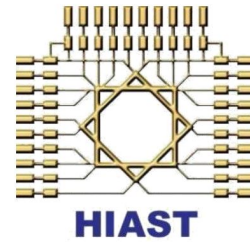


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Using Genetic Algorithms to Find Approximations for the Minimum Vertex Cover Problem

Keywords: genetic algorithms, NP-complete, combinatorial optimization,
non-deterministic algorithms, approximation algorithms, minimum vertex cover.

Author: *Farouk Hjabo*
Academic Supervisor: *Dr. Said Desouki*
General Supervisor: *Dr. Kadan Aljoumaa*
Langauge Supervisor: *Mr. Fahmi Alammareen*

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Abstract

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“It is not the strongest of the species that survives, nor the most intelligent, but the one most responsive to change.”

— Charles Darwin

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1 Introduction

Once the NP-hardness of a combinatorial optimization problem is established, the search for an optimal solution is abandoned. The goal then becomes one of finding a good heuristic, i.e. a polynomial running time algorithm that can find solutions close to the optimal. In most cases, traditional heuristics are problem dependent; a heuristic is tailored to the specific problem it is trying to solve.

In this paper, we present an alternative approach that uses genetic algorithms as a generalized heuristic for solving NP-hard combinatorial optimization problems. The application of a genetic algorithm is demonstrated here for the *minimum vertex cover* problem. These algorithms have been successfully applied to a broad range of problems. This wide range can be tackled by genetic algorithms mainly due to the fact that they work with an encoding of the domain rather than with the problem domain itself.

2 Genetic Algorithms

2.1 The Intuition Behind GAs

Genetic Algorithms (GAs) [3] are population based search algorithms, where by repeated use of genetic operations, such as ***mutation***, ***selection***, ***crossover***, etc... Successive new generations of better populations in the direction of search objectives are created. They are inspired by Darwinian principles based on natural evolution. In other words, the main idea behind genetic algorithms is that only the ***fittest*** individuals will survive.

Main advantage of genetic algorithms is that they ideally do not make any assumption about the underlying problem, hence they are suitable to tackle a wide range of diverse problems in engineering, art, biology, economics, marketing, genetics, operations research, robotics, social sciences, physics, politics, chemistry, etc...

So what is a GA? A typical GA consists of the following:

1. a number, or ***population***, of candidate solutions to the problem.
2. a way of calculating how good or bad the individual solutions within the population are. i.e. how ***fit*** an individual is?

3. a method for mixing fragments of the better solutions to form new, on average even better solutions. Which permits the population to *evolve* naturally.
4. a *mutation* operator to avoid permanent loss of diversity within the solutions. This allows introducing new information in the population.

2.2 Typical GA Schema

The basic iteration cycle of a genetic algorithm proceeds on a population of individuals, each of which represents a search point in the space of potential solutions of a given optimization problem. In case of a canonical genetic algorithm, each individual is a binary vector $\vec{x} = (x_1, x_2, \dots, x_n) \in \{0, 1\}^n$ of fixed length n . The fitness function $f : \{0, 1\}^n \rightarrow \mathbb{R}$ provides a quality measure which is used by the selection procedure to direct the search towards regions of the search space where the average fitness of the population increases. The recombination operator allows for the exchange of information between different individuals, and mutation introduces innovation into the population.

After a uniform random initialization of the population the evolution proceeds by iterating the steps selection, recombination (crossover), and mutation (see figure 1) until a termination criterion is fulfilled. In most cases, the algorithm is terminated after a certain number of iterations of the basic cycle or when a satisfactory fitness level has been reached.

The recombination (crossover) operator allows for the exchange of information between different individuals. The original one-point crossover [9] works on two parent individuals (which are randomly chosen from the population, see the next paragraph) by choosing a crossover point $\chi \in \{1, \dots, n - 1\}$ at random and exchanging all bits after the χ^{th} one between both individuals. The crossover rate p_c (e.g. $p_c \approx 0.6$) determines the probability to undergo crossover (see todo for more details). The crossover operator can be extended to a generalized multi-point crossover [10] or even to uniform crossover, where an it is randomly decided for each bit whether to exchange it or not [19]. The strong mixing effect introduced by uniform crossover is sometimes helpful to overcome local optima.

