Description of Imputation Methodology

Section 1 - Overview

This R Markdown document will demonstrate the calculation of imputation for each of the below measures:

- Available Stay Unit Nights
- $\bullet \ \ Occupied_Nights$
- Guest Nights
- Guest Arrivals
- Domestic_Nights (and by extension, International Nights, which is Guest_Nights Domestic_Nights)

We will first inspect the first 6 rows of the data at the start of the imputation process. Where no data for a particular measure is provided, this is indicated by NA. For these properties, there is a mix of responses and non responses for each the data fields shown (non imputed values).

The imputation process will compute an imputation to fill each NA with an imputed value, in the order of columns as per the table below (left to right). The monthly capacity of each property is always known. This is done by computing an operational ratio, and multiplying the ratio with the value of the field preceding the field for which an imputation is being computed.

For example, to calculate an imputation for available_stay_unit_nights for property 8440, we first calculate an operational ratio given by non-imputed data from donor properties, and multiply that ratio with the value of the field monthly_capacity for property 8440.

This hotel is also missing data for occupied_nights and so this field will need to be computed. As per the previous imputation, an operational ratio is calculated and is multiplied with the imputed value of the preceding field, available_stay_unit_nights

table_properties_head

id	rto	property type	monthly capacity	available stay unit nights	occupied nights	guest nights	guest arrivals	domestic nights	international nights
1706	Queenstown RTO	Hotels (over 20 units)	660	660	369	727	NA	727	0
8440	Dunedin RTO	Hotels (over 20 units)	720	NA	NA	NA	NA	NA	NA
434	Auckland RTO	Hotels (over 20 units)	750	750	632	NA	NA	NA	NA
7054	Nelson Tasman RTO	Hotels (over 20 units)	780	0	0	0	0	0	0
5806	Wairarapa RTO	Hotels (over 20 units)	840	840	685	1384	810	1350	34
731	Rotorua RTO	Hotels (over 20 units)	900	900	366	920	240	920	0

Section 2 - Outlier Processing

We define outliers as unusual values that have the potential to materially influence regional and national results. Values that we considered to be plausible but highly influential were left in the data but are not included in the imputation process for other properties. We currently recognise two types of outliers:

- Managed isolation and quarantine facilities: Because of the short-term nature of the isolation stay, these hotels are included in the counts of available stay-units, occupied nights, guest nights, and guest arrivals.
- Properties with extreme (high/low) occupancy rates: We calculate the z-score for occupancy observations within each property type and multiply this number by 1000 * share of capacity for that property within its type. This provided a measure of the relative influence of a property's performance on the results. Those with a value greater than 10 are flagged as outliers.

2.1 - Calculate Standard Deviation of Occupancy Rate for Each Property Group

```
properties = properties %>%
  mutate(propert_occupancy_rate = ifelse(
    flagged_as_a_response == 1,
    non_imputed_occupied_nights/non_imputed_available_stay_unit_nights,
    NA))

group_sd_occupancy_rates = properties %>%
  group_by(property_type) %>%
  summarise(sd_occupancy_rate = sd(propert_occupancy_rate, na.rm = T))
```

The table below shows the standard deviations of occupancy rates for each property group.

kbl_df

property_type	sd_occupancy_rate
Backpackers (over 20 units)	0.20
Holiday parks and campgrounds	0.18
Hotels (over 20 units)	0.20
Motels and serviced apartments (6-20 units)	0.22
Motels and serviced apartments (over 20 units)	0.20
Other accommodation (over 5 units)	0.24

Merge properties table with the above standard deviation table.

```
properties = left_join(
    x = properties,
    y = group_sd_occupancy_rates,
    by = c('property_type' = 'property_type')
)
```

