Advanced Programming - Appunti

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Introduction

1.1 19 - Settembre

1.1.1 Info and Contact

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1.1.2 Framwork

A software **framework** is a collection of common code providing generic functionality that can selectively overryidden or specialized by user code prvoiding specific functionality.

When using *framworks* htere is an **inversion of control**. Differently from what happens when using libraries, the program-flow is dictated by the framework, not the caller.

1.1.3 Design Patterns

A design pattern is a general reusable solution to a commonly occurring problem within a given context in software design. A design pattern is characterized by:

- ♦ Name
- ⋄ Problem Addressed
- ♦ Context Used to determine applicability
- ♦ Forces Constraints or issues that the solution must address
- ♦ Solution It must resolve all forces

1.2 20 - Settembre

Useful tool, to see preprocessor output, compiling, ecc.

1.2.1 Programming Languages

A PL is defined via syntax, semantics and pragmatics¹.

Syntax

Used by the compiler for *scanning* and *parsing*. The *lexical* grammar defines the syntax of token (e.g. "for" blocks, constants)

Semantics

Semantics might be described using natural language, which even if precise, allows amibguousity. Formal approches to semantics definition are:

- 1. Denotational Mapping every syntactic entity with a mathematical entity
- 2. Operational Defining a computation relation in a form $e \Rightarrow v$, where e is a program
- 3. Axiomatic Based on Hoare-triples $Precondition \land Program \Rightarrow Postcondition$

However, they rarely scale to fully-fledged programming languages.

¹the way in which the PL is intended to be used in practice

Pragmatics

Pragmatics include coding conventions, guidelines for elegant code, etc.

1.2.2 Programming Paradigms

Paradigms belong to languages pragmatics, not to the way the language is defined, i.e. not syntax nor semantics.

- 1. Imperative
- 2. Object-oriented
- 3. Concurrent Processes, communication, ...
- 4. Functional
- 5. Logic Assertions, relations, strange sorceries...

Modern PLs, provide constructs and solutions to program in all these paradigms

1.2.3 Implementing PLs

- ♦ Programs written in **L** must be *executable*
- \diamond Every language **L** implicitly defines and Abstract Machine M_L having **L** as a Machine Language
- \diamond Implementing M_L on an existing host machine M_O via compilation or interpretation (or both) makes programs written in **L** executables

An **Abstract Machine** M_L for L is a collection of data structures and algorithms which can perform the storage and execution of programs written in L.

Viceversa, M defines a language L_M including all programs which can be executed by the interpreter M.

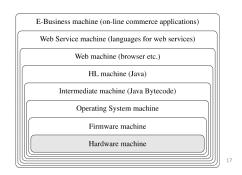
There is a bidirectional correspondance between machines and languages components.



In computer science one of the main focuses is abstraction, as can be seen in this hierarchical scheme.

Hierarchies of Abstract Machines

- Implementation of an AM with another can be iterated, leading to a hierarchy (onion skin model)
- Example:



A software component is a unit of composition with contractually specified interfaces and explicit context dependencies only. A software component can be deployed independently and is subject to composition by third parties.

Implementing PLs - Wrap Up

- $\diamond~L$ High-level programming language
- $\diamond M_L$ Abstract machine for L
- \diamond M_O host machine

Pure Interpretation

...PIC HERE

 M_L is interpreted over M_O . It isn't very efficient, mainly because of fetch-decode phases

Pure Compilation

...PIC HERE

L programs are translated into L_O , the machine laguange of M_O , hence, M_L is not realized at all and the programs are directly executed on M_O .

Compilation is more efficient than Interpretation, but produced code is larger

Both

...PIC HERE

All real languages use both interpretation and compilation,

Some languages, e.g. Java, use an intermediate Abstract Machine, called a *Virtual Machine*, which increases *Portability* and *Interoperability*.

JVM

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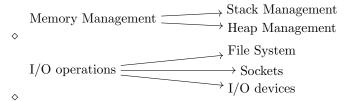
2.1 Runtime System

Every language defines and **execution model**, which is (partially) implemented by a **runtime system**, providing runtime **support** needed by both *compiled* and *interpreted* programs.

A Runtime system includes (eventually):

- ♦ Code:
 - in the executing program generated by the compiler
 - running in other threads/processes]
- ♦ Language libraries
- Operating system functionalities
- ♦ The interpreter/virtual machine itself

Runtime support can be needed for various reasons:



- ♦ Intercation with runtime environment
- ♦ Parallel execution (threads/processes)
- ♦ Dynamic binding type checking
- Dynamic loading and linking of modules
- Debugging
- ♦ ¿Code Generation?
- ♦ ¿Verification and Monitoring?

2.1.1 JRE

The Java Runtime Environment includes JVM and JCL (Java Class Library).

2.2 JVM

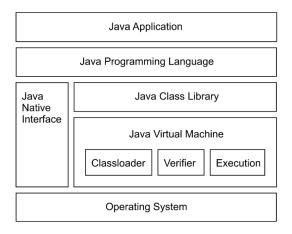
JVM is an abstract machine, defined by the documentation, which omits details on stuff like memory layout of runtime data area, garbage-collection, internal optimization, and even the representation of the null constant. The JVM specification, instead, defines precisely a machine indipendent "class file format" that all JVM implementations must support; it also imposes strong synctatic and structural constraints on the code in a class file.

The \mathbf{JVM} is not register-based, instead it is a multi-threaded \mathbf{stack}^1 based machine. Id est the \mathbf{JVM} pops intructions

¹Not to be confused with the stack of activation records!

from the top of **operand stack** of the current frame, and pushes their result on the top of the **operand stack**. The **operand stack** is used to:

- Pass arguments to functions
- ♦ Return results from a function
- ♦ Store intermediate values while evaluating expressions
- ♦ Store local variables



2.2.1 Data types

.class file are platform independent external representations, which are represented internally by the JVM using simpler data types, which are implementation dependent.

⋄ Primitive types

- Numerica integral
- Numeric floating point
- boolean (support only for arrays)
- internal (for exception handling)

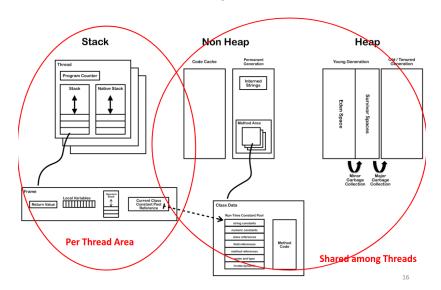
⋄ Reference types

- Class types
- Array types
- Interface types

No type information on local variables at runtime, there are only operand types specified by opcodes e.g. iadd, fadd, ...

2.2.2 Threads

There are some runtime areas of the JVM related to a single thread, while others are shared among threads



All Java Programs are multithreaded, since there is at least a main thread running the user's program, and many

daemons:

- ♦ Garbage collector
- ♦ Signal Dispatching
- ♦ Compilation
- ♦ ¿ ... ?

JVM doesn't poses strong implementation constraints, by defining a precise abstract consistency model, including volatiles, allowing non-atomic longs and doubles, distinguishing working-memory and general store.

2.2.3 per-thread Data Areas

- ⋄ pc pointer to next instruction in method area undefined if current method is native
- ♦ **Java stack**: stack of *frames* (or *activation records*)
- ♦ Native stack: used for invocation of natve functions through the Java Native Interface (JNI)

Considering the **structure** of **frames**, each one is composed by:

- ♦ Local Variable Array (32 bits) containing:
 - 1. Reference to this
 - 2. Method parameters
 - 3. Local variables
- ♦ Operand stack
- ♦ Reference to Constant Pool of current class

Differently from C/C++, where the **linking** phase is done before running an executable, java computes linking **dynamically** at **runtime**; this is achieved using **symbolic** references, which can be resolved using *static* (eager) or *late* (lazy) resolution.

Since the execution of a Java program must **not** depend on the JVM implementation, the JVM always behaves as if the implementation implies *lazy* resolution, even if the actual implementation provides static resolution instead.

2.2.4 shared data areas

Heap

- ♦ Memory for objects and arrays
- ♦ No explicit deallocation, it is demanded to the garbage collection.

Non-Heap

Memory for objects never deallocated

- ♦ Method area
- ♦ Interned strings
- ♦ Code cache for JIT

Just In Time (JIT) compilation refers to profiling as "hot" code areas of bytecode which may be executed many times, and storing the compiled native code in a cache in the Non-heap memory.

Method-area

Here class files are loaded. For each class a classloader reference and the following info from the class file are stored:

- ♦ Runtime Constant Pool
- ♦ Field data
- ♦ Method data
- ♦ Method code

Method area is shared among threads! Access to it must be thread safe.

This should a **permanent** area of the memory, but it may be **edited** when a new class is loaded or when a symbolic link is resolved by dynamic linking.

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Constant Pool

Contains constants and symbolic references for dynamic binding. It is possible to see the constant pool of a compiled .class file using the command:

```
| javap -v name.class
```

Displaying something resembling to:

```
#1 = Methodref
                          #6.#14
                                          // java/lang/Object."<init>":() V
#2 = Fieldref
                          #15.#16
                                          // java/lang/System.out:Ljava/io/PrintStream;
#3 = String
                          #17
                                          // Hello World
                                          // java/io/PrintStream.println:(Ljava/lang/
#4 = Methodref
                          #18.#19
    String;) V
#5 = Class
                          #20
                                          // com/baeldung/jvm/ConstantPool
#6 = Class
                          #21
                                          // java/lang/Object
#7 = Utf8
                          <init>
#8 = Utf8
                          () V
#9 = Utf8
                          Code
#10 = Utf8
                          LineNumberTable
#11 = Utf8
                          sayHello
#12 = Utf8
                          SourceFile
```

2.2.5 Loading

Loading is finding the binary representation of a class or interface type with a given name and creating a class or interface from it.

Class (or Interface) C creation is triggered by other classes **referencing** C or by methods (e.g. reflection). If not previously loaded, loader.loadClass is invoked.

There are 4 Classloaders:

- 1. Bootstrap CL: loads basic Java APIs
- 2. Extension CL: loads classes from standard Java extension APIs
- 3. System CL: loads application classes from *classpath* (default application CL)
- 4. User Defined CLs: can be used for:
 - ⋄ runtime classes reloading
 - ♦ loading network, encrypted files or on-the-fly generated classes
 - supporting separation between different groups of loaded classes as required by web servers

Runtime Constant Pool

2.2.6 Linking

Linking includes verification, preparation, resolution.

- 1. **Verification** multiple checks at runtime, e.g. operand stack under/overflows, validity of variable uses and stores, validity arguments type. Details later on
- 2. **Preparation** Allocation of storage
- 3. Resolution² resolve symbol references by loading referred classes/interfaces

Verification is a relevant part of JVM Specification, it is described in 170pp over a total of 600pp. When a class file is loaded there is a *first* verification pass to check formatting, there is a *second* one when a class file is linked regarding only not instruction-dependant checks. During the linking phase there is a data-flow analysis on each method (*third check*), and lastly (*fourth check*) when a method is invoked for the first time.

2.2.7 Initialization

<clinit> initialization method is invoked on classes and interfaces to initialize class variables; it also executes static
initializers. <init> initialization method instead is used for instances.

 $^{^2}$ Optional, it may be postponed till first use by an instruction

JVM Instr Set & JIT

3.1 Instruction Set

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Let's consider the instructions **format**. Each instr may have different "forms" supporting different kinds of operands. For example there are different forms of iload (i.e. push).

Runtime memory contains - Local variable array (frame) - Operand stack (frame) - Object fields (heap) - Static fields (method area)

Note that Java instructions are explicitly typed through opCodes, e.g. dload,iload,fload.

opCodes are bytes, allowing only for 256 distinct ones; hence it is impossible to have for each instruction on opCode per type. The JVM specification indicates a selection of which types to support for each op instruction, and not supported types have to be converted; resulting in the Instruction Set Architecture to present non-orthogonality. Types like byte, char and short are usually converted to int when performing computations.

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3.1.1 Invoking methods

invokevirtual causes the allocation of a new frame, pops the arguments from the stack into the local variables of the caller (putting this in 0), and passes the control to it by changing the pc.

- ♦ A resolution of the symbolic link is performed
- ireturn pushes the top of the current stack to the stack of the caller, and passes the control to it. Similarly for dreturn, freturn ...
- ⋄ return just passes the control to the caller

There are 4 others kinds of method invocation:

- ♦ invokestatic: call methods with static modifier; this is not passed
- ♦ invokespecial: call constructors, private methods or *superclass* methods; *this* is always passed
- invokeinterface: identical to invokevirtual, but used when the method is declared in an interface, thus a
 different lookup is required
- ♦ invokedynamic: introduced in Java 7 to support dynamic typing¹

 (\ldots)

3.2 JIT

AOT Ahead of Time Compilation leads to better performance in general, exploiting hardware features and variables allocation without runtime lookup; While Interpretation facilitates interactive debugging and testing: it allows

¹lambda functions related?

command-line invocation.

JIT aims to get the advantages of both.

JIT differs from AOT since it runs in the same process of the application and competes with the app for resources, thus compilation time for JIT is more relevant than for an AOT Compiler. Besides, a JIT compiler doesn't verify classes at compile time, it is a task performed by the JVM at load time. JIT can exploit new optimization possibilities, e.g. deoptimization and speculation. A JIT takes bytecode as input and outputs machine code that the CPU executes directly.

Wrapping up:

- ♦ Code starts executing interpreted with no delay
- ♦ Methods that are found commonly executed (hot) are JIT compiled
- ♦ Once compiled code is available, the execution switches to it.

To identify hot methods, there is a **threshold** on two per-method counters:

- 1. Times the method is invoked
- 2. Times a brach back to the start of a loop is taken in the method

A tradeoff between "fast-to-start-but-slow-to-execute" interpreter vs "slow-to- start-but-fast-to-execute" compiled code is managed by a multi tier system.

(...)

3.2.1 Deoptimization and Speculation

Usually method executions pass in three phases:

Interpreter \longrightarrow Low tier compiler \longleftrightarrow Optimizing compiter

But sometimes deoptimization can happen, i.e.:

Interpreter \longrightarrow Low tier compiler \longrightarrow Optimizing compiter

Component-Based software

2 - Ottobre

Component software indicates **composite systems** made of **software components**. In short, component software allows reuse, improving reliability¹ and reducing costs.

Bertrand Meyer suggests some guidelines regarding Object-Oriented software construction (1997):

- 1. modular
- 2. reliable
- 3. efficient
- 4. portable
- 5. timely

4.1 Definitions

A software component is a unit of composition with contractually specified interfaces and explicit context dependencies only. A software component can be deployed independently and is subject to composition by third parties.

A contract, A specification attached to an **interface** (component specification) that mutually binds the clients and providers of the components.

Context dependencies are specification of the deployment environment and run-time environment. This goes beyond the simple interfaces required and provided which are specified in the contract. Context dependencies include required tools, platform and resources.

Deployed independently means that a component can be plugged or unplugged from an architecture, even at runtime in some cases. It is common-practice to deploy "small components" called connectors, to resolve situations where two components supposed to interact do not provide identical interfaces, creating the need for a intermediary.

composition by third party means that a component may interact with third parties components without knowing the internals of such components.

4.2 Concepts of Component Model

- ♦ Component interface describes the operations implemented and exposed by the component
- ♦ Composition mechanism How components can be composed to work together to accomplish a task
- ♦ Component platform A platfom for the development of the components

Concepts should be laguage/paradigm agnostic, laying the ground for language interoperability.

The ancestors of Components are **Modules**, whose support has been introduced in Java 9, but isn't very common. Some concepts related to modules can be found in more modern notions such as classes, components and packages. For example, objects inside a module are visible to each other, but not visible from outside unless exported. Modules

 $^{^{1}}$ Industries may even require to use certified components

worked — pretty much like classes — as abstraction mechanism \rightarrow collection of data with operations defined on them. In OOP the concept of **inheritance**, unknown in modules, is introduced.

