

Section 2

- Review data types in OCaml
- Abstract syntax trees
- Recursion recipe for CS162

Data types in OCaml

only 2 kinds =>

only need to know

2 things



How to build ?

Product type

Example:

`int * string`

Logically: AND

Q1

`(a , b)`

Enum type

Example:

`type t = I of int
| S of string`

Logically: XOR

Q3

`I 123`

or `S "hi"`

`I 123`

`S "hi"`

How to use ?

Q2

`let (x,y) = p in ...`

`match p with`

`| (x,y) → ... x .. y ...`

Q4

`match x with`

`| I x → ... x ...`

`| S x → ... x ...`

Useful predefined data types

1) 'a option = None | Some of 'a

2) 'a list = [] | (::) of 'a * 'a list
(Nil) (cons)

Generic types

Instead repeating the same type def over & over,
define one template:

type int-option
= Some of int | None
type bool-option
= Some of bool | None
...

type □ option = Some of □
↑
hole | None.

which can be instantiated into

int option, bool option, string option,
(int option) option, ...

Abstract Syntax Trees

Code

```
def fact(n):
    if n==0
        return 1
    else:
        return n * fact(n-1)
```

Multiple representations

string representation

"def fact(n): \n if ..."

Good for:

- + Coding using keyboard
- + storage

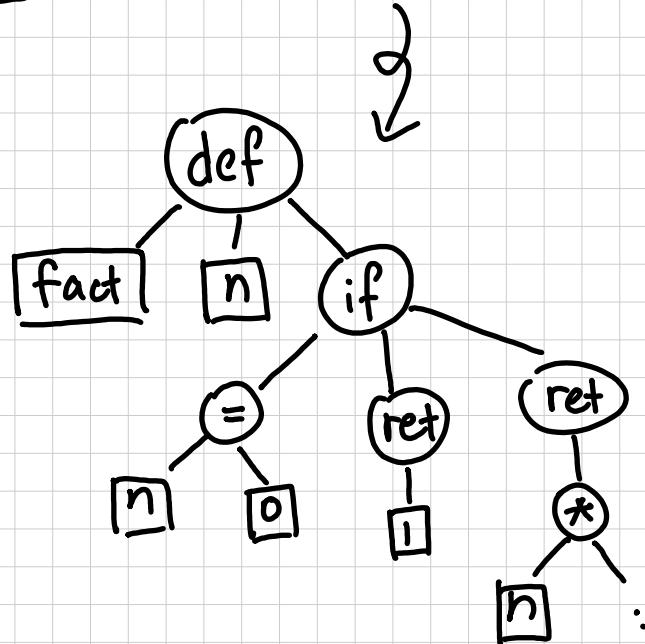
Bad for:

- everything else

String representation

parser

```
def fact(n):
    if n=0:
        return 1
    else:
        return n * fact(n-1)
```



abstract syntax tree (AST)

In CS162, we define language ASTs using context-free grammars (CFG).

A CFG can be easily represented using an OCaml data type.

Example

Language: simple calculator language

CFG :

expr = INT
| expr + expr
| expr - expr
| expr * expr

OCaml type :

type expr = EInt of int
| EAdd of expr * expr
| ESub of expr * expr
| EMul of expr * expr

(isomorphic)

The exact labels don't matter.

An equivalent encoding:

type op = Add | Sub | Mul

type expr = EInt of int

| EArih of expr * op * expr .

Recursion Recipe for CS162

(Pre) 1. Identify the structure of the data:

e.g. 'a list = Nil | Cons of 'a * 'a list

(Free) 2. Decompose data into base case
+ recursive case
using pattern matching

(Easy) 3. Handle base case

4. Handle recursive case

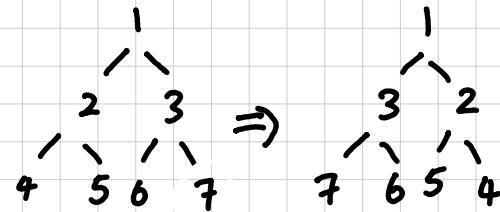
(Free) i) Call function on "smaller data"

ii) Assume that the result of ↴ is correct

compose solution to "bigger data"

only potential
difficult part

Example: Mirror a binary tree.



(1) type tree = Leaf of int
| Node of int * tree * tree

(2) let rec mirror t =
match t with
| Nil → (3) Nil
| Cons(n, l, r) →

(4i)
let l' = mirror l in

let r' = mirror r in

(4ii)
Node(n, r', l')

Assume
 $\text{mirror} \left(\begin{array}{c} 3 \\ 7 \ 6 \end{array} \right) = \begin{array}{c} 3 \\ 6 \ 7 \end{array} = l'$

$\text{mirror} \left(\begin{array}{c} 2 \\ 5 \ 4 \end{array} \right) = \begin{array}{c} 2 \\ 4 \ 5 \end{array} = r'$

Extended example:

Compute the cartesian product of two lists.

product [1 ; 2 ; 3] ["a" , "b" , "c"]
= [(1, "a") ; (1, "b") ; (1, "c") ;
(2, "a") ; (2, "b") ; (2, "c") ;
(3, "a") ; (3, "b") ; (3, "c")]

① Identify the data structure:

type list = Nil | Cons of *

② Decompose the input:

let rec product (l₁: int list) (l₂: string list) : ((int * String) list) list =

match l₁ with

| Nil → (③ exercise for you)

| Cons(h₁, t₁) →

(④ i) let res = product t₁ l₂ in

let first_row = row h₁ l₂ in

first_row @ res follow the recipe again!

Visually:

	a	b	c
1	1,a	1,b	1,c
2	2,a	2,b	2,c
3	3,a	3,b	3,c

Visually:

	a	b	c
1	1,a	1,b	1,c
2	2,a	2,b	2,c
3	3,a	3,b	3,c

= res

Let's define $\text{row } 1 \quad ["a"; "b"; "c"]$
 $= [(1, "a"); (1, "b"); (1, "c")]$

① 'a list = Nil | Cons of 'a * 'a list

② let rec row (x: int) (l: string list) : (int * string) list =

match L with

| Nil \rightarrow ③ Nil

| Cons(h, t) \rightarrow

④ i let res = row x t in

(x, h) :: t

$x=1$ $l=[\underline{a}, \underline{b}, \underline{c}]$

so assume $\text{row } x \ t$

$= [(1, b); (1, c)]$

want $[(1, a); (1, b); (1, c)]$

Extended example:

Compute the power set of a list.

$[1; 2; 3]$ \Rightarrow

$[[];$

$[1]; [2]; [3];$

$[1; 2]; [1; 3]; [2; 3];$

$[1; 2; 3]$]

① $\text{list} = \dots$

let rec power (ℓ : int list) : (int list) list =

② match ℓ with

| Nil \rightarrow (③ exercise for you)

| Cons(h , t) \rightarrow

(4i) let res = power t in

(4ii) let res' = insert h res in

res @ res'

Now you can define insert recursively
using the recipe again (exercise)

let's say $\ell = [1; 2; 3]$
 $h \uparrow$
 $t \uparrow$

So assume

res = power $[2; 3]$

= $[[], [2], [3], [2; 3]]$

Still Missing this,
but we can get
this by inserting 1
at the beginning of every
list in res.

want

$[[], [2], [3], [2; 3], \checkmark^{res}]$
 $\{[1], [1; 2], [1; 3], [1; 2; 3]\}$