1. Parallel LGCM

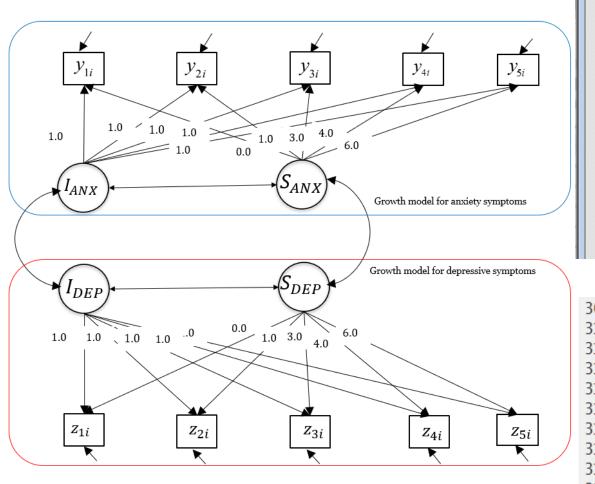
- Covariance between two intercepts
 - Information about association between the two outcomes at the beginning of observation period
- Covariance between two slopes
 - How rate of change in the two outcomes are associated with each other

Sequential LGCM

Change in one subdomain, e.g. Anxiety symptoms (T1-T5) is correlated with change in another subdomain, e.g. depressive symptoms (T6-T10)



- Study distinct but related subdomains
- Developmental associations (codevelopment) between anxiety and depressive symptoms
- Non-directional associations represent co-development/occurrence



```
USEVARIABLES ARE
        anx1 anx2 anx3 anx4 anx5
        dep1 dep2 dep3 dep4 dep5;
 MISSING ARE ALL (-999);
 ANALYSIS:
     ESTIMATOR = ML;
     MODEL = NOCOV;!Suppress Mplus default correlations between the growth factor
                   !That way, you have control over what variables you want to co.
 MODEL:
     I ANX S ANX anx100 anx201 anx303 anx404 anx506; anxiety symptoms growth
     I DEP S DEP | dep100 dep201 dep303 dep404 dep506; ! depressive symptoms
     !Correlate the growth factors
     I ANX WITH S ANX;
     I DEP WITH S DEP;
     I ANX WITH I DEP;
     S ANX WITH S DEP;
 OUTPUT:
     SAMPSTAT;
309 # 010_1_Parallel growth curve models - anxiety and depression symptoms
    parallel <- ' ia =\sim 1*anx1 + 1*anx2 + 1*anx3 + 1*anx4 + 1*anx5
311
                   sa = 0*anx1 + 1*anx2 + 3*anx3 + 4*anx4 + 6*anx5
                   id = 1*dep1 + 1*dep2 + 1*dep3 + 1*dep4 + 1*dep5
312
                   sd = 0*dep1 + 1*dep2 + 3*dep3 + 4*dep4 + 6*dep5
313
    #Growth factor corelations
315 ia ~~ id + sa
    sd ~~ id + sa
    ia ~~ 0*sd
    id ~~ 0*sa
319
320 fit_parallel <- growth(parallel, data = data)
321 summary(fit_parallel, fit.measures = TRUE)
```



 $(\chi^2 = 820.887, df = 43; p < .001; RMSEA = .237 [90\% CI = 0.223, 0.252]; CFI = .584;$ TLI = .564)

Parameter estimates:

Anxiety symptoms

i.	Intercept:	1.397***
ii.	Slope:	-0.032***

Depression symptoms

i.	Intercept:	1.545***
ii.	Slope:	-0.014**

(Co) Variances:

Anxiety symptoms

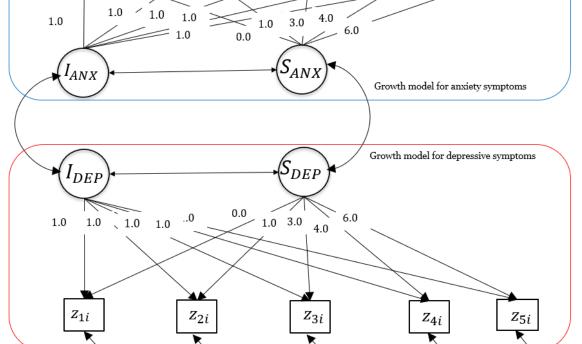
i.	Intercept:	0.097***
ii.	Slope:	0.002***