4.3 Components and Programming Concepts

Components can be anything and can contain anything, they can be *collections of* classes, objects, functions/algorithms, data structures.

$$iNote\ that\ OOP \neq\ COP!$$

OOP isn't focused on reuse, instead its focus in onto appropriate domain and problem representation.

- ♦ **Component Specification** describes the behavior (as a set of *Interfaces*) of a set of Component Objects and defines a unit of implementation.
- \diamond Component Implementation is a realization of Component Specification which can be independently deployed².
- ♦ **Installed Component** is an installed (i.e. *deployed*) copy of a *Component Implementation*. A Component Implementation is deployed by registering it with the runtime environment
- ♦ Component Object is an instance of a Component Implementation. It is a runtime concept, an object with its own data and unique identity. Ideally, it is the "thing that performs the implemented behaviour". An Installed Component may have multiple Component Objects

Some examples of successful components are Plugin architectures, Microsoft's Visual Basic, Operating Systems, Java Beans, and others. It is clear that components can be purchased by independent providers and deployed by the clients, and that multiple components can coexist in the same installation. Besides, components exist on a level on abstraction where they directly mean something to the deploying client.

Recalling the comparison with modules, while modules are usually seen as part of a program, components are parts of a system.

 $^{^2}$ It does **not** mean that it cannot have dependencies nor that it must be a single file

Java Beans

5.1 3 - Ottobre

"A Java Bean is a reusable software component that can be manipulated visually in a builder tool."

Typically a Bean has a GUI representation but is not necessary. What is necessary instead for a class to be recognized as a bean is that it:

- has a public constructor with no arguments
- implements java.io.Serializable
- ♦ is in a jar file with a manifest file that contains: Java-Bean: True

Beans can be **assembled** to build a new bean or application, writing clue code to wire beans together. Connection-oriented programming is based on the **Observer** or (Publish-Subscribe) paradigm. Observers come into play when there is a 1:N dependency between objects and one of them changes state, creating the need for the others to be notified and updated. Beans must be able to run in a design environment allowing the user to customize aspect and behaviour. Beans provide support for some standard features:

- 1. **Properties** e.g. color. **Bounded** properties generate an *event* of type PropertyChangeEvent, while **constrained** can only change value if none of the registered *observers* "poses a veto", by raising an *exception* when they receive the PropertyChangeEvent object.
- 2. **Events**: The **Observer** pattern is based on *Events* and *Events listeners*. An *event* is an object created by an *event source* and propagated to the registered *event listeners*. Sometimes event **adaptors** can be placed between source and listener, which might implement queuing mechanism, filter events, demuxing from many sources to a single listener.
 - ⋄ Design Patterns for Events

```
public void add<EventListType>(<EventListType> a)
public void remove<EventListType>(<EventListType> a)
```

- 3. Customization
- 4. Persistence
- 5. **Introspection**: process of analyzing a bean to determine capabilities. There are implicit methods based on reflection, naming conventions and design patterns, but can be simplified by explicitly defining info for the builder tool in the <BeanName>BeanInfo class. Such class allows exposition of features, specifying customizer class, segregate feats in normal/expert mode, and some other stuff.
 - Design Patterns for Simple Methods

```
public <PropertyType> get<PropertyName>();
public void set<PropertyName>(<PropertyType> a);
```

Design Patterns for Simple Methods

```
public java.awt.Color getSpectrum (int index);
public java.awt.Color[] getSpectrum ();
public void setSpectrum (int index, java.awt.Color color);
public void setSpectrum (java.awt.Color[] colors);
```

Reflection

9 - Ottobre

6.1 Introduction and Definitions

Reflection is the ability of a program to manipulate as data something representing the state of the program during its own execution. Another dimension of reflection is if a program is allowed to **read only**, or also to **change** itself.

- ♦ **Introspection** is the ability of a program to observe and therefore reason about its own state
- ♦ **Intercession** is the ability for a program to modify its own execution state or alter its own interpretation or meaning
- Reification is the mechanism of encoding execution state into data, which is needed by both introspection and intercession

Structural reflection is concerned with the ability of the **language** to provide a complete *reification* of both the *program* executed and its *abstract data types*.

Behavioral reflection is concerned instead with the reification of its 1 semantics & implementation (processor) and the data and implementation of the run-time system.

6.2 Uses and drawbacks

6.2.1 Uses

- ♦ Class Browsers need to be able to enumerate the number of classes
- ♦ Visual Development Environments can exploit type info available in reflection to aid the developer in writing correct code
- ♦ Debuggers need to be able to examine private members on classes
- ♦ Test Tools exploit reflection to ensure a high level of code coverage in a test suite
- Extensibility Features an app may make use of external, user-defined classes by creating instances of extensibility objects.

6.2.2 Drawbacks

- ♦ Performance Overhead
- ♦ Security Restrictions
- ⋄ Exposure of internals

6.3 Reflection in Java

Java supports **introspection** and **reflexive invocation**, but not *code modification*.

¹referred to a language

6.3.1 Introspection

The JVM mantains for every type an associated object of type java.lang.Class which "reflects" the type it represents, acting as entry point for reflection, since it provides all info needed:

- ♦ Class name and modifiers
- \diamond Extended superclasses and implemented inferfaces
- ♦ Methods, fields, constructors, etc.

To retrieve such java.lang.Class object it is sufficient to do Object.getClass(). Class objects are constructed automatically by the JVM as classes are loaded.

Using java.util.reflect.* it is possible also to retrieve class **Members** i.e. *fields, constructors* and *methods*. The extensive java.util.reflect.* API provides many *methods* to achieve this which will not be reported here. There is a class for each Member

- ♦ java.util.reflect.Field: access type info and set/get values.
- ♦ java.util.reflect.Method: type info for parameters and return type; invoking method on a given object.
- java.util.reflect.Constructor: note that constructors have no return values and invocation creates a new
 instance of the given class.

6.3.2 Program Manipulation

By now we have talked only about **introspection** in java, but reflection can be used also to create objects of a type not known at compile time, or to access members (access fields or invoke methods) unknown at compile time.

Annotations

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In java, static, private,... modifiers are *meta-data* describing properties of program elements. Annotations can be understood as (user-) definable modifiers. They are composed by one or two parts:

- 1. name
- 2. finite number of attributes i.e. name=value. There may be no attributes.

The syntax is the following:

constExp are expression which can be evaluated at *compile time*. Besides, attributes have a *type*, thus the supplied values have to convertible to that type.

Annotations can be applied to almost any syntactic element, from packages to parameters and any type use.

7.1 Defining annotations

```
@interface InfoCode {
    String author ();
    String date ();
    int ver () default 1;
    int rev () default 0;
    String [] changes () default {};
}
```

This defines the custom annotation InfoCode, imposing some fields possibly with default values. It can be used as follows:

Polymorphism

Polymorphism basically means "many forms", where forms are **types**. Thus there may be polymorphic function names, or polymorphic types.

There are many "flavors" of polymorphism, many variations. Two main kinds opposed to each other are *ad hoc* and *universal* polymorphism, which however, may coexist:

- ad hoc PM indicates that a single function name denotes different algorithms, determined by the actual types.
- ♦ universal PM indicates a single algorithm (solution) applicable to objects of different types.

When PM is taken into account, it is crucial to consider when happens the **binding** between a function name and the actual code to be executed:

- ⋄ compile time; static/early binding
- linking time
- execution time; late/dynamic binding

In general the earlier the binding happens, the better (for debugging reasons). If the binding spans over more phases (e.g. overriding in Java), as a convention we consider the **binding time** the last phase.

8.1 Classification

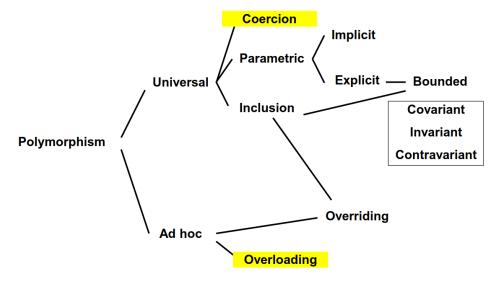


Figure 8.1: Polymorphism classification

8.1.1 Overloading

Overloading is present in every language for basic operators + - *..., and sometimes is supported for user-defined functions, and in some languages it is even allowed the overloading of primitive operator by user-defined functions.

Since this falls under the **ad hoc** polymorphism family, the code to be executed is determined by the type of the arguments; the binding can either happen at *compile* or at *runtime*, depending on the typing of the language, whether it is static or dynamic.

```
// C language doesn't allow overloading for user-defined functions
int sqrInt(int x) { return x * x; }
double sqrDouble(double x) { return x * x; }

// Overloading in Java & C++
int sqr(int x) { return x * x; }
double sqr(double x) { return x * x; }
```

Haskell introduces type classes for handling overloading in presence of type inference

8.2 Coercion

Coercion is the automatic (implicit) conversion of an object to a different type, opposed to casting which is explicit instead. Coercion allows a code snippet to be applied of arguments of different (convertible) types. Sometimes coercion is allowed only if there is no **information loss**.

```
double sqrt(double x){...}
double d = sqrt(5) // applied to int
```

8.3 Inclusion Polymorphism

Inclusion polymorphism is also known as *subtyping polymorphism* or *inheritance*. It is ensured by *Barbara Liskov*'s **substitution principle**:

A subtype object can be used in any context where a supertype object is expected

Methods and fields defined in a superclass may be invoked and accessed by subclasses if not redefined (see *Overriding*).

8.4 Overriding

In Java a method m of a class A can be redefined in a subclass B of A.

Overriding introduces ad hoc polymorphism in the universal polymorphism of inheritance. Notice that overriding requires the final binding to happen at runtime: it happens through the lookup done by invokevirtual in the JVM.

8.5 C++ v Java

```
class A {
  public:
    virtual void onFoo() {}
    virtual void onFoo(int i) {}
};
class B : public A {
  public:
    virtual void onFoo(int i) {}
};
class C : public B {};
int main() {
    C* c = new C();
    c->onFoo();
    // Compile error - doesn't exist
}
```

The equivalent code in Java compiles, because in java invokes the function onFoo() with no arguments defined in the superclass A. In C++ instead, the function onFoo(int i) defined in B is found and stops the search, but there is arguments type mismatch, thus it doesn't compile. This happens because in C++ the method lookup is based on the method name, not on its signature.

8.6 C++ Templates

They are similar to *Generics* in Java, they are used as function and class templates each concrete instantiation produces a copy of the generic code, specialized for that type: monomorphization. In java Generics, instead, **type erasure** happens at runtime, i.e. type variables T are replaced by **Object** variables.

Templates support parametric polymorphism and type parameters can also be primitive types (unlike Java generics)

```
template <class T> // or <typename T>
T sqr(T x) { return x * x; }
```

Assuming to invoke sqr(T x) on variables of different types, the compiler will generated a specific code for each type used. This works even on user-defined types; check the following code for an example:

It is important to check for type ambiguosity; in the following example, it is highlighted a case where it's not clear whether it is i to be converted to long or m to i.

8.6.1 Macros

Macros can be exploited to achieve *polymorphism* and can have the same effect of the templates, but notice that macros are executed by the preprocessor¹ and are only **textual substition**, there is no parsing, no static analysis checks or whatsoever.

```
#define sqr(x) ((x) * (x))
int a = 2;
int aa = sqr(a++); // int aa = ((a++) * (a++));
// value of aa? aa contains 6 :(
#define fact(n) (n == 0) ? 1 : fact(n-1) * n
// compilation fails because fact is not defined
```

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8.6.2 Specialization

A template can be **specialized** by defining a template with the same name but with more specific parameters (*partial specialization*) or with no parameters (*full specialization*). This is kinda similar to *Overriding*, leaving to the compiler the choice of the most appropriate template.

 $^{^{1}}$ Macro expansion can be seen using the option -E when compiling

Templates can be used by a compiler to generate temporary source code, which is merged by the compiler with the rest of the source code and then compiled.

Template compilation happens on demand: the code of a template is not compiled until an instantiation is required, however in case of fully-specialized template, the compiler treats the template as a function, thus it generates its code **regardless** whether it is ever used or not.

Note that in C/C++ while method *prototypes* usually are in a separate .h file, the compiler needs the template declaration and definition in the same place to instatiate it.

Generics

Generics are instance of *Universal Polymorphism* with explicit parameters (see Fig 8.1).

9.1 Methods

```
public static <T> T getFirst(List<T> list)
```

Invocations of generic methods must instantiate all type parameters, either explicitly or implicitly. Some sort of type inference is applied in case of implicit instantiation.

```
class NumList < E extends Number > {
    void m(E arg) {
        arg.intValue(); // OK, since...
        // Number and its subtypes support intValue()
    }
}
```

Type parameters can also be **bounded** as in the above example, allowing methods (and fields) defined in the **bound** to be invoked on objects of the type parameter T.

There may be various kinds of type bounds:

```
<TypeVar extends SuperType>
  // UPPER bound; SuperType and any of its subtype are ok.
<TypeVar extends ClassA & InterfaceB & InterfaceC & ...>
  // MULTIPLE UPPER bounds
<TypeVar super SubType>
  // LOWER bound; SubType and any of its supertype are ok
```

Unlike C++ where *overloading* is resolved and can **fail** after instantiating a template, in Java **type checking** ensures that overloading will succeed.

9.2 Inheritance and Arrays

There are two major issues which came up along with generics. The first one regards **inheritance**; consider the following example:

Since Integer is a *subtype* of Number, is List<Integer> *subtype* of List<Number>?

NO!

In a formal way, *subtyping is invariant* for Generic classes. Informally, given A,B concrete types, MyClass<A> has no relationship to MyClass, even if A,B have one.

On the other hand if A extends B and are *generic* classes, then A<C> extends B<C> for any type C. For example, ArrayList<Integer> extends List<Integer>.

Note that the common parent of MyClass and MyClass<A> is MyClass<?>.

Let's now discuss **covariance** and **contravariance**, with the aid of a few examples.

```
List<Integer> lisInt = new ...;
List<Number> lisNum = new ...;
lisNum = lisInt; // ??? - Reassign pointer
lisNum.add(new Number(...)); // NOT ALLOWED
listInt = lisNum; // ??? - Reassign pointer
Integer n = lisInt.get(0); // NOT ALLOWED
```

List<Integer> is neither a subtype or a supertype of List<Number>, thus the above operations aren't allowed. However there are read-only and write-only situations where they may be allowed.

```
RO_List < Integer > lisInt = new ...;
RO_List < Number > lisNum = new ...;
lisNum = lisInt; // ???
Number n = lisNum.get(0); // OK
```

It is ok to read a supertype starting from a subtype.

covariance is safe if the type is read-only

```
WO_List < Integer > lisInt = new ...;
WO_List < Number > lisNum = new ...;
lisInt = lisNum; // ???
lisInt.add(new Integer(...)); // OK
```

It is ok to write a **subtype** in the place of from a **supertype**.

contravariance is safe if the type is write-only

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Other languages

In the case of C#, generic classes can be marked with the keyword out (covariant) or in (contravariant), otherwise the class is invariant. In Scala the same happens, but with the + or - operators.

Let's now discuss **arrays**.

Let A extends B, then A[] extends B[] even if instead Array<A> is not related to Array.

Thus, arrays in Java are covariant.

However there is a counterpart, since this allows rule-breaking assignments which are allowed by the compiler but which lead to a runtime ArrayStoreException. This happens because the dynamic type of an array is checked at runtime. Knowing this, for each array update, a runtime check is performed by the JVM which throws the exception if needed.

