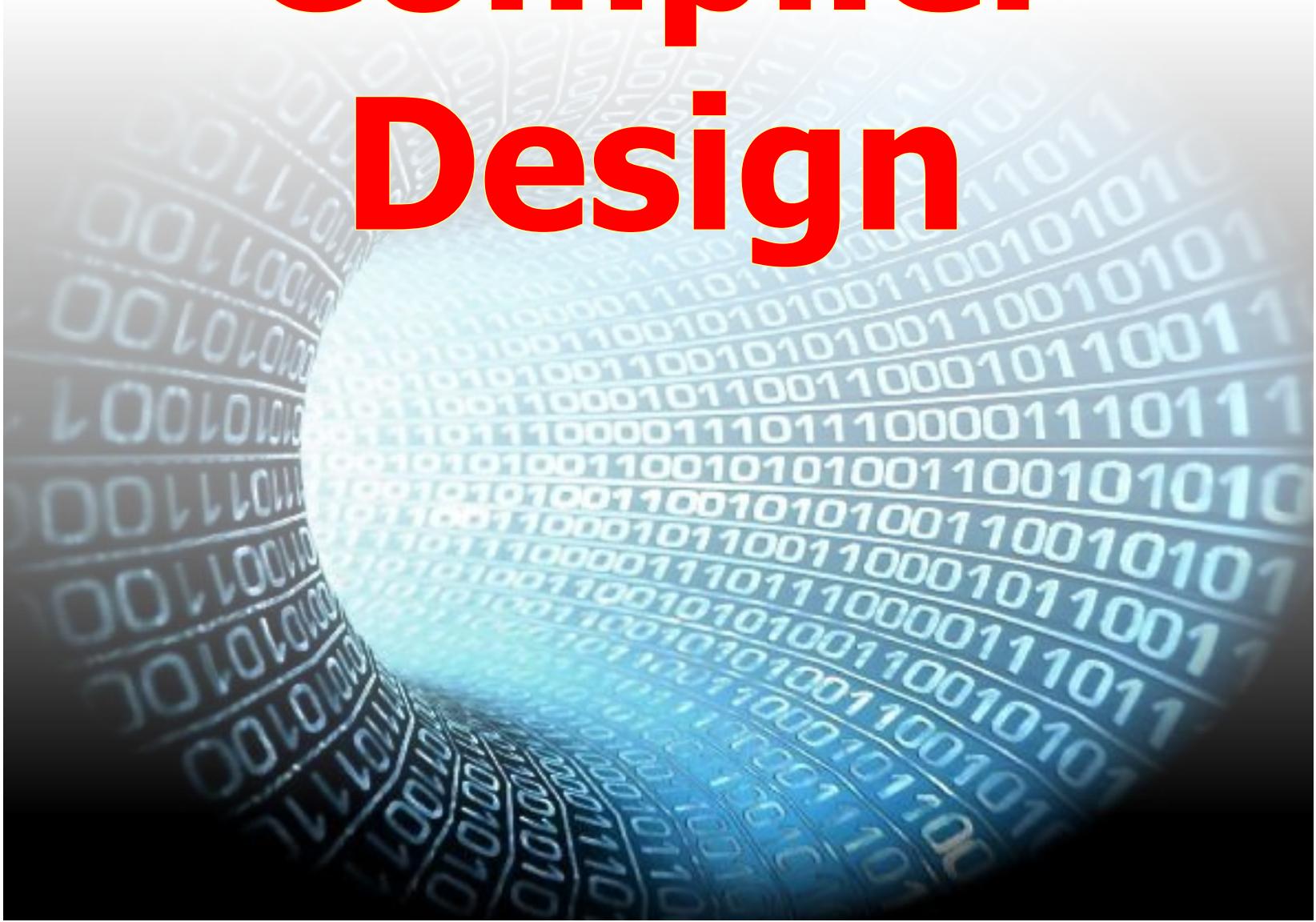


Compiler Design



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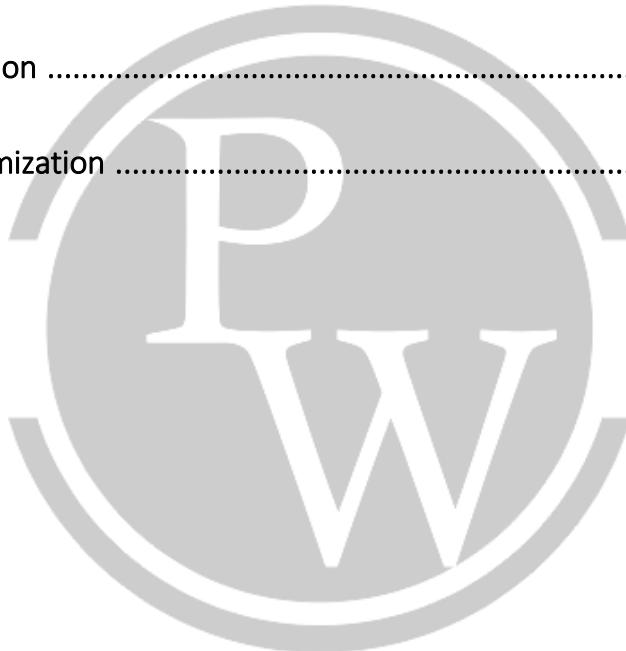
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Compiler Design