Depression symptoms

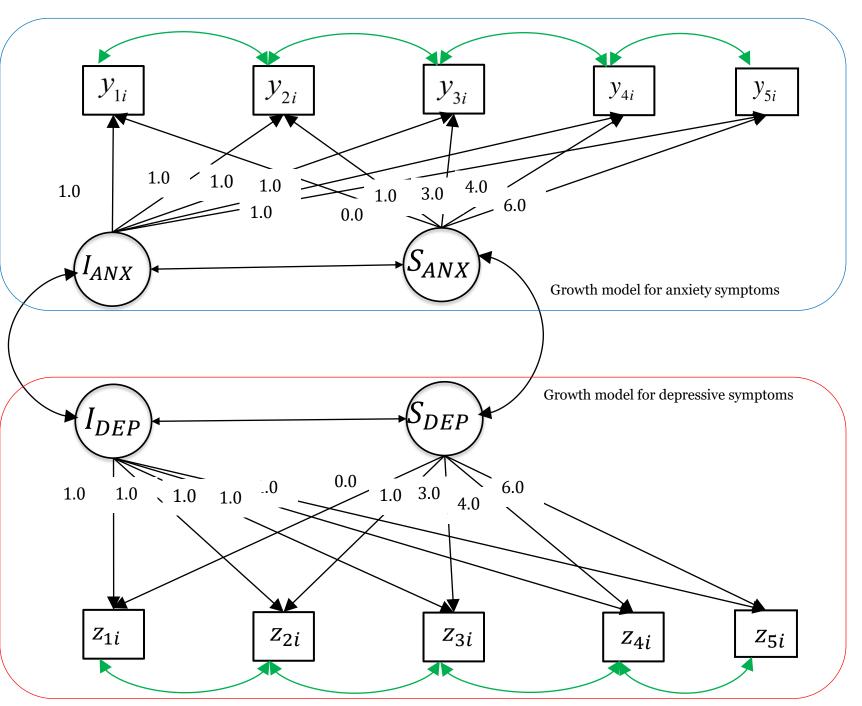
i.	Intercept:	0.171***
ii.	Slope:	0.002**

iii.	I_ANX WITH S_ANX	0.000
iv.	I_ANX WITH I_DEP	0.125***

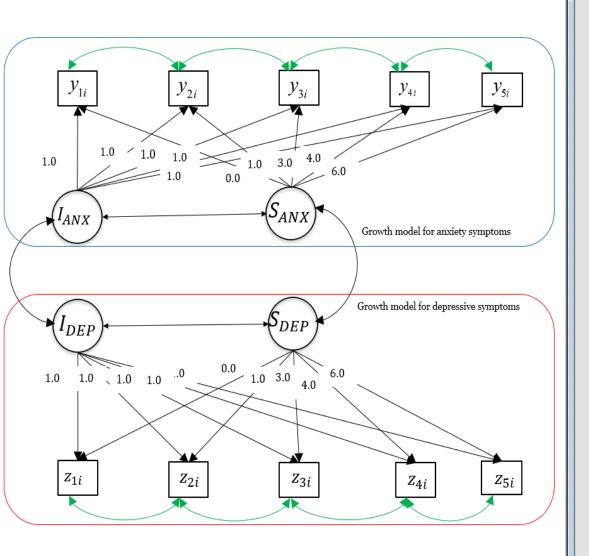
v.	I_DEP WITH S_DEP	0.005
vi.	S ANX WITH S DEP	0.004***



1.0



- Each measure consist of
 - . Item-specific variance component
 - ii. Time-specific variance component
 - Item-specific variance component =
 measurement error (within subdomain
 error correlations autocorrelated
 errors)
 - Autocorrelated error capture unique and methodological biases within a measure (e.g., due to repeated administration, reporting biases)