After compilation Generic are all **type-erasured** to **Object** or to their first *bound*, if present. This choice has been made mainly for compatibility with legacy code, leading all instances of the same generic type to have the same type at runtime; i.e.

```
List < String > lst1 = new ArrayList < String > ();
List < Integer > lst2 = new ArrayList < Integer > ();
assert (lst1.getClass() == lst2.getClass())
```

9.2.1 Generic Arrays

What about arrays of generics? Such arrays in Java are **not allowed**, because every array update needs a runtime check which is impossible to perform on generics, since at runtime generics are all of the same type due to type-erasure.

Wildcards 9.3

Wildcards are strongly related to the topic of covariance and contravariance.

As briefly mentioned before, wildcards are the only relationship between generic classes.

To use wildcards, the PECS principle is applied: Producer Extends, Consumer Super.

- ♦ ? extends T to get values from a *Producer*: covariance allowed
- ♦ ? super T to insert values into a Consumer: contravariance allowed
- ♦ Never use ? when both insertion and retrieving is needed, T is sufficient and way more appropriate.

Wildcards improve type-safety, allowing a program to fail at *compile-time* instead of *runtime*.

```
List<Apple> apples = new ArrayList<Apple>();
List<? extends Fruit> fruits = apples;
fruits.add(new Strawberry()); // COMPILING FAILS
```

Generics Limitations 9.4

♦ Cannot instantiate Generics with primitive types:

```
ArrayList <int> a = ...
                                                                  // compile error
\diamond Cannot create instances of type parameters
```

♦ Cannot declare static fields whose types are type parameters

```
public class C<T>{ public static T local; ...}
```

Because static fields are represented in the unique representation of the class in the dedicated static memory area of the JVM for classes

Cannot use casts or instanceof with parameterized types

```
mylist instanceof ArrayList < Integer >
                                                // fails
                                                // OK
mylist instanceof ArrayList <?>
```

- ♦ Cannot Create arrays of parameterized types
- ♦ Cannot create, catch, or throw objects of parameterized types
- ♦ Cannot overload a method where the formal parameter types of each overload erase to the same raw type.

```
public class Example {
                                               // does not compile
   public void print(Set<String> strSet) { }
   public void print(Set < Integer > intSet) { } }
```

Standard Templates Library

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The goal of STL is to represent algorithms in as general form as possible without compromising efficiency. There is an extensive use of **templates**, **overloading** and **iterators**, which are used for decoupling algorithms from containers, and can be seen as an abstraction of pointers.

STL is very different from the Java Collection Library since it does **not** use dynamic binding and is **not** object oriented; instead the STL uses only static binding and inlining.

10.1 Main Entities

- ♦ Container collection of typed objects
- ♦ Iterator Generalization of pointer or address; used to step through the elements of collections
- ♦ Algorithm initializing, sorting, searching, and transforming contents of containers
- ♦ Adaptor Convert from one form to another e.g. iterator from updatable container; or stack from list
- ♦ Function Object Form of closure (class with "operator()" defined)
- ♦ **Allocator** encapsulation of a memory pool

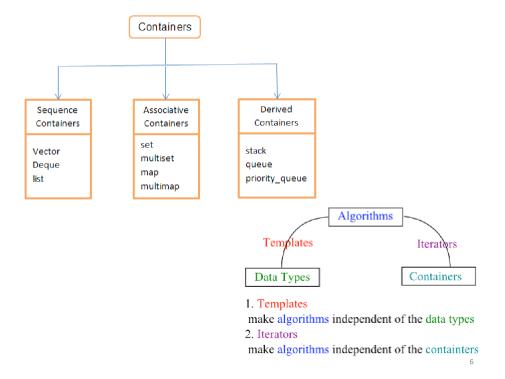


Figure 10.1: TIKZ RE-DO : STL Containers

10.2 Iterators

Since algorithms cannot be used *directly* on different kinds of collections, Iterators come in handy by providing a **uniform**, **linear** access to elements of different collections.

In **Java** iterators are supported by the JCF^1 through the interface Interface<T>. They are related to an **instance** of a class and are usually defined as *nested classes*, more precisely *non-static private member classes*. Collections equipped with iterators must implements Iterable<T> interface.

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In C++ there is no next/hasNext() function, standard ++ -- operators are used instead.

In case of arrays pointers can be trivially used, since int v[] is no different int *v². In the case of vector instead, an actual iterator may be instantiated, but the operator ++ stays the same.

```
vector < int > vec;
vector < int > :: iterator v = vec.begin();
while( v != vec.end()) {
    cout << "value of v = " << *v << endl;
    v++;
}</pre>
```

Every class in C++ has its own iterator; more specifically, containers define and expose a type named iterator in the container's **namespace**, allowing the semantic value of **iterator** to change according to the context.

10.2.1 C++ iterators implementation

Typically iterators are implemented as **struct** and provide a visit of the container, retaining information about the **state** of the visit, e.g. pointer to next element, remaining elements, and so on. Note that in case of *trees* or *graphs* the visit's state may not be trivial to be represented.

```
template <class T>
 struct v_iterator {
            T*v;
            int sz;
            v_{int} = v_{int} + v_{i
             // != implicitly defined
            bool operator == (v_iterator& p) { return v == p->v; }
            T operator*() { return *v; }
             v_iterator& operator++() { // Pre-increment
                         if (sz)
                                    ++v, --sz;
                         else
                                   v = NULL;
                         return *this;
            }
             v_iterator operator++(int) { // Post-increment!
                         v_iterator ret = *this;
                                                                                          // call pre-increment
                         ++(*this);
                        return ret;
            }
};
```

	insert/erase			
Container	beginning	middle	end	
vector	linear	linear	amortized constant	
list	constant	constant	constant	
deque	amortized constant	linear	amortized constant	

Table 10.1: Guaranteed time complexity for iterators

To achieve transparency to third-party algorithms STL assumes *constant* time for every operation, and allows 5 types of operators:

 $^{^1} Java\ Collection\ Framework$

²At least from an "accessing values" point of view, there are some differences in terms of static/dynamic allocation of memory.

- ♦ Formard iterators only dereference and pre/post increment
- ♦ Input (and Output) iterators same as formard iterators but with possible issues when dereferencing
- ♦ Bidirectional iterators dereference, pre/post increment and decrement
- \diamond Random access iterators same as Bidirectional but allow also integer sum (p+n) and difference (p-q)

Each category defines only the functions which take constant time. Not all iterators are defined for all containers, e.g. since random access takes linear time on lists, there is no random access iterator on lists.

10.2.2 Invalidation

When a container is *modified*, iterators *may* become **invalid**: no "exception" is thrown, iterators can still be used, but their behaviour is **undefined**. *Not* every operation invalidates iterators, it depends on the operation and on the container.

The main limiting aspect of STL's iterators is that they provide a **linear view** of the container, allowing the definition of operations only on one-dimensional containers; thus, if it is needed to access the organization of the container (e.g. tree custom visist), the only way-to-go is to define a custom iterator which behaves as desired.

10.3 C++ specific features

10.3.1 Inheritance

STL relies on typedefs combined with namespaces to implement genericity, the programmer always refers to container ::iterator to know the type of the iterator. Note that there is no relation among iterators for different containers (!), if not a semantically abstract one. The reason for this is **performance**: without *inheritance*, types are resolved at compile time and the compiler may produce better and optimized code. On the other hand sacrificing inheritance may lead to lower expressivity and lack of type-checking; in fact, STL relies only on coding conventions: when the programmer uses a wrong iterator the compiler complains of a bug in the library.

10.3.2 Inlining

C++ standard has the notion of **inlining** which is a form of semantic macros. Inline methods should be available in header files and can be labelled *inline* or defined within class definition, invocation on such methods is type-checked and then it is replaced by the method body. The compiler tends to (automatically?) inline methods with small bodies and without iteration; it is able to determine types at compile time and usually does inlining of function objects.

10.3.3 Memory management

STL abstract from the specific memory model using a concept named **allocators**. All the information about the memory model is encapsulated in the **Allocator** class. Each container is parametrized by such an allocator to let the implementation be unchanged when switching memory models.

10.3.4 Potential Problems

The problem may be error checking: almost all facilities of the compiler fail with STL resulting in lengthy error messages that ends with error within the library

Functional Programming

Functional Programming languages radicate their roots in the Church's model of computing known as lambda calculus. Such model is based on the notion Λ – parametrized expressions, with the focus on defining mathematical functions in a constructive and effective way. The computation proceeds by substituting parameters into expressions.

Functional programming languages such as Lisp, Scheme, FP, ML, Miranda and Haskell aim to implement Church's lambda calculus in the form of a programming language which does everything needed by **composing functions**, thus no mutable state and no side effects.

 ${\rm FPL^1}$ needs some key features which are often absent in *imperative* languages:

- \diamond 1st-class order and **high-order** functions: Functions can be *denoted*, passed as *arguments* to other functions, returned as result of function invocation
- ♦ Recursion opposed to "control variables"
- ♦ Powerful list facilities: Recursive functions exploit recursive definition of lists
- Polymorphism typically universal parametric implicit, which plays a key role when handling containers/collections.
- ♦ Fully general aggregates: there is a wide use of tuples and records, besides, data structures cannot be modified (no state!), they have to be re-created.
- Structured function returns allow to pass more meaningful information to the caller, avoiding the need for "side-effects".
- \diamond Gargabe collection

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11.1 FP language families

- 1. **LISP**: currently most used for AI after Python. Original LISP is no longer used, the current standard is $Common\ LISP$ which introduced statical scope opposed to the dynamic one of $Original\ LISP$; another version is called Scheme
- 2. ML: Common languages of this family are *Standard ML*, *Caml*, *OCaml*, *F*#. These are compiled languages, but intended for interactive use. ML results from the combination of Lisp and Algol-like features, including Garbage collection, Abstract data types, Module system and Exceptions
- 3. Haskell: Many features are shared with ML languages, but with some differences.
 - Type inference, Implicit parametric polymorphism, Ad hoc polymorphism (overloading) with type classes
 - ♦ Lazy evaluation, Tail recursion and continuations
 - \diamond **Purely functional** \rightarrow precise management of side effects

 $^{^1\}mathrm{Short}$ for $Functional\ Programming\ Languages$

11.2 Haskell basics

```
♦ Unit
♦ Booleans
                                                           o Patterns
♦ Integers
                                                           o Declarations
♦ Strings
                                                     Other types
                                                          o Functions
♦ Reals
                                                          • Polymorphism
♦ Tuples
                                                          • Type declarations
♦ Lists
                                                           o Type Classes
⋄ Records
                                                           • Monads

    Exceptions
```

Note that basic types are written with the first letter Uppercased.

Haskell provides an interactive read-eval-print interpreter (ghci): many examples are available in the lecture's slides, here we will discuss only some more interesting ones.

Variables (**names**) are bound to expressions, without evaluating them (because of lazy evaluation); the scope of the binding is the rest of the session.

Moving onto anonymous functions i.e. $\x \rightarrow \dots$ lambda notation

To declare explicit functions instead, the syntax is quite simple

```
f (x,y) = x+y --argument must match pattern (x,y)

reverse xs = -- linear, tail recursive
   let rev ([], accum ) = accum
   rev ( y:ys, accum ) = rev ( ys, y:accum )
   in rev ( xs, [] )
```

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11.3 More on Haskell features

Let's recall that Haskell is a **lazy** language, thus functions and data constructor don't evaluate arguments until they actually need them.

```
myData = [1,2,3,4,5,6,7]

twiceData = [2 * x | x <- myData]

-- [2,4,6,8,10,12,14]
```

Datatype declearations

```
data Color = Red | Yellow | Blue
data Atom = Atom String | Number
data List = Nil | Cons (Atom, List)

-- General form:
data <name> = <clause> | ... | <clause>
<clause> ::= <constructor> | <contructor> <type>

-- also possible to define Recursive data types
data Tree = Leaf Int | Node (Int, Tree, Tree)

Node(4, Node(3, Leaf 1, Leaf 2), Node(5, Leaf 6, Leaf 7))

-- it is possible to use constructors in pattern matching
sum (Leaf n) = n
sum (Node(n,t1,t2)) = n + sum(t1) + sum(t2)
```

Besides it is possible to match different cases with a specific case statement; note that Indendation in case statement MATTERS

```
data Exp = Var Int | Const Int | Plus (Exp, Exp)

case e of
   Var n -> ...
   Const n -> ...
   Plus(e1,e2) -> ...

-- Indendation in case statement MATTERS
```

11.3.1 Function Types

 $f :: A \rightarrow B \text{ means that:}$

$$\forall x \in Af(x) = \begin{cases} \exists y = f(x) \in B \\ run \ for ever \end{cases}$$

In other words, if f(x) terminates, then $f(x) \in B$. In ML, functions with type A \to B can throw an exception or have other effects, but **not** in Haskell.

11.3.2 Loops and Recursion

In FP for and while iterative loops are replaced by **recusive** subroutines calling themselves directly or indirectly (mutual recursion).

```
length' [] = 0
length' (x:s) = 1 + length'(s)
   -- definition using guards and pattern matching
   -- take' n lst returns first n elements of a list
```

```
take' :: (Num i, Ord i) => i -> [a] -> [a]
take' n _
| n <= 0 = []
take' _ [] = []
take' n (x:xs) = x : take' (n-1) xs</pre>
```

11.3.3 Higher-Order functions

Functions that take other functions as arguments or return a function as a result are higher-order functions.

```
applyTwice :: (a \rightarrow a) \rightarrow a \rightarrow a
                                      -- function as arg and res
applyTwice f x = f (f x)
> applyTwice (+3) 10 => 16
> applyTwice (++ " HAHA") "HEY" => "HEY HAHA HAHA"
> applyTwice (3:) [1] => [3,3,1]
applyTwice, f = f.f
                                       -- equivalent definition
:t(.)
> (.) :: (b -> c) -> (a -> b) -> a -> c
   -- define the operator |> which inverts the order between function and argument
   (|>) a f = f a
   (|>) :: t1 -> (t1 -> t2) -> t2
   -- Seems dull right?
   -- Look at the following example
   -- Here, the order of invocation is the same,
   -- but the second "infix" form is (might be) more readable
   > length ( tail ( reverse [1,2,3]))
      2
   > [1,2,3] |> reverse |> tail |> length
(+) :: Num a => a -> a -> a
> let f = (+) 5 // partial application
>:t f ==> f :: Num a => a -> a
> f 4 ==> 9
elem :: (Eq a, Foldable t) \Rightarrow a \Rightarrow t a \Rightarrow Bool
> let isUpper = ('elem' ['A'..'Z'])
>:t isUpper ==> isUpper :: Char -> Bool
> isUpper 'A' ==> True
> isUpper '0' ==> False
```

Combinators

map combinator applies argument function to each element in a collection.

```
map :: (a -> b) -> [a] -> [b]
map _ [] = []
map f (x:xs) = f x : map f xs
```

filter takes a collection and a boolean predicate, and returns the collection of the elements satisfying the predicate. It is defined as follows:

And can be applied in the following way

```
> filter (>3) [1,5,3,2,1,6,4,3,2,1]
[5,6,4]
> filter (==3) [1,2,3,4,5]
[3]
> filter even [1..10]
[2,4,6,8,10]
> let notNull x = not (null x)
in filter notNull [[1,2,3],[],[3,4,5],[2,2],[],[]]
[[1,2,3],[3,4,5],[2,2]]
```

reduce (foldl,foldr): takes a collection, an initial value, and a function, and combines the elements in the collection according to the function.

```
-- folds values from end to beginning of list
foldr :: Foldable t => (a -> b -> b) -> b -> t a -> b
foldr f z [] = z
foldr f z (x:xs) = f x (foldr f z xs)
-- folds values from beginning to end of list
foldl :: Foldable t => (b -> a -> b) -> b -> t a -> b
foldl f z [] = z
foldl f z (x:xs) = foldl f (f z x) xs
-- variants for non-empty lists
foldr1 :: Foldable t => (a -> a -> a) -> t a -> a
foldl1 :: Foldable t => (a -> a -> a) -> t a -> a
```

Let's provide some examples:

```
sum' :: (Num a) => [a] -> a
sum' xs = foldl (\acc x -> acc + x) 0 xs
maximum' :: (Ord a) => [a] -> a
reverse' :: [a] -> [a]
reverse' = foldl (\acc x -> x : acc) []
product ' :: (Num a) => [a] -> a
product ' = foldr1 (*)
product ' = foldr (*) 1
-- Notice that product' [] returns 1 !
filter' :: (a -> Bool) -> [a] -> [a]
filter' p = foldr (\x acc -> if p x then x : acc else acc)[]
head' :: [a] -> a
head' = foldr1 (x - > x)
last' :: [a] -> a
last' = foldl1 (\ x \rightarrow x)
```

11.3.4 Recursion and Optimization

From a theoretical point of view recursion and iteration are equivalently expressive, and typically one is preferred over the other depending on the problem being faced to make the code more intuitive. In general a procedure call is *much more expensive* than a conditional branch, however FP compilers can perform many optimizations and produce better code, especially for known blocks; for this reason the use of combinators such as map,reduce,filter, foreach,... is strongly encouraged.

