Parallel Computing

环境

• **OS**: Ubuntu 18.04.2 LTS (GNU/Linux 4.18.0-21-generic x86_64)

• physical processer: 2

cores / processer: 14

processes: 56

• 库: OpenMp, MPI, Eigen

1. 稀疏矩阵求解

实现一个"大规模稀疏矩阵的Conjugate Gradient(共轭梯度)求解器",即,求解Ax=b中的x,其中A为一个大型、稀疏矩阵。

1.1 代码设计及优化

使用高性能矩阵运算库Eigen实现对矩阵的运算加速。对A, x, b的定义如下:

```
VectorXd x = VectorXd::Ones(MSIZE);
VectorXd b = VectorXd::Ones(MSIZE);
SpMat A = generateSparseMat(MSIZE);
```

实现并行计算代码如下:

```
ConjugateGradient<SpMat, Lower|Upper> cg;
// total iterarions
cg.setMaxIterations(MSIZE*10);
// tolerance
cq.setTolerance(1e-3);
void ParallelProcess(SpMat A, VectorXd x, VectorXd b, int core num) {
    initParallel();
    // core numbers
    setNbThreads(core num);
    cout<<"Parallel processing with "<<nbThreads()<<" cores...\n";</pre>
    auto start = chrono::steady clock::now();
    // solve
    cg.compute(A);
    x = cg.solve(b);
    auto end = chrono::steady clock::now();
    cout<<"Total iteration: "<<cg.iterations()<<endl;</pre>
    cout<<"Estimated error: "<<cg.error()<<endl;</pre>
    cout<<"Time elapsed: "</pre>
        << chrono::duration cast<chrono::milliseconds>(end-start).count()
        <<" ms"<<endl<<endl;
```

1.2 运行结果

运行: 在终端该文件夹运行 make 。

• 1000维稀疏矩阵运行结果:

```
Matrix size: 1000
Generating sparse matrix...
Parallel processing with 28 cores...
Total iteration: 2262
Estimated error: 0.000696779
Time elapsed: 1294 ms
Sequential processing with 1 core..
Total iteration: 2262
Estimated error: 0.000696779
Time elapsed: 11533 ms
Parallel processing with 2 cores...
Total iteration: 2262
Estimated error: 0.000696779
Time elapsed: 6080 ms
Parallel processing with 4 cores...
Total iteration: 2262
Estimated error: 0.000696779
Time elapsed: 3344 ms
Parallel processing with 8 cores...
Total iteration: 2262
Estimated error: 0.000696779
Time elapsed: 2009 ms
```

• 10000维稀疏矩阵运行结果:

```
(base) sjy1203@dell-Precision-7920-Towe
Matrix size: 10000
Generating sparse matrix...
Parallel processing with 28 cores...
Total iteration: 15769
Estimated error: 0.000994606
Time elapsed: 507962 ms

}
Parallel processing with 8 cores...
Total iteration: 15769
Estimated error: 0.000994606
Time elapsed: 1099224 ms
```

1.3 分析

并行计算下多核的计算能力远远超过了串行计算的效率,28核计算1000维稀疏矩阵需要1秒而串行则需要12秒。当然计算耗时和核数并不是成线性的,这与核数增加之后进程通信开销增加等都有关系,结果符合预期。

2. Mandelbrot并行化

将分形算法用OpenMP并行化。

2.1 代码设计及优化

OpenMP实现并行化与算法的分离使得使用特别简易,可读性也很好。如下例子:

```
/* Define pseudocolor maps, ramps for red and blue,
  random for green */
    #pragma omp parallel for num_threads(num_trds)
    for(i=0;i<256;i++)
    {
        redmap[i]=i/255.;
        greenmap[i]=drand48();
        bluemap[i]=1.0-i/255.;
}</pre>
```

2.2 运行结果

运行: 在终端该文件夹运行 make 。

• 运行时间对比:

Core numbers: 1 Elapsed time: 2104.88 ms

Core numbers: 2

Elapsed time: 2043.84 ms

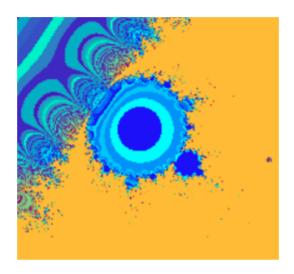
Core numbers: 4

Elapsed time: 1864.31 ms

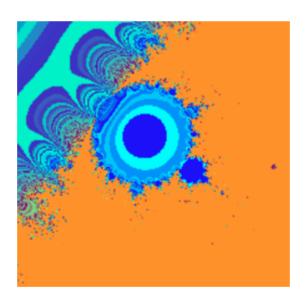
Core numbers: 8

Elapsed time: 1674.32 ms

• 4核加速:



