Natural Language Processing with Deep Learning CS224N/Ling284



Lecture 6: Language Models and Recurrent Neural Networks

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Overview

Today we will:

- Introduce a new NLP task
 - Language Modeling

motivates

- Introduce a new family of neural networks
 - Recurrent Neural Networks (RNNs)

These are two of the most important ideas for the rest of the class!

Language Modeling

 Language Modeling is the task of predicting what word comes next.

• More formally: given a sequence of words $m{x}^{(1)}, m{x}^{(2)}, \dots, m{x}^{(t)}$, compute the probability distribution of the next word $m{x}^{(t+1)}$:

$$P(\boldsymbol{x}^{(t+1)}|\ \boldsymbol{x}^{(t)},\dots,\boldsymbol{x}^{(1)})$$

where $oldsymbol{x}^{(t+1)}$ can be any word in the vocabulary $V = \{oldsymbol{w}_1, ..., oldsymbol{w}_{|V|}\}$

A system that does this is called a Language Model.

Language Modeling

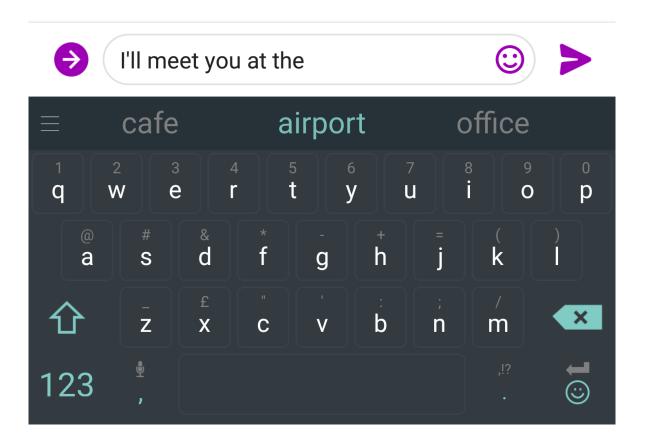
- You can also think of a Language Model as a system that assigns probability to a piece of text.
- For example, if we have some text $x^{(1)}, \dots, x^{(T)}$, then the probability of this text (according to the Language Model) is:

$$P(\mathbf{x}^{(1)}, \dots, \mathbf{x}^{(T)}) = P(\mathbf{x}^{(1)}) \times P(\mathbf{x}^{(2)} | \mathbf{x}^{(1)}) \times \dots \times P(\mathbf{x}^{(T)} | \mathbf{x}^{(T-1)}, \dots, \mathbf{x}^{(1)})$$

$$= \prod_{t=1}^{T} P(\mathbf{x}^{(t)} | \mathbf{x}^{(t-1)}, \dots, \mathbf{x}^{(1)})$$

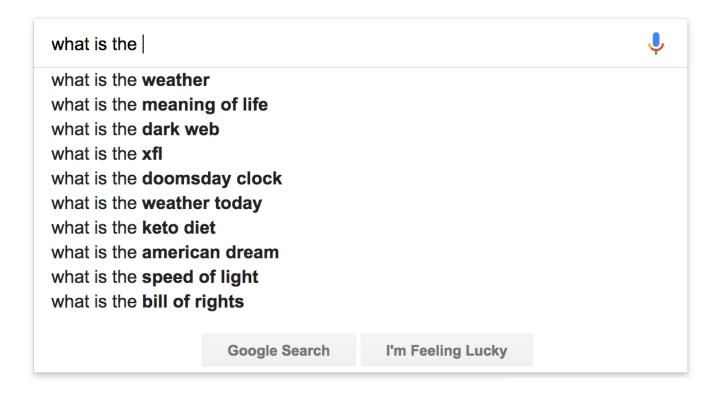
This is what our LM provides

You use Language Models every day!



You use Language Models every day!





n-gram Language Models

the students opened their _____

- Question: How to learn a Language Model?
- Answer (pre- Deep Learning): learn a n-gram Language Model!
- <u>Definition</u>: A n-gram is a chunk of n consecutive words.
 - unigrams: "the", "students", "opened", "their"
 - bigrams: "the students", "students opened", "opened their"
 - trigrams: "the students opened", "students opened their"
 - 4-grams: "the students opened their"
- <u>Idea:</u> Collect statistics about how frequent different n-grams are, and use these to predict next word.

n-gram Language Models

• First we make a simplifying assumption: $x^{(t+1)}$ depends only on the preceding n-1 words.

$$P(oldsymbol{x}^{(t+1)}|oldsymbol{x}^{(t)},\ldots,oldsymbol{x}^{(1)}) = P(oldsymbol{x}^{(t+1)}|oldsymbol{x}^{(t)},\ldots,oldsymbol{x}^{(t-n+2)})$$
 (assumption)

prob of a n-gram
$$= P(\boldsymbol{x}^{(t+1)}, \boldsymbol{x}^{(t)}, \dots, \boldsymbol{x}^{(t-n+2)})$$
 (definition of conditional prob)

- Question: How do we get these n-gram and (n-1)-gram probabilities?
- Answer: By counting them in some large corpus of text!

$$pprox rac{ ext{count}(oldsymbol{x}^{(t+1)},oldsymbol{x}^{(t)},\ldots,oldsymbol{x}^{(t-n+2)})}{ ext{count}(oldsymbol{x}^{(t)},\ldots,oldsymbol{x}^{(t-n+2)})}$$
 (statistical approximation)

n-gram Language Models: Example

Suppose we are learning a 4-gram Language Model.

$$P(\boldsymbol{w}|\text{students opened their}) = \frac{\text{count}(\text{students opened their }\boldsymbol{w})}{\text{count}(\text{students opened their})}$$

For example, suppose that in the corpus:

- "students opened their" occurred 1000 times
- "students opened their books" occurred 400 times
 - \rightarrow P(books | students opened their) = 0.4
- "students opened their exams" occurred 100 times
 - → P(exams | students opened their) = 0.1

Should we have discarded the "proctor" context?

Sparsity Problems with n-gram Language Models



Problem: What if "students opened their w" never occurred in data? Then w has probability 0!

(Partial) Solution: Add small δ to the count for every $\boldsymbol{w} \in V$. This is called *smoothing*.

