

Solution 1Solution 2Solution 3

```
1 // Copyright © 2020 AlgoExpert, LLC. All rights reserved.
2
3 using namespace std;
4
5 // O(n^2) time | O(n) space
6 int numberOfBinaryTreeTopologies(int n) {
7     vector<int> cache{1};
8     for (int m = 1; m < n + 1; m++) {
9         int numberOfTrees = 0;
10        for (int leftTreeSize = 0; leftTreeSize < m; leftTreeSize++) {
11            int rightTreeSize = m - 1 - leftTreeSize;
12            int numberOfLeftTrees = cache[leftTreeSize];
13            int numberOfRightTrees = cache[rightTreeSize];
14            numberOfTrees += numberOfLeftTrees * numberOfRightTrees;
15        }
16        cache.push_back(numberOfTrees);
17    }
18    return cache[n];
19 }
20
```