• 8核加速:



2.3 分析

可见在不同核加速状态下展示的图片颜色有所不同,这是因为图片的色谱与迭代次数相关,在不同核数的加速下迭代次数不同,所以不难理解颜色的变化。

3. Random Reduction

- 读懂并将串行算法Reduction.cpp改成mpi并行。
- 用Random_matrix.py生成随机矩阵。
- 用Validationg_mpi.cpp验证结果。

3.1 代码设计及优化

```
/* Reductions with MPI */
    double values[3]; // for storing matrices mul temp results
    for (int i = 0; i < M; i++) {
        for (int j = 0; j < M; j++) {
            alpha = 0.0;
            beta = 0.0;
            gamma = 0.0;
            for (int k = 0; k < N; k++) {
                values[0] = U t[i][k] * U t[i][k];
                values[1] = U t[j][k] * U t[j][k];
                values[2] = U_t[i][k] * U_t[j][k];
                if (id != 0) {
                    MPI Send(values, 3, MPI DOUBLE, 0, 1, MPI COMM WORLD);
                } else {
                     for (int id = 1; id < nproc; id++) {</pre>
                        MPI Recv(values, 3, MPI DOUBLE, id, 1,
MPI COMM WORLD, &status);
                        alpha += values[0];
                        beta += values[1];
                        gamma += values[2];
                }
            // Global variables
            Alphas[i][j] = alpha;
            Betas[i][j] = beta;
            Gammas[i][j] = gamma;
        }
    }
```

3.2 运行结果

运行: 在终端该文件夹运行 make 。

• 对200 * 200的矩阵进行 Random Reduction:

```
[*] Constructing symmetric matrix with size 200 * 200...
python Random_matrix.py 200 200
[*] Performing orignal reduction...
g++ Reduction.cpp -o Reduction && ./Reduction 200 200 -t -d
Time: 58.525 ms.

[*] Random reduction with MPI...
mpic++ randomRedMPI.cpp -o randomRedMPI && mpirun -np 2 ./randomRedMPI 200 200 -t -d
Time elapesd: 4019.89 ms

[*] Validating...
g++ Validation_mpi.cpp -o Validation_mpi && ./Validation_mpi -p
VALID!

difference in Alphas: 0
difference in Betas: 0
difference in Gammas: 0
```

3.3 分析

通过使用MPI库,通过并行计算加速,同时保证的三个目标矩阵的 difference 都为0,充分说明了并行计算的可靠性。

4. MPI 10

用MPI编写一个并行I/O的例子。

4.1 代码设计及优化

• 创建一维数组并在n个进程均匀分布(无法整除部分分配给编号末尾的进程),数组内容初始化 为随机整数

```
/* Allocate buffer to processes */
if (id != nproc-1)
    blocksize = bufsize/nproc;
else
    blocksize = bufsize-(nproc-1)*(bufsize/nproc);
block = (char*)malloc((blocksize+1)*sizeof(char));

/* Fill blocks with random integers */
srand(time(NULL));
for (int i = 0; i < blocksize; i++) {
    block[i] = (rand() % 10) + 1;
}
block[blocksize] = '\0';</pre>
```

• 利用并行I/O接口把数据写入文件中,输出每个进程写入的 offset

• 执行一个集合操作,把所有进程的分块数据发送给0号进程,0号进程另外开一个1维数组空间a 用户保存这些收取的数据

```
/* 0 process store data sent from slave processes in array A */
   MPI Barrier (comm);
    if (id == 0) {
        A = (char*) malloc((bufsize+1)*sizeof(char));
        B = (char*)malloc((bufsize+1)*sizeof(char));
        /* copy 0's data to A */
        memcpy(A, block, blocksize);
        /* Recieve data from slaves' process and store in A */
        for (int i = 1; i < nproc; i++)</pre>
            if (i != nproc-1) {
                // must specify offset in A to store different processes'
data
                MPI Recv(&A[i*(bufsize/nproc)], bufsize/nproc,
                         MPI CHAR, i, 0, comm, &status);
                cout<<"Process "<<id<<" is recieving data from "<<i<"..."
<<endl;
            } else {
                MPI Recv(&A[(nproc-1)*(bufsize/nproc)], bufsize-
(bufsize/nproc) * (nproc-1),
                         MPI CHAR, i, 0, comm, &status);
                cout<<"Process "<<id<<" is recieving data from "<<i<<"..."</pre>
<<endl;
        cout<<"Process "<<id<<" revieced Done!"<<endl;</pre>
        free (block);
    } else {
        cout<<"Process "<<id<<" sending..."<<endl;</pre>
        MPI Send(block, blocksize, MPI CHAR, 0, 0, comm);
        free (block);
    }
```