 $P(\boldsymbol{w}|\text{students opened their}) =$

|count(students opened their w)|

count(students opened their)

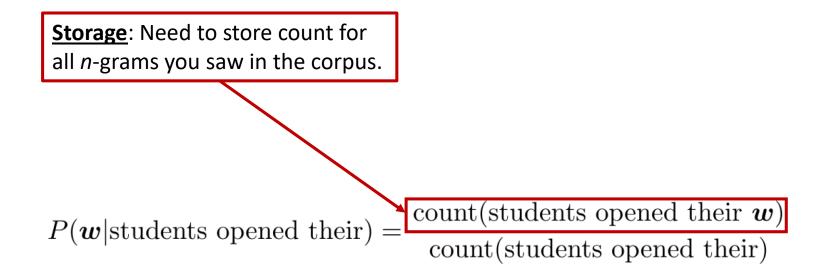
Sparsity Problem 2

Problem: What if "students opened their" never occurred in data? Then we can't calculate probability for any w!

(Partial) Solution: Just condition on "opened their" instead. This is called backoff.

Note: Increasing *n* makes sparsity problems *worse*. Typically we can't have *n* bigger than 5.

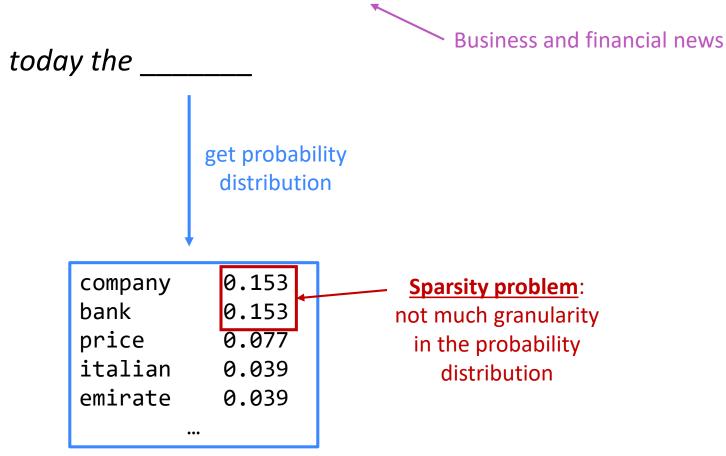
Storage Problems with n-gram Language Models



Increasing *n* or increasing corpus increases model size!

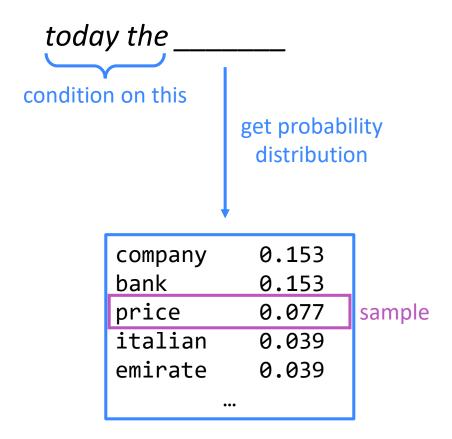
n-gram Language Models in practice

You can build a simple trigram Language Model over a
 1.7 million word corpus (Reuters) in a few seconds on your laptop*

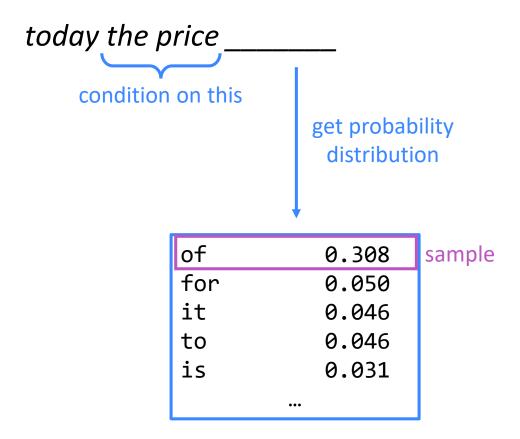


Otherwise, seems reasonable!

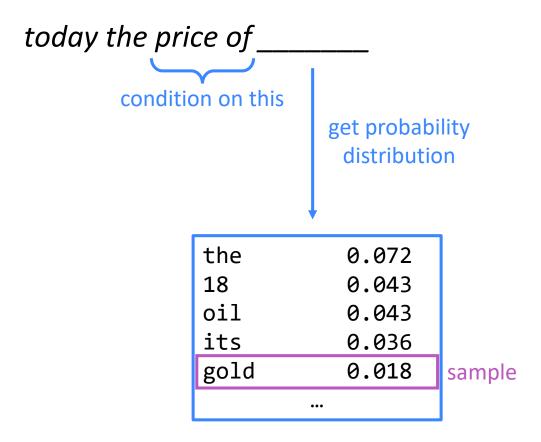
You can also use a Language Model to generate text.



You can also use a Language Model to generate text.



You can also use a Language Model to generate text.



You can also use a Language Model to generate text.

today the price of gold _____

You can also use a Language Model to generate text.

today the price of gold per ton, while production of shoe lasts and shoe industry, the bank intervened just after it considered and rejected an imf demand to rebuild depleted european stocks, sept 30 end primary 76 cts a share.

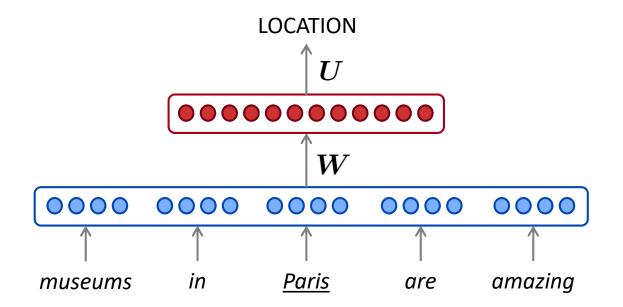
Surprisingly grammatical!

...but **incoherent.** We need to consider more than three words at a time if we want to model language well.

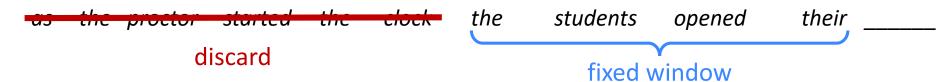
But increasing *n* worsens sparsity problem, and increases model size...

How to build a *neural* Language Model?