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1

INTRODUCTION AND LEXICAL ANALYSIS

1.1 CD Introduction

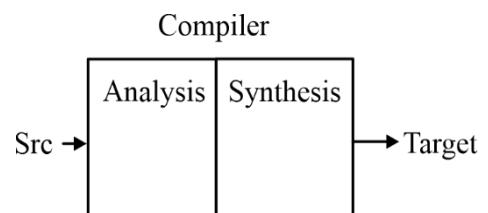
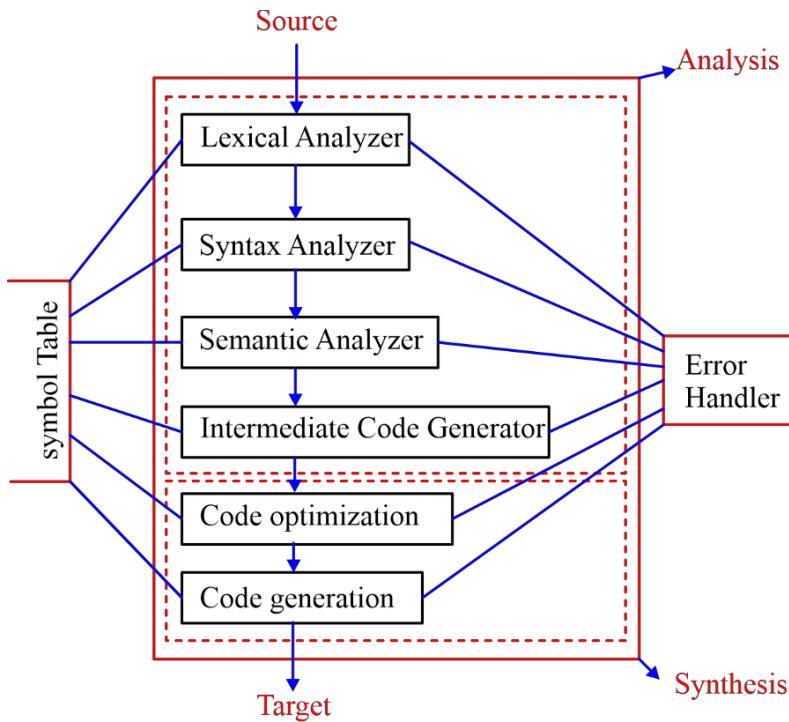
1.1.1 Definition

Convert High Level Language to Low Level Language.



- High Level Language can perform more than one operation in a single Statement.
- Low Level Language can perform atmost one operation in a statement.

1.2 Analysis and Synthesis model of Compiler



- There are 6 phases of the Compiler

1. Lexical Analyzer:

- Program of DFA, it checks for spelling mistakes of program.
- Divides source code into stream of tokens.

2. Syntax Analyzer:

- Checks grammatical errors of the program (Parser).
- Parser is a DPDA.

3. Semantic Analyzer:

Checks for meaning of the program.

Example:

Type miss match, stack overflow

4. Intermediate Code Generation:

- This phase makes the work of next 2 phases much easier.
- Enforces reusability and portability.

5. Code optimization:

- Loop invariant construct
- Common sub expression elimination
- Strength Reduction
- Function inlining

Deadlock elimination

6. Symbol Table:

- (1) Data about Data (Meta data)
- (2) Data structure used by compiler and shared by all the phases.



2

PARSING

2.1 CD - Grammar

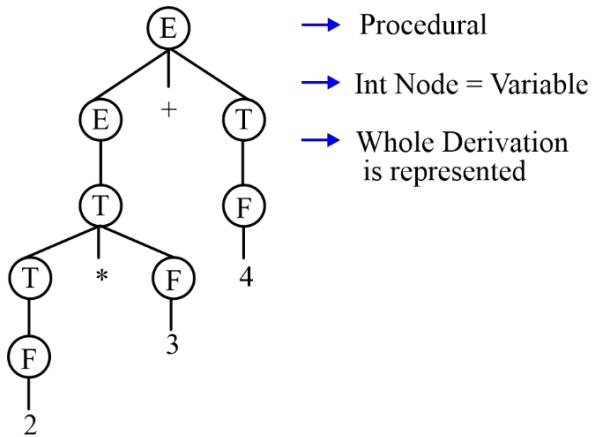
- In compiler we only use: Type – 2 (CFG) and Type – 3 Regular grammar.
- Compiler = Program of Grammar
- Compiler = Membership algorithm
- Every programming Language is Context Sensitive Grammar (Context Sensitive Language)

2.1.1 Parse Tree and Syntax Tree

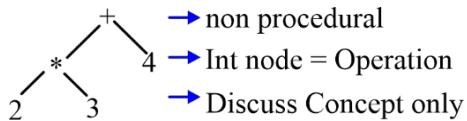
G: $E \rightarrow E + T / T \quad E \rightarrow E + T \rightarrow T + T \rightarrow T * F + T \rightarrow F * F + T \rightarrow 2 * F + T \rightarrow 2 * 3 + T \rightarrow 2 * 3 + F$
 $T \rightarrow T * F / F$

$$E \rightarrow 2 * 3 + 4$$

Parse Tree:

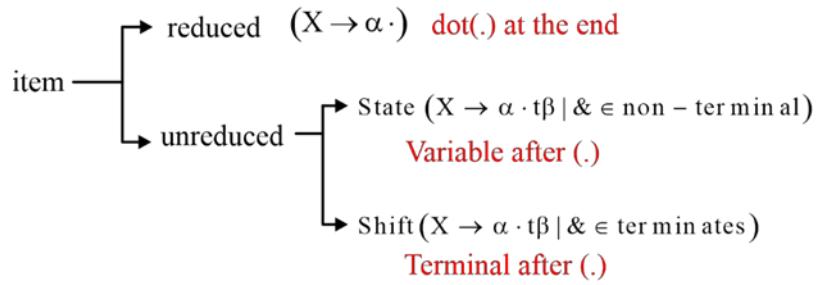


Syntax Tree:



- To check to priority / Associativity:
Randomly derive till you have enough operators, then check which one is done first.
- If priority of 2 operators is same and both Left and Right associative → **Ambiguous Grammar** [Useless]

