Solution

$$=\lim_{z\to\infty} \frac{(1-e^{-t})z}{(z-1)(z-e^{-t})}$$

$$=\lim_{z\to\infty} \frac{(1-e^{-t})z}{z^2-(e^{-t}+1)z+e^{-t}} = 0$$