## Precise reference counting for lazy functional languages with interprocedural points-to analysis

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## Abstract

Precise reference counting is a technique by Reinking et al. that uses ownership to deallocate objects as soon as possible. The algorithm is called Perceus, and as of this writing, it has only been implemented for eager functional languages. This paper describes the implementation of a new lazy compiler backend for the Agda programming language with precise reference counting. The compiler uses Johnsson and Boquist's intermediate language GRIN to compile lazy programs. GRIN uses an interprocedural points-to analysis to inline the evaluation of suspended computations. We extend GRIN with a variant of Perceus, and demonstrate the applicability of combining lazy functional programming with precise reference counting by developing a GRIN interpreter and an LLVM IR code generator. Due to GRIN and reference counting, our compiler does not require an external runtime system<sup>1</sup>, which is uncommon for lazy functional languages.

## 1 Introduction

Reference counting (Collins, 1960) is a memory management technique which can detect and free resources as soon as they are no longer needed, allowing memory reuse and destructive updates. Common reference counting algorithms are easy to implement; each allocation contains an extra field which tracks the number of references to an object. When the reference count reaches zero, the heap space occupied by the object is reclaimed. The number of references to a object is updated

by interleaved reference counting operations (dup and drop), which increments and decrements the reference count at runtime. As a result of the interleaved collection strategy, memory usage remain low and the throughput is continuous throughout the computation<sup>2</sup> (R. Jones & Lins, 1996). Still, tracing garbage collectors are usually favored over reference counting implementations due to cheaper allocations, higher throughput, and the ability to collect cyclic data structures.

Reinking et al. (2021) reexamine reference counting with a new approach, utilizing static guarantees to make the algorithm *precise* so objects can be deallocated as soon as possible. They present a formalized algorithm called Perceus, which ensures precision. Perceus is implemented in the functional language Koka, along with optimizations for reducing reference counting operations and reusing memory. This, builds upon previous work by Ullrich and de Moura (2021) in the Lean programming language and theorem prover.

Both Koka and Lean are, however, eagerly evaluated. Lazy languages pose an extra challenge for compiler writers because of the unintuitive control flow. Additionally, previous implementations of lazy languages require an external runtime system to manage evaluation of suspended computation and garbage collection (Augustsson, 1984; Johnsson, 1984; P. Jones et al., 1992; Turner, 1979). Johnsson (1991), presents a method for evaluating suspended computations without an external runtime system. This is accomplished in the intermediate language GRIN which can express evaluation of suspended computations as a regular pro-

 $<sup>^{1}\</sup>mathrm{Besides}$  initialization code (crt0) and the C standard library, libc.

<sup>&</sup>lt;sup>2</sup>Reference counted programs may introduce pauses similar to tracing garbage collectors. For example, when dropping a long linked list all at once.

cedure. In this paper, we extend GRIN with a variant of the Perceus algorithm. This allivates the requirement of an external runtime system because memory is automatically managed by interleaved reference counting operations — similarly to how GRIN can express evaluation suspended computations within the language. We implement these ideas in a new compiler backend for the Agda programming language and proof assistant.

## 2 Graph Reduction Intermediate Notation

In 1991, Johnsson presented the Graph Reduction Intermediate Notation (GRIN) as an imperative version of the G-machine (Johnsson, 1984), where lexically scoped variables are stored in registers instead of the stack. Later, GRIN was reformulated with a more functional flavor (Boquist, 1995). In this project, we introduce an additional variant of GRIN adapted for the internal representation of Agda and precise reference counting. The syntax of our variant is shown in Figure 1.

A defining feature of GRIN is that suspended computations (closures) and higher-order functions are defunctionalized (Reynolds, 1972), by an interprocedural analysis called the heap points-to analysis. As a result, all unknown function calls are eliminated. Due to defunctionalization, all GRIN values are weak head normal forms. However, in order to destinquish between complex values (closures) and simple values (literals and data types), future mentions of suspended computation and weak head normal form refer to the representation in the corresponding Agda program.