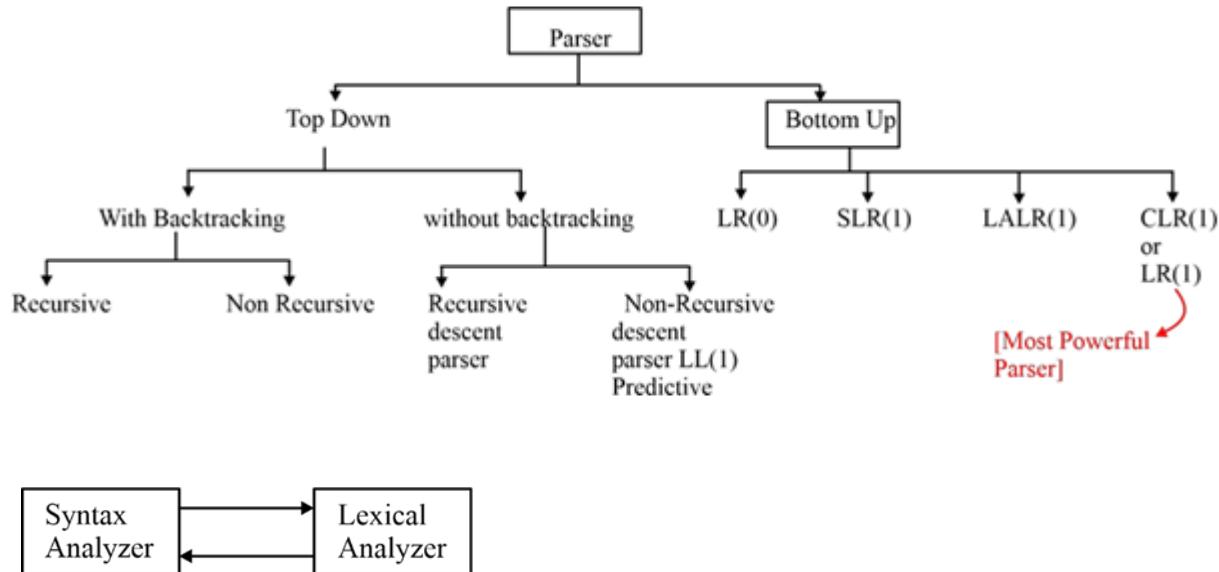
2.1.2 Types of Parsers in Bottom Up: [CD - Parser]



2.2 CD-Syntax Analysis / Parsing

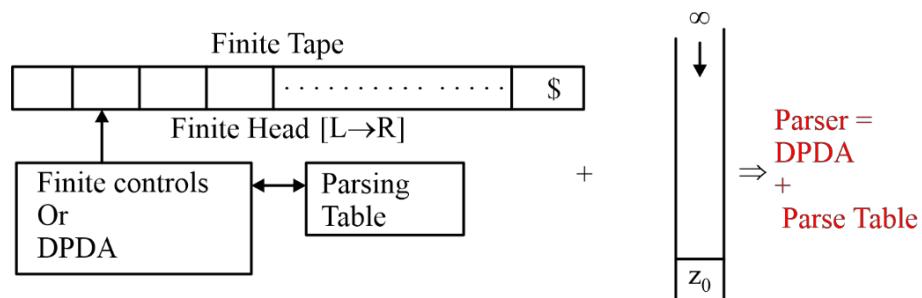
Grammatical Errors are checked by the help of parsers.

- Parsers are basically DPDA



- All of these parsers are table driven.

2.2.1 Mathematical Model of Parser



- Parsers generate Parse Tree, for a given string by the given grammar.

2.2.2 Top-Down Parser (LL (1))

- It uses LMD and is equivalent to DFS in graph.

2.2.3 Algorithm to construct Parsing Table

1. Remove Left Recursion if any.
 2. Left Factor [Remove Common Prefix]
 3. Find first and follow set
 4. Construct the table.
- If we increase the look ahead symbol:

2.2.4 Removal of common Prefix: (Left Factor)

$$1. \quad S \rightarrow a \mid a b \mid a A \quad S \rightarrow a Y$$

$$Y \rightarrow \in \mid b \mid A$$

$$2. \quad A \rightarrow a b A \mid a A \mid b$$

$$A \rightarrow a \times \mid b \quad A \rightarrow a \times \mid b$$

$$X \rightarrow b A \mid A \quad X \rightarrow b A \mid a x \mid b$$

$$A \rightarrow a X \mid b$$

$$X \rightarrow a X \mid b$$

$$Y \quad Y \rightarrow A \mid \in$$

2.2.5 First and Follow

- First Set → extreme Left terminal from which the string of that variable starts.
 - it never contains variable, but may contain ‘ \in ’.
 - we can always find the first of any variable.
- Follow set → Follow set contains terminals and $\$$.
 - It can never contain variable and ‘ \in ’.
 - How to find follow set?
 1. Include $\$$ in follow of start variable.
 2. If production is of type →
 $A \rightarrow \alpha B \beta \quad \alpha \beta \rightarrow \text{strings of grammar symbol}]$.
follow (B) = first (β).
If, $\beta \rightarrow \in$, i.e. $A \rightarrow \alpha B$, then follow(B) = follow(A).
- Productions like: $A \rightarrow \alpha A$ gives no follow set.

2.2.6 Example of first and follow set

1.	S	\rightarrow	AB		CD
	A	\rightarrow	aA		a
	B	\rightarrow	bB		b
	C	\rightarrow	cC		c
	D	\rightarrow	dD		d

	First	Follow
S	a, c	\$
A	a	b
B	b	\$
C	c	D
D	D	\$

2.2.7 Entity into Table: Top Down

1. No of Rows = number of unique variable in Grammar.
 2. No of columns = [Terminals + \$]
 3. For a Variable (Row) fill the column (Terminal) if its P, there in its first with the production required.
 4. If \in is in first put $V \rightarrow \in$ under \$ and its follow.
- If any cell has multiple items, then its not possible to have LL (1) Parser, since that will be ambiguous.
 - In top down we do: Derivation
In Bottom up we do: Production.

