

Solution 1

```
1 // Copyright © 2020 AlgoExpert, LLC. All rights reserved.
2
3 import java.util.*;
4
5 class Program {
6
7     // O(a * (a + r) + a + r + alog(a)) time | O(a + r) space - where a is the number of airports and
8     // r is the number of routes
9     public static int airportConnections(
10         List<String> airports, List<List<String>> routes, String startingAirport) {
11         Map<String, AirportNode> airportGraph = createAirportGraph(airports, routes);
12         List<AirportNode> unreachableAirportNodes =
13             getUnreachableAirportNodes(airportGraph, airports, startingAirport);
14         markUnreachableConnections(airportGraph, unreachableAirportNodes);
15         return getMinNumberOfNewConnections(airportGraph, unreachableAirportNodes);
16     }
17
18     // O(a + r) time | O(a + r) space
19     public static Map<String, AirportNode> createAirportGraph(
20         List<String> airports, List<List<String>> routes) {
21         Map<String, AirportNode> airportGraph = new HashMap<String, AirportNode>();
22         for (String airport : airports) {
23             airportGraph.put(airport, new AirportNode(airport));
24         }
25         for (List<String> route : routes) {
26             String airport = route.get(0);
27             String connection = route.get(1);
28             airportGraph.get(airport).connections.add(connection);
29         }
30         return airportGraph;
31     }
32
33     // O(a + r) time | O(a) space
34     public static List<AirportNode> getUnreachableAirportNodes(
35         Map<String, AirportNode> airportGraph, List<String> airports, String startingAirport) {
36         Set<String> visitedAirports = new HashSet<String>();
37         depthFirstTraverseAirports(airportGraph, startingAirport, visitedAirports);
38
39         List<AirportNode> unreachableAirportNodes = new ArrayList<AirportNode>();
40         for (String airport : airports) {
41             if (visitedAirports.contains(airport)) continue;
42             AirportNode airportNode = airportGraph.get(airport);
43             airportNode.isReachable = false;
44             unreachableAirportNodes.add(airportNode);
45         }
46         return unreachableAirportNodes;
47     }
48
49     public static void depthFirstTraverseAirports(
50         Map<String, AirportNode> airportGraph, String airport, Set<String> visitedAirports) {
51         if (visitedAirports.contains(airport)) return;
52         visitedAirports.add(airport);
53         List<String> connections = airportGraph.get(airport).connections;
54         for (String connection : connections) {
55             depthFirstTraverseAirports(airportGraph, connection, visitedAirports);
56         }
57     }
58
59     // O(a * (a + r)) time | O(a) space
60     public static void markUnreachableConnections(
61         Map<String, AirportNode> airportGraph, List<AirportNode> unreachableAirportNodes) {
62         for (AirportNode airportNode : unreachableAirportNodes) {
63             String airport = airportNode.airport;
64             List<String> unreachableConnections = new ArrayList<String>();
65             Set<String> visitedAirports = new HashSet<String>();
66             depthFirstAddUnreachableConnections(
67                 airportGraph, airport, unreachableConnections, visitedAirports);
68             airportNode.unreachableConnections = unreachableConnections;
69         }
70     }
71
72     public static void depthFirstAddUnreachableConnections(
73         Map<String, AirportNode> airportGraph,
74         String airport,
75         List<String> unreachableConnections,
76         Set<String> visitedAirports) {
77         if (airportGraph.get(airport).isReachable) return;
78         if (visitedAirports.contains(airport)) return;
79         visitedAirports.add(airport);
80         unreachableConnections.add(airport);
81         List<String> connections = airportGraph.get(airport).connections;
82         for (String connection : connections) {
83             depthFirstAddUnreachableConnections(
84                 airportGraph, connection, unreachableConnections, visitedAirports);
85         }
86     }
87
88     // O(alog(a) + a + r) time | O(1) space
89     public static int getMinNumberOfNewConnections(
90         Map<String, AirportNode> airportGraph, List<AirportNode> unreachableAirportNodes) {
91         unreachableAirportNodes.sort(
92             (a1, a2) -> a2.unreachableConnections.size() - a1.unreachableConnections.size());
93         int numberOfNewConnections = 0;
94         for (AirportNode airportNode : unreachableAirportNodes) {
95             if (airportNode.isReachable) continue;
96             numberOfNewConnections++;
97             for (String connection : airportNode.unreachableConnections) {
98                 airportGraph.get(connection).isReachable = true;
99             }
100         }
101         return numberOfNewConnections;
102     }
103
104     static class AirportNode {
105         String airport;
106         List<String> connections;
107         boolean isReachable;
108         List<String> unreachableConnections;
109
110         public AirportNode(String airport) {
111             this.airport = airport;
112             connections = new ArrayList<String>();
113             isReachable = true;
114             unreachableConnections = new ArrayList<String>();
115         }
116     }
117 }
```

