

GCSE Maths: Exam-Style Booklet

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This exam booklet covers topics intended for the 2024 iGCSE exam diet. It is still largely suitable for students on other exam boards. For solutions and marking email fredserdickinson@gmail.com. Good luck!

Give your solutions on a separate piece of paper or digital notebook. Attempt to answer all questions and make your workings clear. You may use a calculator.

1. (a) Write $x^2 + 10x + 3$ in the form $(x + a)^2 + b$ where a and b are integers. (3)
(b) Hence, or otherwise, give the coordinates of the turning point of the graph $y = x^2 + 10x + 3$. (1)

2. (a) Factorise $x^2 - 4x - 21$. (1)
(b) Hence, or otherwise, solve (2)

$$\frac{x^2 - 4x - 21}{x + 3} = x^2 - 37.$$

3. (a) Write $\sqrt{50}$ in the form $k\sqrt{2}$, where k is an integer. (1)
(b) Show that (3)

$$\frac{5 + 2\sqrt{3}}{2 + \sqrt{3}}$$

can be written in the form $a + b\sqrt{3}$, stating your values of a and b .

4. Solve $3x^2 - 11x - 13 = 0$. Give your solutions correct to 3 significant figures. (2)

5. (a) A line L_1 is shown in the figure below. It passes through points $A(0, 3)$ and $B(6, 0)$.

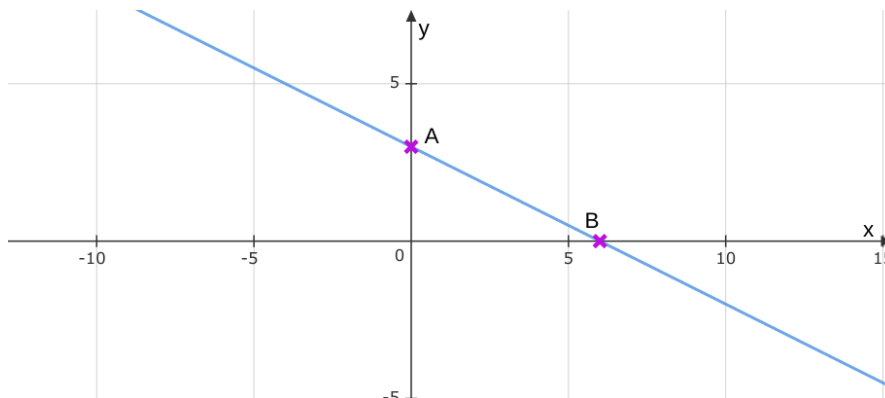


Figure 1: The graph of some straight line L_1 .

- i. Find the equation of the line L_1 . (2)
 - ii. The midpoint of the line segment between A and B is denoted C . Find the coordinates of C . (1)
- (b) A second line L_2 is perpendicular to L_1 and passes through the point C . Find the equation of L_2 . (3)
6. Jeffrey has a bag containing a selection of red, green and blue marbles. There are 16 blue marbles in the bag and the number of red and green marbles are split in the ratio 4 : 2. (4)

Jeffrey puts his hand into the bag and selects a marble at random. Given that the chance he picks a blue marble is 25%, how many green marbles are in the bag?

7. Solve the following system of simultaneous equations (5)

$$\begin{aligned}x^2 + y^2 &= 34 \\x - y &= 2,\end{aligned}$$

stating clearly your solutions for x and y .

8. The triangle ABC has been drawn in the figure below. Find the angle $\angle ABC$, fully justifying your answer. (2)

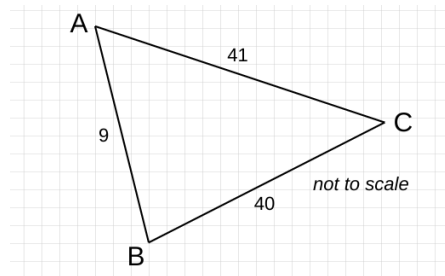


Figure 2: The triangle ABC , drawn not to scale.

9. Jack's football team is having a mass bake sale. Arthur bought 7 cookies and 3 brownies for a total cost of 31.25. Louis bought 2 cookies and 8 brownies for a total cost of 25.
- (a) What is the individual cost of both items? (4)
- (b) Lewis bought 15 cookies and 20 brownies to share with his class. How much did he pay? (1)

10. Consider the triangle ABC drawn below.

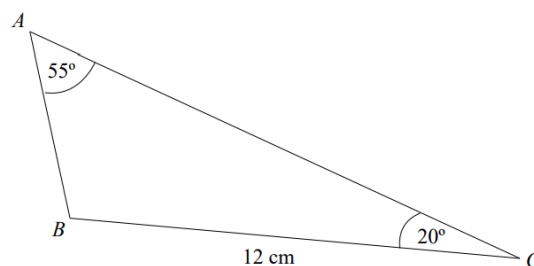


Figure 3: Some other triangle ABC , drawn not to scale.

- (a) Find the length AC . (3)
- (b) Hence, or otherwise, find the area of the triangle ABC . (2)

END OF EXAM BOOKLET.