Question: Construct LL (1) Parsing Table for the given Grammar: $E \rightarrow E + T \mid T; T \rightarrow T * F \mid F; F \rightarrow (E) \mid id; \Rightarrow G_0$

\Rightarrow Removing Left Recursion:

$$\begin{aligned} E &\rightarrow TE' \\ E' &\rightarrow + TE' \mid \in \\ T &\rightarrow FT' \quad G_1 \\ T' &\rightarrow *FT' \mid \in \\ F &\rightarrow (E) \mid id \end{aligned}$$

	First	Follow
E	C, id	\$,)
E'	+, \in	\$,)
T	C, id	+, \$,)
T'	*, \in	+, \$,)
F	C, id	*, +, \$,)

- Left Factoring not Required:

Construction of Table: [LL (1)]

	+	*	()	id	\$
E	Error	Error	$E \rightarrow TE'$	Error	$E \rightarrow TE'$	Error
E'	$E' \rightarrow TE'$	Error	Error	$E' \rightarrow \in$	Error	$E' \rightarrow \in$
T	Error	Error	$T \rightarrow FT'$	Error	$T \rightarrow FT'$	error
T'	$T' \rightarrow \in$	$T' \rightarrow *FT'$	Error	$T' \rightarrow \in$	Error	$T' \rightarrow \in$
F	Error	Error	$F \rightarrow (\in)$	Error	$F \rightarrow id$	error

- Since for G_1 , Table constructed with no multiple entries. Hence successfully completed. Hence G_1 is LL (1)

Question: Construct LL (1) Parsing Table for the following Grammar:

$$S \rightarrow L = R \mid R; L \rightarrow * R \mid id; R \rightarrow L \Rightarrow G_0$$

Solution: Left Factoring:

$$\begin{array}{l}
 S \rightarrow L = R \mid L \quad S \rightarrow LX \\
 L \rightarrow *R \mid id \Rightarrow \times \Rightarrow R \mid \epsilon \quad L \rightarrow *R \mid id \Rightarrow G_1 \\
 R \rightarrow L \quad \quad \quad R \rightarrow L
 \end{array}$$

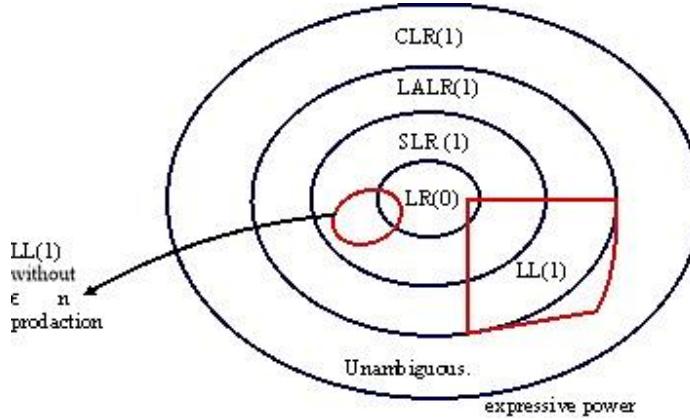
	First	Follow
S	*, id	\$
\times	=, \in	\$
L	*, id	\$
R	*, id	\$

Construction of Table:

	*	=	Id	\$
S	$S \rightarrow LX$	Error	$S \rightarrow L$ X	Error
L	$L \rightarrow *R$	Error	$L \rightarrow id$	Error
R	$R \rightarrow L$	Error	$R \rightarrow L$	Error
\times	Error	$X \rightarrow = R$	Error	$X \rightarrow \epsilon$

- G_1 is a LL (1) Grammar.

2.2.8 Hierarchy of Parsers: [for ϵ - free Grammar]



- For ϵ - producing grammars every LL (1) may not be LALR (1).

Note:

We can't construct any parser for ambiguous grammar. Except: Operator precedence, parser possible for some ambiguous grammar.

Example:

$G: S \rightarrow a S a \mid b S b \mid a \mid b$ (Unambiguous but no parser) $L(G) = \omega(a + b) \omega R$
(Odd palindrome)

- Every RG is not LL (1) as it may be ambiguous, or Recursive or Common Prefix.
- Parsers exists only for the grammar if its Language is DCFL.
- There are some grammars whose Language is DCFL but no parser is possible for it.

2.4.9 Operator Precedence Grammar

Format: (1) No 2 or more variable side by side
 (2) No \in production.

Example:

$$\begin{array}{ll}
 E \rightarrow E + T \mid T & E \rightarrow E + E \\
 T \rightarrow T * F \mid F & \text{or} \quad E \rightarrow E * E \quad \text{or} \quad S \rightarrow aSa \mid bSb \mid a \mid b \\
 F \rightarrow (E) \mid id & E \rightarrow a / b \quad \text{or} \quad O.G \\
 O.G. & O.G \\
 & \text{Or} \\
 S \rightarrow AB & \\
 A \rightarrow aA \mid \epsilon & \boxed{\text{Not O.G}} \\
 B \rightarrow bB \mid \epsilon &
 \end{array}$$

2.2.10 Checking LL (1) without Table

$A \rightarrow \alpha_1 | \alpha_2 | \alpha_3$ then \rightarrow

$$\begin{array}{ll}
 \text{first } (\alpha_1) \cap \text{first } (\alpha_2) = \emptyset & \text{first } (\alpha_1) \cap \text{first } (\alpha_2) = \emptyset \\
 \text{first } (\alpha_1) \cap \text{first } (\alpha_3) = \emptyset & \text{first } (\alpha_1) \cap \text{first } (\alpha_3) = \emptyset \\
 \text{first } (\alpha_2) \cap \text{first } (\alpha_3) = \emptyset & \text{first } (\alpha_2) \cap \text{first } (\alpha_3) = \emptyset \\
 & \text{follow } (A) \cap \text{first } (\alpha_1) = \emptyset \\
 & \text{follow } (A) \cap \text{first } (\alpha_2) = \emptyset \\
 & \text{follow } (A) \cap \text{first } (\alpha_3) = \emptyset
 \end{array}$$

2.2.11 Bottom-UP Parser

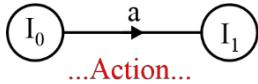
- It uses RMD in reverse and has no problem with:
 - (a) Left recursion
 - (b) Common Prefix
- SLR (1) LR (0) CLR (1) LR (1)
- LR (0) items LALR (1) items
- $LR(1) = LR(0) + 1$ Lookahead
- No parser possible for ambiguous grammar.
- There are some unambiguous grammars for which, there are no Parser.

