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1. Code

```
function divideAndConquerSum (a) {  
  if (a.constructor == Array) {  
  
    if (a.length == 0) {  
      return 0;  
    }  
  
    if (a.length == 1) {  
      return a[0];  
    }  
  
    else {  
      return divideAndConquerSum(a.splice(0,1)) +  
divideAndConquerSum(a.splice(0,1)) + divideAndConquerSum(a.splice(0));  
    }  
  }  
  
  else {  
    console.log("Function argument must be an array.");  
  }  
}
```

2. $T(n)$

Let n be the number of elements in the array. In the base case, where $n = 0$, it is clear that $T(0) = \Theta(1)$. In general, $T(n) = \Theta(2) + T(n - 2)$. I solve the recurrence relation below.

$$T(n) = \Theta(2) + T(n - 2)$$

$$\begin{aligned}
&= 2 + T(n - 2) \\
&= 2 + [2 + T(n - 4)] \\
&= 4 + T(n - 4) \\
&= 4 + [2 + T(n - 6)] \\
&= 6 + T(n - 6) \\
&= \dots
\end{aligned}$$

It is clear that the number of operations increases linearly with n . k is a constant factor. Since we have $T(0) = \Theta(1) = 1$, we allow $n - k = 0$.

$$\begin{aligned}
&= k + T(n - k) \\
&= n + T(0) \\
&= n + 1 \\
&= \Theta(n)
\end{aligned}$$