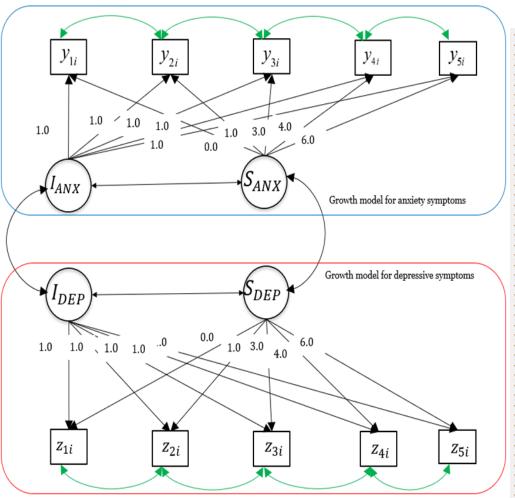


```
USEVARIABLES ARE
       anx1 anx2 anx3 anx4 anx5
       dep1 dep2 dep3 dep4 dep5;
MISSING ARE ALL (-999);
ANALYSIS:
    ESTIMATOR = ML;
    MODEL = NOCOV;!Suppress Mplus default correlations between the growth fa
                  !That way, you have control over what variables you want t
MODEL:
    I ANX S ANX anx 100 anx 201 anx 303 anx 404 anx 506; lanxiety symptoms growth
    I DEP S DEP dep100 dep201 dep303 dep404 dep506;!depressive symptoms
    !Correlate the growth factors
    I ANX WITH S ANX;
    I DEP WITH S DEP;
    I ANX WITH I DEP;
    S ANX WITH S DEP;
    !Within subdomain autocorrelations
    anx1 anx2 anx3 anx4 PWITH anx2 anx3 anx4 anx5 (an); !PWITH means pair w:
    dep1 dep2 dep3 dep4 PWITH dep2 dep3 dep4 dep5 (dp);
```

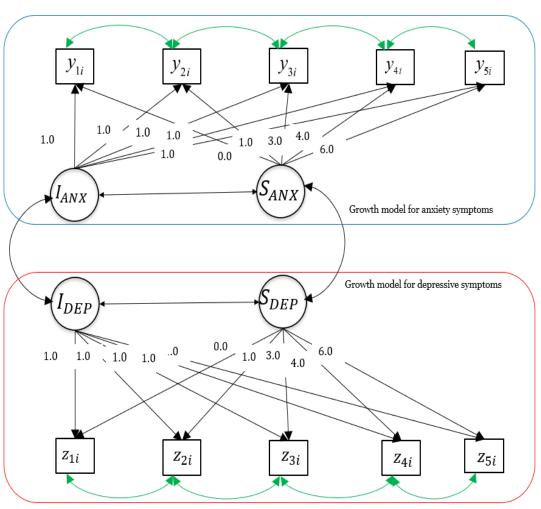
OUTPUT:

SAMPSTAT;

Frederick Anyan, PhD - NTNU



```
324 # 010_2_Parallel growth curve models - anxiety and depression symptoms with autocorrelations
    parallelautocor \leftarrow ' ia \Rightarrow 1*anx1 + 1*anx2 + 1*anx3 + 1*anx4 + 1*anx5
                          sa = 0*anx1 + 1*anx2 + 3*anx3 + 4*anx4 + 6*anx5
327
                         id = 1*dep1 + 1*dep2 + 1*dep3 + 1*dep4 + 1*dep5
328
                         sd = 0*dep1 + 1*dep2 + 3*dep3 + 4*dep4 + 6*dep5
329 #Growth factor corelations
330 ia ~~ id + sa
331 sd ~~ id + sa
332 ia ~~ 0*sd
333 id ~~ 0*sa
334
335 #Autocorrelations
336 anx1 ~ ega*anx2
337 anx2 ~~ eqa*anx3
338 anx3 ~~ eqa*anx4
339 anx4 ~ eqa*anx5
340
341 dep1 ~~ eqd*dep2
342 dep2 ~~ eqd*dep3
343 dep3 ~~ eqd*dep4
344 dep4 ~~ eqd*dep5
345
346 fit_parallelautocor <- growth(parallelautocor, data = data)
347 summary(fit_parallelautocor, fit.measures = TRUE)
```



Model fit:

 $(\chi^2 = 813.952, df = 41; p < .001; RMSEA = .242 [90\% CI = 0.228, 0.257]; CFI = .586; TLI = .546)$

Parameter estimates:

Anxiety symptoms

i. Intercept: 1.395***
ii. Slope: -0.031***

Depression symptoms

i. Intercept: 1.544***
ii. Slope: -0.014**

(Co) Variances:

