Q why
$$\overline{X}(0) = 0$$

 $\overline{X}(k+1) = A\overline{X}(k) + Bu(k) + L_0(Y(k) - C\overline{X}(k))$

Solution

let
$$k = -1$$
, $\overline{X}(0) = A\overline{X}(-1) + Bu(-1) + L_0(g(-1) - c\overline{X}(-1))$
 $\overline{X}(0) = 0 + 0 + L_0(0 - 0)$
 $\overline{X}(0) = 0$