2.2 - Calculate Aggregate Measures for Each Property Group

Calculate the sum of available_stay_unit_nights and occupied_nights for each property group.

```
# Statistics for Target Population
target_pop_stats = properties_all %>%
group_by(property_type) %>%
summarise(
    # Total number of available stay unit nights across each property type
    stats_sum_available_stay_unit_nights = sum(imputed_available_stay_unit_nights, na.rm = T),

# Total number of occupied nights across each property type
    stats_sum_occupied_stay_unit_nights = sum(imputed_occupied_nights, na.rm = T)
    ) %>%

# Calculate occupancy rate across each property type
mutate(stats_occupancy_rate = stats_sum_occupied_stay_unit_nights / stats_sum_available_stay_unit_nights)
```

kbl_df

property type	stats sum available stay unit nights	stats sum occupied stay unit nights	stats occupancy rate
Backpackers (over 20 units)	410179	127089	0.31
Holiday parks and campgrounds	1145807	243264	0.21
Hotels (over 20 units)	827962	443085	0.54
Motels and serviced apartments (6-20 units)	375192	215845	0.58
Motels and serviced apartments (over 20 units)	323278	187178	0.58
Other accommodation (over 5 units)	89857	27952	0.31

```
# Merge with target pop stats to get the group measures
properties = left_join(
    x = properties,
    y = target_pop_stats,
    by = c("property_type" = "property_type")
)
```

2.3 - Calculate Z-Score

```
# Calculate Z-score
properties = properties %>%
mutate(
    z_score = abs(
        (non_imputed_occupied_nights / non_imputed_available_stay_unit_nights) - stats_occupancy_rate
    )
    //
    sd_occupancy_rate
    *
        (imputed_available_stay_unit_nights / stats_sum_available_stay_unit_nights)
    * 1000
)
```

2.4 - Remove Properties based on z-score

```
properties = properties %>%
  mutate(outlier_excluded = ifelse(z_score > 10, 'excluded', 'not_excluded'))
```

The below table shows two hotel properties in which one has been determined to be an outlier based on its occupancy rate.

kbl_df

property type	property	stats occupancy	z score	outlier excluded	non imputed	non imputed
	occupancy rate	rate			occupied nights	available stay
						unit nights
Hotels (over 20	0.14	0.54	10.11	excluded	610	4320
units)						
Hotels (over 20	0.60	0.54	3.22	not_excluded	5037	8400
units)						

Section 3 - Imputation Process

3.1 Derive Donor Property Set

This step involves finding the set of other comparable properties for each property. The set of comparable properties will consist of either

- properties sharing the same property type within the same RTO, or
- properties sharing the same property type nationwide.

The former is used when there are sufficient respondents who have submitted data for a given attribute. If there are insufficient respondents, data from all respondents across the country sharing the same property type is used for imputation. This is done to protect the confidentiality of respondents, and also to increase the diversity of responses and to reduce the risk of one or two properties exerting undue influence on the imputation calculation.

We define property A as a property for which an imputation calculation is required. We also define the donor property set as the set of properties which will 'donate' or provide values for the calculation of the imputation for property A.

When calculating the imputation for any given field, the donor property set is determined by:

- Property Type
- RTO If there are three or more active and responding properties of the same type within the same RTO (including property A), then the donor set will consist of these properties (excluding property A); otherwise the donor set will consist of all properties of the same property type across New Zealand.
- Whether a property has submitted data for a specified field. This field depends on the field which is being imputed. For example, when calculating the imputation for the field Available_Stay_Unit_Nights for hotels in the Auckland RTO, the donor property set consists of all hotels in Auckland RTO which have submitted data for Occupied_Nights. If there are less than three properties which fulfill this criteria, then the donor property set would instead consist of hotels across New Zealand.

Field to be imputed	Field to determine donor
Available_Stay_Unit_Nights Occupied_Nights Guest_Nights Guest_Arrivals Domestic_Nights	Occupied_Nights Occupied_Nights Guest_Arrivals Guest_Arrivals Domestic Nights

The following code examples will demonstrate the process for calculating the ratio which is used to impute the field $Occupied_Nights$; This code is then generalised to apply for all of the imputation calculations.

