

Example 3-3

Q: Figure 3-12 (a) $G(z) = ?$ 3.12(b) $Y(z) = ?$

Solution

$$G(s) = \frac{1}{s+a} \quad X(t) = 1(t)$$

(i) 有输入采样 $G(z) = Z(G(s)) = \frac{1}{1 - e^{-aT} z^{-1}}$

(ii) 对于 $G(s)$, 有输入采样

$$G(s) = \frac{U(s)}{X^*(s)} \quad (1)$$

对于 $H(s)$, 没输入采样

$$H(s) = \frac{Y(s)}{U(s)} \quad (2)$$

from (1)(2), 消去 $U(s)$

$$G(s) X^*(s) = \frac{Y(s)}{H(s)}$$

$$Y(s) = G(s) H(s) X^*(s)$$

$$Y^*(s) = [G(s) H(s) X^*(s)]^*$$

$$= G H^*(s) X^*(s)$$

$$X(t) = 1(t)$$

$$G(s) = \frac{Y(s)}{H(s) X^*(s)}$$

$$\text{assume } H(s) = 1$$

$$Y(s) = G(s) X^*(s)$$

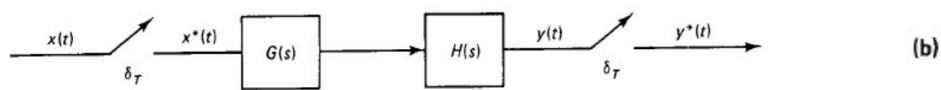
$$Y^*(s) = G^*(s) X^*(s)$$

$$Y(z) = G(z) X(z)$$

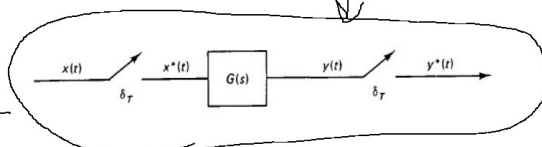
$$X(z) = \frac{1}{1-z^{-1}} = \frac{1}{1-e^{-aT} z^{-1}} \frac{1}{1-z^{-1}}$$

$$Y(z) = G H(z) \frac{1}{1-z^{-1}}$$

$$\text{答案 } Y(z) = \frac{1}{a} \frac{(1-a^{-aT}) z^{-1}}{(1-z^{-1})(1-e^{-aT} z^{-1})}$$



假设 $H(s) = 1$



Therefore, the presence or absence of the **input sampler** is **crucial**. But the presence or absence of **a sampler at the output** of the element (or the system) does not affect the pulse transfer function.

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3.3.3. General Procedure of Obtaining Pulse Transfer Functions

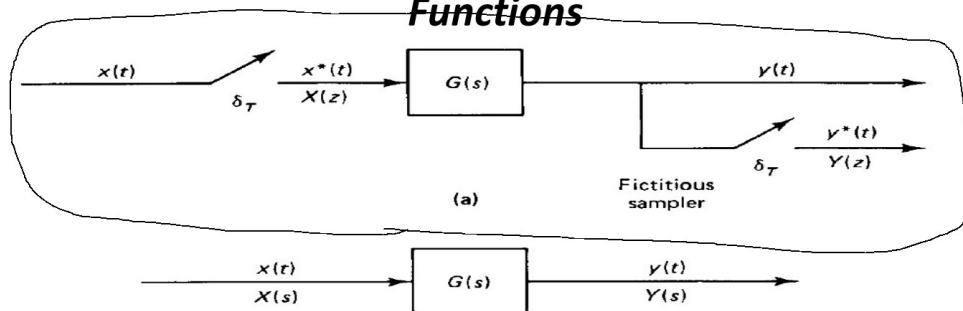


图3.10 (a) 输入有脉冲采样器的连续时间系统; (b) 连续时间系统

Figure 3.10 (a) Continuous-time system with an impulse sampler at the input
(b) Continuous-time system

For Figure 3-10(a), input sampler is present. Then

$$Y(s) = G(s)X^*(s)$$

对于图3-10(a), 存在输入采样器。然后

$$Y(s) = G(s)X^*(s)$$

So $Y^*(s) = G^*(s)X^*(s)$ and hence $Y(z) = G(z)X(z)$

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same $\rightarrow Y^*(s) = G^*(s)X^*(s)$