

Gradient Checking

Gradient checking will assure that our backpropagation works as intended. We can approximate the derivative of our cost function with:

$$\frac{\partial}{\partial \theta} J(\theta) \approx \frac{J(\theta + \epsilon) - J(\theta - \epsilon)}{2\epsilon}$$

With multiple theta matrices, we can approximate the derivative **with respect to θ_J** as follows:

$$\frac{\partial}{\partial \theta_J} J(\theta) \approx \frac{J(\theta_1, \dots, \theta_{J+\epsilon}, \dots, \theta_n) - J(\theta_1, \dots, \theta_{J-\epsilon}, \dots, \theta_n)}{2\epsilon}$$

A small value for ϵ (epsilon) such as $\epsilon = 10^{-4}$, guarantees that the math works out properly. If the value for ϵ is too small, we can end up with numerical problems.

Hence, we are only adding or subtracting epsilon to the θ_J matrix. In octave we can do it as follows:

```
1 epsilon = 1e-4;
2 for i = 1:n,
3     thetaPlus = theta;
4     thetaPlus(i) += epsilon;
5     thetaMinus = theta;
6     thetaMinus(i) -= epsilon;
7     gradApprox(i) = (J(thetaPlus) - J(thetaMinus))/(2*epsilon)
8 end;
9 |
```

We previously saw how to calculate the deltaVector. So once we compute our gradApprox vector, we can check that $\text{gradApprox} \approx \text{deltaVector}$.

Once you have verified **once** that your backpropagation algorithm is correct, you don't need to compute gradApprox again. The code to compute gradApprox can be very slow.