# **Evolutionary Image Segmentation Based on Multiobjective Clustering**

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Abstract—In the fields of image processing and recognition, image segmentation is an important basic technique in which an image is partitioned into multiple regions (sets of pixels). In this paper, we propose a method for evolutionary image segmentation based on multiobjective clustering. In this method, two objectives, overall deviation and edge value, are optimized simultaneously using a multiobjective evolutionary algorithm. These objectives are important factors for image segmentation. The proposed method finds various solutions (image segmentation results) by the use of an evolutionary process. We apply the proposed method to several image segmentation problems and confirm that various solutions are obtained. In addition, we use a simple heuristic method to select one solution from the original Pareto solutions and show that a good image segmentation result is selected.

#### I. INTRODUCTION

Image processing and recognition technologies are becoming increasingly important. In the fields of image processing and recognition, image segmentation is a basic and important technique in which an image is partitioned into multiple regions (sets of pixels). Each of the pixels in a region is similar to the other with respect to some characteristic or computed property, such as color, intensity, or texture. Recently, many image segmentation methods have been proposed and their effectiveness have been demonstrated [1], [2]. Typical examples include clustering methods, histogrambased methods, region growing methods [3], and graph partitioning methods [4], [5]. In clustering methods, the kmeans algorithm is the most popular technique, and is used to partition an image into k clusters. The quality of the solution using k-means depends on the initial set of clusters and the value of k. Region growing methods examine the neighboring pixels of initial gseed pointsh and determine whether the pixel should be added to the seed point.

The minimum spanning tree (MST) technique is also used in image segmentation [6], [7]. Each pixel is a node in a graph. The weight of an edge is a measure of the similarity between pixels. The image is partitioned into segments by removing the edges whose weight is more than the threshold.

Evolutionary computation (EC) techniques are also applied to image segmentation problems. Several algorithms using genetic algorithms (GAs) have been proposed [8], [9]. Poli applied genetic programming (GP) [10] to construct pixel-classification-based segmentation algorithms [11].

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The multiobjective clustering algorithm, multi-objective clustering with automatic k-determination (MOCK), was developed by Handl and Knowles [12], [13], and various improvements and applications have been investigated [14]–[18]. This algorithm optimizes two complementary objectives based on cluster compactness and connectedness using a multiobjective evolutionary algorithm (MOEA) [19], [20]. MOCK has been applied mainly to artificial datasets. MOCK is reported to find partitions better than other conventional clustering algorithms, such as the k-means method.

In this paper, we propose a method for evolutionary image segmentation based on multiobjective clustering. In the proposed method, two objectives, overall deviation and edge value, are optimized simultaneously using an MOEA. These objectives are important factors in image segmentation. The proposed method finds various solutions (image segmentation results) through an evolutionary process. We apply the proposed method to several image segmentation problems and confirm that various solutions are obtained. Since there is no general solution to image segmentation problems, image segmentation techniques often have to be combined with domain knowledge to solve such problems effectively for a problem domain. Therefore, we believe that it is significant to obtain various types of image segmentation results simultaneously. In addition, we use a simple heuristic method to select one solution from the original Pareto solutions and show that a good image segmentation result is selected.

The next section of this paper presents an overview of MOCK. In Section 3, we describe our proposed method for evolutionary image segmentation based on multiobjective clustering. Next, in Section 4, we apply the proposed method to image segmentation problems and show several experimental results. Finally, in Section 5, we describe our conclusions and future work.

# II. MULTIOBJECTIVE CLUSTERING WITH AUTOMATIC K-DETERMINATION (MOCK) [12], [13]

MOCK is a recent clustering algorithms based on an MOEA. MOCK optimizes two clustering objectives, *overall deviation* and *connectivity*, which reflect two fundamentally different aspects of a good clustering solution. Therefore, MOCK returns not just one solution, but an entire set of solutions. The first objective, overall deviation, is defined in equation (1). This equation described the overall summed distances between data items and their corresponding cluster center.

$$Dev(C) = \sum_{C_k \in C} \sum_{i \in C_k} \delta(i, \mu_k)$$
 (1)

where C is the set of all clusters,  $\mu_k$  is the centroid of cluster  $C_k$ , and  $\delta()$  is the distance function. Overall deviation should be minimized. Minimizing overall deviation increases the number of clusters.