Tail-recursive functions are functions in which no operations follow the recursive call(s) in the function, thus the function returns immediately after the recursive call, allowing the compiler to reuse the subroutine's frame on the run-time stack, since the current subroutine state is no longer needed. Besides many compilers instead of re-invoking the function, simply jump to the beginning of the function.

Let's provide the classic example of Fibonacci to illustrate how to convert a normal recursive function to its tail-recursive correspondant one:

```
-- typical Fibonacci

fib = \n -> if n == 0 then 1

else if n == 1 then 1

else fib (n - 1) + fib (n - 2)

fibTR = \n -> let fibhelper (f1, f2, i) =

if (n == i) then f2

else fibhelper (f2, f1 + f2, i + 1)

in fibhelper(0,1,0)
```

Notice that fibTR takes only $\mathcal{O}(n)$ since it builds the Fibonacci sequence starting from 1 to n, while the more canonical approach calculates multiple times the same values, and starts from n until 1 is reached.

foldl is tail-recursive, foldr is not. But because of laziness Haskell has no tail-recursion optimization. Despite this, it provides a more efficient variant of foldl called foldl' where f is evaluated strictly.

Strictly means that the compiler evaluates the accumulator at each step of the folding process, ensuring that intermediate values are not built up as unevaluated thunks i.e. Haskell's term for delayed computations. Due to its strictness fold' is less likely to cause space leaks (see note below), and it generally has better performance for many common folding operations.

[&]quot;Space leaks" many happen when a program retains references to data that should no longer be needed, preventing the garbage collector from reclaiming memory. This can lead to inefficient memory usage and, in some cases, cause the program to run out of memory. This (generally) occurs only when handling large data sources or *infinite data structures* (which are allowed in Haskell); space leaks may be very hard to debug, tools like memory profilers and heap profiling can be helpful in identifying them

λ Lambda calculus

Due to Haskell's **laziness**, functions and data constructors don't evaluate their arguments until they need them. In several languages there are forms of lazy evaluations (if-then-else, shortcutting && and ||).

12.1 Syntax

```
t ::= x | λ x.t | t t | (t)
x variable, name, symbol,...
λ x.t abstraction, defines an anonymous function
t t' application of function t to argument t'
```

We say that an occurrence of x is **free** in a term t if it is not in the body of an abstraction $\lambda x.t$, otherwise it is **bound**; λx instead is a **binder**. Examples $\lambda z.\lambda x.\lambda y.x(yz)$ $(\lambda x.x)x$

Terms without free variables are **combinators**. Identity function: $id = \lambda x.x$ First projection: $fst = \lambda x.\lambda y.x$.

β -Reduction

 β -reduction, i.e. function application, also called **redex**:

$$(\lambda x.t)t' = t[t'/x]$$

$$(\lambda x.x)y \longrightarrow y \tag{12.1}$$

$$(\lambda x. x(\lambda x. x))(ur) \longrightarrow ur(\lambda x. x) \tag{12.2}$$

$$(\lambda x.(\lambda w.xw))(yz) \longrightarrow \lambda w.yzw \tag{12.3}$$

$$(\lambda x.xx)(\lambda x.xx) \longrightarrow (\lambda x.xx)(\lambda x.xx) \tag{12.4}$$

12.2 Functions and lambdas

A definition of a function with a single argument associates a name with a λ -abstraction, while a function with several arguments is equivalent to a sequence of λ -abstractions

```
f x = \langle \exp \rangle -- is equivalent to

f = \lambda x.\langle \exp \rangle

f(x,y) = \langle \exp \rangle -- is equivalent to

f = \lambda x. \lambda y.\langle \exp \rangle

-- Curriend and uncurried functions

curry :: ((a, b) \rightarrow c) \rightarrow a \rightarrow b \rightarrow c

curry f x y = f(x,y)
```

```
uncurry :: (a \rightarrow b \rightarrow c) \rightarrow (a, b) \rightarrow c
uncurry f(x,y) = f x y
```

Well-known functions 12.3

```
• T = \lambda t \cdot \lambda f \cdot t -- first
                                                                    and T F
• F = \lambda t . \lambda f . f -- second
                                                                    \rightarrow (\lambdab.\lambdac.bcF) T F
                                                                    \rightarrow (\lambdac.TcF) F
• and = \lambda b.\lambda c.bcF
                                                                    \rightarrow TFF
                                                                    \rightarrow _{\rm F}
• or = \lambda b \cdot \lambda c \cdot bTc
• not = \lambda x.xFT
• test =\lambda l.\lambda m.\lambda n.lmn
                                                                    not F
                                                                    \rightarrow (\lambdax.xFT) F
 test F u w
                                                                    \rightarrow FFT
 \rightarrow (\lambda1.\lambdam.\lambdan.1mn) F u w
                                                                    \rightarrow T
 \rightarrow (\lambdam.\lambdan.Fmn) u w
 \rightarrow (\lambdan.Fun) w
 → Fuw
 \rightarrow w
```

Figure 12.1: Church Booleans using λ -calculus

$$pair = \lambda f.\lambda s.\lambda b.b \ f \ s$$

$$fst = \lambda p.p \ T$$

$$snd = \lambda p.p \ F$$

$$fst(pairuw) \\ \longrightarrow (\lambda p.p \ T)(pair \ u \ w) \\ \longrightarrow (pair \ u \ w) \ T \\ \longrightarrow (\lambda f.\lambda s.\lambda b.b \ f \ s) \ u \ wT \\ \longrightarrow (\lambda s.\lambda b.b \ u \ s) \ w \ T \\ \longrightarrow (\lambda b.b \ u \ w) \ T \\ \longrightarrow T \ u \ w \\ \longrightarrow u$$

$$0 = \lambda s. \lambda z. z \tag{12.5}$$

$$1 = \lambda s. \lambda z. s \ z \tag{12.6}$$

$$2 = \lambda s. \lambda z. s \ (s \ z) \tag{12.7}$$

$$B = \lambda s. \lambda z. s \ (s(s \ z)) \tag{12.8}$$

 $\begin{array}{ll} \mathbf{\tilde{g}} & 0 = \lambda s. \lambda z.z \\ 1 = \lambda s. \lambda z.s \ z \\ 2 = \lambda s. \lambda z.s \ (s \ z) \\ 3 = \lambda s. \lambda z.s \ (s(s \ z)) \\ & \\ \mathbf{\tilde{g}} \\ Numerals \ n \ \text{takes a function } s \ \text{as argument and returns the } n\text{-}th \ \text{composition of } s \ \text{with itself, } s^n. \end{array}$

e.g. $succ = \lambda n.\lambda s.\lambda z.s(nsz)$

Fix-point Y combinator 12.4

The following fix-point combinator Y, when applied to a function R, returns a fix-point of R, i.e. R(YR) = YR

37

$$Y = (\lambda y.(\lambda x.y(x\ x))(\lambda x.y(x\ x))) \tag{12.9}$$

$$YR = (\lambda x.R(x x))(\lambda x.R(x x))$$

$$= R((\lambda x.R(x x))(\lambda x.R(x x)))$$

$$= R(YR)$$
(12.10)

12.5 Evaluation ordering

Consider the two following ways of evaluating a redex, but remember that *regardless* of the evaluation order, the evaluation result is only one, and it is **unique**¹.

Applicative order evaluation implies eager evaluation of arguments before applying them to the function

```
(\lambda x.(+ x x)) (+ 3 2)

→ (\lambda x.(+ x x)) 5

→ (+ 5 5)

→ 10
```

Normal order evaluation implies functions to be evaluated first, and delay argument evaluation only when needed. Note that this may lead to multiple re-evaluations of the same argument.

```
(\lambda x.(+ x x)) (+ 3 2) 

\rightarrow (+ (+ 3 2) (+ 3 2)) 

\rightarrow (+ 5 (+ 3 2)) 

\rightarrow (+ 5 5) 

\rightarrow 10
```

Haskell realizes **lazy evaluation** by using **call by need** parameter passing: an expression passed as argument is bound to the formal parameter, but it is evaluated *only if* its value is **needed**. Besides, the argument is evaluated *only* the **first time**, using the **memoization** technique: the result is saved and further uses of the argument do not need to re-evaluate it.

Combined with lazy data constructors, this allows to construct potentially infinite data structures and to call infinitely recursive functions without necessarily causing non-termination.

Note: lazy evaluation works fine with purely **functional languages**. Side effects such as IO operations force the programmer to reason about the order in which things happen, which not predictable in lazy languages. We will address this fact when introducing Haskell's IO-Monad.

12.6 Post-lecture Takeaway message

While discussing with the professor after the lecture, an important intuition emerged about evaluation an memoization.

```
a = 5b = a + 3
```

b would evaluate to 8 but it is not evaluated until it is strictly necessarily.

```
a = 5
b = a + 3
a = 2
-- b?
```

Someone may think that due to lazy evaluation, b would now evaluate to 5. However, this is NOT Haskell's case. Due to **memoization**, even if b = a + 3 doesn't get evaluated, the current value of a is memoized and its re-definition doesn't affect b evaluation. Thus this snippet code leads b to be evaluated as 8, regardless of a redefinition.

```
a = 5
b = a + 3
a = 2
b
```

¹Proved by Church and Rosser

Type Inference

Polymorphism in Haskell

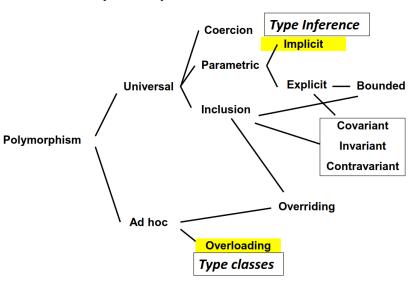


Figure 13.1: Haskell Polymorphism Recap

13.1 Overloading

Haskell allows **overloading** even of **primitive types**: the code to be executed is determined by the type of the arguments, leading to have *early binding* in *statically* typed languages or *late binding* in *dynamically* typed languages.

In Haskell we can write the following, but what is the type?

```
sqr x = x * x
```

When considering overloading besides arithmetic, we find that some functions are fully polymorphic:

```
\texttt{length} \; :: \; \texttt{[w]} \; \to \; \texttt{Int}
```

While others not so much; for example, *membership* works only for types that support equality, while *sorting* works only for types which support *ordering*.

13.2 Type Classes

Type Classes solve many overloading problems concerning arithmetic and equality (and similar properties) support.

implementation summary

The idea is to generalize ML's equippes to arbitrary types and provide concise types to describe overloaded functions, so no exponential blow-up (i.e. defining functions for every possible combination of type arguments).

Type classes allow users to define functions using overloaded operations —e.g. square, squares, and member— and to declare new collections of overloaded functions: equality and arithmetic operators are not privileged built-ins. Haskell's solutions fits perfectly within type inference framework.

The intuition is that a sorting function may allow to be passed a comparison cmp operator as argument, thus making the function parametric.

```
qsort:: (a \rightarrow a \rightarrow Bool) \rightarrow [a] \rightarrow [a] qsort cmp [] = [] qsort cmp (x:xs) = qsort cmp (filter (cmp x) xs) ++ [x] ++ qsort cmp (filter (not.cmp x) xs)
```

Developing this idea, consider rewriting the parabola function to take operators as argument

```
parabola x = (x * x) + x
parabola' (plus, times) x = plus (times x x) x
```

Here the extra parameter is a *dictionary* that provides implementations for the overloaded ops. These implies rewriting calls to pass appropriate implementations for plus and times:

```
y = parabola'(intPlus,intTimes) 10
z = parabola'(floatPlus, floatTimes) 3.14
```

- 1. Type class declarations
 - i. Define a set of operations, give it a name
 - ii. Example: Eq a type class \bullet operations == and \= with type a \rightarrow a \rightarrow Bool
- 2. Type class instance declarations
 - i. Specify the implementations for a particular type
 - ii. For Int instance, == is defined to be integer equality
- 3. Qualified types (or Type Constraints) Concisely express the operations required on otherwise polymorphic type member:: Eq w ⇒ w → [w] → Bool
- 1. Each overloaded symbol has to be introduced in at least one type class
- 2. The compiler translates each function that uses an overloaded symbol into a function with an extra parameter: the dictionary.
- 3. References to overloaded symbols are rewritten by the compiler to lookup the symbol in the dictionary.
- 4. The compiler converts each type class declaration into a dictionary type declaration and a set of selector functions.
- 5. The compiler converts each instance declaration into a dictionary of the appropriate type.
- 6. The compiler rewrites calls to overloaded functions to pass a dictionary. It uses the static, qualified type of the function to select the dictionary.

13.2.1 Compositionality

```
class Eq a where

(==) :: a \rightarrow a \rightarrow Bool

instance Eq Int where

(==) = intEq -- intEq primitive equality
instance (Eq a, Eq b) => Eq(a,b) where

(u,v) == (x,y) = (u == x) && (v == y)
instance Eq a => Eq [a] where

(==) [] [] = True

(==) (x:xs) (y:ys) = x==y && xs == ys

(==) _ = False
```

13.2.2 Compound Translation

13.2.3 Subclasses

A subclass declaration expresses this relationship:

```
class Eq a => Num a where (+) :: a \rightarrow a \rightarrow a (*) :: a \rightarrow a \rightarrow a
```

• With that declaration, we can simplify the type of the function

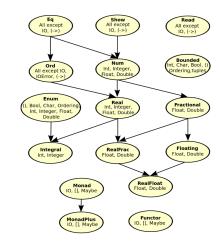


Figure 13.2: Haskell Subclasses relationships

13.2.4 Deriving

For Read, Show, Bounded, Enum, Eq. and Ord, the compiler can generate instance declarations automatically.

```
data Color = Red | Green | Blue
    deriving (Show, Read, Eq, Ord)

Main>:t show
show :: Show a => a → String
Main> show Red
"Red"
Main> Red < Green
True
Main>:t read
read :: Read a => String → a
Main> let c :: Color = read "Red"
Main> c
Red
```

13.2.5 Numeric Literals

```
class Num a where (+) :: a \rightarrow a \rightarrow a
(-) :: a \rightarrow a \rightarrow a
fromInteger :: Integer \rightarrow a
-- Even literals are overloaded.
-- 1 :: (Num a) => a
...
inc :: Num a => a \rightarrow a
inc x = x + 1
```

Numeric literals can be interpreted as values of any appropriate numeric type, for example: 1 can be an Integer or a Float or a user- defined numeric type.

13.2.6 Missing Notes

Look at slides 34...64 for more on Type Inference.