We first need to count the number of properties which fulfill the three matching criteria as defined above.

rto	property_type	count
Bay of Plenty RTO	Backpackers (over 20 units)	3
Bay of Plenty RTO	Holiday parks and campgrounds	7
Bay of Plenty RTO	Hotels (over 20 units)	0
Bay of Plenty RTO	Motels and serviced apartments (6-20 units)	17
Bay of Plenty RTO	Motels and serviced apartments (over 20 units)	5
Bay of Plenty RTO	Other accommodation (over 5 units)	1

We then proceed to name the donor property set. Based on the counts shown above, we must confidentialise the rto + property groups which have less than three properties. These groups will have group type donor_set_type = 'property_type' as they consist of properties from across the country sharing the same property type. Groups which have counts of three or greater will consist of properties only within the same rto, and so have donor_set_type = rto_and_property_type

```
# Determine comp set type and name

df_grouped = df_grouped %>%
  mutate(
    donor_set_type = ifelse(
    count >= 3,
    "rto_and_property_type",
    "property_type"),

    donor_set_name = ifelse(
    count >= 3,
    paste(rto, property_type, sep = ""),
    property_type)
)
```

table_df_grouped

rto	property_type	count	donor_set_type	donor_set_name
Bay of Plenty RTO	Backpackers (over 20 units)	3	rto_and_property_type	Bay of Plenty RTOBackpackers (over 20 units)
Bay of Plenty RTO	Holiday parks and campgrounds	7	rto_and_property_type	Bay of Plenty RTOHoliday parks and campgrounds
Bay of Plenty RTO	Hotels (over 20 units)	0	property_type	Hotels (over 20 units)
Bay of Plenty RTO	Motels and serviced apartments (6-20 units)	17	rto_and_property_type	Bay of Plenty RTOMotels and serviced apartments (6-20 units)
Bay of Plenty RTO	Motels and serviced apartments (over 20 units)	5	rto_and_property_type	Bay of Plenty RTOMotels and serviced apartments (over 20 units)
Bay of Plenty RTO	Other accommodation (over 5 units)	1	property_type	Other accommodation (over 5 units)

3.2 - Compute Operational Ratios for each possible donor group

For each donor_set_name, we will compute an operational ratio which will be used as an imputation ratio for all accommodation providers within this group (where an imputation is required).

Example: Available Stay Unit Nights: In this example, the occupancy rate is being calculated. This operational ratio will be used to impute the available stay unit nights for any properties in this group where data has not been provided for this field.

The numerator represents the total number of occupied nights and the denominator represents the total number of available stay unit nights across all the properties belonging to donor_set_name.

$$r = \frac{\sum_{i \in \{i || available_stay_unit_nights_i > 0\}} available_stay_unit_nights_i}{\sum_{i \in \{i || available_stay_unit_nights_i > 0\}} monthly_capacity_i}$$