- Recall the Language Modeling task:
 - Input: sequence of words $oldsymbol{x}^{(1)}, oldsymbol{x}^{(2)}, \dots, oldsymbol{x}^{(t)}$
 - Output: prob dist of the next word $P(\boldsymbol{x}^{(t+1)}|\ \boldsymbol{x}^{(t)},\dots,\boldsymbol{x}^{(1)})$
- How about a window-based neural model?
 - We saw this applied to Named Entity Recognition in Lecture 3:



A fixed-window neural Language Model



A fixed-window neural Language Model

output distribution

$$\hat{\boldsymbol{y}} = \operatorname{softmax}(\boldsymbol{U}\boldsymbol{h} + \boldsymbol{b}_2) \in \mathbb{R}^{|V|}$$

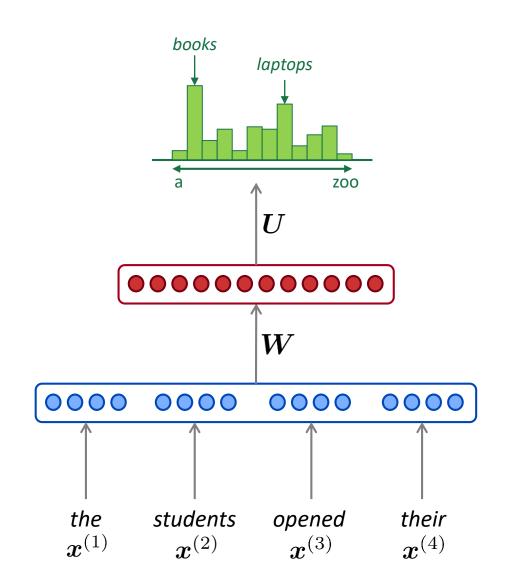
hidden layer

$$\boldsymbol{h} = f(\boldsymbol{W}\boldsymbol{e} + \boldsymbol{b}_1)$$

concatenated word embeddings

$$e = [e^{(1)}; e^{(2)}; e^{(3)}; e^{(4)}]$$

words / one-hot vectors $oldsymbol{x}^{(1)}, oldsymbol{x}^{(2)}, oldsymbol{x}^{(3)}, oldsymbol{x}^{(4)}$



A fixed-window neural Language Model

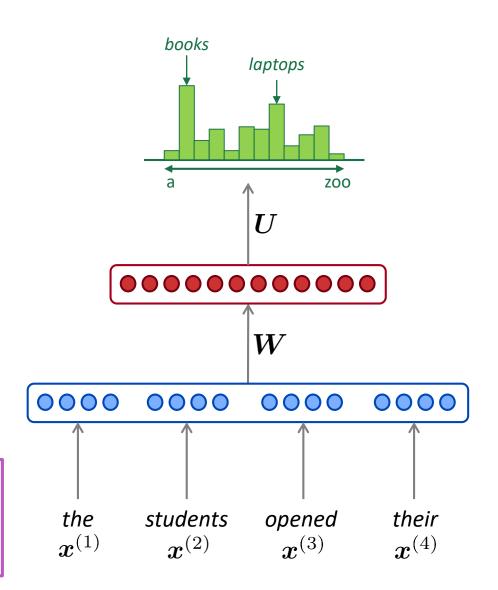
Improvements over *n*-gram LM:

- No sparsity problem
- Don't need to store all observed n-grams

Remaining **problems**:

- Fixed window is too small
- Enlarging window enlarges W
- Window can never be large enough!
- $x^{(1)}$ and $x^{(2)}$ are multiplied by completely different weights in W. No symmetry in how the inputs are processed.

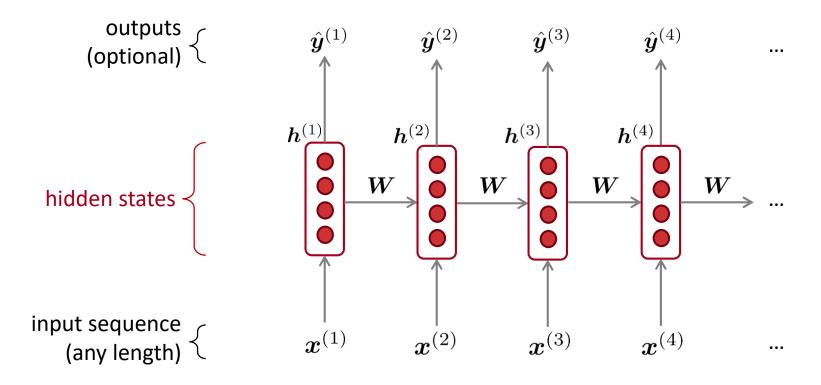
We need a neural architecture that can process any length input



Recurrent Neural Networks (RNN)

A family of neural architectures

Core idea: Apply the same weights $oldsymbol{W}$ repeatedly



A RNN Language Model

output distribution

$$\hat{m{y}}^{(t)} = \operatorname{softmax}\left(m{U}m{h}^{(t)} + m{b}_2\right) \in \mathbb{R}^{|V|}$$

hidden states

$$\boldsymbol{h}^{(t)} = \sigma \left(\boldsymbol{W}_h \boldsymbol{h}^{(t-1)} + \boldsymbol{W}_e \boldsymbol{e}^{(t)} + \boldsymbol{b}_1 \right)$$

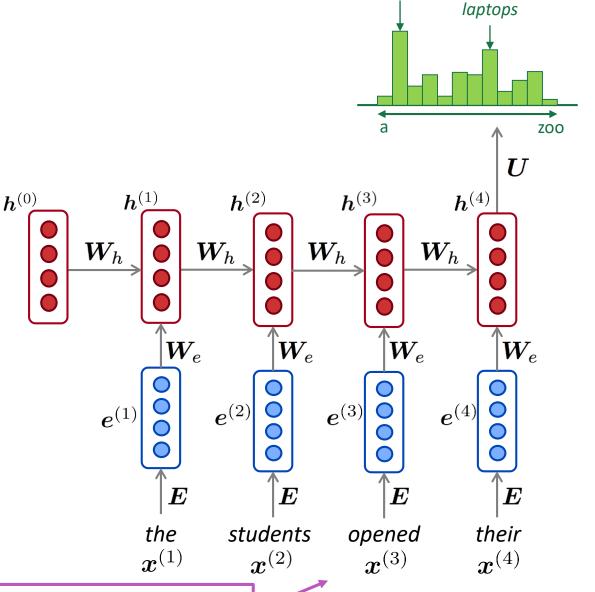
 $m{h}^{(0)}$ is the initial hidden state

word embeddings

$$\boldsymbol{e}^{(t)} = \boldsymbol{E} \boldsymbol{x}^{(t)}$$

words / one-hot vectors

$$\boldsymbol{x}^{(t)} \in \mathbb{R}^{|V|}$$



 $\hat{\boldsymbol{y}}^{(4)} = P(\boldsymbol{x}^{(5)}|\text{the students opened their})$

books

Note: this input sequence could be much longer, but this slide doesn't have space!