13.3 Inferencing types

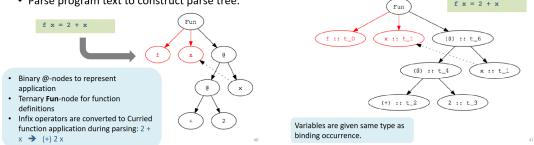
In standard type checking the compiler examine body of each function and uses declared types to check agreement; type inference instead consists in examining code without type information, and infer the most general types that could have been declared

13.3.1 Steps schematics

Step 1: Parse Program

Step 2: Assign type variables to nodes

• Parse program text to construct parse tree.



Constraints can be deduced from (function) Application nodes f x and from Abstractions f x = e.

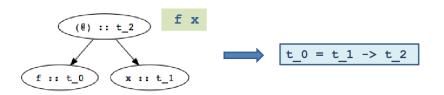


Figure 13.2: Deducing constraints from function application

- \diamond Type of f (t_0 in figure) must be $domain \longrightarrow range$.
- ♦ Domain of f must be type of argument x (t_1)
- \diamond Range of f must be result of application (t_2)
- \diamond Constraint: t_0 = t_1 \rightarrow t_2

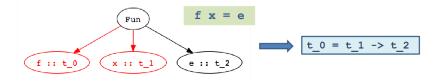


Figure 13.3: Deducing constraints from abstractions

- \diamond Type of f (t_0) must $domain \longrightarrow range$
- \diamond **Domain** is type of abstracted variable x (t_1)
- ♦ Range is type of function body e (t_2)
- \diamond Constraint: t_0 = t_1 \rightarrow t_2

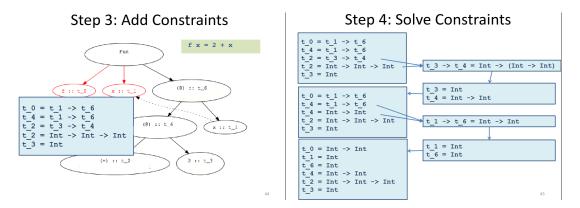
Steps summary

- 1. Parse program to build parse tree
- 2. Assign type variables to nodes in tree
- 3. Generate constraints:
 - i. From environment: constants (2), built-in operators (+), known functions (tail).
 - ii. From shape of parse tree: e.g., application and abstraction nodes.
- 4. Solve constraints using unification
- 5. Determine types of top-level declarations

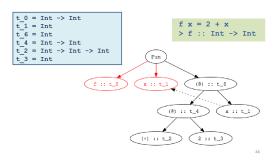
13.3.2 Polymorphism

In general unconstrained type variables become polymorphic types; for instance, in the example below t_4 is unconstrained, hence we get a polymorphic type:

For functions with multiple clauses, i.e. *polymorphic datatypes*, for each clause a separate type is inferred, and then the resulting types are combined by adding constraints such as that all clauses have the same type. In case of *recursive calls*: the function has same type as its definition.



Step 5: Determine type of declaration



```
append ([],r) = r
append (x:xs, r) = x : append (xs, r)
```

- 1. Infer type of each clause
 - i. First clause:

```
\rightarrow append :: ([t_1], t_2) \rightarrow t_2
```

ii. Second clause:

```
> append :: ([t_3], t_4) \rightarrow [t_3]
```

2. Combine by equating types of two clauses

```
\mid > append :: ([t_1], [t_1]) \rightarrow [t_1]
```

13.3.3 Overloading

In presence of **overloading** (*Type Classes*), type inference infers a **qualified type** $Q \Rightarrow T$

- ⋄ T is a Hindley Milner type, inferred as seen before
- ♦ Q is set of type class predicates, called a constraint

```
example :: Ord a => a \rightarrow [a] \rightarrow Bool example z xs = case xs of [] \rightarrow False (y:ys) \rightarrow y > z || (y==z && ys == [z])
```

```
In the example Type T is a \rightarrow [a] \rightarrow Bool while the Constraint Q is { Ord a, Eq a, Eq [a]}. Q later simplifies 1 to \Rightarrow Eq a because y=z \Rightarrow Eq [a] because y == [z]
```

13.4 Type Constructors

Type Classes are predicates over types, while [Type] Constructor Classes are predicates over type constructors.

 $^{^{1}}$ According to some rules not discussed here

For example, consider three versions of the map function (implementation is omitted): the basic one for lists, one for trees and one for Maybe.

They all share the same structure, thus they can all be written as

```
\texttt{fmap::} \;\; (\texttt{a} \; \rightarrow \; \texttt{b}) \; \rightarrow \; \texttt{g} \;\; \texttt{a} \; \rightarrow \; \texttt{g} \;\; \texttt{b}
```

where g is a function from types to types, i.e. a type constructor; it is: [-] for lists, Tree for trees, and Maybe for options.

13.4.1 Functor

This pattern can be captured in a constructor class Functor. A constructor class is simply a type class where the predicate is over a type constructors rather than on a type:

```
class Functor g where fmap :: (a \rightarrow b) \rightarrow g a \rightarrow g b
```

Compare with the definition of a standard type class:

```
class Eq a where (==) :: a \rightarrow a \rightarrow Bool
```

So, wrapping up, we can instantiate Functor on all three data structures, and then simply use the *overloaded* symbol fmap, instead of map, mapTree and mapMaybe.

```
class Functor f where
   fmap :: (a → b) → f a → f b
instance Functor [] where // [] is an instance of Functor
   fmap f [] = []
   fmap f (x:xs) = f x : fmap f xs
instance Functor Tree where // Tree is an instance of Functor
   fmap f (Leaf x) = Leaf (f x)
   fmap f (Node(t1,t2)) = Node(fmap f t1, fmap f t2)
instance Functor Maybe where // Maybe is an instance of Functor
   fmap f (Just s) = Just(f s)
   fmap f Nothing = Nothing
```

Monads

14.1 Type Constructors

14.1.1 Towards Monads

Often type constructors can be thought of as defining "boxes" for values, and Functors with fmap allow to apply functions inside such "boxes".

Monad is a constructor class introducing operations for *putting a value* into a "box" (return) and *composing* functions that return "boxed" values (bind)

"Monads" are type constructors that are instances of Monad

14.1.2 Maybe

A function $f :: a \rightarrow Maybe b$ is a partial function from a to b.

14.1.3 Bind operator

We introduce a higher order operator to compose partial functions in order to "propagate" undefinedness automatically.

The bind operator will be part of the definition of a monad.

```
y \ge g = case y of
Nothing \rightarrow Nothing
Just x \rightarrow g x

(>>=) :: Maybe a \rightarrow (a \rightarrow Maybe b) \rightarrow Maybe b
```

do{} is an alternative equivalent syntax, more imperative-like.

```
gf2 <- father mom
return (gf1, gf2)</pre>
```

14.2 Monads as *

14.2.1 ...containers

```
class Monad m where -- definition of Monad type class return :: a \rightarrow m \ a (>>=) :: m \ a \rightarrow (a \rightarrow m \ b) \rightarrow m \ b -- "bind" ... -- + something more + a few axioms
```

The monadic constructor can be seen as a container: let's see this for lists

```
map :: (a \rightarrow b) \rightarrow [a] \rightarrow [b] -- seen. "fmap" for Functors return :: a \rightarrow [a] -- container with single element return x = [x] concat :: [[a]] \rightarrow [a] -- flattens two-level containers Example: concat [[1,2],[],[4]] = [1,2,4] (>>=) :: [a] \rightarrow (a \rightarrow [b]) \rightarrow [b] xs >>= f = concat(map f xs) Exercise: define map and concat using bind and return
```

14.2.2 ... computations

```
class Monad m where -- definition of Monad type class return :: a \rightarrow m \ a (>>=) :: m \ a \rightarrow (a \rightarrow m \ b) \rightarrow m \ b -- "bind" (>>) :: m \ a \rightarrow m \ b \rightarrow m \ b -- "then" ... -- + something more + a few axioms
```

A value of type m a is a "computation returning a value of type a"

For any value, there is a computation which "does nothing" and produces that result. This is given by function return

Given two computations x and y, one can form the computation $x \not\in y$ which intuitively "runs" x, throws away its result, then runs y returning its result

Given computation x, we can use its result to decide what to do next. Given f: a -i m b, computation x i = f runs x, then applies f to its result, and runs the resulting computation.

Note that we can define then using bind:

```
x \gg y = x \gg (/ \rightarrow y)
```

eturn, bind and then define basic ways to compose computations • They are used in Haskell libraries to define more complex composition operators and control structures (sequence, for-each loops, ...) • If a type constructor defining a library of computations is monadic, one gets automatically benefit of such libraries

Example: MAYBE • f:a - ξ Maybe b is a partial function • bind applies a partial function to a possibly undefined value, propagating undefinedness Example: LISTS • f:a - ξ [b] is a non-deterministic function • bind applies a non-deterministic function to a list of values, collecting all possible results

14.3 IO Monad

14.3.1 FP pros & cons

- Concise and powerful abstractions
 - higher-order functions, algebraic data types, parametric polymorphism, principled overloading, ...
- ♦ Close correspondence with mathematics
 - Semantics of a code function is the mathematical function
 - Equational reasoning: if x = y, then f x = f y
 - Independence of order-of-evaluation (Confluence, aka Church-Rosser)

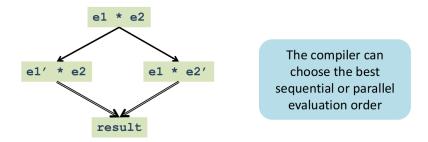


Figure 14.1: Evaluation order freedom

- ♦ Input/Output
- ♦ Imperative update
 - ♦ Error recovery (eg, timeout, divide by zero, etc.)

 $\diamond\,$ For eign-language interfaces

Concurrency control

sides, recall that the whole point of a running a program is to interact with the external environment and affect

Be-

14.3.2 Towards IO

To overcome the problem of interaction, an approach is to add imperative constructs to the language, for instance:

```
res = putchar 'x' + putchar 'y'
```

Seems easy right? Well, in fact no, because in lazy languages like Haskell, the evaluation order is **undefined**; so, in the previous example, which char will be printed first, x or y? The answer is not trivial for Haskell. However it is not an impossible problem. Haskell's approach is to exploit the concept of Monads.

Recall that the bind operator i.i = forces a sequence between the evaluation of terms; the IO monad exploits this and defines monadic values which are called actions, and prescribes how to compose them sequentially

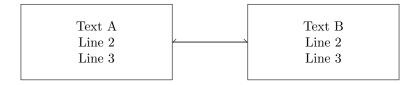


Figure 14.2: ¡caption,

Before Monads

Before Monads there were Streams, which allowed a program to send stream of requests to OS and receive stream of responses, or the user could supply **continuations** to I/O routines to specify how to process results. However, both of these approaches revealed to be not so useful.

14.3.3 Key Ideas - Monadic I/O

10 is a type constructor, instance of Monad, and a value of type (10 t) is an action (i.e. computation) that, when performed, may do some input/output before delivering a result of type t

- ♦ return returns the value without making I/O
- ♦ then (>>) [and also \lstinlinebind (¿;=)——] composes two actions sequentially into a larger action
- ♦ The only way to perform an action is to call it at some point, directly or indirectly, from Main.main, which is the standard entry point for Haskell programs.

An action is a first-class value, and evaluating has no effect: performing the action has the effect.

The actual meaning of this statement is unclear even to the professor ©

```
return :: a \rightarrow IO a
              IO a \rightarrow (a \rightarrow IO b) \rightarrow IO b
(>>=) m k = \setminusw \rightarrow case m w of (r,w')
```

By writing case m w ... we force the evaluation of m, resulting in the application of k to r w' to be performed (evaluated?) after the evaluation of m.

$14.3.4 \rightarrow = and >> combinators$

Operator is called **bind** because it binds the result of the left-hand action in the action on the right. Performing compound action $a \gg x \to b$:

- 1. performs action a, to yield value r
- 2. applies function $\x \rightarrow b$ to r
- 3. performs the resulting action $b\{x \leftarrow r\}$
- 4. returns the resulting value v

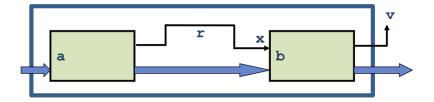


Figure 14.3: Bind Combinator

The then combinator (>>) instead does sequencing when there is no value to pass:

```
m >> n = m >>= (\setminus_{-} \rightarrow n)
```

14.3.5 Restrictions

In pure Haskell, there is no way to transform a value of type IO a into a value of type a. Suppose you wanted to read a configuration file at the beginning of your program:

```
configFileContents :: [String]
configFileContents = lines (readFile "config") -- WRONG!
useOptimisation :: Bool
useOptimisation = "optimise" 'elem' configFileContents
```

The problem is that readFile returns an IO String, not a String.

Possible workarounds

- 1. Write entire program in IO monad. But then we lose the simplicity of **pure** code.
- 2. Escape from the IO Monad using a function from 10 String →String. But this is disallowed!

We know the configuration file will not change during the program, so it doesn't matter when we read it. This situation arises sufficiently often that Haskell implementations offer one last unsafe I/O primitive: unsafePerformIO

The operator has a deliberately long name to *discourage* its use. Besides, its use comes with a proof obligation: a promise to the compiler that the *timing* of this operation relative to all other operations doesn't matter.

It is called *unsafe* because it breaks the soundness of the type system; thus, claims that Haskell is type safe are valid only when unsafePerformIO is **not** used.

14.4 Summary

♦ A complete Haskell program is a single IO action called main. Inside IO, code is single-threaded.

- ♦ Big IO actions are built by gluing together smaller ones with bind (>>=) and by converting pure code into actions with return.
- ♦ IO actions are first-class. They can be passed to functions, returned from functions, and stored in data structures; so, it is easy to define new "glue" combinators.
- $\diamond\,$ The IO Monad allows Haskell to be pure while efficiently supporting side effects.
- \diamond The type system separates the *pure* from the *effectful* code.
- ♦ In languages like ML or Java, the fact that the language is in the IO monad is baked in to the language. There is no need to mark anything in the type system because it is everywhere.
- ♦ In Haskell, the programmer can choose when to live in the IO monad and when to live in the realm of pure functional programming.
- ♦ So it is not Haskell that lacks imperative features, but rather the other languages that lack the ability to have a statically distinguishable pure subset.

Lambdas

15.1 Java 8

```
List < Integer > intSeq = Arrays.asList(1,2,3);
intSeq.forEach(x \rightarrow System.out.println(x));
// equivalent syntax
intSeq.forEach((Integer x) \rightarrow System.out.println(x));
intSeq.forEach(x \rightarrow {System.out.println(x);});
intSeq.forEach(System.out::println); //method reference
```

Note that local variables used inside the body of a lambda must be final or effectively final, or have to be static.

```
int var = 10; // must be [effectively] final
  intSeq.forEach(x \rightarrow System.out.println(x + var));
  // var = 3; // uncommenting this line it does not compile

public class SVCExample { // static variable capture
  private static int var = 10;
  public static void main(String[] args) {
    List<Integer> intSeq = Arrays.asList(1,2,3);
    static int var = 10;

    intSeq.forEach(x \rightarrow System.out.println(x + var));
    var = 3; // OK! it compiles
}}
```

15.2 Functional Interfaces

Java 8 lambdas are instances of functional interfaces, which are java interfaces with exactly one abstract method.

```
public interface Comparator <T> { //java.util
    int compare(T o1, T o2);
}
public interface Runnable { //java.lang
    void run();
}
public interface Consumer <T> { //java.util.function
    void accept(T t)
}
public interface Callable <V> { //java.util.concurrent
    V call() throws Exception;
}
```

The lambda is invoked by calling the only abstract method of the functional interface; lambdas can be interpreted as instances of anonymous inner classes implementing the functional interface.