Anxiety symptoms

i. Intercept: 0.084***ii. Slope: 0.001

Depression symptoms

i. Intercept: 0.156***ii. Slope: 0.001

iii. I_ANX WITH S_ANX 0.003

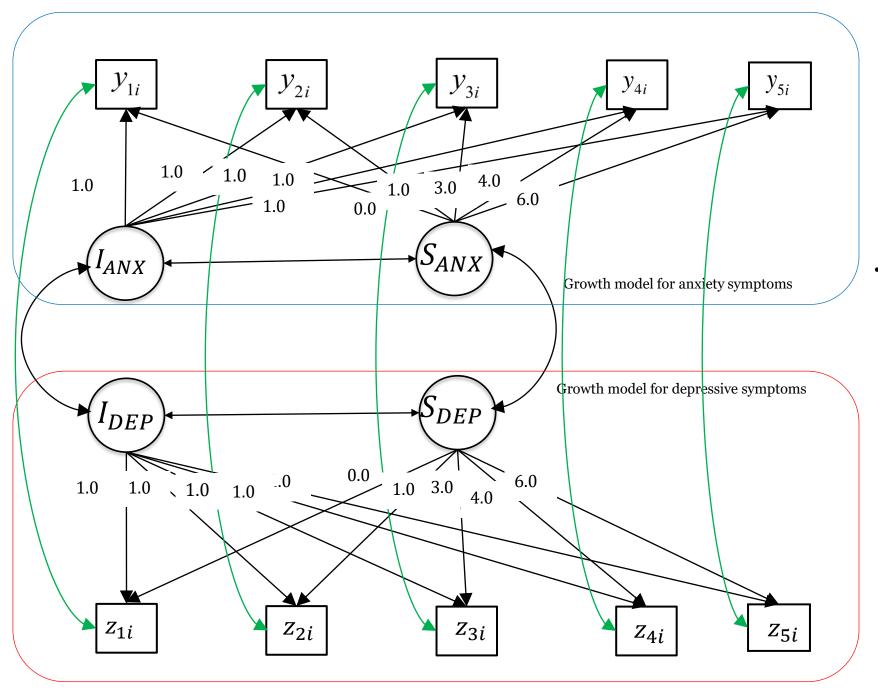
iv. I_ANX WITH I_DEP 0.124***

v. I_DEP WITH S_DEP 0.007*

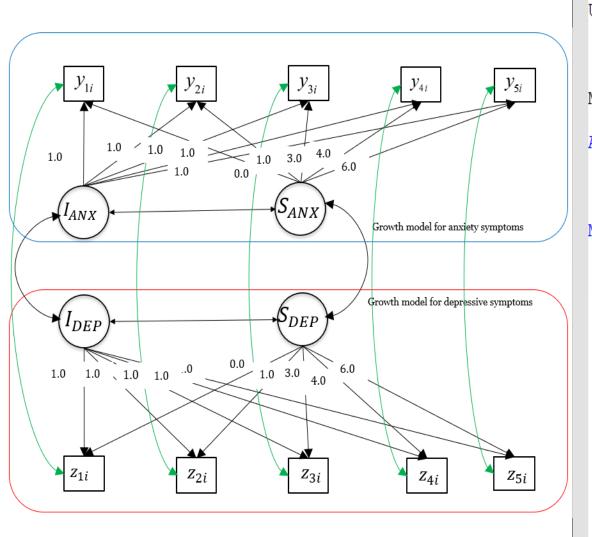
i. $S_ANX WITH S_DEP$ 0.004***

Autocorrelations

i. Anxiety 0.012*ii. Depression 0.013



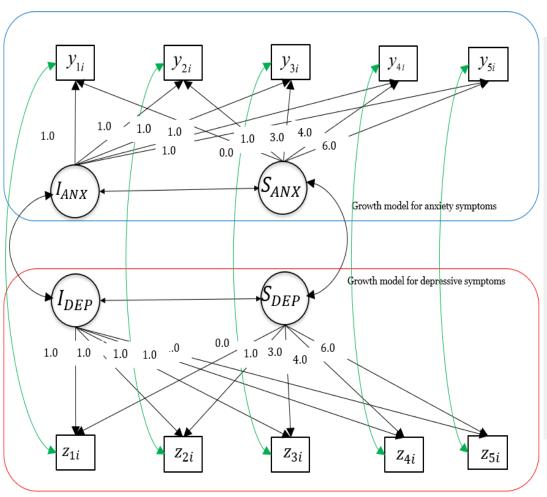
- Each measure consist of
 - . Item-specific variance component
 - ii. Time-specific variance component
- ii. Time-specific variance component = between subdomains
 - Attributed to time-specific trends/patterns reporting biases (e.g., reporting lower level of symptoms at first timepoint)



```
USEVARIABLES ARE
       anx1 anx2 anx3 anx4 anx5
       dep1 dep2 dep3 dep4 dep5;
MISSING ARE ALL (-999);
ANALYSIS:
    ESTIMATOR = ML;
    MODEL = NOCOV;!Suppress Mplus default correlations between the growth
                  !That way, you have control over what variables you want
MODEL:
    I ANX S ANX anx100 anx201 anx303 anx404 anx506; anxiety symptoms growt
    I DEP S DEP|dep1@0 dep2@1 dep3@3 dep4@4 dep5@6;!depressive symptoms
    !Correlate the growth factors
    I ANX WITH S ANX;
    I DEP WITH S DEP;