books

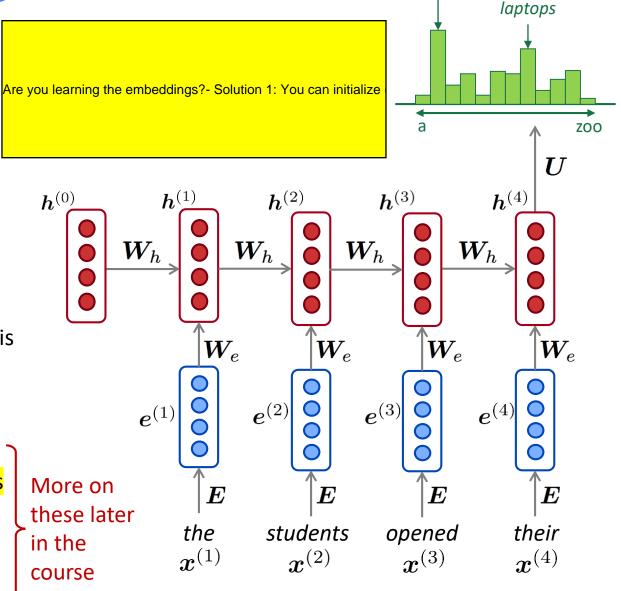
A RNN Language Model

RNN **Advantages**:

- Can process any length input
- Computation for step t can (in theory) use information from many steps back
- Model size doesn't increase for longer input
- Same weights applied on every timestep, so there is symmetry in how inputs are processed.

RNN Disadvantages:

- Recurrent computation is slow
- In practice, difficult to access information from many steps back

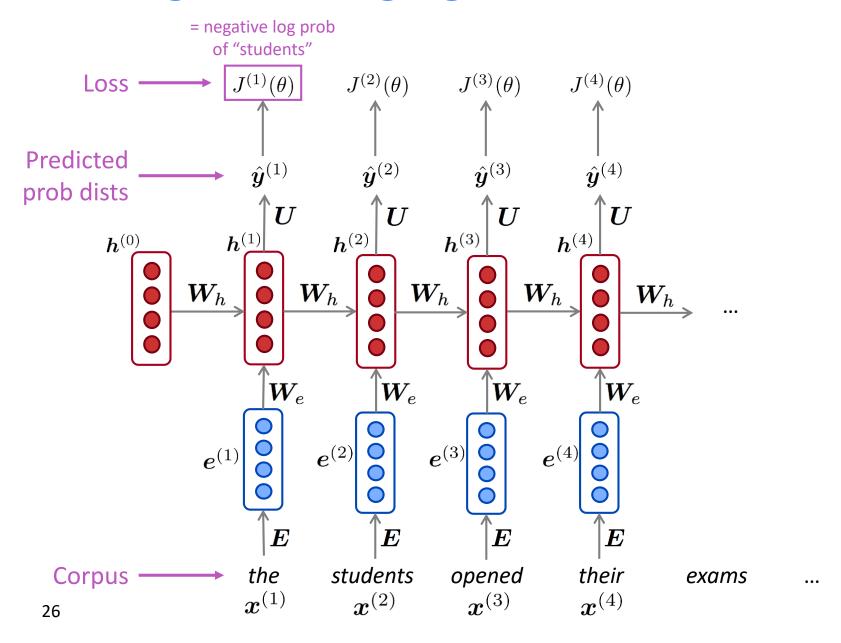


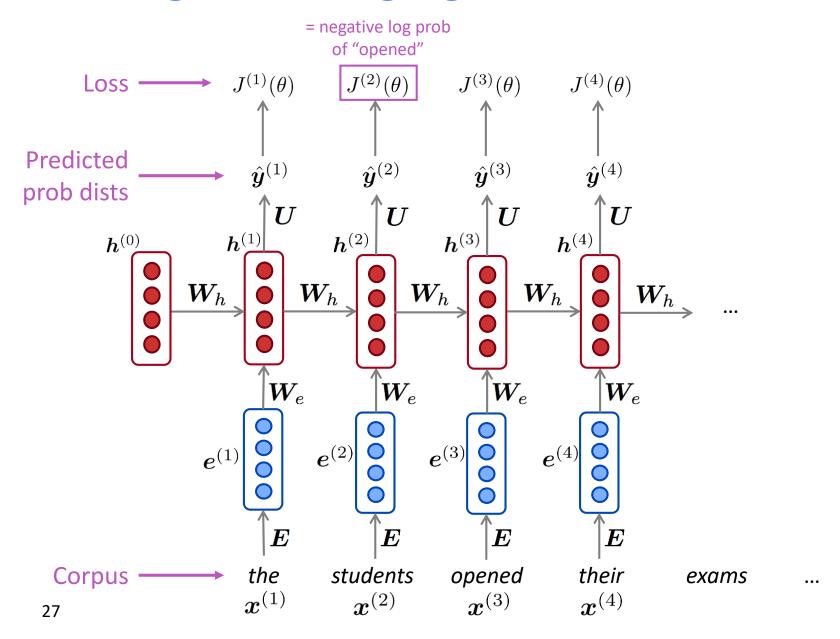
- Get a big corpus of text which is a sequence of words $x^{(1)}, \dots, x^{(T)}$
- Feed into RNN-LM; compute output distribution $\hat{m{y}}^{(t)}$ for *every step t.*
 - i.e. predict probability dist of every word, given words so far
- Loss function on step t is cross-entropy between predicted probability distribution $\hat{y}^{(t)}$, and the true next word $y^{(t)}$ (one-hot for $x^{(t+1)}$):

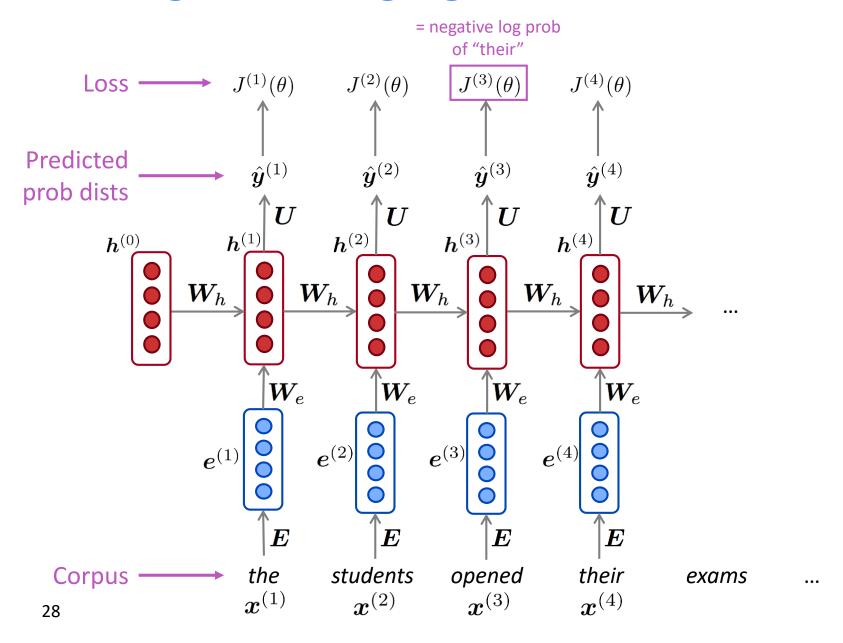
$$J^{(t)}(\theta) = CE(\boldsymbol{y}^{(t)}, \hat{\boldsymbol{y}}^{(t)}) = -\sum_{w \in V} \boldsymbol{y}_w^{(t)} \log \hat{\boldsymbol{y}}_w^{(t)} = -\log \hat{\boldsymbol{y}}_{\boldsymbol{x}_{t+1}}^{(t)}$$