#### 2.1 Code generation

Currently, our compiler only accepts a subset of Agda which is lambda lifted, first-order, and monomorphic.<sup>3</sup> Following is an Agda program that computes the sum of the first 100 numbers in descending order.

```
\begin{array}{l} \operatorname{downFrom}: \, \mathbb{N} \to \operatorname{List} \, \mathbb{N} \\ \operatorname{downFrom} \, \operatorname{zero} = [] \\ \operatorname{downFrom} \, (\operatorname{suc} \, n) = n :: \operatorname{downFrom} \, n \\ \\ \operatorname{sum}: \, \operatorname{List} \, \mathbb{N} \to \mathbb{N} \\ \operatorname{sum} \, [] = 0 \\ \operatorname{sum} \, (x :: xs) = x + \operatorname{sum} \, xs \\ \\ \operatorname{main} = \operatorname{sum} \, (\operatorname{downFrom} \, 100) \end{array}
```

Before generating GRIN code, the program is tranformed into an untyped lambda calculus with let and case expressions called Treeless (Hausmann, 2015). The Treeless intermediate language uses administrative normal form, which means that the case scrutinee is always a variable, and the patterns cannot be nested or overlap. Following is the Treeless representation of downFrom (1). The implementation uses de Bruijn indices to represent variables, but this paper uses variable names to make it human readable.

downFrom x7 = case x7 of  

$$0 \rightarrow []$$
  
 $\rightarrow let x5 = 1$   
 $x4 = -- x7 x5$   
 $x3 = downFrom x4 in$   
 $\therefore x4 x3$  (2)

When compiling Treeless to GRIN we need to be explicit about evaluation of suspended computations and memory operations. GRIN uses a builtin state monad to sequence computations. The monadic operations are unit, bind (written ";"), store, fetch, and update. For example, to compile the Treeless expression

```
let x = val in foo x
```

lazily, we allocate the value and pass the pointer as an argument to the function

store val ; 
$$\lambda$$
  $\mathbf{x}_{ptr}$   $\rightarrow$  foo  $\mathbf{x}_{ptr}$ 

Here, val must be a constant node value, which is a tag followed by a sequence of arguments (see Figure 1). We can pattern match on a tag with the case expression to determine the kind. Tags are prefixed with either a C if it is a constructor value or an F for suspended function applications. The node arguments are usually pointers to other heap-allocated nodes, but they can also be unboxed values. For example, the boxed integer tag Cnat accepts one unboxed integer. Following is the corresponding GRIN representation of downFrom (2).

<sup>&</sup>lt;sup>3</sup>Some lambda expressions and higher-order functions compile successfully because they are reduced to another representation during optimization. See Section 5 for an example.

```
term ::= term ; \lambda lpat \rightarrow term
                                              binding
              \verb|case| val of term \{calt\} *
                                              case
              val \{val\}*
                                              application
              \mathtt{unit}\ val
                                              return value
              \mathtt{store}\; val
                                              allocate new heap node
              \mathtt{fetch}\; \{tag\}\; n\; \{i\}
                                              load heap node
              \mathtt{update}\ \{tag\}\ n\ \{i\}\ val
                                              overwrite heap node
              unreachable
                                              unreachable
val \ ::= \ tag\left\{val\right\} *
                           constant\ node
            n \{val\} *
                           variable node
                           single tag
            tag
            ()
                           empty
            lit
                           literal
                           variable (de Bruijn index)
                           function definition
            def
            prim
                           primitive definition
lpat \ ::= \ tag \ \{x\} *
                          constant node pattern
             x \{x\}*
                          variable node pattern
             ()
                          empty pattern
                          variable pattern
                          constant node pattern
             tag \{x\}*
cpat ::=
                           single tag pattern
             tag
             lit
                           literal pattern
        means 0 or 1 times
\{...\}* means 0 or more times
```

Figure 1: GRIN syntax.

Note the explicit call to eval prior to the case expression which forces weak head normal form.

```
downFrom x7 =
  eval x7 ; λ Cnat x6 →
  case x6 of
    0 → unit (C[])
    _ →
        store (Cnat 1) ; λ x5 →
        store (F_- x7 x5) ; λ x4 →
        store (FdownFrom x4) ; λ x3 →
        unit (C_::_ x4 x3)
```

### 2.2 Interpreter

The semantics of our language are presented in Figure 2. We use two semantic functions,  $\mathcal{E}$  and  $\mathcal{V}$ , to assign semantic values to terms and syntactic values, respectively. The semantics values are are a subset of the syntactic values with an additional construct representing undefined behaviour  $(\bot)$ . Moreover, we have a new construct for heap allocated nodes. A heap allocated node consist of a reference count, a tag, and a sequence of values.

