

22-52-Q2

Q (a) SSL/TLS

DH \rightarrow RSA

TLS 3.1

X 不考

(b) DH

$$p = 37 \quad g = 13$$

$$a = 10 \quad b = 7$$

(i) $A = ? \quad B = ?$

(ii) $S = ?$

(iii) $a \rightarrow S ? \quad b \rightarrow S ? \quad \checkmark$

Solution (b) (i)

① we define Alice public key A
private key a

Bob public key B
private key b
share key s
prime number p
generator g

② Alice generate A

$$\begin{aligned} A &= g^a \bmod p \\ &= 13^{10} \bmod 37 \\ &= (13^5)^2 \bmod 37 \\ &= (35)^2 \bmod 37 \\ &= 4 \end{aligned}$$

③ Bob $\rightarrow B$

$$\begin{aligned} B &= g^b \bmod p \\ &= 13^7 \bmod 37 \end{aligned}$$

$$= 32$$

(ii) ① Alice

$$s = B^a \bmod p$$

$$= 32^{10} \bmod 37$$

$$= (32^5)^2 \bmod 37$$

$$= 20^2 \bmod 37$$

$$= 30$$

② Bob

$$s = A^b \bmod p$$

$$= 4^7 \bmod 37$$

$$= 30$$

(iii) ① can find

② due to $s = A^b \bmod p$ or $s = B^a \bmod p$

③ So no security remains.