The second objective, connectivity, is defined in equation (2). This objective evaluates the degree to which neighboring data points have been placed in the same cluster.

$$Conn(C) = \sum_{i=1}^{N} \sum_{j=1}^{L} x_{i,nn_i(j)},$$
where  $x_{r,s} = \begin{cases} \frac{1}{j} & if \not\equiv C_k : r, s \in C_k \\ 0 & otherwise \end{cases}$  (2)

where N is the number of data points,  $nn_i(j)$  is the jth-nearest neighbor of datum i, and L is a parameter determining the number of neighbors that contribute to the connectivity measure. Connectivity is also minimized. By minimizing these two objectives, a variety of different solutions are generated in MOCK.

Each individual in MOCK can be represented as a graph. Each datum is represented as a node, and an edge between two nodes indicates that these data are in the same cluster. Each individual has an N-length gene (N is the number of data points). The range of the gene value is [1, N]. When the ith gene value is j, data item i links to data item j. The decoding of this representation requires the identification of all subgraphs. Thus, the number of clusters is determined automatically in the decoding step.

In the MOCK algorithm, MST is used for the initialization of individuals. MST is the shortest tree that contains all nodes in the graph and has no loops. The shortest tree means that the total cost of all edges is the minimum. MOCK uses Prim's algorithm to create the MST. In the initialization of the ith individual in the population, the (i-1) long links are removed from the MST individual. In this manner, MOCK creates high-quality initial solutions.

In addition, MOCK has a scheme for determining the number of clusters automatically (automatically selecting the best solution). This scheme is based on the Gap statistic [21]. In this scheme, random data are created based on the principal component of original data, and these data are divided into clusters by MOCK. The solutions of the random and original data are different. The appropriate number of clusters is determined using these solutions of random and original data.

# III. EVOLUTIONARY IMAGE SEGMENTATION BASED ON MULTIOBJECTIVE CLUSTERING

In this section, we describe the proposed method for evolutionary image segmentation based on multiobjective clustering.

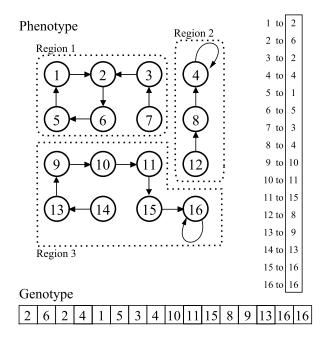


Fig. 1. Example of the phenotype (graph representation) and genotype (string of integers) of an individual in the proposed method. The graph corresponds to an image plane.

#### A. Representation of individuals

Figure 1 illustrates the phenotype and genotype of an individual in the proposed method. The representation of individuals is a graph structure. The phenotype corresponds to an image plane. Each pixel in the image is represented as a node, and an edge between two nodes indicates that these pixels are in the same region (cluster). Each node can connect only with either itself or the four neighboring pixels. This graph representation indicates image segmentation. Each individual has an N-length gene (N is the number of pixels). When the ith gene value is j, pixels i and j are in the same region. For instance, nodes (pixels) numbered 1, 2, 3, 5, 6, and 7 in Figure 1 are in the same region. The decoding of this representation requires identification of all subgraphs. Thus, the number of regions is determined automatically in the decoding step. Because of the constraint on connections, regions far from each other on the image plane do not appear as the same region. A very large search space can be limited using this constraint, and it also reduces the computational time required to create the MST. We use an MOEA to optimize image segmentation represented by the graph structure.

In the proposed algorithm, MST under the constraint on node connections is used for the initialization of individuals. We use Prim's algorithm, as used in MOCK, to create the MST. We assume to the initial individuals, MST is used as it is (do not remove the links from MST). Therefore, initial individuals have the potential for creating high-quality solutions.