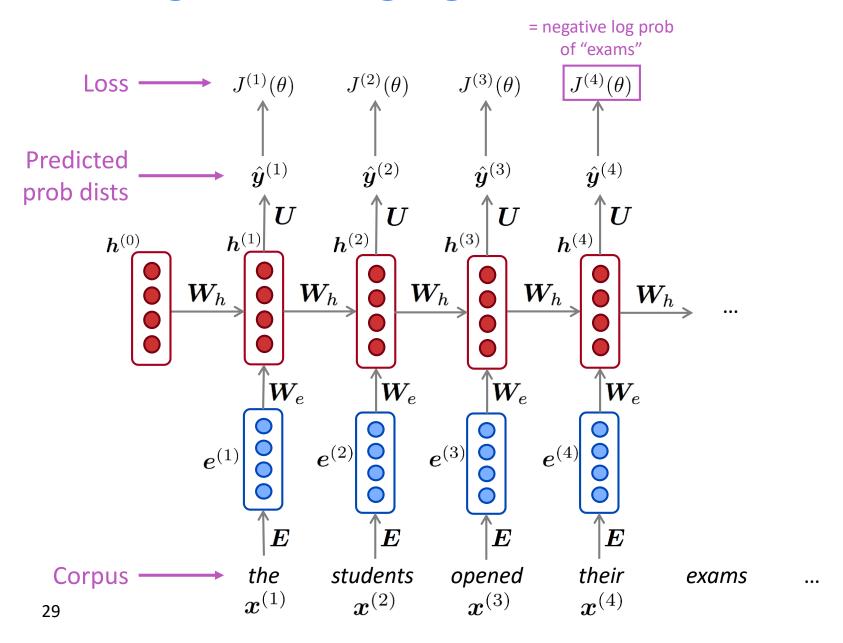
Average this to get overall loss for entire training set:

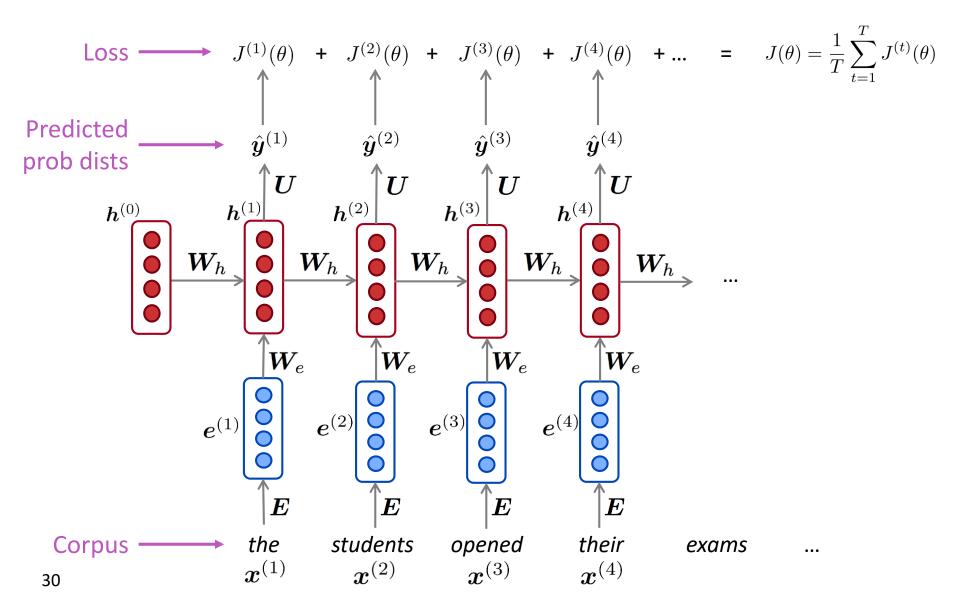
$$J(\theta) = \frac{1}{T} \sum_{t=1}^{T} J^{(t)}(\theta) = \frac{1}{T} \sum_{t=1}^{T} -\log \hat{\boldsymbol{y}}_{\boldsymbol{x}_{t+1}}^{(t)}$$









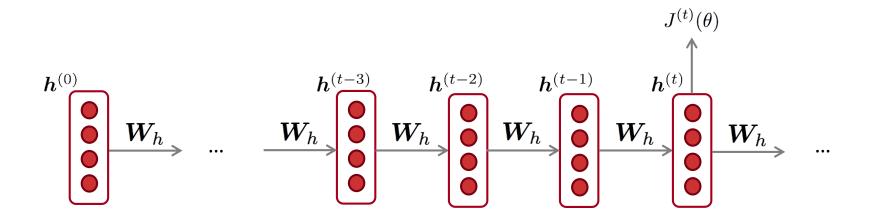


• However: Computing loss and gradients across entire corpus $\boldsymbol{x}^{(1)},\dots,\boldsymbol{x}^{(T)}$ is too expensive!

$$J(\theta) = \frac{1}{T} \sum_{t=1}^{T} J^{(t)}(\theta)$$

- In practice, consider $x^{(1)}, \dots, x^{(T)}$ as a sentence (or a document)
- Recall: Stochastic Gradient Descent allows us to compute loss and gradients for small chunk of data, and update.
- Compute loss $J(\theta)$ for a sentence (actually a batch of sentences), compute gradients and update weights. Repeat.