We have implemented the semantics as an interpreter, to test that transformations do not change the semantics of the program. Due to the lower level of GRIN, we can also collect information about resource usage. For instance, our example program (1) allocates the following nodes: 101 Cnat, 101 FdownFrom, 100 F\_-, and 100 Fsum. In total, our program allocates 402 nodes and the worst-case bound for heap consumption is 202 nodes. With 16 this information we can estimate the performance characteristics of the program and identify optimization opportunities (more on this in Section 5).

```
SemVal = tag \{val\}* | tag | loc | () | lit | \bot
HeapNode = ref\text{-}count \ tag \{val\}*
Stack = Var \rightarrow Loc
Heap = Loc \rightarrow HeapNode
\mathcal{E}: Stack \rightarrow Heap \rightarrow Term \rightarrow SemVal \times Heap
\mathcal{V}: Stack \rightarrow Val \rightarrow SemVal \times Heap
```

Figure 2: GRIN semantics.

## 2.3 Analysis and transformations

The most important GRIN transformation is eval inlining. eval is a normal GRIN function which forces a suspended computation to weak head normal form. For instance, "eval x7 ;  $\lambda$  Cnat x6  $\rightarrow$  ..." (3) evaluates the value at the pointer x7 to a boxed integer Cnat x6. Eval inlining generates a specialized eval function for each call site. Following (4) is the eval-inlined version of downFrom (3). To evaluate a suspended computation, we load the node from the heap using fetch (line 2). Then, we pattern match on the possible nodes. Constructor nodes are already in weak head normal form so they are left unchanged (line 4). Function nodes are evaluated by applying the corresponding function to the arguments (line 5). Finally, the heap is updated with the evaluated value (line 7).

```
1 downFrom x7 =
     (fetch x7; \lambda x34 \rightarrow
       (case x34 of
           Cnat x36 → unit (Cnat x36)
           F_{-} = x37 x38 \rightarrow _{-} x37 x38
       ); λ x35 →
       update x7 x35 ; \lambda () \rightarrow
       unit x35
                                                         (4)
     ); \lambda Cnat x6 \rightarrow
     case x6 of
        0 → unit (C[])
           store (Cnat 1); \lambda x5 \rightarrow
           store (F_-_ x7 x5) ; \lambda x4 \rightarrow
           store (FdownFrom x4) ; \lambda x3 \rightarrow
           unit (C_::_ x4 x3)
```

The pattern-matching step (lines 3-5) requires a set of possible nodes for each abstract heap location. One option is to pattern match on all the possible nodes, but this does not scale to large programs. Instead, we use the *heap points-to* analysis (Johnsson, 1991) to create a conservative approximation.<sup>4</sup> The analysis is interprocedural, meaning that multiple functions need to be analyzed together. We will not go into detail about the algorithm, as it is thoroughly described in (Boquist & Johnsson, 1996; Johnsson, 1991). Instead, this paper will only provide a general intuition of the algorithm. Consider the inlined evaluation in downFrom (4). There

 $<sup>^4{</sup>m The}$  analysis does not consider the context or order (flow) of operations, which means that certain phases of the analysis can be executed in parallell and cached.

are two tags in the case expression: F<sub>-</sub> (line 4) and Cnat (line 5). The former comes from the suspended recursive call inside downFrom (line 15). The latter is from the **update** operation (line 7), and the suspended call to downFrom (line 3) in the main function:

```
main = 

store (Cnat 100); \lambda x20 \rightarrow

store (FdownFrom x20); \lambda x19 \rightarrow (5)

sum x19; \lambda Cnat x18 \rightarrow

printf x18
```

Boquist's thesis presents 24 transformations divided into two groups: simplifying transformations and optimizing transformations (Boquist, 1999). The simplifying transformations are necessary for the LLVM IR code generator and are all implemented, except inlining calls to apply which is used for partially applied functions. The optimizing transformations significantly alter the program and achieve similar effects to deforestation (Wadler, 1988) and listlessness (Wadler, 1984). Of these, we have only implemented copy propagation. This project aims to combine lazy functional programming with precise reference counting. Producing the most optimized code is out of scope. However, this is something we would like to explore in future research.