where i represents the i-th donor property, and N is the total number of properties within the donor property set.

```
df_grouped = properties%>%
  # Filter out properties with outlying occupancy rates (z-score > 10)
  filter(outlier excluded != 'excluded') %>%
 group_by_at(c("rto", "property_type")) %>%
  summarise(
    # Count properties with at least one occupied night - This is used to determine 'donor set type'
    count = sum(non imputed available stay unit nights > 0, na.rm = T),
    # Numerator
      sum non imputed available stay unit nights = sum(non imputed available stay unit nights[
        (non imputed available stay unit nights > 0) & (non imputed occupied nights > 0)
       ], na.rm = T),
    # Denominator
    sum_monthly_capacity = sum(monthly_capacity[
      (non_imputed_available_stay_unit_nights > 0) & (non_imputed_occupied_nights > 0)
     ], na.rm = T)
    )%>%
  ungroup()
```

```
# Determine comp set type and name
df_grouped = df_grouped %>%
  mutate(
    donor_set_type = ifelse(
      count \geq 3,
      "rto_and_property_type",
      "property_type"),
   donor_set_name = ifelse(
      count \geq 3,
     paste(rto, property_type, sep = ""),
      property_type)
# For donor_set_type == 'property_type'
aggregations_comp_set_property.df <- df_grouped %>%
  group_by(donor_set_name = property_type) %>%
  summarise(
    sum_non_imputed_available_stay_unit_nights = sum(sum_non_imputed_available_stay_unit_nights),
   sum_monthly_capacity = sum(sum_monthly_capacity)
aggregations_comp_set_property.df
## # A tibble: 6 x 3
   donor_set_name
                                    sum_non_imputed_available_st~ sum_monthly_capa~
   <chr>
                                                             <dbl>
                                                                               <dbl>
## 1 Backpackers (over 20 units)
                                                           133735
                                                                              145350
## 2 Holiday parks and campgrounds
                                                           592883
                                                                              712740
## 3 Hotels (over 20 units)
                                                           453360
                                                                              479790
## 4 Motels and serviced apartment~
                                                           148101
                                                                              157380
## 5 Motels and serviced apartment~
                                                           133531
                                                                              144330
## 6 Other accommodation (over 5 u~
                                                             27428
                                                                               35250
imputation_per_property_type.df = inner_join(
 x = df_grouped %>% select(donor_set_name, donor_set_type, rto, property_type, count),
```

```
y = aggregations_comp_set_property.df,
  by = c("donor set name" = "donor set name")
)
# For donor set type == 'rto and property type'
imputation per rto and property type.df = df grouped %>%
  filter(donor set type == "rto and property type")
imputation schedule available stay unit nights = rbind(imputation per property type.df, imputation per rto and property type.df)
# Compute Ratio
num = imputation_schedule_available_stay_unit_nights$sum_non_imputed_available_stay_unit_nights
den = imputation_schedule_available_stay_unit_nights$sum_monthly_capacity
imputation_schedule_available_stay_unit_nights$ratio_available_stay_unit_nights = num / den
imputation_schedule_available_stay_unit_nights %>%
 filter(count <3)</pre>
## # A tibble: 51 x 8
      donor_set_name donor_set_type rto property_type count sum_non_imputed~
##
      <chr>
                     <chr>
                                    <chr> <chr>
                                                        <int>
                                                                         <dbl>
## 1 Other accommo~ property_type Bay ~ Other accomm~
                                                           1
                                                                         27428
## 2 Backpackers (~ property_type Cent~ Backpackers ~
                                                                        133735
## 3 Hotels (over ~ property_type Cent~ Hotels (over~
                                                           1
                                                                        453360
## 4 Backpackers (~ property type Clut~ Backpackers ~
                                                           1
                                                                       133735
## 5 Holiday parks~ property type Clut~ Holiday park~
                                                                        592883
                                                           1
## 6 Backpackers (~ property type Coro~ Backpackers ~
                                                                       133735
## 7 Motels and se~ property_type Coro~ Motels and s~
                                                                       133531
## 8 Holiday parks~ property type Dune~ Holiday park~
                                                                        592883
## 9 Other accommo~ property_type Dune~ Other accomm~
                                                                        27428
## 10 Backpackers (~ property type East~ Backpackers ~
                                                                        133735
## # ... with 41 more rows, and 2 more variables: sum monthly capacity <dbl>,
## # ratio_available_stay_unit_nights <dbl>
```

table_imputation_schedule_available_stay_unit_nights_bop

donor set name	donor set type	rto	property_type	count of properties	sum available stay	donor set name	ratio occupancy
Other accommodation	property_type	Bay of Plenty RTO	Other accommodation	1	27428	35250	0.7780993
(over 5 units)			(over 5 units)				
Bay of Plenty	rto_and_property_type	Bay of Plenty RTO	Backpackers (over 20	3	4688	5220	0.8980843
RTOBackpackers (over 20			units)				
units)							
Bay of Plenty	rto_and_property_type	Bay of Plenty RTO	Holiday parks and	7	36053	40860	0.8823544
RTOHoliday parks and			campgrounds				
campgrounds							
Bay of Plenty RTOMotels	rto_and_property_type	Bay of Plenty RTO	Motels and serviced	17	5977	6720	0.8894345
and serviced apartments			apartments (6-20 units)				
(6-20 units)							
Bay of Plenty RTOMotels	rto_and_property_type	Bay of Plenty RTO	Motels and serviced	5	4077	4920	0.8286585
and serviced apartments			apartments (over 20				
(over 20 units)			units)				

The formula to derive the operational ratio for each imputation calculation is given in the table below.