Backpropagation for RNNs



Question: What's the derivative of $J^{(t)}(\theta)$ w.r.t. the repeated weight matrix $m{W}_h$?

w.r.t: with respect to

Answer:
$$\frac{\partial J^{(t)}}{\partial \boldsymbol{W_h}} = \sum_{i=1}^t \frac{\partial J^{(t)}}{\partial \boldsymbol{W_h}} \Big|_{(i)}$$

"The gradient w.r.t. a repeated weight is the sum of the gradient w.r.t. each time it appears"

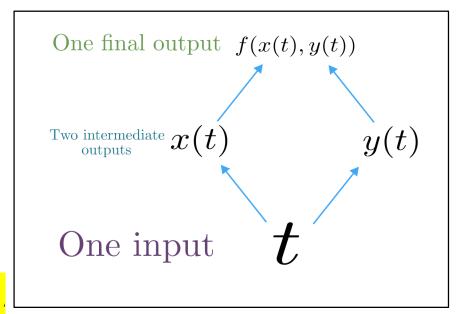
Why?

Multivariable Chain Rule

ullet Given a multivariable function f(x,y), and two single variable functions x(t) and y(t), here's what the multivariable chain rule says:

$$\left(rac{d}{dt} f(oldsymbol{x}(t), oldsymbol{y}(t))
ight) = rac{\partial f}{\partial oldsymbol{x}} rac{doldsymbol{x}}{dt} + rac{\partial f}{\partial oldsymbol{y}} rac{doldsymbol{y}}{dt}
ight)$$

Derivative of composition function



Multivariable chain rule KHAN

Source:

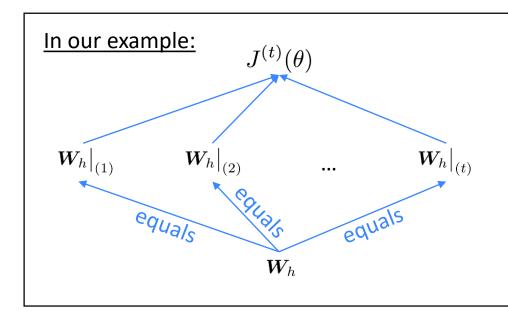
nttps://www.khanacademy.org/math/multivariable-calculus/multivariable-derivatives/differentiating-vector-valued-functions/a/multivariable-chain-rule-simple-version

Backpropagation for RNNs: Proof sketch

ullet Given a multivariable function f(x,y), and two single variable functions x(t) and y(t), here's what the multivariable chain rule says:

$$\left(rac{d}{dt} \, f(oldsymbol{x}(t), oldsymbol{y}(t))
ight) = rac{\partial f}{\partial oldsymbol{x}} \, rac{doldsymbol{x}}{dt} + rac{\partial f}{\partial oldsymbol{y}} \, rac{doldsymbol{y}}{dt}
ight)$$

Derivative of composition function



Apply the multivariable chain rule:

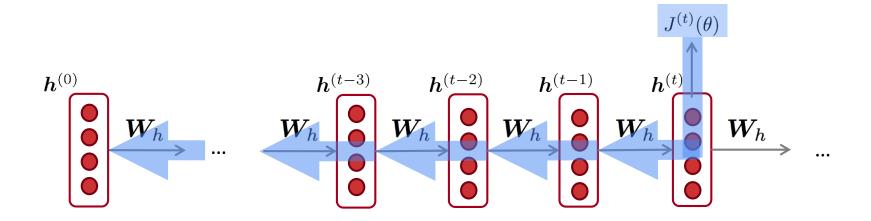
$$oxed{oxed{W_h}}_{oxed{W_h}}_{(t)} = \sum_{i=1}^t rac{\partial J^{(t)}}{\partial oldsymbol{W}_h}\Big|_{(i)} rac{\partial oldsymbol{W}_hig|_{(i)}}{\partial oldsymbol{W}_h}$$

$$=\sum_{i=1}^t rac{\partial J^{(t)}}{\partial oldsymbol{W}_h}igg|_{(i)}$$

Source:

https://www.khanacademy.org/math/multivariable-calculus/multivariable-derivatives/differentiating-vector-valued-functions/a/multivariable-chain-rule-simple-version

Backpropagation for RNNs



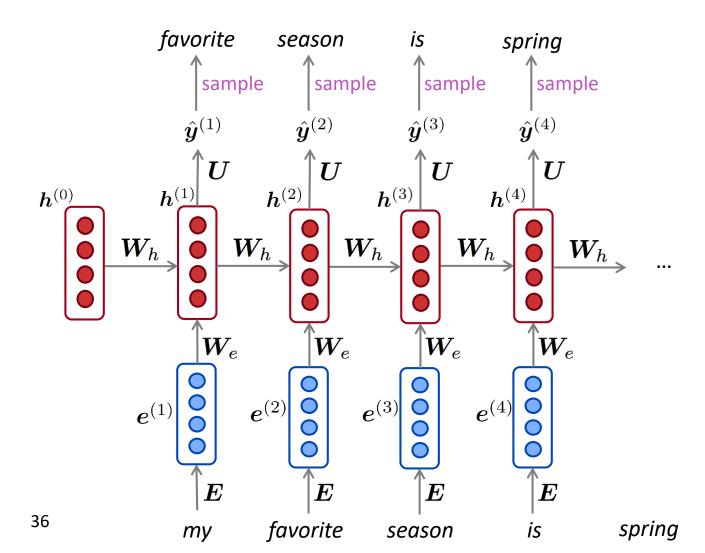
$$\frac{\partial J^{(t)}}{\partial \boldsymbol{W_h}} = \underbrace{\sum_{i=1}^t \frac{\partial J^{(t)}}{\partial \boldsymbol{W_h}}\Big|_{(i)}}_{\text{Question: How do we}}$$

calculate this?

Answer: Backpropagate over timesteps *i=t,...,*0, summing gradients as you go. This algorithm is called "backpropagation through time"

Generating text with a RNN Language Model

Just like a n-gram Language Model, you can use a RNN Language Model to generate text by repeated sampling. Sampled output is next step's input.



- Let's have some fun!
- You can train a RNN-LM on any kind of text, then generate text in that style.
- RNN-LM trained on Obama speeches:

The United States will step up to the cost of a new challenges of the American people that will share the fact that we created the problem. They were attacked and so that they have to say that all the task of the final days of war that I will not be able to get this done.

- Let's have some fun!
- You can train a RNN-LM on any kind of text, then generate text in that style.
- RNN-LM trained on Harry Potter:

"Sorry," Harry shouted, panicking—"I'll leave those brooms in London, are they?"