## 3 Precise reference counting

After the GRIN transformations, we insert reference counting operations to automatically manage memory. We use an algorithm based on Perceus (Reinking et al., 2021). Perceus is a deterministic syntax-directed algorithm for the linear resource calculus  $\lambda_1$ , which is an untyped lambda calculus extended with explicit binds and pattern matching. Our implementation uses GRIN which have explicit memory operations and different calling conventions. In this section, we give a brief overview of the algorithm and describe two optimizations: drop specialization and dup/drop fusion. We also discuss some challenges when adapting Perceus to GRIN in Section 3.1.

The algorithm uses two sets of resource tokens; an owned environment  $\Gamma$  and a borrowed environment  $\Delta$ . Elements in the owned environment must be consumed exactly once. We consume a value by calling the function drop, or by transferring ownership to another consumer. An example of this is main (5) which requires no reference counting operations because it transfers ownership of both of its allocations. The allocation "store (Cnat 100);  $\lambda$  x20  $\rightarrow$ " (line 2) is consumed by the suspended computation "store (FdownFrom x20);  $\lambda$  x19  $\rightarrow$ " (line 3), which in turn is consumed by "sum x19" (line 4). Elements in the borrowed environment can only be applied to non-consuming operations, such as pattern matching. We can promote an element from the borrowed environment to the owned environment by calling the function dup.

Figure 3a presents the function sum with reference counting operations inserted and highlighted in gray. Many aspects of adapting Perceus to GRIN are present in sum. On line 2, "fetch x14 [2] ;  $\lambda_{\Gamma}$  x40  $\rightarrow$ " extends the owned environment with a resource token for the variable x40. The resource token is subsequently consumed by "downFrom x40 ;  $\lambda_{\Delta}$  x59 x60 x61  $\rightarrow$ ", which in turn extends the borrowed environment with tokens for x60 and x61. There is no resource token for x59 because the first argument of a node is always a tag, represented by an unboxed integer stored in registers. Similarly, unannotated bindings, such as "update x14 (C[]);  $\lambda$  ()  $\rightarrow$ " (line 6), do not extend any of the environments. Additionally, we can conclude that fetch and update must be borrowing operations, because both use x14 prior to it being dropped (line 7).