2.2.12 Basic Algorithm for Construction

- Augment the grammar and expand it, and give numbers to it
- Construct LR (0) or LR (1) item set.
- From that fill the entries in the Table Accordingly.

2.2.13 Types of Entries

- (1) **Shift Entries:** Transitions or Terminals



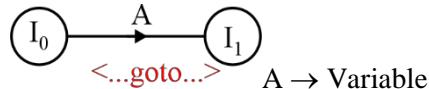
Entry:

	a
I ₀	S ₁

a ∈ Terminal, I₀, I₁: Item sets.

- Shift entries are some for all Bottom – up Parser.

- (2) **State Entry:** Transition or non – terminal (variable)



Entry:

	A
I ₀	I

- Same for all Bottom-up Parser.

- (3) **Reduce Entity:** done for each separate production in the item set of type:

i > x → α

where, i → Production Number

x → Producing Variable

α → Grammar String

- (a) LR (0) Parser:

Put R_i in every cell of the set-in action table (**ALL**).

- (b) SLR (1) Parser:

Put R_i only in the follow(x) form the Grammar. (**Follow(x)**)

- (c) LALR (1) and CLR (1):

Put R_i only in the look ahead of the production (**Lookaheads**)

2.2.14 Conflicts

LR (0) Parser:

SR: Shift Reduce Conflict

$$S \rightarrow X \rightarrow \alpha \cdot t\beta \Rightarrow \text{then SR}$$

$$R \rightarrow Y \rightarrow \delta \cdot \quad \text{conflict}$$

RR: Reduce Reduce conflict

$$R \rightarrow X \rightarrow \alpha \cdot \Rightarrow \text{then RR}$$

$$R \rightarrow X \rightarrow \beta \cdot$$

SLR (1) Parser:

SR:

$$S \rightarrow X \rightarrow \alpha \cdot t\beta \quad \left. \begin{array}{l} \\ \end{array} \right\} \$ \Rightarrow \text{then SR}$$

$$R \rightarrow Y \rightarrow \delta \cdot \quad \text{conflict} \quad \left. \begin{array}{l} \\ \end{array} \right\}$$

$t \in \text{follow}(Y)$

RR:

$$X \rightarrow \alpha \cdot \quad \left. \begin{array}{l} \\ \end{array} \right\} \$ \Rightarrow \text{then RR}$$

$$Y \rightarrow \beta \cdot \quad \left. \begin{array}{l} \\ \end{array} \right\}$$

$\text{Follow}(x) \cap \text{follow}(y) \neq \emptyset$

LALR (1) and CLR (1): Same as SLR (1), but instead

SR:

$$X \rightarrow \alpha \cdot t\beta \cdot L_1 \quad \left. \begin{array}{l} \\ \end{array} \right\} \$ \Rightarrow \text{then SR}$$

$$Y \rightarrow \delta \cdot L_2 \quad \text{conflict} \quad \left. \begin{array}{l} \\ \end{array} \right\}$$

$$T \in L_2$$

RR:

$$X \rightarrow \alpha \cdot, L_1 \quad \left. \begin{array}{l} \\ \end{array} \right\} \$ \quad \text{then RR}$$

$$Y \rightarrow \beta \cdot, L_2 \quad \text{conflict} \quad \left. \begin{array}{l} \\ \end{array} \right\}$$

$$L_1 \cap L_2 \neq \emptyset$$

2.4.15 Inadequate Static

A static having ANY conflict is called a conflicting state or independent state.

Note:

The state $S' \rightarrow S$. or $S' \rightarrow S, \$$ is accepted state, and this is not a reduction.

- The only difference between CLR (1) and LALR (1) is that, the states with the similar items, but different Lookaheads are merged together to Reduce space.

Important Points

- If CLR (1) doesn't have any conflict, then conflict may or may not arise after merging in LALR (1).
- If LALR (1) has SR – conflict, then we can conclude that CLR (1) also has SR – Conflict.
- LALR (1) has SR – conflict if and only if CLR (1) also has SR.

- We can construct parser for every unambiguous regular grammar: [CLR (1) Parser].

				L Left to right scan of i/p	R Using reverse RMD	(0) No Lookhead
S	L	R	(1)			
Simple	L to R Scan	Using Reverse RMD	Lookahead			
L	A	L	R	(1)		
Look	Ahead	L to R Scan	Revers RMD	Lookahead		
C	L	R	(1)			
Canonical	L to R Scan	reverse RMD	Lookahead			

Very Important Point:

LALR (1) Parser can Parse non LALR (1) grammar, when only non-SR – Conflict by favouring shift over reduce.

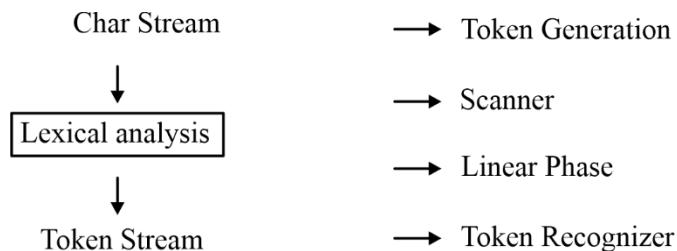
Example: $E \rightarrow E + E \mid E * E \mid id \mid 2 + 3 * 5 \Rightarrow E + E \cdot * 5$



3

LEXICAL ANALYSIS

3.1 Lexical Analysis



3.1.1 Definition

Scan the whole program, char by char and produces the corresponding token.

- Also produces /Lexical Errors (if any).
- Functions of Lexical Analyzer.
 - (1) Scans all the character of the program.
 - (2) Token recognizer.
 - (3) Ignores the comment & spaces.
 - (4) Maximal Munch Rule [Longest Prefix Match].

