

Solution 1

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1  # Copyright © 2020 AlgoExpert, LLC. All rights reserved.
2
3  # O(a * (a + r) + a + r + alog(a)) time | O(a + r) space - where a is the number of airports and r is the number of routes
4  def airportConnections(airports, routes, startingAirport):
5      airportGraph = createAirportGraph(airports, routes)
6      unreachableAirportNodes = getUnreachableAirportNodes(airportGraph, airports, startingAirport)
7      markUnreachableConnections(airportGraph, unreachableAirportNodes)
8      return getMinNumberOfNewConnections(airportGraph, unreachableAirportNodes)
9
10
11 # O(a + r) time | O(a + r) space
12 def createAirportGraph(airports, routes):
13     airportGraph = {}
14     for airport in airports:
15         airportGraph[airport] = AirportNode(airport)
16     for route in routes:
17         airport, connection = route
18         airportGraph[airport].connections.append(connection)
19     return airportGraph
20
21
22 # O(a + r) time | O(a) space
23 def getUnreachableAirportNodes(airportGraph, airports, startingAirport):
24     visitedAirports = {}
25     depthFirstTraverseAirports(airportGraph, startingAirport, visitedAirports)
26
27     unreachableAirportNodes = []
28     for airport in airports:
29         if airport in visitedAirports:
30             continue
31         airportNode = airportGraph[airport]
32         airportNode.isReachable = False
33         unreachableAirportNodes.append(airportNode)
34     return unreachableAirportNodes
35
36
37 def depthFirstTraverseAirports(airportGraph, airport, visitedAirports):
38     if airport in visitedAirports:
39         return
40     visitedAirports[airport] = True
41     connections = airportGraph[airport].connections
42     for connection in connections:
43         depthFirstTraverseAirports(airportGraph, connection, visitedAirports)
44
45
46 # O(a * (a + r)) time | O(a) space
47 def markUnreachableConnections(airportGraph, unreachableAirportNodes):
48     for airportNode in unreachableAirportNodes:
49         airport = airportNode.airport
50         unreachableConnections = []
51         depthFirstAddUnreachableConnections(airportGraph, airport, unreachableConnections, {})
52         airportNode.unreachableConnections = unreachableConnections
53
54
55 def depthFirstAddUnreachableConnections(airportGraph, airport, unreachableConnections, visitedAirports):
56     if airportGraph[airport].isReachable:
57         return
58     if airport in visitedAirports:
59         return
60     visitedAirports[airport] = True
61     unreachableConnections.append(airport)
62     connections = airportGraph[airport].connections
63     for connection in connections:
64         depthFirstAddUnreachableConnections(airportGraph, connection, unreachableConnections, visitedAirports)
65
66
67 # O(alog(a) + a + r) time | O(1) space
68 def getMinNumberOfNewConnections(airportGraph, unreachableAirportNodes):
69     unreachableAirportNodes.sort(key=lambda airport: len(airport.unreachableConnections), reverse=True)
70
71     numberOfNewConnections = 0
72     for airportNode in unreachableAirportNodes:
73         if airportNode.isReachable:
74             continue
75         numberOfNewConnections += 1
76         for connection in airportNode.unreachableConnections:
77             airportGraph[connection].isReachable = True
78     return numberOfNewConnections
79
80
81 class AirportNode:
82     def __init__(self, airport):
83         self.airport = airport
84         self.connections = []
85         self.isReachable = True
86         self.unreachableConnections = []
87
```

