

Example 3-2.

Q: verify $[G(s)X^*(s)]^* = G^*(s)X^*(s)$?

T $G(s) = \frac{1}{s+1}$ $x(t) = 1(t)$ & $Y(z) = ?$

Solution $G(s)X^*(s) = Y(s)$

$G^*(s)X^*(s) = G(z)X(z) = Y(z)$

Prove $Y^*(s) = Y(z)|_{z \rightarrow e^T}$ clearly same

$G(s) = \frac{1}{s+1}$ $G(z) = \frac{1}{1-e^{-T}z^{-1}} = \frac{Y(z)}{X(z)}$

$x(t) = 1(t)$ $X(z) = \frac{1}{1-z^{-1}}$

$Y(z) = \frac{1}{(1-z^{-1})} \frac{1}{1-e^{-T}z^{-1}}$

$Y^*(s) = \frac{1}{1-e^{-sT}} \frac{1}{1-e^{-T}e^{-sT}}$