

Q: Z 平面转 S 平面, 与求 damping ratio

Example 11.2 - Lect 3. P13

close-loop poles at $0.888 \pm j0.173$

Solution ① Z 平面 $a \pm bj \rightarrow r \pm \theta$

method 1: $r = \sqrt{a^2 + b^2}$ $\theta = \tan^{-1}(\frac{b}{a})$

method 2:

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菜单 \rightarrow 2: 复数 $\rightarrow 0.888 + 0.173i$

\rightarrow OPTN \rightarrow \downarrow \rightarrow 1: $r \angle \theta \rightarrow =$

$0.905 \angle 0.1924 \text{ radians}$
 $0.193 \rightarrow \text{ppt 错}$

$$\zeta = -\frac{\ln r}{\sqrt{\ln^2 r + \theta^2}}$$

$$= -\frac{\ln 0.905}{\sqrt{\ln^2 0.905 + 0.193^2}}$$

$$= 0.46 \quad \checkmark$$

$$\textcircled{2} \quad z = e^{sT} \quad s = \frac{\ln z}{T} \quad s = \sigma + j\omega$$

$$0.905 \text{ \& } 0.193 \quad T = 0.1$$

$$\sigma = \frac{\ln 0.905}{0.1} = -0.9982$$

$$\omega = \frac{\ln 0.193}{0.1} = -16.4507$$

$$s = -0.9982 - j16.4507$$