For instance, recalling the forEach presented earlier, the corresponding interface is the following. Note that it must be checked that the lambda matches the forEach signature defined in the interface:

```
intSeq.forEach(x \rightarrow System.out.println(x));

// List<T> extends Iterable<T>
interface Iterable<T>{ //java.lang
  default void forEach(Consumer<? super T> action)
  for (T t : this)
      action.accept(t);
```

Method References

Method references can be used to pass an existing function in places where a lambda is expected, but their signature needs to match the signature of the functional interface method required.

static	ClassName::StaticMethodName	String::valueOf
constructor	ClassName::new	ArrayList::new
specific object instance	objectReference::MethodName	x::toString
arbitrary object of a given type	ClassName::InstanceMethodName	Object::toString

Table 15.1: Method references examples

Streams

Let's consider the properties of Streams, and we'll clearly see how they are different from Collections.

⋄ No storage

A stream is not a data structure that stores elements; instead, it conveys elements from a $source^{-1}$ through a pipeline of computational operations.

- \diamond **Functional** in nature
 - An operation on a stream produces a *result*, but does *not* modify its source.
- ♦ Laziness-seeking Many stream operations can be implemented lazily, exposing opportunities for optimization. Stream operations are divided into intermediate (stream-producing) operations —which are always lazy— and terminal (value- or side-effect-producing) operations.
- ♦ Possibly unbounded

While collections have a *finite size*, streams need *not*. Short-circuiting operations such as limit(n) or findFirst() can allow computations on *infinite streams* to complete in *finite time*.

♦ Consumable

The elements of a stream are only *visited once* during the life of a stream. Like an Iterator, a new stream must be generated to *revisit* the same elements of the source.

The Stream is considered *consumed* when a *terminal* operation is invoked. No other operation can be performed on the Stream elements afterwards.

16.1 Pipelines

A typical pipeline contains

- 1. A **source**, producing (by need) the elements of the stream
- 2. Zero or more **intermediate** operations, producing streams
- 3. A **terminal** operation, producing side-effects or non- stream values

Example of typical pattern: filter / map / reduce

```
double average = listing // collection of Person
    .stream() // stream wrapper over a collection
    .filter(p \rightarrow p.getGender() == Person.Sex.MALE) // filter
    .mapToInt(Person::getAge) // extracts stream of ages
    .average() // computes average (reduce/fold)
    .getAsDouble(); // extracts result from OptionalDouble
```

16.1.1 Sources

Common sources are Collections via stream() and parallelStream() methods, but there are several and various other sources, like IntStream.range(int, int), Stream.iterate(Object, UnaryOperator), BufferedReader.lines(), Random. ints(), and many others.

 $^{^{1}\}mathrm{e.g.}$ a data structure, an array, a generator function, an I/O channel,...

16.1.2 Intermediate operations

An intermediate operation keeps a stream *open* for further operations. Intermediate operations are lazy, and several of them have arguments of *functional interfaces*, thus **lambdas** can be used.

Example are map(), peek(), distinct(), sorted()

16.1.3 Terminal operations

A terminal operation must be the *final operation* on a stream. Once a terminal operation is invoked, the stream is consumed and is no longer usable. As said before, the typical approach is to collect values in a data structure, reduce to a value, and lastly print or cause other side effects.

Examples are reduce(), forEach(), allMatch() and others.

reduce() is basically our well-known fold

16.2 Mutable Reduction

Suppose we want to concatenate a stream of strings:

```
String concatenated = listOfStrings
    .stream()
    .reduce("", String::concat)
```

The above works, but is highly inefficient: it builds one new string for each element, since Strings are immutable in Java.

It would be better to "accumulate" the elements in a mutable object (e.g. a StringBuilder, a collection, ...). In our aid comes the mutable reduction operation which is called collect(), which requires three functions:

- 1. a **supplier** function to *construct* new instances of the result container,
- 2. an **accumulator** function to *incorporate* an input element into a result container,
- 3. a **combining** function to *merge* the contents of one result container into another.

```
<R> R collect( Supplier <R> supplier,
                BiConsumer <R, ? super T> accumulator,
                BiConsumer < R, R > combiner);
// NO streams
ArrayList < String > strings = new ArrayList <>();
for (T element : stream) {
   strings.add(element.toString());
// with streams and \lambda s
ArrayList < String > strings =
stream.collect(
   () \rightarrow new ArrayList<>(),
   (c, e) \rightarrow c.add(e.toString()),
                                       // Accumulator
   (c1, c2) \rightarrow c1.addAll(c2));
                                        // Combining
// with streams and method references
ArrayList < String > strings = stream.map(Object::toString)
             ArrayList::new,
                                  // Supplier
.collect(
                                    // Accumulator
             ArrayList::add,
             ArrayList::addAll); // Combining
```

However, collect() can also be invoked with a Collector argument, which encapsulates the functions used as arguments to collect (Supplier, BiConsumer, BiConsumer), allowing for reuse of collection strategies and composition of collect operations.

```
Map<String, List<Person>> peopleByCity =
   personStream.collect(Collectors.groupingBy(Person::getCity));
```

16.3 Parallelism

Streams facilitate parallel execution: stream operations can execute either in serial (default) or in parallel, with the runtime support transparently taking care of using multithreading for parallel execution. If operations don't have

side-effects, thread-safety is guaranteed even if non-thread-safe collections are used (e.g. ArrayList).

Also concurrent mutable reduction is supported for parallel streams, however Order of processing stream elements depends on serial/parallel execution and intermediate operations, and may not be predictable.

16.3.1 Summing up

One should use Parallelism

- When operations are independent, and
- ♦ Either or both:
 - Operations are computationally expensive
 - Operations are applied to many elements of efficiently splittable data structures

16.3.2 Critical Issues

⋄ Non-interference

- Behavioural parameters (like lambdas) of stream operations should not affect the source (i.e. non-interfering behaviour)
- Risk of ConcurrentModificationExceptions, even in single-threaded execution

♦ Stateless behaviours

- Stateless behaviour for intermediate operations is encouraged, as it facilitates parallelism, and functional style, thus maintenance

Parallelism and thread safety

- For parallel streams with *side-effects*, ensuring thread safety is the programmers' responsibility

```
String concatenatedString = listOfStrings
.stream()
.peek(s \rightarrow listOfStrings.add("three")) // DON'T DO THIS!
    // Interference occurs here.
.reduce((a, b) \rightarrow a + " " + b)
.get();
```

16.4 Monads in Java

```
public static <T> Optional <T> of(T value)
// Returns an Optional with the specified present non-null value.
<U> Optional <U> flatMap(Function <? super T,Optional <U>> mapper)
```

If a value is present, flatMap applies the provided *Optional-bearing* mapping function to it, return that result, otherwise return an empty Optional.

```
static <T> Stream <T> of(T t)
// Returns a sequential Stream containing a single element.
<R> Stream <R> flatMap(
Function <? super T,? extends Stream <? extends R>> mapper)
```

Here flatMap returns a Stream consisting of the results of replacing each element of this stream with the contents of a mapped stream produced by applying the provided mapping function to each element.

[&]quot;Always measure before and after parallelizing!"

Frameworks and IOC

17.1 Frameworks

A **Software Framework** is a collection of common code providing generic functionality that can be selectively overridden or specialized by user code providing specific functionality.

An **Application Framework** is a software framework used to implement the standard structure of an *application* for a specific development environment.

- 1. General Software Frameworks
 - i. .NET
 - ii. Android SDK
 - iii. Cocoa
 - iv. Eclipse
- 2. GUI Frameworks
 - i. MFC
 - ii. Gnome
 - iii. Qt
- 3. Web Frameworks
 - i. ASP.NET
 - ii. Rails
 - iii. GWT
 - iv. Spring
 - v. Flask

A framework embodies some abstract design, with more behavior built in. In order to use it you need to insert your behavior into various places in the framework either by subclassing or by plugging in your own classes, then the framework's code, which handles the program's **control flow** (the "main execution"), then calls your code at these points.

This realizes a very general concept, emphasizing **inversion of control** as opposed to libraries, where the user's code calls the library one, here is the code of the framework that calls the user's one.

17.1.1 Component Frameworks

Component Frameworks support development, deployment, composition and execution of components designed according to a given Component Model. More specifically, they support composition/connection of components according to the mechanisms provided by the *Component Model*, allowing instances to be "plugged" into the component framework itself, and regulating their interaction.

IDE and Frameworks

NetBeans is both an IDE and supports the JavaBeans *Component Framework*. In general A framework can be supported by several IDEs

e.g. Spring supported by Spring Tool Suite (based on Eclipse), NetBeans, IntelliJ IDEA, Eclipse, ...

While an IDE can support several frameworks

e.g NetBeans supports JavaBeans, Spring, J2EE, Maven, Hibernate, JavaServer Faces, Struts, Qt, ...

17.1.2 Features

Consist of parts that are found in many apps of that type

- ♦ **Libraries** with APIs (classes with methods etc.)
- ♦ Ready-made extensible programs ("engines")
- ♦ Sometimes also **tools** (e.g. for development, configuration, content)

They also provide reusable abstractions of code wrapped in a well-defined API, however recall that, unlike in libraries, the overall program's **flow of control** is *not* dictated by the caller, but by the *framework*.

Frameworks usually support extensibility, either by extending within the framework language — using, subclassing, overriding, implementing interfaces, registering event handlers, ...— or through plug-ins defined in a specific format.

17.2 Inversion of Control

17.2.1 GUI

In text-based interaction, the order of interactions and of invocations is decided by the the code, while in the **GUI**-based interaction, the GUI loop decides when to invoke the methods (listeners), based on the order of events.

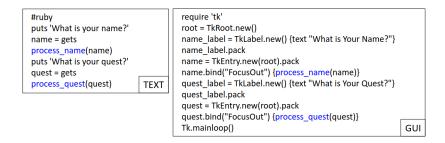


Figure 17.1: Text vs GUI interaction

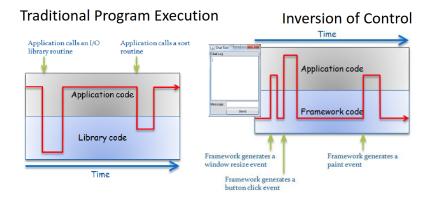


Figure 17.2: IoC: Library vs Framework approach

17.2.2 Containers

Often Frameworks provide **containers** for deploying *components*: a container may provide at *runtime functionalities* needed by the components to execute.

For examples EJB containers are responsible of the persistent storage of data and of the availability of EJB's for all authorized clients.

17.3 Loosely Coupled Systems

Good OO Systems should be organised as network of interacting objects, keeping in mind as a goal to have high cohesion, low coupling.

Low coupling has as key advantages

- ♦ Extensibility
- ♦ Testability
- ♦ Reusability

17.3.1 Dependecy Injection

When discussing **IoC** in Frameworks, "Control" does not refer only to control flow, but also control over dependencies, coupling, configuration.

We can make a few considerations on IoC with respect to dependencies:

- something outside a component handles:
 - configuration (properties)
 - wiring / dependencies (components)
- component-oriented
- ⋄ removes coupling
 - coupling of configuration and dependencies to the point of use
 - coupling of component to concrete dependent components
- somewhat contrary to encapsulation

17.4 Trade Monitor

Let's discuss this example to see how all of this comes into practice.

A trader wants that the system rejects trades when the exposure reaches a certain limit

Thus the component (class) TradeMonitor provides a method TryTrade (below) which checks the condition, accessing current exposure and exposure limit from a DAO (Data Access Object), a persistent storage.

```
public bool TryTrade(string symbol, int amount){
   int limit = limitDao.GetLimit(symbol);
   int exposure = limitDao.GetExposure(symbol);
   return (exposure + amount > limit) ? false : true;
}
```

How can we limit dependencies among the two components?

17.4.1 Interfaces - Refactoring 1

Let's consider a possible refactoring, introducing **interface** and implementation separation, which still has a static dependency on DAO:

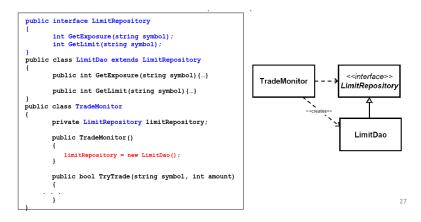


Figure 17.3: Refactoring 1

17.4.2 Factory - Refactoring 2

Here we introduce a **factory** which resolves the previous problem, but LimitDao is still tightly coupled, but to Factory.

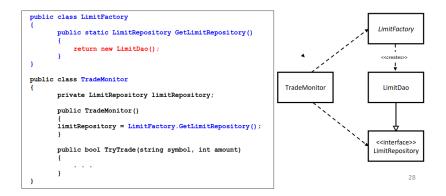


Figure 17.4: Refactoring 2

17.4.3 ServiceLocator - Refactoring 3

Introduce a ServiceLocator. This object acts as a (static) registry for the LimitDao you need, giving us extensibility, testability, reusability.

However ote that an external Assembler sets up the registry.

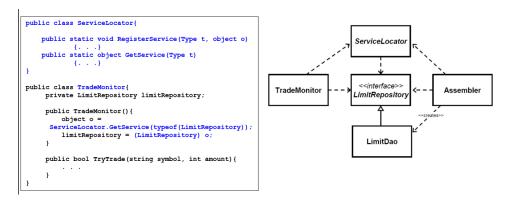


Figure 17.5: Refactoring 3

- ♦ The Service Locator pattern succeeds in decoupling the TradeMonitor from the LimitDao
- ♦ Allows new components to be dynamically created and used by other components later
- ♦ It can be generalized in several ways, eg. to cover dynamic lookup
- ♦ Every component that needs a dependency must have a reference to the service locator
- ♦ All components need to be registered with the service locator
- ♦ If bound by name:
 - Services can't be type-checked
 - Component has a dependency to the dependent component names
 - if many components share an instance but later you want to specify different

instance for some, this becomes difficult

- ♦ If bound by type can only bind one instance of a type in a container
- \diamond Code needs to handle lookup problems

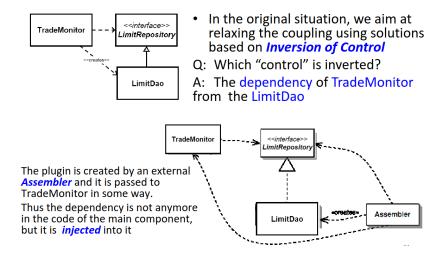
17.5 Dependency Injection

Dependency injection allows avoiding *hard-coded* dependencies (strong coupling) and changing them, and allows selection among multiple implementations of a given dependency interface at run time. It can be achieved through:

- 1. Setter injection
- 2. Constructor injection
- 3. (Interface injection)

Both **Service Locator** and **Dependency Injection** provide the desired decoupling, but let's compare the two solutions:

With service locator there is no IoC, since the desired component is obtained after request by the TradeMonitor to the Locator; this makes the application still depending on the locator.



♦ With dependency injection there is no explicit request: the component appears in the application class.

Inversion of control a bit harder to understand, however, it is easier to find dependencies of component if *Dependency Injection* is used

 $\begin{array}{c} \text{Check } constructors \text{ and } setters \\ \text{vs} \\ \text{Check } all \ invocations \text{ to Locator in the source code} \end{array}$

17.6 Designing Frameworks

Frameworks are normally implemented in an object- oriented language such as Java. It is important to learn to analyze a potential software family, identifying its possible common and variable aspects, and evaluating alternative framework architectures.

A possible idea is to start from a known divide-and-conquer algorithm such as:

Listing 17.1: Example pseudocode of a Divide-and-Conquer algorithm

```
function solve (Problem p) returns Solution {
   if isSimple(p)
      return simplySolve(p);
   else
      sp[] = decompose(p);
      for (i= 0; i < sp.length; i = i+1)
        sol[i] = solve(sp[i]);
      return combine(sol);
}</pre>
```

We can apply known techniques and patterns to **define** a *framework* for a **software family**. Instances of the defined framework, obtained by standard extension mechanism, will be concrete algorithms of the *family*.

