

# Math for Computer Science - In class Problems - Week 3

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## Problem 1

## Problem 2

a.

$$\exists u(uuu = x)$$

Name: THREE-COPIES( $x$ )

b.

$$\exists u(uu = x \text{ AND NO-1S}(u))$$

Name: EVEN-LENGTH-AND-NO-1S( $x$ )

c.

$$\text{NOT}(\text{SUBSTRING}(1, x)) \text{ OR } \text{NOT}(\text{SUBSTRING}(0, x))$$

Name: ONLY-0S-OR-ONLY-1S( $x$ )

d.

$$\exists u(1u1 = x \text{ AND NO-1S}(u))$$

Name: IS-2k+1( $x$ )

e. Let's assume  $x$  contains at least a 1. This way  $x$  will not be the prefix of '0x', since each 1 would shifted to the right.

## Problem 3

$$\exists s \forall t_1 \forall t_2 \forall t_3 (E(s, t_1) \wedge E(s, t_2) \implies t_1 = t_2 \vee t_1 = t_3 \vee t_2 = t_3)$$

## Problem 4

## Problem 5

- a. There are at least three different people, x, y and z which belongs to the cabal.
- b. Either Siggi is not a cabal, or Annie is not a cabal, or neither one of them is a cabal.
- c. If Elizabeth is a cabal, then everyone is a Cabal. So, Elizabeth can not be a cabal, considering the previous item.
- d. If Annie is a cabal then Siggi is a cabal. So Annie is not a Cabal, considering at least one of them is not a cabal.
- e. If either Ben or Albert are cabal, then Tom is not a cabal.
- f. if eight Ben or Siggi are cabal, then Adam is not a cabal.
- g. So, at least three cabal, with the possibilities: Adam, Tom, Albert, Ben, Siggi
- h. Suppose Ben is Cabal, then Tom and Adam are not cabal. The group would be: Ben, Albert, Siggi.
- i. If Tom is cabal, then Albert and Ben are not. The group would have at most two people, since if Siggi is cabal, then Adam is not.
- j. If Adam is cabal, then Siggi and Ben are not. The group would have at most two people, since if Albert is cabal, then Tom is not.
- k. The only possible group is Ben, Albert, and Siggi.