Note:

The Lexical Analyser uses, the Regular Expression.

Prioritization of Rules.

Longest Prefix match .

- Lexeme → smallest unit of program or Logic.
- Token → internal representation of Lexeme.

3.1.2 Types of Token

- (1) Identifier
- (2) Keywords
- (3) Operators
- (4) Literals/Constants
- (5) Special Symbol

3.1.3 Token Separation

- (1) Spaces
- (2) Punctuation

3.1.4 Implementation

- LEX tool \Rightarrow Lex.yy.e
- All identifiers will have entry in symbol Table/ LA, gives entries into the symbol Table.
Regular Expression \rightarrow DFA \rightarrow Lexical Analyzer

3.1.5 Find number of Tokens

- (1) void main () {
 Printf("gate");
}
 [11 Tokens]
- (2) int x, *P;
 x = 10; p = &x; x++;
[18 Tokens]
- (3) int x;
 x = y;
 x == y;
[11 Tokens]
- (4) int 1x23; [Lexical Error]
- (5) char ch = 'A';
[5 Token]
- (6) char ch = 'A;
Lexical Error.
- (7) char *p = "gate";
[6 Tokens]
- (8) char * p = "gate;
Error.
- (9) int x = 10;
/* comment x = x + 1; ERROR
x = x + 1; [11 Tokens]



4

SYNTAX DIRECTED TRANSACTION

4.1 Syntax Directed Transaction

CFG + Transition }
Syntax + Transition

SDT: CFG + Transition → 1) Meaning 2) Semantic

4.1.1 Application of SDTL

- (1) Used to perform Semantic Analysis.
- (2) Produce Parse Tree.
- (3) Produce intermediate representation.
- (4) Evaluate an expression.
- (5) Convert infix to prefix or postfix.

Example: $S \rightarrow S_1S_2$ [S.count = S₁.count + S₂.count]

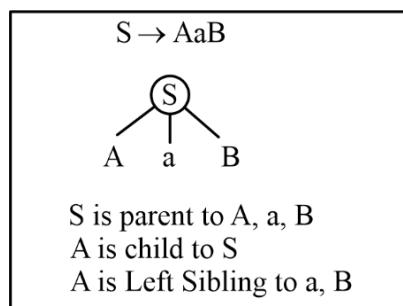
$S \rightarrow (S_1)$ [S.count = S₁.count + 1]

$S \rightarrow \epsilon$ [S.count = 0]

- Count is an attribute for non-terminal

4.1.2 Attributes

- (1) Inherited Attribute
- (2) Synthesized Attribute



- (1) Inherited Attribute: (RHS)

$S \rightarrow AaB$ {A.x = f(B.x | S.x)}

- The computation at any node (non-terminal) depends on parent or siblings (S).

- In above Example, x is inherited attribute.

(2) Synthesized Attribute: (LHS)

$$S \rightarrow A \ B \ \{S.x = f(A.x \mid B.x)\}$$

x is synthesized attribute.

The computation at any node (non-terminal) depends on children.

4.1.3 Identifying Attribute Type

- Always check every Translation.

- | | |
|---|--|
| 1) $D \rightarrow T : L ; \{L.Type = T.Type\}$ inherited
$L \rightarrow L1, id ; \{L1.Type = L.Type\}$ inherited
$L \rightarrow id$
$T \rightarrow integer \{T.Type = int\}$ synthesized | Type is neither inherited nor synthesized |
| 2) $E \rightarrow E1 + T \{E.val = E1.val + T.val\}$ synthesized
$E \rightarrow T \{E.val = T.val\}$ Synthesized
$T \rightarrow T1 - F \{T.val = T1.val - F.val\}$ Synthesized
$F \rightarrow id \{F.val = id.val\}$ synthesized | Val is synthesized attribute |
| 3) $S \rightarrow AB \{A.a = B.x; S.y = A.x\}$ x is inherited y is synthesized
$A \rightarrow a \{A.y = a\}$ y is synthesized
$B \rightarrow b \{B.y = a.y\}$ y is synthesized | x \Rightarrow inherited
y \Rightarrow synthesized |
| 4) $D \rightarrow T \ L \ \{L.in = T.type\}$ inherited(in)
$T \rightarrow int \ \{T.type = int\}$ /synthesized
$L \rightarrow id \ \{\text{Add type}(id.entry, L.in)\}$ | in \Rightarrow inherited
type \Rightarrow synthesized |

4.1.4 Syntax Directed Definitions (SDDs): (Attribute Grammar)

(1) L-Attributed Grammar

- Attribute is synthesized or restricted inherited. (1) Parent 2) Left sibling only).
- Translation can be appended anywhere is RHS of production.
- Example: $S \rightarrow AB \{A.x = S.x + 2\}$
 or, $S \rightarrow AB \{B.x = f(A.x \mid S.x)\}$
 or, $S \rightarrow AB \{S.x = f(A.x \mid B.x)\}$
- Evaluation: In Order (Topological).

(2) S-Attributed Grammar:

- Attribute is synthesized only.
- The transaction is placed only at the end of production.
- Example: $S \rightarrow AB \{S.x = f(Ax \mid Bx)\}$.
- Evaluation:** Reverse RMD (Bottom-Up Parsing).

4.1.5 Identify SDD

(1) $E \rightarrow E_1 + E_2 \{E.type = \text{if } (E_1.type == \text{int} \& \& E.type == \text{int}) \text{ then int}\}$ Synthesizer else type – error.
 $E \rightarrow \text{id } \{E.type = \text{Lookup (id.entry)}\}$ synthesizer.