17.6.1 Terminology

- ⋄ Frozen Spot
 - common (shared) aspect of the software family
- ♦ Hot Spot
 - variable aspect of the family
- $\diamond \ \, \mathbf{Template} \,\, \mathbf{method} \,\,$
 - concrete method of base (abstract) class implementing behavior common to all members of the family
- ♦ A hot spot is represented by a group of abstract *hook methods*.
- A template method calls a hook method to invoke a function that is specific to one family member —Inversion of Control—.
- ♦ A hot spot is realized in a framework as hot spot subsystem:

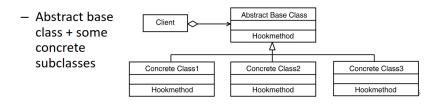


Figure 17.6: *Hotspot* implementation

- 1. The unification principle [Template Method Design Pattern]
 - i. It uses inheritance to implement the hot spot subsystem
 - ii. Both the template methods and hook methods are defined in the same abstract base class
 - iii. Hook methods are implemented in subclasses of the base class
- 2. The separation principle [Strategy Design Pattern]
 - i. It uses delegation to implement the hot spot subsystem
 - ii. The template methods are implemented in a concrete context class; the hook methods are defined in a separate abstract class and implemented in its subclasses
 - iii. The template methods delegate work to an instance of the subclass that implements the hook methods

17.6.2 Template Method design pattern

It is one of the behavioural pattern of the *Gang of Four*; Its intent is to define the skeleton of an algorithm in an operation, *deferring* some steps to subclasses: A **template method** belongs to an *abstract* class and it defines an algorithm in terms of *abstract* operations that subclasses **override** to provide *concrete behavior*.

Template methods call, among others, the following operations:

- 1. **concrete** operations of the abstract class \longrightarrow fixed parts of the algorithm
- 2. **primitive** operations, \longrightarrow abstract operations that subclasses have to implement
- 3. **hook** operations \longrightarrow provide default behavior that subclasses may override if necessary. A hook operation often does nothing by default.

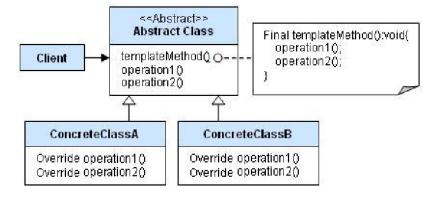


Figure 17.7: Template method

Applying Unification Principle

Let's consider the result of applying unification principle to the example code 17.1 provided before.

```
-- hotspots
function solve (Problem p) returns Solution { -- templatemethod
   if isSimple(p)
      return simplySolve(p);
   else
      sp[] = decompose(p);
    for (i= 0; i < sp.length; i = i+1)
      sol[i] = solve(sp[i]);
   return combine(sol);
}</pre>
```

rincinles

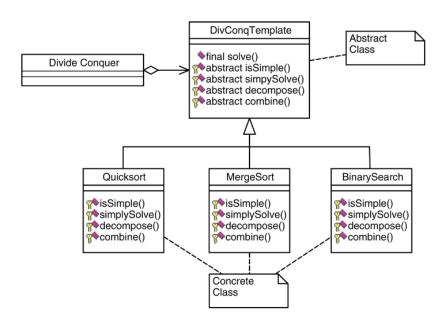


Figure 17.8: The generic schema of a Divide-and-Conquer Template Method designed Framework

17.6.3 Strategy design pattern

Another one of the behavioural pattern of the *Gang of Four*; Its intent is to allow to select (part of) an algorithm at runtime, leading the client to use an object implementing the interface and invoking methods of the interface for the hot spots of the algorithm.

Applying Separation Principle

```
public final class DivConqContext
                                      public DivConqContext (DivConqStrategy dc)
                                           this.dc = dc:
                                      public Solution solve (Problem p)
                                           Problem[] pp;
Code of the framework
                                           if (dc.isSimple(p)) { return dc.simplySolve(p); }
 (separation principle)
                                                                   { pp = dc.decompose(p);
                                           Solution[] ss = new Solution[pp.length];
                                           for (int i = 0; i < pp.length; i++)
The client delegates
                                               ss[i] = solve(pp[i]);
                                           return dc.combine(p, ss);
the hot spots to an
object implementing
                                      public void setAlgorithm (DivConqStrategy dc)
the strategy
                                           this.dc = dc:
                                      private DivConqStrategy dc;
The implementations
of DivCongStrategy are
similar to the previous
                                                            Fig. 8. Strategy context class implementation
case
                                 abstract public class DivConqStrategy
                                     abstract public boolean isSimple (Problem p);
abstract public Solution simplySolve (Problem p);
abstract public Problem[] decompose (Problem p);
abstract public Solution combine(Problem p, Solution[] ss);
```

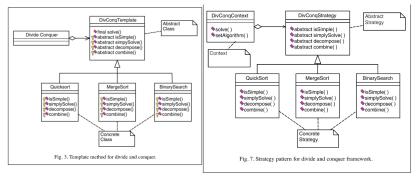
Figure 17.9: Result of applying the Separation principle on the example code

17.7 Development by generalization

Recalling what said earlier, we try to address:

Learning to analyze a potential software **family**, identifying its possible common and variable aspects, and evaluating alternative framework architectures. Framework design involves incrementally **evolving** a design rather than discovering it in one single step

Where the *evolution* consists of examining **existing designs** for family members, identifying the **frozen** and **hot spots** of the family, and ultimately **generalizing** the program structure to enable *code reusing* for frozen spots and multiple *different implementations* for each hot spot.



- The two approaches differ in the coupling between client and chosen algorithm
- With Strategy, the coupling is determined by dependency (setter) injection, and could change at runtime

Figure 17.10: Comparison between the two pattern's schemas

We will consider an example based on binary tree traversals, and discuss each generalization step.

17.7.1 Identifying Frozen and Hot spots

Frozen Spots, which are fixed for the whole family:

- 1. The structure of the tree, as defined by the BinTree hierarchy
- 2. A traversal accesses every element of the tree once, but it can stop before completing
- 3. A traversal performs one or more visit actions accessing an element of the tree meaning that there may be different and multiple actions after visiting a node, since it may represent the end of a left subtree visit, a right subtree visit or a root.

Let's identify possible **Hot Spots**, which have to be fixed in each element of the family.

- 1. Variability in the visit operation's action: a function of the current node's value and the accumulated result
- 2. Variability in **ordering** of the visit *action* with respect to subtree traversals; Should support *preorder*, *postorder*, *in-order*, and their combination.
- 3. Variability in the **tree navigation** technique. Should support any access order. not only left-to-right, depth-first, total traversals

17.8 Visitor Pattern

The ${f Visitor}$ pattern guarantees separation between algorithm and data structure.

The data structure can be made of different types of components (*ConcreteElements*), and each component implements an accept(Visitor) method. The Visitor defines one visit method for each type, including the navigation logic in itself. At each step, the correct visit method is selected by overloading.

```
public interface BinTreeVisitor
                    abstract void visit(Node t);
                    abstract void visit(Nil t);
 abstract public class BinTree
      public void setValue(Object v) { }
                                                                               // mutators
       public void setLeft(BinTree 1) { }
public void setRight(BinTree r) { }
                                                                                    default
      public void setRight(BinIree r) { }
abstract public void accept(BinTreeVisitor v); // accept Visitor
public Object getValue() { return null; } // accessors
public BinTree getLeft() { return null; } // default
public BinTree getRight() { return null; }
public class Node extends BinTree
      public Node(Object v, BinTree 1, BinTree r)
{  value = v; left = 1; right = r; }
       public void setValue(Object v)
public void setLeft(BinTree 1)
                                                            { value = v; } { left = 1; }
       public void setRight(BinTree r) { right = r; }
       // accept a Visitor object
       // accept a visitor object
public void accept(BinTreeVisitor v) { v.visit(this); }
public Object getValue() { return value; } // access
public BinTree getLeft() { return left; }
public BinTree getRight() { return right; }
private Object value; // instance data
                                                                                        // accessors
       private BinTree left, right;
public class Nil extends BinTree
      private Nil() { } // private to require use of getNil()
// accept a Visitor object
       public void accept(BinTreeVisitor v) { v.visit(this); }
       static public BinTree getNil() { return theNil; } // Singleton static public BinTree theNil = new Nil();
```

Figure 17.11: Visitor Pattern applied to the BinTree visit

Even if in the *Visitor* pattern, as in the *Template Method* pattern, an abstract class is defined and later implemented by subclasses which provide concrete behaviour, in the *Visitor* pattern such classes are *intended* to be used directly by *clients*, while in the *Template Method* pattern they are *intended* to be called by the *Frozen Spots* inside the abstract class itself, not by *clients*.

Java Memory Model

A **memory model** for *multithreaded* systems specifies how mem actions in a program will appear to execute to the programmer, i.e. —more specifically— which value each read of a memory location may return.

Every hardware and software interface of a system that admits multithreaded access to shared memory requires a memory model. such model determines the transformations that the system can apply to a program

In the case of high-level programming languages such as Java the memory model determines

- 1. the transformations the compiler may apply to a program when **producing bytecode**
- 2. the transformations a VIrtual-Machine may apply to bytecode when **producing native code**
- 3. the **optimizations** that hardware may perform on the native

Besides, the model also impacts the programmer, since such transformations determine the possible outcomes of a program.

Without a well defined memory model for a programming language, it is impossible to known what the legal results are for a program in such language.

When we programming "correctly" in Java, using volatile keywords and related constructs, we can however —in some sense—ignore the memory model

Memory Hierarchy In modern architectures memory is stratified ranging from mass memory (hard disks) to CPU registers, passing through different cache levels (L1,L2,L3), obtaining a memory hierarchy; depending on CPU architectures, cache levels may be shared or not among cores.

18.1 Java Memory Model

For incorretly synchronized programs, the behaviour is *bounded* by a well-defined notion of **causality**, so the semantics are *not* completely undefined as they were in the early (pre Java 5 - 2004) versions of the memory model.

The causality constraints are *strong enough* to *respect* the **safety** and **security properties** of java, and *weak enough* to *allow* standard compiler and hardware **optimizations**.

18.1.1 Runtime Data Areas

Local -primitive type- variables of methods are allocated on thread stacks, and cannot be accessed by other threads; Objects are instead allocated on the Heap.

For what concerns the distribution of data in Java, it may be spread orthogonally around the memory hierarchy, i.e. anything can go anywhere.

This leads to two key issues:

- 1. Visibility of variable updates
- 2.

(...)

18.2 volatile modifier

volatile is a modifier that can only be applied to fields of a class, and intuitively it declares that a field can be modified by multiple threads¹. The JMM guarantees that the write of a volatile variable is visible when it is read. An implementation should guarantee that the new value is flushed from the cache to the RAM, if a read happens "after" a write.

What does it mean that "a read happens after a write"?

This will be discussed later on in Sec 18.3, however, When threads do not use any synchronization mechanism, their behavior is described as the sequence of performed read/write actions, along with the results of the read operations; such sequence has a partial ordering whose legitimacy is checked by the JMM which aims to ensure that a read results in the actual last value written in this partial ordering.

Notice that volatile doesn't solve Data Races, which need synchronization mechanism; the typical example is incrementing a shared counter, which actually consists of three operations, read, increment the value read, and write it; such actions are **not** performed atomically², thus a second thread may read the "old" before the first one writes the updated one, resulting in only one incrementation instead of two.

Monitors

Monitors are the default Java synchronization mechanisms. Every object has a monitor exposing a lock which can be held only by one thread at a time. methods and ... with the synchronized modifier are guarded by the lock.

18.3 Describing thread behaviour

The JMM has no explicit global ordering of all actions by time consistent with each thread's perception of time, and has no global store.

Executions are instead described in terms of memory actions, partial orders on these actions, and a visibility function that assigns a write action to each read action.

1. Volatile read

- 2. Volatile write 3. lock
- 4. TODO

An execution of a single-threaded program fixes a total order \leq_{po} on its actions, called **program order**; while for a multi-threaded the program order consists in the union the program order of its threads, so it does not relate actions of different threads.

An execution of a multi-threaded program is sequentially consistent if there is a total order of its actions consistent with the program order —and such that each read has the value of the last write—.

For datarace-free³ mt-programs, the JMM guarantees that only **sequential consistent** executions are legal.

JMM has been designed to guarantee three things:

- 1. Promise for programmers
 - Sequential consistency must be sacrificed to allow optimizations, but it still holds for datarace-free program
- 2. Promise for security
 - Values should not appear "out of thin air", allowing for information leakage
- 3. Promise for compilers
 - HW and SW optimizations should be applied without violating (both) the first two requirements

TODO

int r1

Instr reordering may be performed as long as it guarantees sequential consistency in the single thread

TODO

¹Clearly incompatible with **final**

²So... which operations are atomic and which are not?

³Also called corretly or <u>well</u> synchronized programs

$$r1 = x;$$
 $y = r1;$ $r2 = y$ $x = r2$

x = y = 0 initially; can we obtain r1 == r2 == 42 at the end?

"Well no, but actually yes..."

In some situations the Runtime environment may guess that, at some point, x evaluates to 42: we say that 42 comes "out-of-thin-air". Then it checks by looking at the two thread instructions if it may happen that r1 = r2 = 42:

"Yes! So x actually really evaluates to 42! I guessed right! ©"

This was an accepted guess before the JMM introduced with Java 5 (2004), but currently such claims at runtime are forbidden.

18.3.1 Synchronization order

Each execution of a program is associated with a **synchronization order** \leq_{so} which is a total order over all synchronization actions satisfying:

- 1. Consistency with program order
- 2. Read to a volatile variable v returns the value of the write to v that is ordered last before the read by the synchronization order.

TODO

Formally Defining Data Races Two accesses x and y form a data race in an execution of a program if they are from different threads, they conflict, and they are not ordered by happens-before.

A program is said to be correctly synchronized or datarace-free if and only if all sequentially consistent executions of the program are free of data races.

The first requirement for the JMM is to ensure sequential consistency for correctly synchronized or datarace free programs

Programmers should not worry about code transformations for datarace-free programs. TODO

 $E = (P, A, \leq_{po}, \leq_{so}, W, V, \leq_{sw}, \leq_{hb})$ is a well-formed execution if:

- 1. Each read of a var x sees a write to x, and all reads and writes of volatile variables are volatile actions
- 2. Synchronization order is consistent with program order and mutual exclusion
- 3. The execution obeys intra-thread consistency
- 4. The execution obeys intra-thread and happens-before consistency on TODO

Now, which well-formed executions are legal? Legal executions are built iteratively: in each iterations, the JMM commits a set of memory actions; actions can be committed if they occur in some well-behaved...

A well-formed $E = (P, A, \leq_{po}, \leq_{so}, W, V, \leq_{sw}, \leq_{hb})$ is validated by *committing* actions in A; if all actions of A are committed, then E is legal. There must exists a sequence of subsets of a

$$C_0C_1 = A$$

and one $\{E_i\}$ of well-formed executions such that each E_i witnesses the actions in C_i

18.4 Intructions reordering

RUST

Rust is a general purpose, system programming language with a focus on safety, especially safe concurrency, supporting both functional and imperative paradigms. Its main goal is to ensure <u>safety</u> without penalizing <u>efficiency</u>. C/C++ provide more control but less safety, while Python/Haskell provide less control but more safety. Rust aims to get the best of both worlds, providing both control and safety.

Despite its syntax resemblance to C/C++, in a deeper sense Rust is closer to the ML family languages; in fact almost every part of a function body is an expression, include if-then-else constructs, which returns a value.