### B. Multiobjective evolutionary algorithm

We adopt an evolutionary method to obtain the optimum structure. The genotype of the proposed method is a linear string, as in MOCK. Therefore, the method can use a typical simple genetic operator. In this study, we use *uniform crossover* and *mutation* as the genetic operators. In uniform crossover, randomly selected genes are swapped between two parents, which generate offsprings. In mutation, randomly selected genes with a mutation rate  $P_m$  are randomly changed under the constraints on connections.

We use Strength Pareto Evolutionary Algorithm 2 (SPEA2) [22] as the MOEA technique. SPEA2 assigns fitness values to individuals according to dominance and density criteria. The selection of individuals is also based on these criteria. It maintains two populations, a current population and an archive population. In each generation, the nondominated solutions in the current population and the archive are copied into the archive of the next generation. Selection occurs from both the population and archive. The procedure of the SPEA2 algorithm is as follows:

- 1) **Initialization:** Generate an initial population  $P_0$  and create the empty archive population  $\bar{P}_0 = \emptyset$ . Set the generation counter t = 0.
- 2) **Fitness assignment:** Calculate fitness values of individuals in  $P_t$  and  $\bar{P}_t$ .
- 3) Environmental selection: Copy all nondominated individuals in  $P_t$  and  $\bar{P}_t$  to  $\bar{P}_{t+1}$ . If the size of  $\bar{P}_{t+1}$  exceeds  $\bar{N}$  (archive size), reduce  $\bar{P}_{t+1}$  by means of the truncation operator; otherwise, if the size of  $\bar{P}_{t+1}$  is less than  $\bar{N}$ , fill  $\bar{P}_{t+1}$  with dominated individuals in  $P_t$  and  $\bar{P}_t$ .
- 4) **Termination:** If a certain specified condition is satisfied, return nondominated individuals in  $\bar{P}_{t+1}$  as the outputs of the system.
- 5) **Mating selection:** Select parents from  $\bar{P}_{t+1}$  based on binary tournament selection.
- 6) Variation: Apply crossover and mutation operators to the parents and set  $P_{t+1}$  to the resulting population. Increment generation counter (t=t+1) and go to step 2.

In the fitness assignment step, a strength value S(i) and a fitness F(i) are calculated for each individual i in the population  $P_t$  and archive  $\bar{P}_t$ . S(i) shows the number of dominated solutions by the ith individual. F(i) is the sum of the strength values of its dominators. In the environmental selection step, the nondominated individuals whose fitness is 0 are placed in  $\bar{P}_{t+1}$ . If the number of such individuals is greater than the archive size, the archive is truncated using a special operator. In this operator, the individual that has the minimum distance to another individual is chosen at each stage. If the nondominated individuals cannot fill the archive exactly, the best dominated individuals are copied to  $\bar{P}_{t+1}$ .

## C. Objective functions

In the proposed method, two objectives, *overall deviation* and *edge value*, are optimized simultaneously using an

MOEA. These objectives are important factors of image segmentation.

Overall deviation is defined in equation (3). This equation gives the overall summed distances between the pixels and the center value of the corresponding region (cluster) they belong to. Overall deviation is a measure of the similarity of pixels in the same region.

$$Dev(R) = \sum_{R_k \in R} \sum_{i \in R_k} \delta(i, \mu_k)$$
 (3)

where R is the set of all regions,  $\mu_k$  is the centroid of the pixels in the region  $R_k$ , and  $\delta()$  is the distance function. Overall deviation should be minimized. Minimizing overall deviation roughly increases the number of regions (clusters). We calculate the distance function  $\delta()$  defined as a Euclidean distance, and use either RGB or CIE L\*a\*b\* [23] as the color space. The distance function using the RGB color space is defined in equation (4).

$$\delta_{RGB} = \sqrt{\Delta R^2 + \Delta G^2 + \Delta B^2} \tag{4}$$

The distance function using the CIE L\*a\*b\* color space is defined in equation (5). The CIE L\*a\*b\* color space has a uniform chromaticity scale.