As a result of GRIN's explicit memory operations, we can describe the Perceus primitives dup, drop, is-unique, decref, and free with GRIN's existing constructs. GRIN lacks a primitive for deallocating memory, so free is just a foreign function call to libc's free. However, our implementation of drop is unsatisfactory. Nodes of different tags vary in arity and the arguments can be either boxed or unboxed. Therefore, we need to pattern match on all possible tags to drop the child references. This is similar to the problem with a general eval function (Section 2.3). A crucial difference is that drop is recursive, so we cannot always eliminate the general function by specialization and inlining. Still, we can specialize the initial call to drop if tag is known. The points-to analysis already require us to keep track of the possible nodes of each variable, so in practice we can almost always spe-

```
_{1} sum x14 =
                                   fetch x14 [2] ; \lambda_{\Gamma} x40 \rightarrow
                                   downFrom x40 ; \lambda_{\Delta} x59 x60 x61 \rightarrow
                                    {\tt case} x59 {\tt of}
                             5
                                       [] →
                                          update x14 (C[]) ; \lambda () \rightarrow
                             6
                                          drop x14 ; \lambda () \rightarrow
                                         unit (Cnat 0)
                             8
                                       _::_ →
                             9
                                          dup x61 ; \lambda () \rightarrow
                             10
                                          dup x60 ; \lambda () \rightarrow
                                          update x14 (C_::_ x60 x61) ; \lambda () \rightarrow
                            12
                                          drop x14 ; \lambda () \rightarrow
                            13
                                          store (Fsum x61) ; \lambda_{\Gamma} x10 \rightarrow
                             14
                                          + x10 x60
                                               (a) dup/drop insertion
 _{1} sum x14 =
                                                             sum x14 =
       fetch x14 [2] ; \lambda_{\Gamma} x40 \rightarrow
                                                                fetch x14 [2]; \lambda_{\Gamma} x40 \rightarrow
                                                                downFrom x40 ; \lambda_{\Delta} x59 x60 x61 \rightarrow
       downFrom x40 ; \lambda_{\Delta} x59 x60 x61 \rightarrow
 3
       case x59 of
                                                                case x59 of
          [] →
                                                                   [] →
             update x14 (C[]); \lambda () \rightarrow
                                                                      update x14 (C[]); \lambda () \rightarrow
             fetch x14 [0]; \lambda x499 \rightarrow
                                                                      fetch x14 [0] ; \lambda x499 \rightarrow
             (case x499 of
                                                                       (case x499 of
                 1 → free x14
                                                                           1 → free x14
10
                     PSub x499 1 ; \lambda x498 \rightarrow
                                                                              PSub x499 1 ; \lambda x498 \rightarrow
11
                    update x14 [0] x498
                                                                              update x14 [0] x498
             ) ; λ () →
                                                                      ) ; λ () →
             unit (Cnat 0)
                                                                      unit (Cnat 0)
14
          _::_ →
15
                                                                      update x14 (C_::_ x60 x61) ; \lambda () \rightarrow
             dup x61 ; \lambda () \rightarrow
                                                                      fetch x14 [0] ; \lambda x501 \rightarrow
             dup x60 ; \lambda () \rightarrow
17
                                                                      (case x501 of
             update x14 (C_::_ x60 x61) ; \lambda () \rightarrow
18
             fetch x14 [0] ; \lambda x501 \rightarrow
                                                                           1 →
19
             (case x501 of
                                                                              free x14
                  1 →
                                                                              dup x61 ; \lambda () \rightarrow
                     drop x61 ; \lambda () \rightarrow
                                                                              dup x60 ; \lambda () \rightarrow
                     drop x60 ; \lambda () \rightarrow
                     free x14
                                                                              PSub x501 1 ; \lambda x500 \rightarrow
                                                                              update x14 [0] x500
                                                                      ) ; \lambda () \rightarrow
                     PSub x501 1 ; \lambda x500 \rightarrow
26
                    update x14 [0] x500
                                                                      store (Fsum x61) ; \lambda_{\Gamma} x10 \rightarrow
             ); \lambda () \rightarrow
                                                                      _+_ x10 x60
             store (Fsum x61) ; \lambda_{\Gamma} x10 \rightarrow
             _+_ x10 x60
30
                   (b) drop specialization
                                                                  (c) dup push-down and dup/drop fusion
```

**Figure 3:** Perceus transformations

cialize drop.

In Figure 3b, we specialize both calls to drop. This eliminates all reference counting operations in the branch for the empty list (lines 5-14). Then, we push down the dup operations (lines 16-17) and eliminate dup/drop pairs. This optimization is called dup/drop fusion and the result is presented in Figure 3c. We can eliminate the general drop function completely for our example program, but this is not always the case. Reinking et al. presents an additional optimization called reuse analysis, which perfoms destructive updates when possible. This optimization is not yet implemented in our project. However, we will definitely implement this optimization in the future because it enables in-place updates for pure functional languages. In-place updates are desirable because they reduce the number of allocations and deallocations, which is especially important for reference counting implementations because the overhead is proportional to the amount of allocations, deallocations, and reference counting operations (Wilson, 1992).

# 3.1 Challenges adapting Perceus to GRIN

One of the goals of GRIN is to improve register utilization for lazy functional languages (Boquist, 1999). As such, the result of function applications, fetch, and unit are stored in registers. Registers can either hold regular values such as integers or pointers to heap allocated nodes. Only heap allocated values contain a reference count, so the implementation need to keep track and only reference count variables which are pointers. For example, primitive subtraction returns an integer stored in registers "PSub x499 1;  $\lambda$  x498  $\rightarrow$ " (Figure 3c, line 11), so x498 should not be reference counted. This is in contrast to the calculus which Perceus is defined for,  $\lambda_1$ , where all variables are pointers to heap-allocated values (Reinking et al., 2021). Another difference is that functions in GRIN are not allowed to return un-Moreover, all function calls reboxed pointers. turn explicit nodes rather than node variables. For example: "downFrom x40 ;  $\lambda_{\Delta}$  x59 x60 x61  $\rightarrow$ " (Figure 3c, line 3). This is problematic because x60 and x61 are undefined when downFrom returns the empty list. Therefore, we are only allowed to dup/drop the variables once the tag is known.

