

Homework Assignment #2 - Theory Problems

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We know that each pixel corresponds to $0.01mm$. This implies that the sphere has a projected radius of $20pixels = 20 * 0.01 = 0.2mm$.

Therefore $0.2mm * Z = 10mm * 1m \Rightarrow Z = 50$ meters

Problem 2 a)

$$O_{cor}[0,0] = 0 * (1) + 1 * (1) + 2 * (-1) = -1$$

$$O_{cor}[0,1] = 1 * (1) + 2 * (1) + 3 * (-1) = 0$$

$$O_{cor}[0,2] = 2 * (1) + 3 * (1) + 0 * (-1) = 5$$

$$O_{cor}[1,0] = 0 * (1) + 4 * (1) + 0 * (-1) = 4$$

$$O_{cor}[1,1] = 4 * (1) + 0 * (1) + 5 * (-1) = -1$$

$$O_{cor}[1,2] = 0 * (1) + 5 * (1) + 0 * (-1) = 5$$

$$O_{cor}[2,0] = 0 * (1) + 0 * (1) + 0 * (-1) = 0$$

$$O_{cor}[2,1] = 0 * (1) + 0 * (1) + 1 * (-1) = -1$$

$$O_{cor}[2,2] = 0 * (1) + 1 * (1) + 0 * (-1) = 1$$

$$O_{cor} = \begin{bmatrix} -1 & 0 & 5 \\ 4 & -1 & 5 \\ 0 & -1 & 1 \end{bmatrix}$$

Problem 2 b)

$$O_{cov}[0,0] = 0 * (-1) + 1 * (1) + 2 * (1) = 3$$

$$O_{cov}[0,1] = 1 * (-1) + 2 * (1) + 3 * (1) = 4$$

$$O_{cov}[0,2] = 2 * (-1) + 3 * (1) + 0 * (1) = 1$$

$$O_{cov}[1,0] = 0 * (-1) + 4 * (1) + 0 * (1) = 4$$

$$O_{cov}[1,1] = 4 * (-1) + 0 * (1) + 5 * (1) = 1$$

$$O_{cov}[1,2] = 0 * (-1) + 5 * (1) + 0 * (1) = 5$$

$$O_{cov}[2,0] = 0 * (-1) + 0 * (1) + 0 * (1) = 0$$

$$O_{cov}[2,1] = 0 * (-1) + 0 * (1) + 1 * (1) = 1$$

$$O_{cov}[2,2] = 0 * (-1) + 1 * (1) + 0 * (1) = 1$$

$$O_{cov} = \begin{bmatrix} 3 & 4 & 1 \\ 4 & 1 & 5 \\ 0 & 1 & 1 \end{bmatrix}$$

Problem 3 a)

$$h = \begin{bmatrix} 1 & 3 & 1 \\ 0 & 0 & 0 \\ -1 & -3 & -1 \end{bmatrix}$$

Problem 3 b)

Yes, h is separable

$$h_1 = \begin{bmatrix} 1 & 0 & -1 \end{bmatrix}$$

$$h_2 = \begin{bmatrix} 1 \\ 3 \\ 1 \end{bmatrix}$$