

Propositions: Proposition is a declarative sentence that is either true or false, but not both.
or statement.

For example: (i) 5 is an integer.

Example 1:

(ii) $\sqrt{5}$ is an integer.

(iii) ^{New} Delhi is the capital of India

(iv) Toronto is the capital of Canada.

→ Ottawa

Each of above statement is a declarative sentence. As

Sentence (i) & (iii) are true, whereas (ii) & (iv) are false.

* Typically lowercase letters with or without subscripts are used to denote propositions. For example, we might write

p : 4 is an integer

q : 5 is an even integer

r : $\sqrt{5}$ is an irrational number.

Here p , q , and r denotes the propositions.

Example 2: Consider the following sentences:

p : what are you doing? →

q : Enjoy the lovely weather!

Here p and q are not declarative sentences, so these are not propositions.

e 3: (i) $x+1=2$

(ii) $x+y=z$

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Equation (i) & (ii) are not propositions because they are neither true nor false.

But it is noted here, that these equations can be turned into propositions by assigning particular values to x, y & z .

* We use letters to denote propositional variables (or statement variables). The conventional letters used for propositional variables are p, q, r, s, \dots

If the truth value of proposition is True, it is denoted by T.

If the truth value of proposition is False, it is denoted by F.

* The area of logic that deals with propositions is called the propositional calculus or propositional logic. It was first developed by the Greek philosopher Aristotle.

Compound Propositions: Propositions formed from existing propositions using logical operators.

Negation: Let p be a proposition. The negation of p , denoted by $\sim p$ (also written as \bar{p}), is the statement:
"It is not the case that p "

proposition $\sim p$ is read as "not p ".

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The truth value of the negation of p , " $\sim p$ " is opposite of the truth value of p .

Formation.

*Typically, if p is a statement, then its negation is formed by writing "it is not the case that p ".

For example, if

p : 2 is positive, then

$\sim p$: It is not the case that 2 is positive.

OR

$\sim p$: 2 is not positive (In simple English).

Example 2:

Find the negation of the proposition "Today is Friday"

Express in simple English.

The negation is "It is not the case that today is Friday".

In simple English "Today is not Friday".

Truth Table for negation of p

p	$\sim p$
T	F
F	T

Logical Operators: That are used to form new propositions from two or more existing propositions. These logical operators are also called connectives.

Compound Proposition: When one or more propositions are connected through various connectives are called Compound proposition

Primitive proposition: A proposition is said to be primitive if it cannot be broken into simpler propositions.

Connectives: Logical operators that are used to form new propositions from two or more existing propositions. These logical operators are called connectives.

Def. 2:

Conjunction: Let p and q be propositions. The conjunction of p and q , denoted by $p \wedge q$ is the proposition " p and q ".

The conjunction $p \wedge q$ is true if both p and q are true and is false otherwise.

Truth table for conjunction of two proposition p & q is given by

p	q	$p \wedge q$
T	T	T
T	F	F
F	T	F
F	F	F

Example 1: Let

p : 2 divides 4

q : 3 is greater than 5. , then

$p \wedge q$: 2 divides 4 and 3 is greater than 5.

Because p is T &

q is F ; #

$\therefore p \wedge q$ is F.

* The symbol \wedge is called "and".

* In logic the word "but" can be used instead of "and".

For Example: "The sun is shining and it is raining," can also be written as "The sun is shining but it is raining".