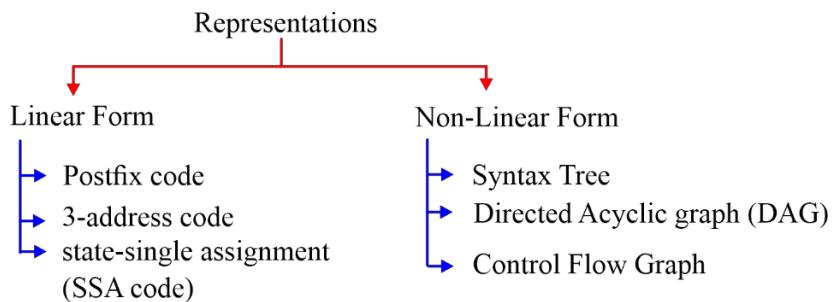
- type is synthesized, hence S-attributed and also L-attributed Grammar.
- Every S-attributed Grammar is also L-attributed Grammar.
- For L-attributed Evaluation, use the In-order of annotated Parser Tree.
- For S-attributed, reverse of RMD is used.
 - find RMD Order.
 - Consider its reverse.



5

INTERMEDIATE, CODE OPTIMIZATION

5.1 Introduction



Example Expression:

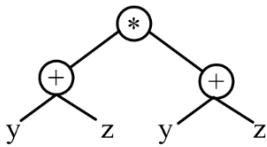
$$(y + z) * (y + z)$$

Post fix → yz + yz + *

SSA → $t_1 = y + z$
 $t_2 = t_1 * t_2$ ⇒ f_1 and f_2 cannot be reassigned

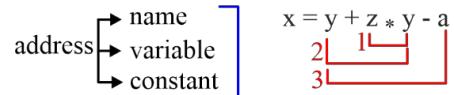
3AC → $t_1 = y + z$
 $t_2 = t_1 \times t_2$

Syntax Tree →



DAG → Reuse the already existing common sub expression

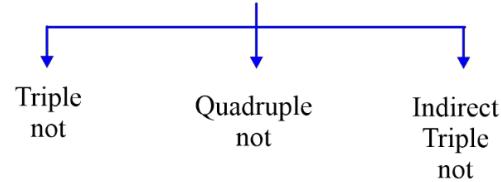
3-address Code: Code in which, at most 3 addresses. [including LHS]



\rightarrow [$t_1 = z * y$
 $t_2 = y + t_1$
 $t_3 = t_2 - a$] Equivalent
3 - address
Code

 $x = t_3$

Representation of 3AC



0	*	z	y
1	+	y	(0)
2	-	(1)	a
3	=	(2)	

0	*	z	y	t_1
1	+	y	t_1	t_2
2	-	t_2	a	t_3
3	=	t_3		x

6	(0)
7	(1)
8	(2)
9	(3)

→ Indirect notation
pointers to the
numbers of Triple

- Triple Notation Quadruple
 → Space efficient → space inefficient
 → time inefficient → time efficient

- 3AC done using operator precedence.

Find minimum number of variables required in equivalent 3AC:

1. $x = u - t$ $x * y \Rightarrow x * (t - z) \Rightarrow (y + w) * (t - z)$

$y = x * v$ $\Rightarrow ((x * v) + w) * (t - z)$

$x = y + w$ $\Rightarrow (((u - t) * v) + w) * (t - z)$

$y = t - z$

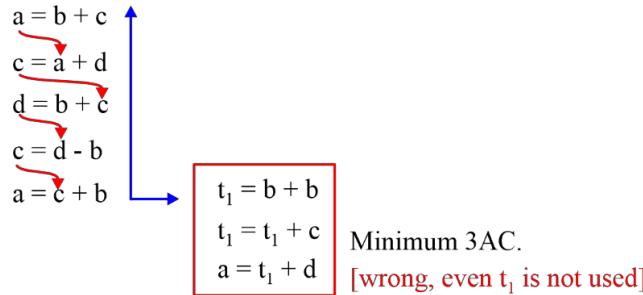
$y = *x *y$

7 variables

$$\begin{bmatrix} u = u - t & u = t - z \\ v = u * u & z = w * v \\ w = v + w \end{bmatrix} \Rightarrow 5 \text{ variables only}$$

⇒ Evaluating the expression:

$$\begin{aligned} a &\Rightarrow c + b \Rightarrow d - b + b \Rightarrow b + c - b + b \\ &\Rightarrow b + a + d - b + b \\ &\Rightarrow b + b + c + d - b + b \\ &\Rightarrow b + b + c + d \end{aligned}$$



∴ Minimum:

$$\left\{ \begin{array}{l} b = b + b \\ c = b + c \\ a = c + d \end{array} \right\} \Rightarrow \text{only 3 variables [most optimal]}$$

5.1.1 Static Single Assignment Code: (SSA Code)

Every variable (address) in the code has single assignment [single meaning] + 3AC.

1.

$$\begin{aligned} x &= u - t \\ y &= x * u \\ x &= y + w \\ y &= t - z \\ y &= x * y \end{aligned}$$

Find SSA?

⇒ [u, t, v, w, z] are already assigned so we can't use them.

Equivalent SSA Code:

$$x = u - t \quad y = x * v$$

$$p = y + w$$

$$q = t - x$$

$$r = p * q$$

in use: x, y, p, q, r ⇒ additional

∴ Total Variable ⇒ 10.