$$\delta_{L*a*b*} = \sqrt{\Delta L *^2 + \Delta a *^2 + \Delta b *^2} \tag{5}$$

The second objective, the edge value, is defined in equation (6). This objective evaluates the overall summed distances on boundaries between the regions. This value is a measure of the difference in the boundary between the regions.

$$Edge(R) = -\sum_{i=1}^{N} \sum_{j \in F_i} x_{i,j},$$
 where  $x_{r,s} = \begin{cases} \delta(r,s) & \text{if } \nexists R_k : r,s \in R_k \\ 0 & \text{otherwize} \end{cases}$  (6)

where N is the number of pixels,  $F_i$  indicates the four neighboring pixels of pixel i, and  $\delta()$  is the distance function. This edge value is also minimized, which roughly decreases the number of regions (clusters). By minimizing these two objectives, a variety of different image segmentations are generated. In other words, the proposed method returns a range of solutions that have different numbers of regions.

# D. Solution selection method

The main objective of this study is to obtain a variety of image segmentation results. However, it is necessary to obtain one solution suitable for a circumstances. In MOCK, the number of clusters is determined based on the Gap statistic. However, its determination scheme requires random data clustering in several trials. Therefore, the computational time for determining the number of clusters is high [17].

In the proposed approach, we use a simple heuristic method to select one solution and find the "knee" of the

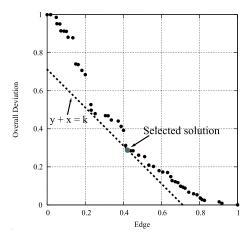


Fig. 2. Example of the selection scheme in the proposed method.

 $\label{eq:table I} \textbf{TABLE I}$  Settings of parameters used in the experiments.

Parameters	Values
Gene length	image size
_	$(96 \times 96[pixels])$ or $128 \times 96[pixels])$
Color space	RGB or CIE L*a*b*
MOEA model	SPEA2
Number of generations	300
Population size	50
Archive size	50
Crossover	Uniform crossover
Crossover rate $P_c$	0.7
Mutation rate $P_m$	0.0001
Constraints	1 < region num < 50
	region size $> 100$ [pixels]

original Pareto solutions. The most interesting solutions of the Pareto-optimal front are those where a small improvement in one objective would lead to a large deterioration in at least one other objective. These solutions are sometimes also called knees [24].

Our selection scheme is as follows:

- 1) Normalize the fitness value of all the solutions to the range of [0.0, 1.0] using the original Pareto solutions.
- 2) Calculate the sum of "normalized Dev(R)" and "normalized Edge(R)", and select the solution with the minimal value as the best solution.

In other words, the solution that has the minimal distance from the line y=-x is selected as the adequate solution in this selection scheme. An example of our selection scheme is shown in Figure 2.

### IV. EXPERIMENTS AND RESULTS

In this section, we apply the proposed method to image segmentation problems, and confirm that a variety of image segmentation results are obtained. In addition, we select one solution from the original Pareto solutions.

# A. Settings of the experiments

The parameters used by the proposed method are shown in Table I. We use either RGB or CIE L\*a\*b\* as the color





(a) pepper





(c) terra



(d) paprika

Fig. 3. Original color images used in the experiments.

space. We constrain the number of pixels in one cluster to be less than 100 to prevent the existence of very small regions (clusters). The original color images used in the experiments are shown in Figure 3. In these experiments, we use four images; (a) pepper, (b) sailboat, (c) terra, and (d) paprika.

### B. Results and discussion

The obtained Pareto solutions by the proposed method are shown in Figures 4 and 5. The values of the axes are normalized. Figure 4 shows the obtained Pareto solutions using the RGB color space, and Figure 5 shows those using CIE L\*a\*b\* color space. The obtained solutions of each image have different Pareto front. The solutions obtained with the RGB and CIE L\*a\*b\* color spaces are also different. Although the shapes of the Pareto front are different, a wide range of solutions is found in all cases. Therefore, we conclude that the evolutionary algorithm is efficient. We use SPEA2 as the MOEA model in the experiments. It would be interesting to analyze the behaviour of NAGA-II [25] and other MOEA models. Nebro et al. show that the convergence speed of SPEA2 is slowest for test problems [26].