Field	Description	Formula
Available Stay Unit Nights	Stay units made available for short-term guests multiplied by the number of days of availability. This includes occupied and unoccupied stay units, and those located for managed isolation.	$r = \frac{\sum_{i \in \{i \mid available_stay_unit_nights_i > 0\}} available_stay_unit_nights_i}{\sum_{i \in \{i \mid available_stay_unit_nights_i > 0\}} monthly_capacity_i}$
Occupied Nights	Stay units occupied by short-term guests during the month.	$r = \frac{\sum_{i \in \{i occupied_nights_i > 0\}} occupied_nights_i}{\sum_{i \in \{i occupied_nights_i > 0\}} available_stay_unit_nights_i}$
Guest Nights	Cumulative number of nights spent short-term guests. Equivalent to one guest spending one night in a property. This includes managed isolation guests.	$r = \frac{\sum_{i \in \{i guest_nights_i > 0\}} guest_nights_i}{\sum_{i \in \{i guest_nights_i > 0\}} occupied_nights_i}$
Guest Arrivals	Number of individual short-term guests checking in during the reference month. This includes managed isolation guests.	$r = \frac{\sum_{i \in \{i guest_arrivals_i > 0\}} guest_arrivals_i}{\sum_{i \in \{i guest_arrivals_i > 0\}} guest_nights_i}$
Domestic Nights	Nights spent by guests that were identified as being from New Zealand.	$r = \frac{\sum_{i \in \{i domestic_nights_i \geq 0\}} domestic_nights_i}{\sum_{i \in \{i domestic_nights_i \geq 0\}} guest_nights_i}$

We parameterise the The below function computes an imputation schedule for a particular imputation measure.

```
compute imputation schedule <- function(</pre>
  df,
 numerator field,
 denominator field,
 imputation name,
  imputation_comp_set_field
  ){
  df_grouped = df %>%
    # filter_at(vars(numerator_field), ~ .>0) %>%
   group_by_at(c("rto", "property_type")) %>%
    summarise (
      count = interp(
       ~sum((numerator_var > 0) & (imputation_comp_set_var > 0), na.rm = T),
       numerator var = as.name(numerator field),
        imputation_comp_set_var = as.name(imputation_comp_set_field)
       ),
     numerator = interp(~sum(numerator_var[(numerator_var > 0) & (imputation_comp_set_var > 0)], na.rm = T),
                         imputation_comp_set_var = as.name(imputation_comp_set_field),
                         numerator var = as.name(numerator field)
                         ),
      denominator = interp(~sum(denominator_var[(numerator_var > 0) & (imputation_comp_set_var > 0)], na.rm = T),
                           imputation_comp_set_var = as.name(imputation_comp_set_field),
                           denominator_var = as.name(denominator_field),
                           numerator_var = as.name(numerator_field))
      ) %>% ungroup()
  # Determine comp set type and name
  df_grouped = df_grouped %>%
   mutate(
      donor set type = ifelse(
       count \geq 3.
        "rto and property type",
        "property_type"),
```

```
donor_set_name = ifelse(
      count >= 3,
      paste(rto, property_type, sep = ""),
     property_type)
aggregations_comp_set_property.df <- df_grouped %>%
group_by(donor_set_name = property_type) %>%
summarise(
  numerator = sum(numerator),
 denominator = sum(denominator)
)
imputation_per_property_type.df = inner_join(
  x = df_grouped %>%
    select(donor_set_name, donor_set_type, rto, property_type, count),
  y = aggregations_comp_set_property.df,
  by = c("donor_set_name" = "donor_set_name")
imputation_per_rto_and_property_type.df = df_grouped %>%
  filter(donor_set_type == "rto_and_property_type")
# Row bind the imputation schedules for both 'rto and property type' and either 'rtop' or 'property type'
imputation_schedule = rbind(imputation_per_property_type.df, imputation_per_rto_and_property_type.df)
imputation_schedule = imputation_schedule %>%
  rename_at("donor_set_type", ~paste(imputation_name, "donor_set_type", sep = "_")) %>%
  rename_at("donor_set_name", ~paste(imputation_name, "donor_set_name", sep = "_")) %>%
  rename at("count", ~ paste(imputation name, "imputation donors count", "count", sep = " ")) %>%
# Calculate Ratio
mutate(ratio = numerator/denominator) %>%
# Rename Columns
rename_at("numerator", ~ paste(imputation_name, "sum", numerator_field, sep = "_")) %>%
rename_at("denominator", ~ paste(imputation_name, "sum", denominator_field, sep = "_")) %>%
rename_at("ratio", ~paste(imputation_name, "ratio", sep = "_"))
```

```
return(imputation_schedule)
}
```