Normally, selection in genetic algorithms is a probabilistic operator which uses the relative fitness $p_s(\vec{x}_i) = f(\vec{x}_i) / \sum_{j=1}^u f(\vec{x}_j)$ to serve as selection probabilities (u denotes the population size). This selection operator is called proportional selection. If the problem under consideration is a minimization one, or if the fitness function

can take negative values, then $f(\vec{x}_i)$ has to be linearly transformed before calculating selection probabilities. This technique known as linear dynamic scaling is commonly used in genetic algorithms (see [13], pp. 123-124, or [14]).

Innovation, i.e. new information, is introduced into the population by means of mutation, which works by inverting bits with a small probability p_m (e.g. $p_m \approx 0.001$). Though mutation is often interpreted as a rather unimportant operator in genetic algorithms [9], recent theoretical work gives strong evidence for an appropriate choice of a mutation rate $p_m = 1/n$ on many problems [2; 12].

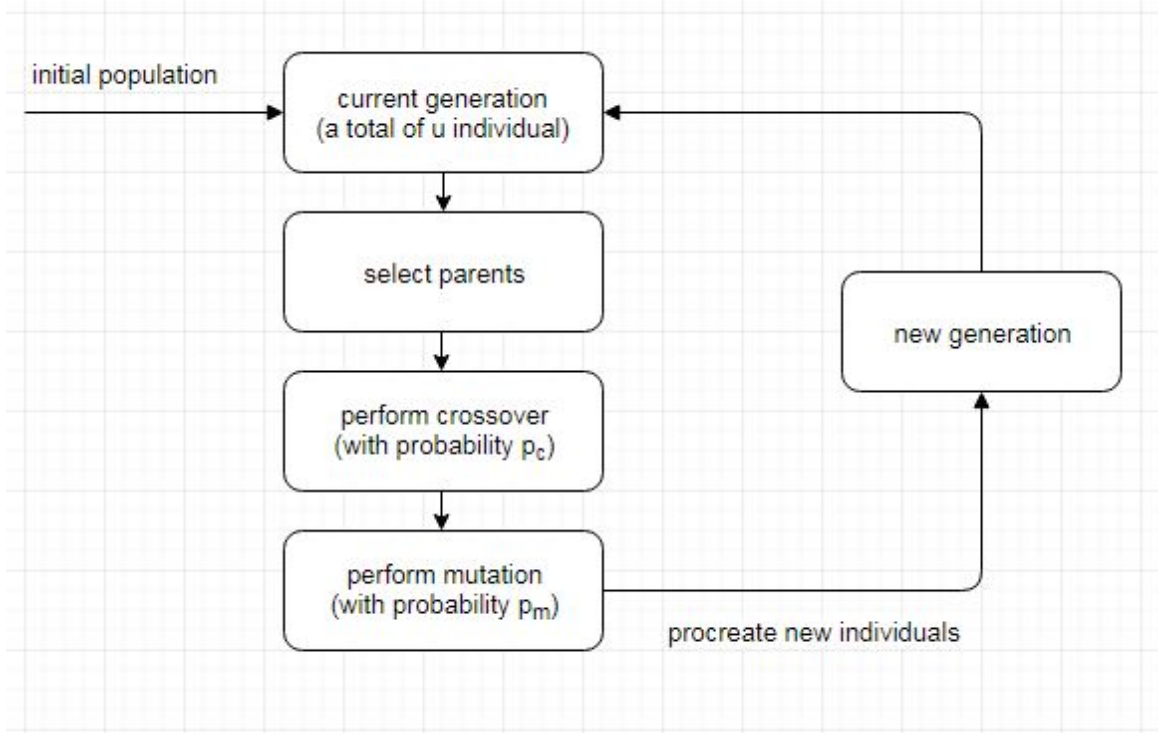


Figure 1: general schema for genetic algorithms

3 The Minimum Vertex Cover Problem

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4 Experimental Results

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5 Conclusion

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