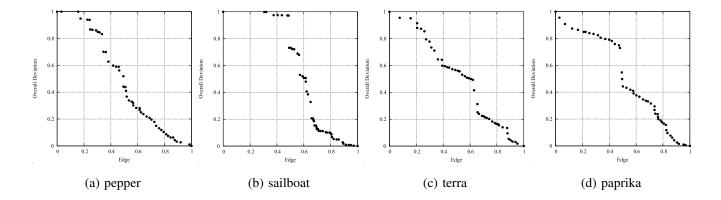


Fig. 4. Obtained Pareto solutions by the proposed method using the RGB color space. The horizontal axis represents normalized edge values, and the vertical axis represents normalized overall deviation.

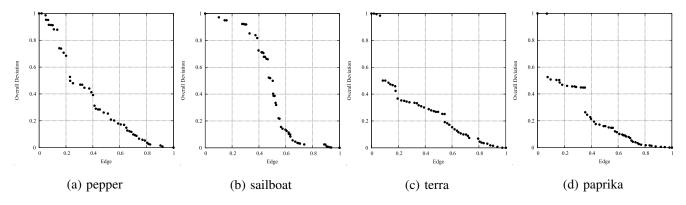


Fig. 5. Obtained Pareto solutions by the proposed method using the CIE L\*a\*b\* color space. The horizontal axis represents normalized edge values, and the vertical axis represents normalized overall deviation.

Another objective of this study is to verify whether various image segmentation results are obtained. Figure 6 shows examples of the image segmentation results in the case of the "pepper" image using the RGB color space. The black lines in the images indicate the boundaries of the regions. The results show that various image segmentations (various numbers and shapes of regions) are obtained. Also, the image segmentations are considered to be relatively good.

Next, we select one solution from the Pareto front using the selection scheme. Figure 7 shows the selected solutions. In general, these image segmentations are considered good results. In the case of "paprika" the three peppers are partitioned into a single region when the CIE L\*a\*b\* color space is used. Thus, the best solution is not selected in this case.

The results of image segmentation using the k-means method, which is one of the clustering methods, are shown in Figure 8. In this case, we apply the k-means method to the "paprika" image using the RGB color space. In this method, the user has to choose an appropriate number of clusters. Image segmentation is overdone when there are many clusters. Also, the k-means method assigns regions separated on the image plane to the same region. It is confirmed that the proposed method obtains good solutions

compared with the k-means method.

In the experiment, we only compared the proposed method with k-means method. We might have to compare the proposed method with other methods such as graph partitioning based methods [4], [5] and ensemble based methods [27].

# V. CONCLUSIONS AND FUTURE WORK

In this paper, we proposed evolutionary image segmentation based on multiobjective clustering. In the proposed method, two objectives, *overall deviation* and *edge value*, are optimized simultaneously using an MOEA. These objectives are important factors in image segmentation. The proposed method finds various solutions (image segmentation results) by an evolutionary process. We applied the proposed method to several image segmentation problems and confirmed that various solutions are obtained. In addition, one solution was selected from the original Pareto solutions by a simple heuristic method. We also show that a good image segmentation result is selected.

In future work, we will apply the proposed method to other types of images, such as medical images. Moreover, we plan to examine more appropriate objectives for image segmentation.

