

Notation Key:

- **Inputs:** A (MSB), B, C (LSB).
- **String:** Represents outputs for inputs counting up (e.g., for 2 inputs: 00, 01, 10, 11).
- **Operators:** ! (NOT), * (AND), + (OR), # (XOR).

1 Input (A)

Total Functions: 4

| Truth String | Reduced Expression |
|--------------|--------------------|
| 00 | 0 |
| 01 | A |
| 10 | !A |
| 11 | 1 |

2 Inputs (A, B)

Total Functions: 16

Input order: 00, 01, 10, 11

| Truth String | Reduced Expression | Function |
|--------------|--------------------|------------------|
| 0000 | 0 | False |
| 0001 | A * B | AND |
| 0010 | A * !B | A and Not B |
| 0011 | A | A |
| 0100 | !A * B | Not A and B |
| 0101 | B | B |
| 0110 | A # B | XOR |
| 0111 | A + B | OR |
| 1000 | !(A + B) | NOR |
| 1001 | !(A # B) | XNOR |
| 1010 | !B | Not B |
| 1011 | A + !B | Implies (B -> A) |
| 1100 | !A | Not A |
| 1101 | !A + B | Implies (A -> B) |
| 1110 | !(A * B) | NAND |
| 1111 | 1 | True |

3 Inputs (A, B, C)

Total Functions: 256

Input order: 000, 001, 010, 011, 100, 101, 110, 111

Listing all 256 reduced expressions is impractical for this format. Below are the most significant mathematical and logical functions from the set.

| Truth String | Reduced Expression | Function |
|--------------|----------------------------------|--------------------------|
| 00000000 | 0 | False |
| 00000001 | $A * B * C$ | 3-input AND |
| 00010111 | $(A * B) + (B * C) + (A * C)$ | Majority Gate |
| 00110101 | $(A * C) + (!A * B)$ | MUX (A=Select, B=0, C=1) |
| 01101001 | $A \# B \# C$ | 3-input XOR (Parity) |
| 01111111 | $A + B + C$ | 3-input OR |
| 10000000 | $!(A + B + C)$ | 3-input NOR |
| 10010110 | $!(A \# B \# C)$ | 3-input XNOR |
| 11101000 | $!((A * B) + (B * C) + (A * C))$ | Minority Gate |
| 11111110 | $!(A * B * C)$ | 3-input NAND |
| 11111111 | 1 | True |