• 0号进程另起一个串行I/O读入并行I/O操作写入文件的数据, 0号进程串行读入的输入放在1维数组空间b中, 1.1.9. 对比a和b验证I/O和通信是否正确

```
if (id == 0) {
       /* 0 process sequential read slave processes' I/O data into array B
*/
        B = fileWrite("mpiio.dat", B, bufsize);
       if (P == "-p") {
           cout<<"A: "<<endl;</pre>
            for (int i = 0; i < bufsize; i++)
               cout<<int(A[i])<<' ';
           cout<<'\n';
           cout<<"B: "<<endl;</pre>
           for (int i = 0; i < bufsize; i++)
               cout<<int(B[i])<<' ';
           cout<<'\n';
        }
       /* Validation */
        if (resultValidate(A, B, bufsize))
           cout<<"PASS"<<endl;
        else cout<<"FAIL"<<endl;</pre>
       free(A);
       free(B);
    }
```

4.2 运行结果

运行: 在终端该文件夹运行 make。

• 5核40个数据并行IO:

```
parallel > parallelIO > mpirun --oversubscribe -np 5 MPIIO 40 -p
Process 0: 2 6 6 8 7 3 6 4
Process 2: 2 6 6 8 7 3 6 4
Process 3: 2 6 6 8 7 3 6 4
Process 4: 2 6 6 8 7 3 6 4
Process 1: 2 6 6 8 7 3 6 4
Offset of process 2: 16
Offset of process 4: 32
Offset of process 0:0
Offset of process 1:8
Offset of process 3: 24
Process 1 sending...
Process 2 sending...
Process 3 sending...
Process 4 sending...
Process 0 is recieving data from 1...
Process 0 is recieving data from 2...
Process 0 is recieving data from 3...
Process 0 is recieving data from 4...
Process 0 revieced Done!
Writing files...
A:
2 6 6 8 7 3 6 4 2 6 6 8 7 3 6 4 2 6 6 8 7 3 6 4 2 6 6 8 7 3 6 4 2 6 6 8 7 3 6 4 2 6 6 8 7 3 6 4
B:
2 6 6 8 7 3 6 4 2 6 6 8 7 3 6 4 2 6 6 8 7 3 6 4 2 6 6 8 7 3 6 4 2 6 6 8 7 3 6 4
Validating results...
PASS
```

• 8核1000个数据并行IO:

```
Performing MPI IO using 8 cores...
mpic++ MPIIO.cpp -o MPIIO
mpirun -- oversubscribe -np 8 MPIIO 1000
Offset of process 4:500
Offset of process 6: 750
Offset of process 1: 125
Offset of process 2: 250
Offset of process 3: 375
Offset of process 5: 625
Offset of process 7: 875
Offset of process 0:0
Process 5 sending...
Process 1 sending...
Process 2 sending...
Process 4 sending...
Process 6 sending...
Process 3 sending...
Process 7 sending...
Process 0 is recieving data from 1...
Process 0 is recieving data from 2...
Process 0 is recieving data from 3...
Process 0 is recieving data from 4...
Process 0 is recieving data from 5...
Process 0 is recieving data from 6...
Process 0 is recieving data from 7...
Process 0 revieced Done!
Writing files...
Validating results...
PASS
```

通过对A和B的对比可以知道I/O没有出错,可以使用 "-p" 来输出进程通讯的信息来debug,从两个例子中可以看出通讯过程没有出现错误,结果符合预期。

总结

通过这学期对并行计算课程的学习,我受益匪浅,收获颇丰。深度理解了并行计算的基本原理,并且通过去无锡的参观,了解到并行计算技术在工业界的应用进展。此次的四个任务也让我充分地了解了并行计算编程的细节,学习并使用了并行计算库MPI和OpenMP解决和优化算法。

在后深度学习时代,并行计算无疑是充分利用好计算力的一把利剑,在今后的学习和实践中,我也应 当将并行计算的优势发挥到其中。

References

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