## 4 LLVM IR code generation

We have implemented an LLVM code generator to test that our compiler works and that the programs reclaim all the allocated memory. Our implementation of the code generator is simple. GRIN does not demand a specific memory layout for the node values. The only requirements are that tags should be unique and easy to extract (Boquist, 1999). We use an array of four 64-bit integer values for all heapallocated nodes. The first two address spaces contain the reference count and the tag, respectively. The node arguments occupy the rest of the array. LLVM IR is a statically typed language, while GRIN is untyped. This discrepancy is not an issue because all functions return nodes, and all variables are pointers or integers. Hence, we store the pointers as integer values and convert them to the pointer type (ptr) as required. However, we will probably develop a type system for GRIN once we switch to a more sophisticated memory layout and implement the general unboxing optimization (Boquist, 1999).

## 5 Discussion and future work

Section 2.1 presents the resource information about our example program (1). The program allocates  $\mathcal{O}(n)$  nodes with respect to the instance size, and the worst-case heap consumption is also  $\mathcal{O}(n)$ . Ideally, the compiler should produce a program similar to the following C program which have no allocations.

```
int sum_down_from(int n) {
  int m = 0;
  for (int i = n - 1; i >= 1; i--)
    m += i;
  return m;
}
```

To address the total amount of allocations, we would like to implement the GRIN optimizations such as general unboxing and late inlining. These optimizations are sufficient to remove all allocations for this simple program (Boquist, 1999). However, for complex programs, implementing the Perceus reuse-analysis avoids additional allocations by updating nodes in-place.

The total allocation count impacts performance due to the overhead of the allocations, deallocations, and reference count operations. On the other hand, a poorly optimized worst-case heap consumption can lead to out of memory errors and stack overflows. Our example program (1) stack overflows for larger instances. We can prevent the stack overflow by making sum tail recursive and eager in the first argument, by using the primitive primForce. Evaluating (n + m) prior to the recursive call, achieves several favorable properties. Firstly, we prevent the stack overflow by not building and then evaluating a large suspended computation. Secondly, forcing \_+\_ drops the last reference count to n, which means it can be freed directly. Which in turn, eliminates all out of memory errors and makes the worst-case heap consumption  $\mathcal{O}(1)$ . Following is the final program.

```
\begin{array}{lll} \operatorname{downFrom} & : \mathbb{N} \to \operatorname{List} \, \mathbb{N} \\ \operatorname{downFrom} & \operatorname{zero} = [] \\ \operatorname{downFrom} & (\operatorname{suc} \, n) = n :: \operatorname{downFrom} \, n \\ \\ \operatorname{sum} & : \mathbb{N} \to \operatorname{List} \, \mathbb{N} \to \mathbb{N} \\ \\ \operatorname{sum} & m \, [] = m \\ \\ \operatorname{sum} & m \, (n :: ns) = \\ \\ \operatorname{sum} & (\operatorname{primForce} \, n \, \_+\_ \, m) \, ns \\ \\ \\ \operatorname{main} & = \operatorname{sum} \, (\operatorname{downFrom} \, 100) \\ \end{array}
```

## 6 Related work

Reference counting implementations are uncommon in the literature of lazy functional languages. Kaser et al. (1992) uses a reference counting for the lazy parallel language EQUALS. They observe that reference counting minimizes memory contention<sup>5</sup> because memory operations are interleaved througout the computation. Additionally, they note that their reference counting implementation achieved greatly reduced heap usage and good memory locality, compared to a tracing garbage collector.

To our knowledge, precise reference counting which utilizes ownership to free objects as soon as possible have not yet been implemented in any lazy functional language. The Perceus algorithm have been implemented for multiple eager languages (Pinto, 2023; Reinking et al., 2021; Teeuwissen, 2023; Ullrich & de Moura, 2021).

## 7 Conclusions

In this paper, we combine lazy functional programming with precise reference counting. Our implementation compiles Agda to GRIN and extends GRIN with precise reference counting instructions. Then, we compile GRIN to LLVM and show that the program reclaims all the memory. Currently, our implementation allocates a lot of nodes. In future research, we would like to minimize allocations by implementing the rest of the GRIN optimizing transformations and the Perceus reuse analysis. We are also interested in developing a type system for GRIN and compiling a larger set of Agda programs.

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 $<sup>^5{\</sup>rm That}$  is, multiple processes trying to access the same memory at once.

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