Our five imputation schedules are as follows. Note that in the imputation for available stay unit nights and occupied nights, properties with outlying occupancy rates are excluded.

```
imputation_available_stay_unit_nights = compute_imputation_schedule(
 df = properties %>% filter(outlier_excluded != 'excluded'), # Exclude properties with z-score > 10
 numerator_field = "non_imputed_available_stay_unit_nights",
  denominator field = "monthly capacity",
  imputation name = "available stay unit nights",
 imputation_comp_set_field = "non_imputed_occupied_nights"
imputation_occupied_nights = compute_imputation_schedule(
  df = properties %>% filter(outlier excluded != 'excluded'),
 numerator_field = "non_imputed_occupied_nights",
  denominator_field = "non_imputed_available_stay_unit_nights",
  imputation_name = "occupied_nights",
  imputation_comp_set_field = "non_imputed_occupied_nights"
imputation_guest_nights = compute_imputation_schedule(
  df = properties,
 numerator field = "non imputed guest nights",
  denominator field = "non imputed occupied nights",
 imputation_name = "guest_nights",
 imputation comp set field = "non imputed guest arrivals"
imputation_guest_arrivals = compute_imputation_schedule(
  df = properties,
 numerator_field = "non_imputed_guest_arrivals",
  denominator field = "non imputed guest nights",
  imputation_name = "guest_arrivals",
  imputation_comp_set_field = "non_imputed_guest_arrivals"
```

```
imputation_domestic_nights = compute_imputation_schedule(
    df = properties,
    numerator_field = "non_imputed_domestic",
    denominator_field = "non_imputed_guest_nights",
    imputation_name = "domestic_nights",
    imputation_comp_set_field = "non_imputed_domestic"
)
```

3.3 - Calculating the Imputation

The below code demonstrates how the operational ratio is used to compute an imputation for guest_nights. In this scenario, property 1318 is a property in the Bay of Plenty RTO with property type Holiday parks and campgrounds. We look up the property and the rto in the respective imputation schedule for occupied_nights. Since there are 6 other properties with the same property type within the Bay of Plenty RTO, the set of donors will consist of those 6 properties.

table_1318

fresh_id	rto	property type	occupied nights	guest nights
1318	Bay of Plenty RTO	Holiday parks and campgrounds	3150	NA

To compute the imputed occupied nights, we simply multiply the operational ratio with with the occupied_nights of property 1318:

$$guest_nights_{1318} = r \times occupied_nights_{1318}$$

where

$$r = \frac{\sum_{i \in \{i | guest_nights_i > 0\}} guest_nights_i}{\sum_{i \in \{i | guest_nights_i > 0\}} occupied_nights_i}$$

where i represents the i-th donor property, and N is the total number of properties within the donor property set which comprises of (Holiday parks and camp-grounds in Bay of Plenty.

```
filtered.df = properties%>%
  filter(fresh_id == 1318) %>%
  select(fresh_id, rto, property_type, non_imputed_occupied_nights, non_imputed_guest_nights)

# Lookup the rto and property type in the imputation comp set table
filtered.df = left_join(
  x = filtered.df,
  y = imputation_guest_nights,
  by = c("rto", "property_type")
)
```

```
# Multiply the ratio by the respective field
filtered.df$imputed_guest_nights = filtered.df$guest_nights_ratio * filtered.df$non_imputed_occupied_nights
# Final Imputed Value
round(filtered.df$imputed_guest_nights, 0)
```

[1] 8231

table_1318_imputed

fresh id	rto	property	occupied	guest nights	imputed						
		type	nights		donor set	donor set	imputation	sum guest	sum	ratio	guest nights
					name	type	donors count	nights	occupied		
							count		nights		
1318	Bay of	Holiday	3150	NA	Bay of	rto_and_prop	erty_type 5	12414	4751	2.612924	8230.709
	Plenty RTO	parks and			Plenty						
		camp-			RTOHoliday						
		grounds			parks and						
					camp-						
					grounds						