Solution

$$Z(te^{-at}) = Z(t)|_{z=ze^{aT}}$$

$$= \frac{Tz^{-1}}{(1-z^{-1})^2}|_{z=ze^{aT}}$$