19.1 Key Points

Rust, similarly to C, compilates to **object code** for bare-metal performance, but it supports **memory safety**: programs can *dereference* only previously allocated pointers that have not been freed, and *out-of-bound* array accesses not allowed; Besides, the **overhead** introduced is very low, since it's the *compiler* which checks that memory safety rules are followed, and there's <u>no</u> garbage collection, so zero-cost abstraction in managing memory.

This is achieved through and advanced type system and three key concepts to prevent memory corruption:

- 1. Ownership
- 2. Borrowing
- 3. Lifetime

Again, Rust is designed to be **memory safe** even in the presence of concurrency, and guarantees the following properties **statically**, meaning that if the program *compiles* it will *never manifest a violation* of these properties:

- ♦ No null pointers
 - longrightarrow accessing a variable which does not hold a value
- ♦ No dangling pointers
 - longrightarrow Pointers to invalid memory location
 - Pointers to explicitly deallocated objects;
 - Pointers to locations beyond the end of an array;
 - Pointers to objects allocated on the stack;
- ♦ No double frees
 - longrightarrow A memory location in the heap is reclaimed twice
- ♦ No data races
 - longrightarrow unpredictable results in concurrent computations
- ♦ No iterator invalidation

19.2 null and Primitive types in Rust

A null value does **not** exist in Rust, so in some way it must address the problem of accessing a variable which does not hold a value.

Data values can only be initialized through a fixed set of forms, requiring their inputs to be already initialized, and if any branch of code fails to assign a value to the variable, we get a **compile time error**.

Static/global variables must be initialized at declaration time.

Nullable types, are managed with a generic Option<T>, playing the role of Haskell's Maybe or Java's Optional

```
enum std::option::Option<T> {
    None,
    Some(T)
}
```

19.2.1 Primitive Types

Listing 19.1: Rust primitive types

```
// Numeric types:
i8 / i16 / i32 / i64 / isize
u8 / u16 / u32 / u64 / usize
f32 / f64

bool
char // (4-byte unicode)
```

- ♦ **Type inference** for variables declarations with let
- ♦ No overloading for literals: type annotations to disambiguate
- ♦ **Tuples** like in Haskell
- \diamond **Arrays** with fixed length.

out-of-bound access is checked at runtime, but it's just a single comparison, its overhead is negligible

19.3 Memory Management

As usual, Rust uses a stack of activation records, and a heap for dynamically allocated data structures.

The user is forced to be aware of where the data are stored: there is no implicit boxing¹.

```
fn main() {
   let x = 3; // 'let' allocates a variable on the stack
   let y = Box::new(3); // y is a reference to 3 on the heap
   println!("x == y is {}", x == *y); // "x == y is true"
   }
```

To avoid the overhead of a Garbage collection mechanism and the possible subtle errors introduced a programmer to whom memory management is delegated, Rust provides $deterministic \ management \ of \ resources$, with very low overhead, using RAII ($\underline{Resource} \ \underline{Acquisition} \ \underline{Is} \ \underline{Initialization}$).

By default, Rust variables are **immutable**, and their usage is statically checked by the compiler. **mut** is used to declare a resource as mutable.

```
Listing 19.2: Compilation error
```

Listing 19.2: Compilation ✓

```
fn main() {
   let a: i32 = 0;
   a = a + 1;
   println!("a == {}", a);
}

fn main() {
   let mut a: i32 = 0;
   a = a + 1;
   println!("a == {}", a);
}
```

The Resource Acquisition Is Initialization (RAII) programming idiom states that Resource allocation is done during object initialization, by the constructor, while resource deallocation (release) is done during object destruction (specifically finalization), by the destructor.

19.3.1 Ownership

This approached is adopted in modern C++: small objects are allocated on *stack*, while larger resources are on the *heap* –or elsewhere– and are **owned** by an object on the *stack*, who is responsible for *releasing* the resource in its destructor.

Each resource has a **unique owner**.

Rust supports RAII in a strict way through an ownership system, based on the concepts of ownership and

¹Act of boxing an int in Integer, or extracting an int from Integer

```
01 - Every value is owned by a variable, identified by a name (possiby a path); 02 - Each value has at most one owner at a time; 03 - When the owner goes out-of-scope, the value is reclaimed / destroyed.
```

By default, an assignment between variables has a \underline{move} semantics: the ownership is moved from the RHS to the LHS

```
fn main() {
   let x = Box::new(3);
   let _y = x; // underscore to avoid 'unused' warning
   println!("x = {}", x); // error!
   }
```

For primitive types and types implementing the Copy trait, assignment has a copy semantics;

Here O2 is satisfied because a new value is created

```
fn main() {
    let x = 3;
    let _y = x;
    println!("x = {:?}", x); // OK
}

fn main() {
    let x = Option::Some(3);
    let _y = x;
    println!("x = {:?}", x); // OK
}
```

The same move semantics apply also for parameter passing: Any value passed to the function will be reclaimed when it returns, as the formal parameters gets out of scope; only returned values can survive.

tuples allow to return more

```
struct Dummy { a: i32, b: i32 }
fn foo() {
    let mut res = Box::new(Dummy {
        a: 0,
        b: 0
});
take(res);
println!("res.a = {}", res.a); \\ compilation error
}
fn take(arg: Box<Dummy>) {...}
```

When invoking take(res) the ownership of Dummy is moved from res to arg: when take() returns arg goes out of scope, so the resource gets freed automatically, making it no longer usable in println: this result in a compilation error. To use again the resource, we would have to make take return it, i.e. res = take(res).

This looks rather limiting, but allows to completely avoid the *Double-free* problem: memory is freed automatically when the owner goes out of scope, and by rule 02, each value has only one owner.

Rust does not allow explicit memory allocation

19.3.2 Borrowing

Since Ownership rules in some case may be too restrictive, **borrowing** is introduced: a resource can be *borrowed* from its owner via assignment or parameter passing. To guarantee memory safety, borrowing rules ensure that *aliasing*² and *mutability cannot coexist*.

Values can be passed

- 1. by immutable reference $\longrightarrow x = \&y$
- 2. by mutable reference $\longrightarrow x = \&mut y$
- 3. or by value $\longrightarrow x = y$

²Both the owner and the borrower can access the resource. More generally indicates that there are multiple ways to access a resource on the heap.

About mutable and immutable references:

- Borrowing
- ${\tt O1}$ At most one mutable reference to a resource can exist at any time
- 02 If there is a *mutable* reference, **no** *immutable* references can exist
- 03 If there is **no** *mutable* reference, **several** *immutable* references to the same resource can exist During borrowing, ownership is reduced or suspended:
- 04 Owner cannot free or mutate its resource while it is immutably borrowed
- 05 Owner cannot even read its resource while it is mutably borrowed

19.3.3 Strings

ring types

- 1. String does not require to know the length at compilation time, thus allocated on the heap.
- 2. &str size must be known statically, allocated on the stack.

Method String::from() allocates memory on the heap: it takes an argument of type &str and returns a String.

A String object has three components:

- 1. a reference to the heap location containing the character sequence
- 2. capacity (unsigned integer)
- 3. length (unsigned integer)

String does not implement Copy, thus assignment is subject to move semantics; assignment creates a copy of length, capacity and reference, but not of the char sequence in the heap.

19.3.4 Lifetime

A **lifetime** is a construct that the borrow checker uses to ensure the validity of the *borrowing rules* 19.3.2. Lifetimes are associated with each individual ownership and borrowing: a lifetime *begins* when the ownership starts, and *ends* when it is moved / destroyed, while for borrowings, it ends where the borrowed value is accessed the last time.

Lifetimes are mostly *inferred*, but sometimes they must be made explicit using the same syntax of generics. Using lifetimes, the compiler checks the validity of the rules of ownership and borrowing in the expected way; in particular, it ensures that –the *owner* of– every borrowed variable/reference has a lifetime that is longer than the borrower [B4,B5].

Borrowed (reference) formal parameters (arguments, return value) of a function have a lifetime, and if borrowed values are returned, each must have a lifetime.

The compiled tries to infer output lifetimes according to the following rules, but when not sufficient explicit lifetimes are necessary:

R1 - The lifetimes of the borrowed paramers are, by default, all distinct

- R2 If there is exactly **one input** lifetime, it will be assigned to **each output** lifetime
- R3 If a method has more than one input lifetime, but one of them is &self or &mut self, then this lifetime is assigned to all output lifetimes

```
fn longest(s1: &str, s2: &str) → &str { //does not compile
   if s1.len() > s2.len() { s1 }
   else { s2 }
}
```

Here the lifetime of the parameters depends on whether s1 or s2 is returned, so the compiler cannot infer the lifetime of the output parameters; hence, an **explicitly named lifetime** for input parameters is requires, as in the following snippet.

```
fn longest<'a>(s1: &'a str, s2: &'a str) \rightarrow &'a str { if s1.len() > s2.len() { s1 } else { s2 }
```

19.4 More on Types

19.4.1 Enums

```
enum RetInt {
    Fail(u32),
    Succ(u32)
}

fn foo_may_fail(arg: u32) → RetInt {
    let fail = false;
    let errno: u32;
    let result: u32;
    ...
    if fail {
        RetInt::Fail(errno)
    } else {
        RetInt::Succ(result)
    }
}
```

```
#[derive(Debug)] // needed to print
enum Tree<T> {
   Empty,
   Node(T, Box<Tree<T>>, Box<Tree<T>>)
fn main() {
   let tree = Tree::Node(
      42,
      Box::new(Tree::Node(
         0.
         Box::new(Tree::Empty),
         Box::new(Tree::Empty)
      )),
      Box::new(Tree::Empty));
   println!("{:?}", tree);
   //>Node(42, Node(0, Empty, Empty), Empty)
}
```

println!("{:?}", tree); indicates to print tree in "debug
mode".

19.4.2 Pattern Matching

```
let x = 5; // try others...
match x {
   1
                  => println!("one"),
   2
                  => println!("two"),
                  => println!("three or four"),
   3 | 4
                  => println!("five to ten"),
   5..=10
                  => println!("{}", e),
   e @ 11..=20
                  => println!("less than zero"),
   i32::MIN..=0
                  => println!("large"),
   21..
                  => println!("???"),
```

19.4.3 Classes

Rust is **not** Object Oriented and there is **no inheritance**, instead it pushes for composition over inheritance.

```
#[derive(Debug)]
struct Rectangle { // class
      width: u32, // instance variable
      height: u32,
impl Rectangle { // methods
      fn area(&self) \rightarrow u32 { // first argument is this
            self.width * self.height
            // self.width = 20; // <- illegal, self is immutable
fn main() {
      let rect1 = Rectangle {
            width: 30,
            height: 50,
         };
      println!(
      "The area of the rectangle is {} square pixels.", rect1.area()
  }
```

19.4.4 Traits

Traits are equivalent to *Type Classes* in Haskell and to *Concepts* in C++20, similar to Interfaces in Java. A trait can include *abstract* and *concrete* (default) **methods**, but <u>not</u> fields or variables. A struct can implement a trait

providing an implementation for at least its abstract methods

```
impl <TraitName > for <StructName > { ... }
```

The #[derive] clause can be used -if possible- to derive automatically an implementation of a trait.

Rust supports **bounded universal explicit polymorphism** with **generics**, as in Java, where bounds are one or more traits. Generic functions may have the generic type of parameter bound by one or more traits, so within such a function, the generic value can only be used through those traits, allowing for generic function to be **type-checked** when defined, as it happens in Java, unlike C++ templates.

• However, implementation of Rust generics uses *monomorphization* and is similar to typical implementation of C++ templates, where a separate copy of the code is generated for each instantiation, in contrast with the type erasure scheme of Java.

19.5 Smart Pointers

Smart pointers act as a pointer but with additional metadata and capabilities, and are typically structs, implementing Deref (*) and Drop (reclaiming when out of scope).

```
fn main() {
   let b = Box::new(5);
   println!("b = {}", b);
}
```

Box<T> Allow to store a data of type T on the heap, with no performance overhead. Deref (*) returns the value. Optional by coercion.

TODO

What does "Optional by coercion" mean?

Rc<T> supports immutable access to resource with reference counting. Method Rc::clone() doesn't clone! It simply returns a new reference, incrementing the counter, whose value can be obtained by Rc::strong_count; when the counter is 0 the resource is reclaimed.

RefCell<T> supports shared access to a mutable resource through the **interior mutability** pattern. It provides two methods borrow() and borrow_mut() which return a smart pointer (Ref<T> or RefMut<T>). RefCell<T> keeps track of how many Ref<T> and RefMut<T> are active, and panics if the ownership/borrowing rules are invalidated. Its implementation is single-threaded, and it is typically used with Rc<T> to allow multiple accesses.

Туре	Sharable?	Mutable?	Thread Safe?
&	yes *	no	no
&mut	no *	yes	no
Box	no	yes	no
Rc	yes	no	no
Arc	yes	no	yes
RefCell	yes **	yes	no
Mutex	yes, in Arc	yes	yes

^{*} but doesn't own contents, so lifetime restrictions.

Figure 19.1: Pointers comparison

19.6 Functional elements

Closures can capture non-local variables in three ways, corresponding to ownership, mutable and immutable borrowing; this is reflected in the trait they implement: FnOnce, FnMut and Fn. The trait implemented is inferred. With

^{**} while there is no mutable borrow

move before || FnOnce is enforced.

```
let greater_than_x = |y| y > x; // Parameters within ||
let vector = vec![1, 2, 3, 4, 5]; // stream-like
vector.iter()
    .map(|x| x + 1)
    .filter(|x| x % 2 == 0)
    .for_each(|x| println!("{}", x));
```

19.6.1 Race conditions

TODO Listen to lecture

19.6.2 Sync and Send

Send and Sync are two strongly related traits regarding multithreading: an error is signaled by the compiler if the ownership of a value *not* implementing Send is passed to another thread; for a value to be referenced by multiple threads, it has to implement Sync.

T
$$implements$$
 Send \Leftrightarrow &T $implements$ Sync (19.1)

vamnle

- \diamond Arc<T> is the thread-safe version of Rc<T> which implements Send and Sync
- ♦ Mutex<T> supports mutual exclusive access to a value via a lock. It is both Send and Sync, and typically wrapped in Arc

Python

Python is very concise and good for scripting. It is the most used general purpose language, and there are many nice Machine Learning libraries.

Its two key aspects are that it is **interpreted** (\neq compiled) and **dynamically typed**.

Aside from these two main aspects, we can discuss a few others: even if not as much as Java, it's **object** oriented; Python supports both **imperative** and **functional** paradigms. Python **Iterators** can be associated with **Lists** in Haskell and **Streams** in Java. Other Python features are:

- ♦ Powerful subscripting (slicing)
- ♦ Higher-order functions
- ♦ Flexible signatures, which compensate the lack of complex polymorphism
- ♦ Java-like exceptions
- ♦ (bad) Multithreading support

Let's discuss how Python addresses typing:

- 1. Variables come into existence when first assigned to
- 2. Variables are not typed, but Values are!
- 3. A variable can refer to an object of any type
- 4. It is **Strongly typed** in the sense that the *value type* does not change in unexpected ways
- 5. It is **Type-safe** since no conversion or operation can be applied to values of the **wrong** type

Variables come into existence when first assigned and a variable can refer to an object of any type, besides all types are (almost) treated the same way. Even if this allows for concise syntax and intuitive code writing, it also implies a main drawback: **type errors** are only caught at *runtime*.

20.1 Some Python aspects

- ♦ **Indentation** matters, and is used opposed to brackets {}
- ♦ A variable is created when some value is assigned to it
- Assignments in Python do not create a copy Even for Integers!
- ♦ Objects are deleted by the garbage collector once they become unreachable
 - CPython uses reference counting along with Mark & Sweep for garbage collection

20.2 Data Types and operators

Integers are unbounded, while Floats are represented with 64 bits.

There are no logical symbols, the operators are and, or, not.

Strings can be enclosed in '', "", """ """, with the third that allows multiline strings (cool!).