"No idea," said Nearly Headless Nick, casting low close by Cedric, carrying the last bit of treacle Charms, from Harry's shoulder, and to answer him the common room perched upon it, four arms held a shining knob from when the spider hadn't felt it seemed. He reached the teams too.

Let's have some fun!

You can train a RNN-LM on any kind of text, then generate text in that style.

RNN-LM trained on recipes:

Title: CHOCOLATE RANCH BARBECUE

Categories: Game, Casseroles, Cookies, Cookies

Yield: 6 Servings

2 tb Parmesan cheese -- chopped

1 c Coconut milk

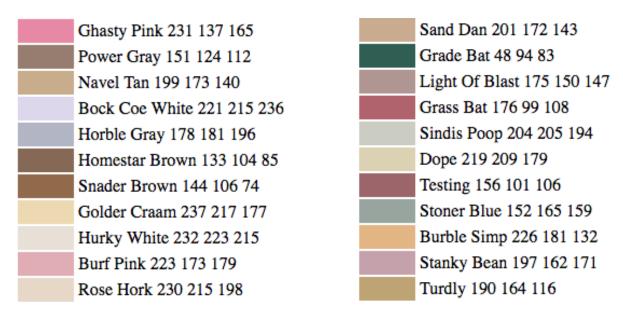
3 Eggs, beaten

Place each pasta over layers of lumps. Shape mixture into the moderate oven and simmer until firm. Serve hot in bodied fresh, mustard, orange and cheese.

Combine the cheese and salt together the dough in a large skillet; add the ingredients and stir in the chocolate and pepper.

Source: https://gist.github.com/nylki/1efbaa36635956d35bcc

- Let's have some fun!
- You can train a RNN-LM on any kind of text, then generate text in that style.
- RNN-LM trained on paint color names:



This is an example of a character-level RNN-LM (predicts what character comes next)

Evaluating Language Models

The standard evaluation metric for Language Models is perplexity.

$$\text{perplexity} = \prod_{t=1}^T \left(\frac{1}{P_{\text{LM}}(\boldsymbol{x}^{(t+1)}|\ \boldsymbol{x}^{(t)},\dots,\boldsymbol{x}^{(1)})} \right)^{1/T}$$
 Normalized by number of words

Inverse probability of corpus, according to Language Model

• This is equal to the exponential of the cross-entropy loss J(heta) :

$$= \prod_{t=1}^{T} \left(\frac{1}{\hat{\boldsymbol{y}}_{\boldsymbol{x}_{t+1}}^{(t)}} \right)^{1/T} = \exp \left(\frac{1}{T} \sum_{t=1}^{T} -\log \hat{\boldsymbol{y}}_{\boldsymbol{x}_{t+1}}^{(t)} \right) = \exp(J(\theta))$$

Lower perplexity is better!

RNNs have greatly improved perplexity

	Model	Perplexity
-gram model ——	→ Interpolated Kneser-Ney 5-gram (Chelba et al., 2013)	67.6
Increasingly complex RNNs	RNN-1024 + MaxEnt 9-gram (Chelba et al., 2013)	51.3
	RNN-2048 + BlackOut sampling (Ji et al., 2015)	68.3
	Sparse Non-negative Matrix factorization (Shazeer et al., 2015)	52.9
	LSTM-2048 (Jozefowicz et al., 2016)	43.7
	2-layer LSTM-8192 (Jozefowicz et al., 2016)	30
	Ours small (LSTM-2048)	43.9
	Ours large (2-layer LSTM-2048)	39.8

Perplexity improves (lower is better)

Source: https://research.fb.com/building-an-efficient-neural-language-model-over-a-billion-words/

Why should we care about Language Modeling?

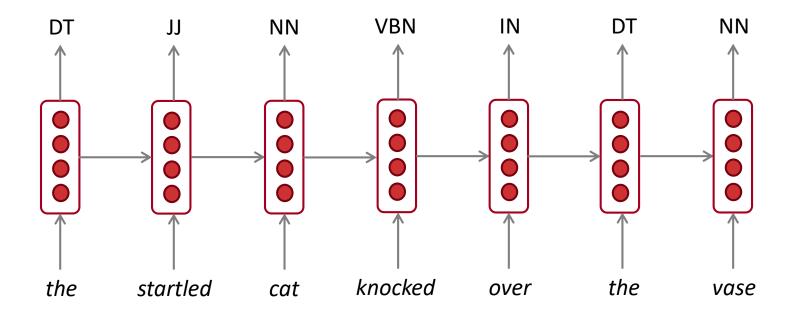
- Language Modeling is a benchmark task that helps us measure our progress on understanding language
- Language Modeling is a subcomponent of many NLP tasks, especially those involving generating text or estimating the probability of text:
 - Predictive typing
 - Speech recognition
 - Handwriting recognition
 - Spelling/grammar correction
 - Authorship identification
 - Machine translation
 - Summarization
 - Dialogue
 - etc.

Recap

- Language Model: A system that predicts the next word
- <u>Recurrent Neural Network</u>: A family of neural networks that:
 - Take sequential input of any length
 - Apply the same weights on each step
 - Can optionally produce output on each step
- Recurrent Neural Network ≠ Language Model
- We've shown that RNNs are a great way to build a LM.
- But RNNs are useful for much more!

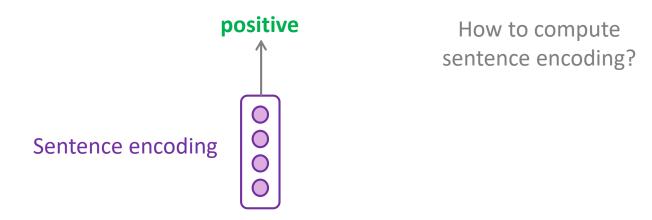
RNNs can be used for tagging

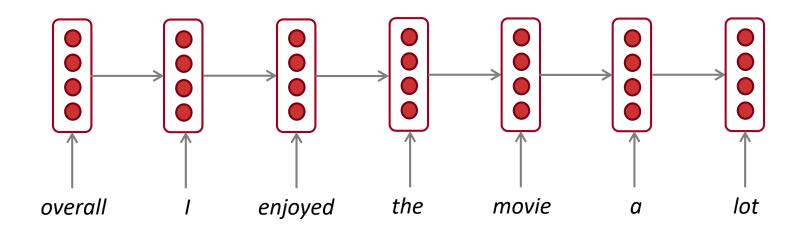
e.g. part-of-speech tagging, named entity recognition