    I ANX WITH I DEP;
    S ANX WITH S DEP;
    !Cross subdomain correlations
    anx1 anx2 anx3 anx4 anx5 PWITH dep1 dep2 dep3 dep4 dep5 (cros);!Label
```

OUTPUT:

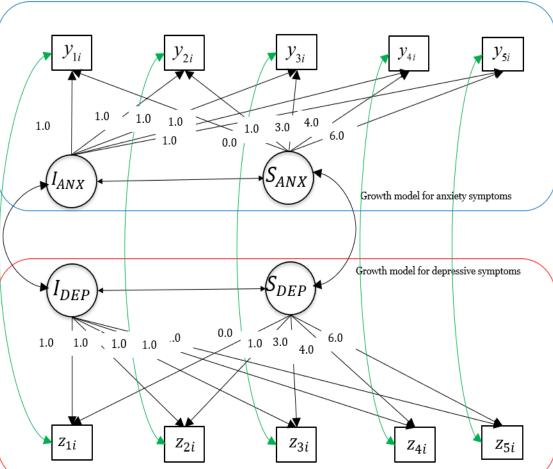
SAMPSTAT;



```
350 # 010_3_Parallel growth curve models - anxiety and depression symptoms with cros
351 parallelcross <- ' ia =~ 1*anx1 + 1*anx2 + 1*anx3 + 1*anx4 + 1*anx5
352
                       sa = 0*anx1 + 1*anx2 + 3*anx3 + 4*anx4 + 6*anx5
353
                       id = 1*dep1 + 1*dep2 + 1*dep3 + 1*dep4 + 1*dep5
354
                       sd = 0*dep1 + 1*dep2 + 3*dep3 + 4*dep4 + 6*dep5
355 #Growth factor corelations
356 ia ~~ id + sa
357 sd ~~ id + sa
358 ia ~~ 0*sd
359 id ~~ 0*sa
360
361 #Cross domain correlations
362 anx1 ~~ eq*dep1
363 anx2 ~ eq*dep2
364 anx3 ~~ eq*dep3
365 anx4 ~~ eg*dep4
366 anx5 ~~ eq*dep5
367
368 fit_parallelcross <- growth(parallelcross, data = data)
369 summary(fit_parallelcross, fit.measures = TRUE)
```

Model fit:

 $(\chi^2 = 178.746, df = 42; p < .001; RMSEA = .101[90\% CI = 0.086, 0.116]; CFI = .927; TLI = .922)$



arameter estimates:

nxiety symptoms

Intercept: 1.399***
Slope: -0.030***

epression symptoms

Intercept: 1.552***

Slope: -0.013*

Co) Variances:

nxiety symptoms

Intercept: 0.085***

Slope: 0.001*

epression symptoms

Intercept: 0.144***

Slope: 0.000

i. I_ANX WITH S_ANX -0.004**

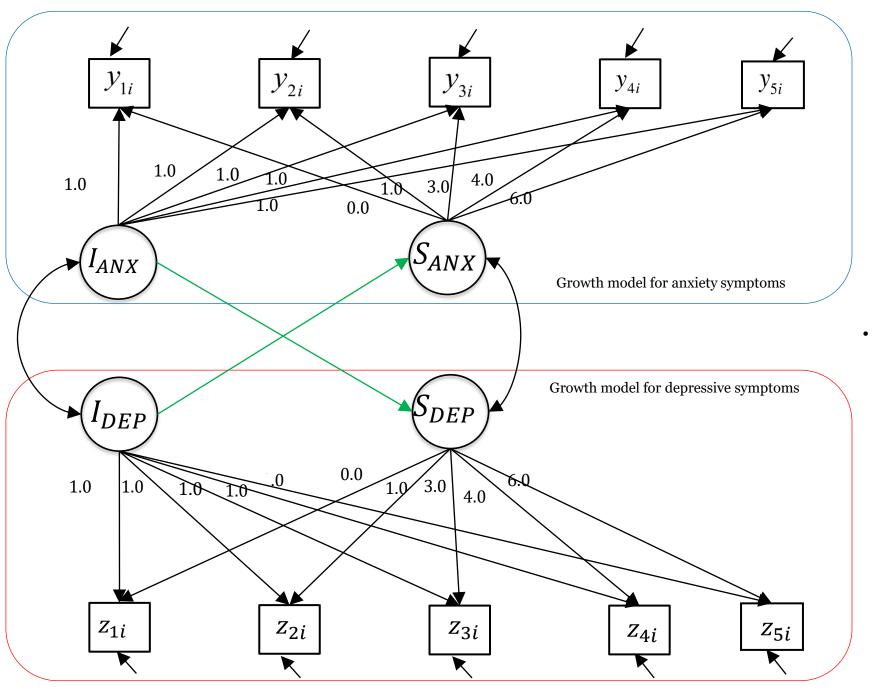
I_ANX WITH I_DEP 0.082***

I_DEP WITH S_DEP -0.002

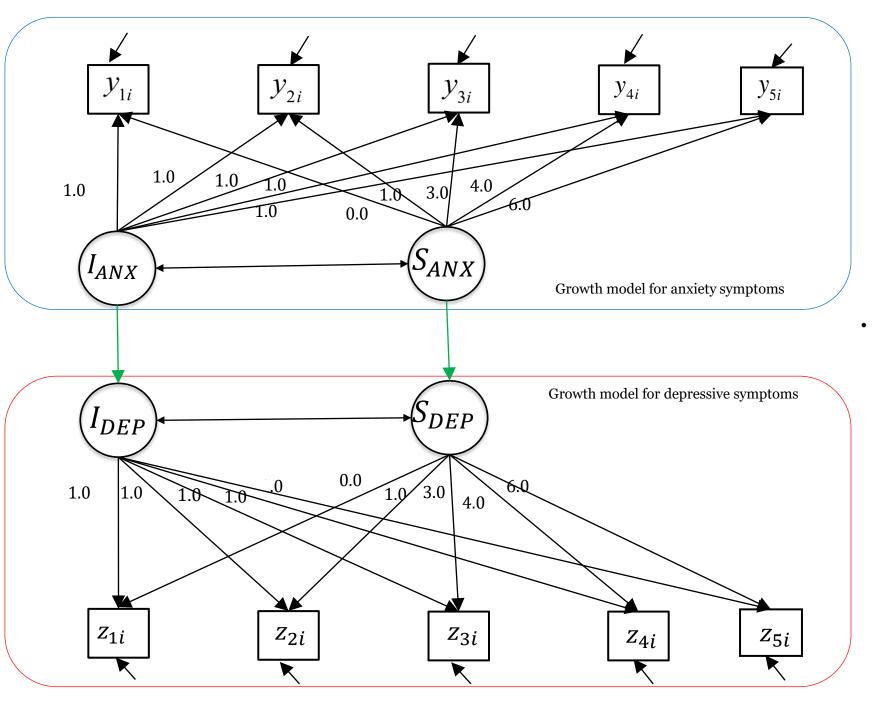
S_ANX WITH S_DEP 0.000

Cross-domain correlations

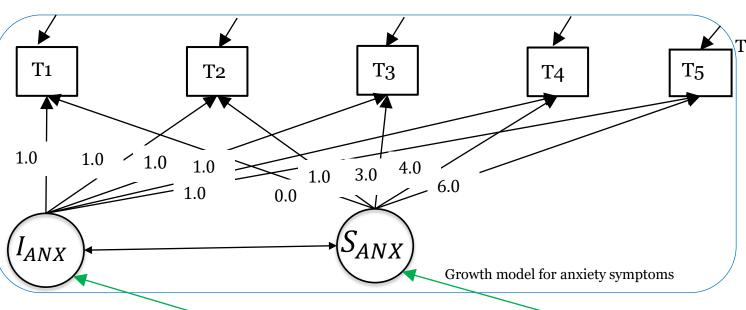
i. Anxiety - Depression 0.098***



- Parallel growth process with regressions of the slope growth factor
 - Higher initial levels of anxiety symptoms influence the growth rate of depressive symptoms?