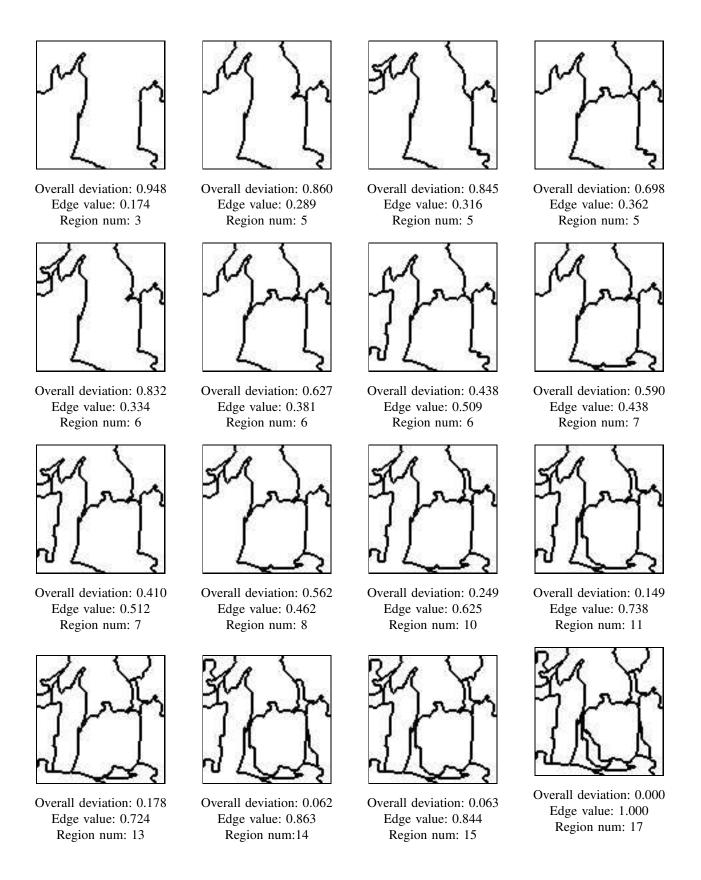


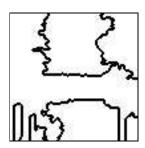
Fig. 6. Examples of the image segmentation results in the case of the "pepper" image using the RGB color space. The black lines indicate the boundaries of the regions. Each result also shows the normalized overall deviation, normalized edge value, and number of regions.



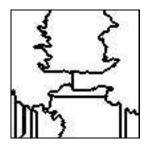
pepper Color space: RGB Overall deviation: 0.302 Edge value: 0.567 Region num: 9



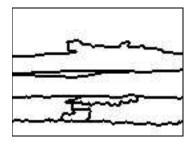
pepper Color space: CIE L\*a\*b\* Overall deviation: 0.290 Edge value: 0.422 Region num: 9



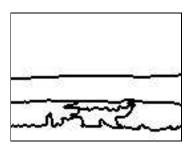
sailboat Color space: RGB Overall deviation: 0.114 Edge value: 0.710 Region num: 7



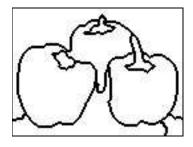
sailboat
Color space: CIE L\*a\*b\*
Overall deviation: 0.056
Edge value: 0.651
Region num: 10



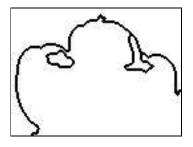
terra Color space: RGB Overall deviation: 0.240 Edge value: 0.666 Region num: 9



terra
Color space: CIE L\*a\*b\*
Overall deviation: 0.366
Edge value: 0.195
Region num: 7



paprika Color space: RGB Overall deviation: 0.042 Edge value: 0.883 Region num: 9

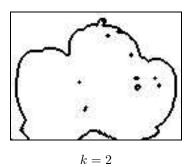


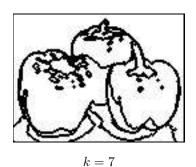
paprika
Color space: CIE L\*a\*b\*
Overall deviation: 0.526
Edge value: 0.076
Region num: 4

Fig. 7. Selected image segmentation results obtained by the proposed method. The black lines indicate the boundaries of the regions. The normalized overall deviation, normalized edge value, and number of regions are also given for each selected solution.

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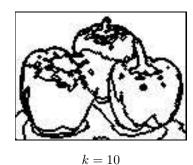


Fig. 8. Image segmentation results in the case of "paprika" image using k-means method (k = 2, 7, 10). RGB is used as the color space. The black lines in the images indicate the boundaries of the regions.

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