23 - S(-Qq  
(a) (i) 
$$k? \rightarrow Z_{12} = 0.9 \pm j0.1$$
  
Solwein:  $k = [01]$  Wc  $[-]$ 

$$d_0(z) = z^2$$

$$do(A) = A^2 = \begin{bmatrix} 4 - 1 \\ 2 & 0 \end{bmatrix}^2 = \begin{bmatrix} 14 & -47 \\ 8 & -2 \end{bmatrix}$$

$$W_{0} = \begin{bmatrix} C \\ CA \end{bmatrix} = \begin{bmatrix} 2 & 1 \\ 0 & -2 \end{bmatrix}$$

$$CA = \begin{bmatrix} 2 & 1 \end{bmatrix} \begin{bmatrix} 4 & -1 \\ 2 & 0 \end{bmatrix}$$

$$W_{0}^{-1} = \begin{bmatrix} \frac{1}{7} & \frac{1}{4} \\ \frac{5}{7} & -\frac{1}{7} \end{bmatrix} \in \begin{bmatrix} 0.1428 & 0.0714 \end{bmatrix} = \begin{bmatrix} 10 & -2 \end{bmatrix}$$

$$\begin{bmatrix} 0 = \begin{bmatrix} 14 & -4 \\ 8 & -2 \end{bmatrix} \begin{bmatrix} \frac{1}{7} & \frac{1}{4} \\ \frac{5}{7} & -\frac{1}{7} \end{bmatrix} \begin{bmatrix} 0 \\ 1 \end{bmatrix} = \begin{bmatrix} \frac{11}{7} \\ \frac{6}{7} \end{bmatrix} = \begin{bmatrix} 1.5714 \\ 0.8571 \end{bmatrix}$$

$$= \begin{bmatrix} \overline{z} - 4 & 1 \\ -2 & \overline{z} \end{bmatrix} + \begin{bmatrix} 1 \\ 0 \end{bmatrix} \begin{bmatrix} 2.2 & -0.59 \end{bmatrix}$$

The Poles are  $z_{1,2}=0.9\pm0.1j$  we can see all poles of Y(z) lie inside the unit circle,

$$Y(z) = \frac{1}{2} \frac{z^{2}+2}{z^{2}-1.83+0.82} \quad R(z)$$

$$\lim_{k \to \infty} y(k) = \lim_{z \to 1} (1-z^{2}) \quad Y(z)$$

$$= \lim_{z \to 1} (1-z^{2}) \quad \frac{z^{2}+2}{z^{2}-1.83+0.82} \quad \frac{1}{1-z^{2}}$$

$$= \frac{4}{1-1.8+0.82}$$

$$= 200 \quad kr$$

$$So \quad 200 \quad kr = 1 \quad kr = 0.005$$

$$(c) \quad (i) \quad (0) \quad (0)$$

$$S = 45 + 1 - \frac{365^{2}}{95 + 5}$$

$$-35 = 1 - \frac{365^{2}}{75 + 5}$$

$$-35(95 + 5) = 95 + 5 - 365^{2}$$

$$365^{2} - 275^{2} - 155 - 95 - 5 = 0$$

$$95^{2} - 245 - 5 = 0$$

$$S_{12} = \frac{4 \pm \sqrt{21}}{3}$$

$$S_{1} = 2.8609$$

$$S_{2} = 2.8609$$

$$S_{3} = 2.8609$$

$$S_{4} = 2.8609$$

$$S_{5} = 2.8609$$

$$S_{5$$

(ii)  $x(k+1) = 2x(k) - 3x0.5583 \times (k)$   $= 0.3251 \times (k)$ gince [0.3251|<1], x(k) converges to zero  $for \qquad x(0) \neq 0$ So, the final value of x(k) = 0