 - Higher initial levels of depression symptoms influence the growth rate of anxiety symptoms



- Parallel growth process with unidirectional effects
 - Evidence of co-development
 - Influence of growth factors of one subdomain on the growth factors of another subdomain



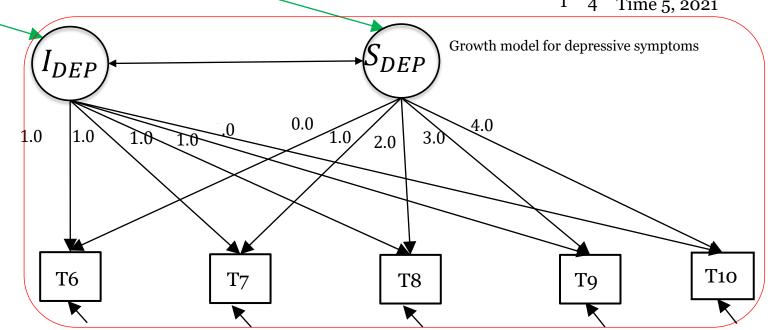
Time scores/factor loading matrix

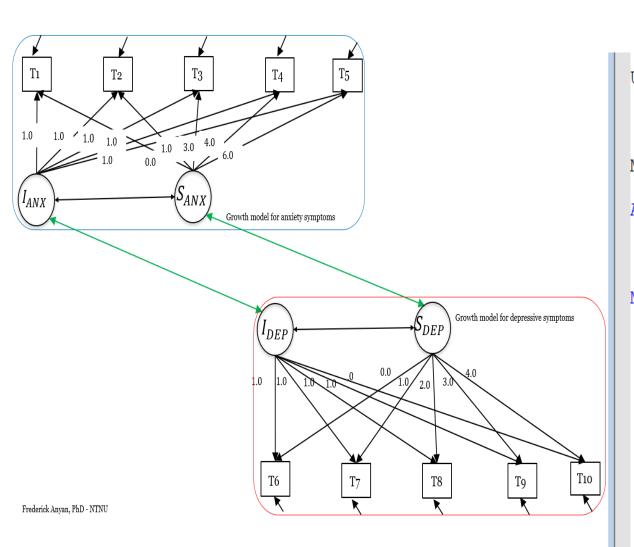
- Time 1, 2010
- Time 2, 2011
- Time 3, 2013
- Time 4, 2014
- Time 5, 2016

Time scores/factor loading matrix

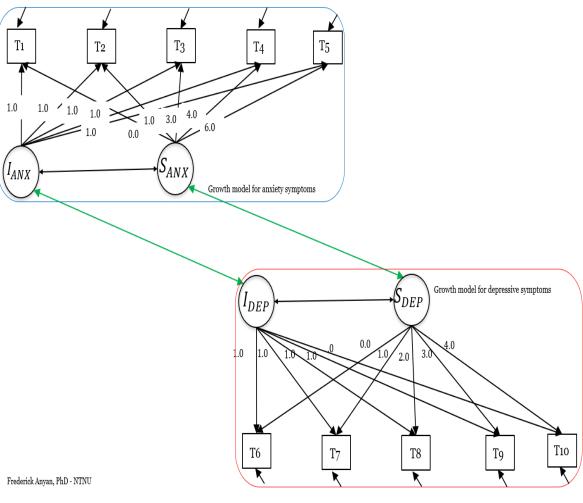
- Time 1, 2017
- Time 2, 2018
- Time 3, 2019
- Time 4, 2020
- Time 5, 2021