RNNs can be used for sentence classification

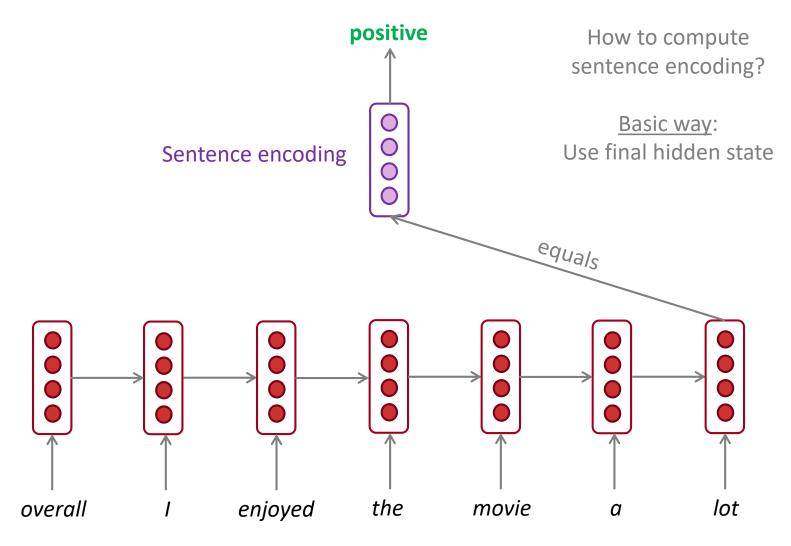
e.g. sentiment classification





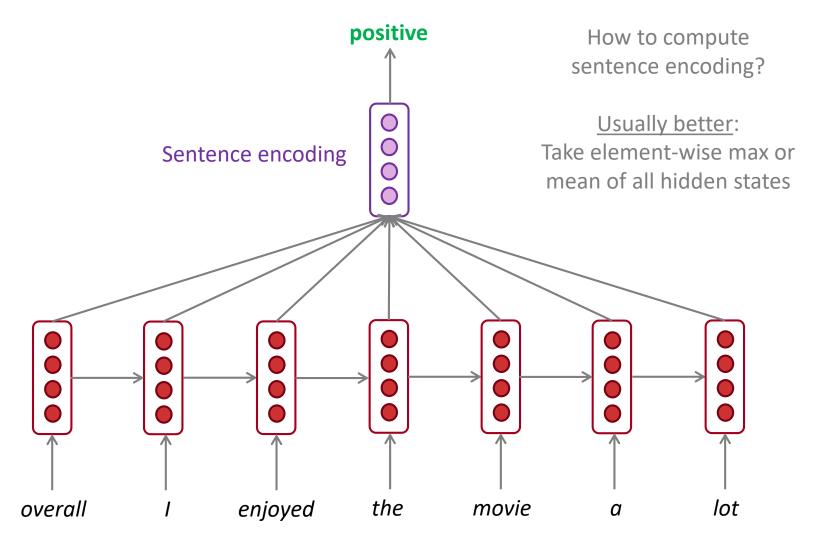
RNNs can be used for sentence classification

e.g. sentiment classification



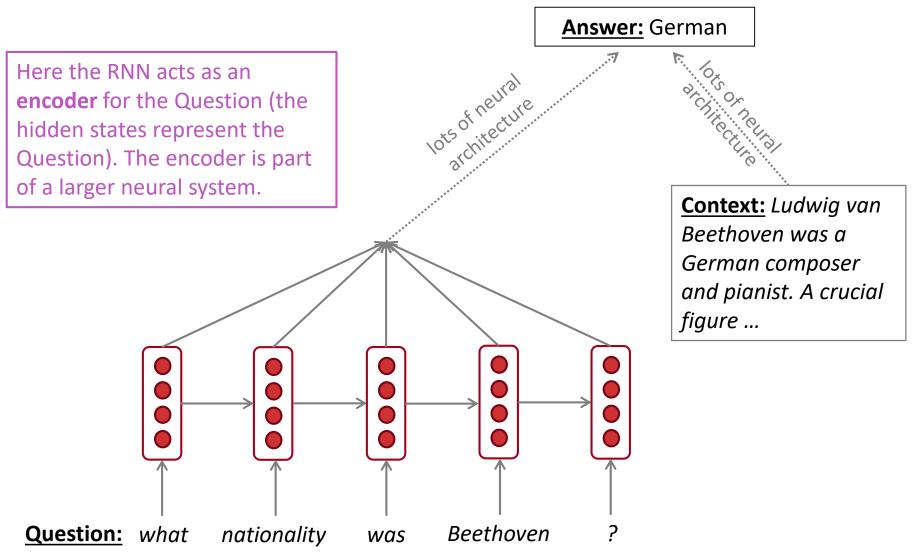
RNNs can be used for sentence classification

e.g. sentiment classification



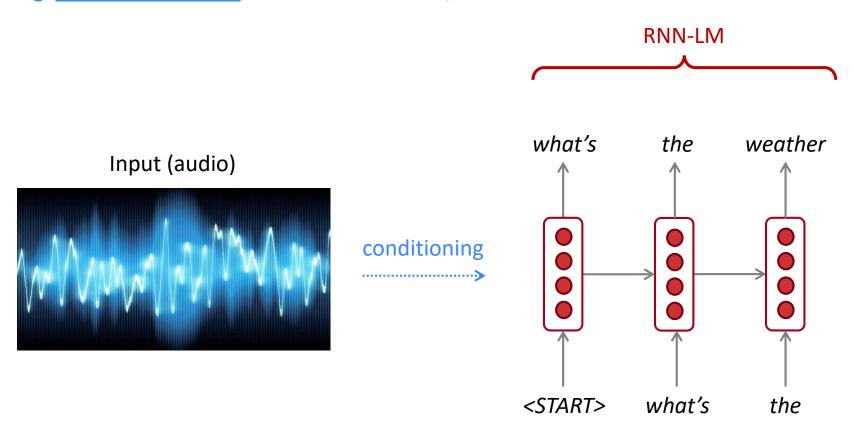
RNNs can be used as an encoder module

e.g. question answering, machine translation, many other tasks!



RNN-LMs can be used to generate text

e.g. speech recognition, machine translation, summarization



This is an example of a *conditional language model*. We'll see Machine Translation in much more detail later.

A note on terminology

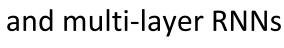
RNN described in this lecture = "vanilla RNN"



Next lecture: You will learn about other RNN flavors









By the end of the course: You will understand phrases like "stacked bidirectional LSTM with residual connections and self-attention"



Next time

- Problems with RNNs!
 - Vanishing gradients

motivates

- Fancy RNN variants!
 - LSTM
 - GRU
 - multi-layer
 - bidirectional