

Ex. 1.

Does the function

$$\langle \underline{x}, \underline{y} \rangle = 3x_1y_1 - 2x_1y_2 - 2x_2y_1 + x_2y_2$$

satisfy the conditions imposed for a scalar product for vectors $\underline{x} = [x_1, x_2]$ and $\underline{y} = [y_1, y_2]$?

Ex. 2.

Use the Gram-Schmidt procedure to orthogonalize the system $[0, 1, 1, 0]$, $[-2, 0, 2, 0]$, $[3, 1, 1, 1]$ in E^4 .

Ex. 3.

Let $\underline{u} = [1, 3, -2]$, $\underline{v} = [-1, 1, 1]$, $\underline{w} = [5, 1, 4]$.

- Check if the system of vectors $\{\underline{u}, \underline{v}, \underline{w}\}$ is an orthogonal or orthonormal basis of E^3 .
- Find the coordinates of the vector $[1, 0, 1]$ in this basis.

Ex. 4.

Find the projection of vector $[1, -1, 2, 0]$ onto the space spanned by vectors $[2, 0, 1, -1]$, $[1, 1, -2, 0]$ and $[1, 1, 1, 3]$.