- Sequentially contingent process over time
 - One growth trajectory influencing a later growth trajectory
 - Change in one subdomain (T1-T5) predicting change in another subdomain(T6-T10)
 - Life-course studies

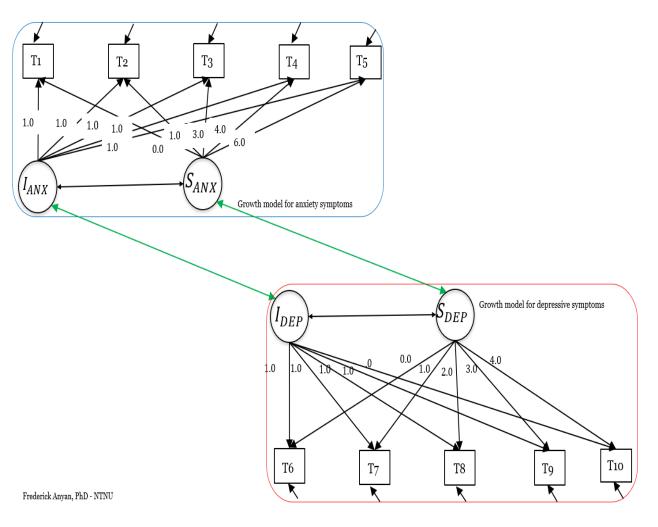




```
USEVARIABLES ARE
       anx1 anx2 anx3 anx4 anx5
       dep6 dep7 dep8 dep9 dep10;!Time of observations modified for ped
MISSING ARE ALL (-999);
ANALYSIS:
    ESTIMATOR = ML;
    MODEL = NOCOV; !Suppress Mplus default correlations between the grow
                   !That way, you have control over what variables you w
MODEL:
    I ANX S ANX anx100 anx201 anx303 anx404 anx506; lanxiety symptoms gr
    I DEP S DEP dep 600 dep 701 dep 802 dep 903 dep 1004; ! Equidistant time s
    !Correlate the growth factors
    I ANX WITH S ANX;
    I DEP WITH S DEP;
    !Add sequentially contingent growth factors
    I ANX WITH I DEP;
    S ANX WITH S DEP;
OUTPUT:
    SAMPSTAT;
```



```
375 # 011_Sequentially contigent growth curve model anxiety t1-t5 predicting depress
376 sequential < ' ia = 1*anx1 + 1*anx2 + 1*anx3 + 1*anx4 + 1*anx5
377
                    sa = 0*anx1 + 1*anx2 + 3*anx3 + 4*anx4 + 6*anx5
                    id = 1*dep6 + 1*dep7 + 1*dep8 + 1*dep9 + 1*dep10
378
                    sd = 0*dep6 + 1*dep7 + 2*dep8 + 3*dep9 + 4*dep10
379
380
381 #Growth factor corelations
382 ia ~~ sa
383 id ~~ sd
384 ia ~~ 0*sd
385 id ~~ 0*sa
386
387 #Correlate growth factors across domain (may use regressions depending on theory
388 ia ~~ id
389 sa ~~ sd
390 '
391 #Rename multiple columns using rename()
392 # We rename them to pretend that these variables are actually measured
393 # at a later date.
394 library(dplyr)
    data <- data %>%
      rename("dep6" = "dep1",
396
397
             "dep7" = "dep2",
398
             "dep8" = "dep3",
399
             "dep9" = "dep4",
400
             "dep10" = "dep5")
401
402 fit_sequential <- growth(sequential, data = data)
403 summary(fit_sequential, fit.measures = TRUE)
```



Model fit:

 $(\chi^2 = 825.260, df = 43; p < .001; RMSEA = .238[90\% CI = 0.224, 0.252]; CFI = .581; TLI = .562)$

Parameter estimates:

Anxiety symptoms

i. Intercept: 1.397***

i. Slope: -0.032***

Depression symptoms

i. Intercept: 1.546***

ii. Slope: -0.021**

(Co) Variances:

Anxiety symptoms

Intercept: 0.097***

ii. Slope: 0.002***

Depression symptoms

i. Intercept: 0.171***

i. Slope: 0.005**

iii. I_ANX WITH S_ANX 0.000

iv. I_ANX WITH I_DEP 0.124***

v. I_DEP WITH S_DEP 0.007

vi. S_ANX WITH S_DEP 0.005***

Course/workshop evaluations Click here