2.

$$\begin{aligned} p &= a - b \\ q &= p * c \\ p &= u * v \\ q &= p + q \end{aligned}$$

⇒ [a, b, c, u, v] are already assigned,

Equivalent SSA Code:

$$p = a - b$$

$$q = p * c$$

$$p_1 = v * u$$

$$q_2 = p_1 + q$$

in use: p, q, p₁, q₂

∴ Total Variable = 9

5.1.2 Control Flow Graphs

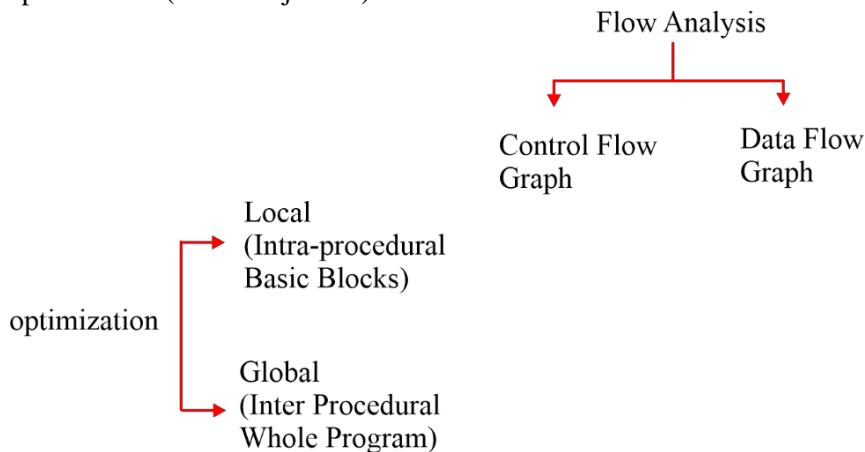
- CFG contain group of basic blocks and controls. CFG has nodes and edges to define basic blocks and controls.
- Basic Blocks: Sequence of 3-address code statements, in which control enters only from 1st statement (called as leader), and leaves from last statement.

Example:

```
1. i = 1          } LB1
2. j = 1          } LB2
3. t1 = 5 * i    }
4. t2 = t1 + 5   }
5. t3 = 4*t2    }
6. t4 = t3      }
7. a[t4] = 1    }
8. j = j + 1    }
9. if j ≤ 5 goto 3 } LB4
10. i = i + 1   }
11. if i < 5 goto 2 } LB6
```

5.2 Code Optimization

Saves space / time. (Basic Objective)



5.2.1 Optimization Methods

1. Constant folding
2. Copy propagation
3. Strength Reduction
4. Dead code elimination
5. Common sub expression elimination.
6. Loop Optimization
7. Peephole Optimization

1. Constant Folding

(i) $x = 2 * 3 + y \Rightarrow x = 6 + y$

Folding

ii) $x = 2 + y * 3 \}$ can't fold the constant

2. Copy Propagation

i) Variable Propagation:

$x = y;$

$z = y + 2;$

$\Rightarrow z = x + 2;$

ii) Constant Propagation:

$x = 3$

$z = 3 + a;$

$\Rightarrow z = x + a$

3. Strength Reduction:

Replace expensive statement / instruction with cheaper one.

(i) $x = 2 * y$ **costly** $\Rightarrow x = y + y$; **Cheap**

(ii) $x = 2 * y \Rightarrow x = y << 1$; **Much Cheaper**

(iii) $x = y / 8 \Rightarrow x = y >> 3;$

4. Dead Code Elimination:

$x = 2;$ **FALSE**

if ($x > 2$)

 printf("code"); **DEAD CODE CAN BE REMOVED**

else

 printf("optimization");

- Hence, above dead code never executes during execution. We can always delete such code.

5. Common Sub Expression Elimination:

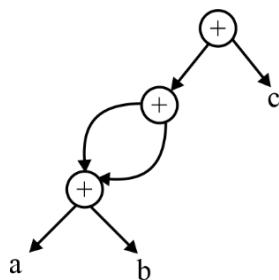
DAG is used to eliminate common sub expression.

Example: $x = (a + b) + (a + b) + c;$

$\Rightarrow t_1 = a + b$

$x = t_1 + t_1 + c$

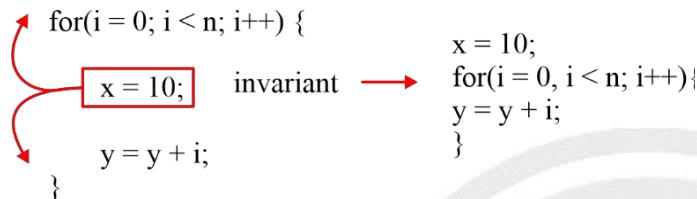
$x = 2;$
printf("optimization");



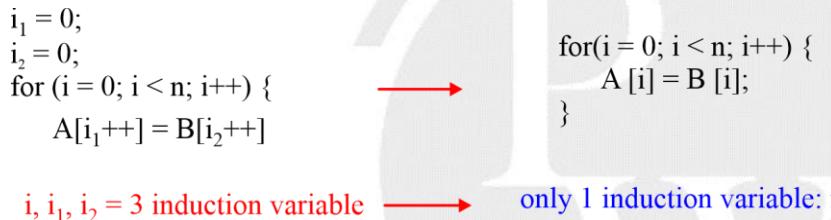
6. Loop Optimization:

(i) Code Motion – Frequency Reduction:

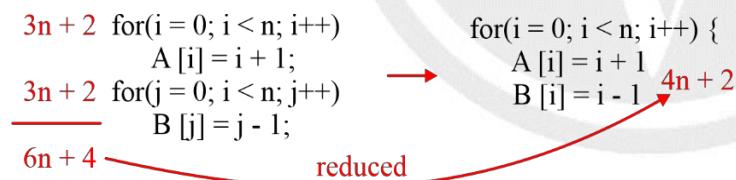
Move the loop invariant code outside of loop.



(ii) Induction Variable elimination:



(iii) Loop Merging / Combining: (Loop Jamming)



(iv) Loop Unrolling:

1) for (i = 0; i < 3; i++) printf("CD");
 printf("CD");
 printf("CD");

$3 \times 3 + 2 = 11$ Statements → 3 statements

2) for (i = 0; i < 2n; i++) { for (i = 0; i < n; i++) {
 printf("CD"); printf("CD");
 } printf("CD");
 }

$(2 \times 3n + 2) = 6n + 2$ → $(4n + 2)$

7. Peephole Optimization:

Examines a short sequence of target instructions in a window (*peephole*) and replaces the instructions by a faster and/or shorter sequence when possible.

- Applied to intermediate code or target code
- Following Optimizations can be used:

- Redundant instruction elimination
- Flow-of-control optimizations
- Algebraic simplifications
- Use of machine idioms

