Q: (a) discretisel?

Solution O State transform matrix

$$\begin{bmatrix} S2 - A3^{-1} = \begin{bmatrix} S & -1 \\ 2 & S+3 \end{bmatrix}^{-1} = \frac{1}{S(S+3)+2} \begin{bmatrix} S+3 & 1 \\ -2 & S \end{bmatrix}$$

$$= \frac{1}{S^2 + 3S + 2} \begin{bmatrix} S+3 & 1 \\ -2 & S \end{bmatrix}$$

$$= \frac{1}{(S+1)(S+2)} \begin{bmatrix} S+3 & 1 \\ -2 & S \end{bmatrix}$$

$$= \begin{bmatrix} S+3 & 1 \\ \hline (S+1)(S+2) & (S+1)(S+2) \end{bmatrix}$$

$$= \begin{bmatrix} S+3 & 1 \\ \hline (S+1)(S+2) & S \end{bmatrix}$$

table #19

$$\frac{b-a}{(5fa)(5fb)} = \frac{1}{(5f1)(5f2)}$$
 we get $e^{-t} - e^{-2t}$

$$\frac{S}{(S+1)(S+2)} = \frac{A}{S+1} + \frac{B}{S+2} \qquad PFE$$

A(St2) + B(St1) = (A+B)S+ 2A+B

$$\begin{cases} A+B=1\\ 2A+B=0 \end{cases} \Longrightarrow \begin{cases} A=-1\\ B=2 \end{cases}$$

$$\frac{S}{(Sf1)(Sf2)} = \frac{-1}{Sf1} + \frac{2}{Sf2}$$

$$#4$$
 $\frac{1}{S+a}$, we get $-e^{-t}+2e^{-2t}$

Therefore

$$\left(-\frac{5+3}{(5+1)(5+2)}\right) = -e^{-t} + 2e^{-2t} = 2e^{-t} - e^{-2t}$$

$$[f] = e^{-t} - e^{-2t}$$

$$[-1] \frac{s}{(s_{11})(s_{12})} = -e^{-t} + 2e^{-2t}$$

$$\frac{\partial (t)}{\partial (t)} = \left[\frac{2e^{-t}}{e^{-t}} - e^{-2t} - e^{-2t} - e^{-2t} - e^{-2t} - e^{-2t} \right]$$

$$= \begin{bmatrix} 2e^{-1} - e^{-2T} & e^{-1}e^{-2T} \\ -2e^{-1} + 2e^{-2T} & -e^{-1} + 2e^{-2T} \end{bmatrix}$$

@input mastrix

$$\begin{aligned}
&\Theta(T) = \int_{0}^{T} \overline{\phi}(t) dt \, \beta \\
&= \int_{0}^{T} \begin{bmatrix} 2e^{-t} - e^{-\lambda t} & e^{-t} - e^{-\lambda t} \\ -2e^{-t} + 12e^{-\lambda t} & -e^{-t} + 2e^{-\lambda t} \end{bmatrix} \int_{0}^{T} dt \\
&= \int_{0}^{T} \begin{bmatrix} 8e^{-t} - 8e^{-\lambda t} \\ -8e^{-t} + 16e^{-\lambda t} \end{bmatrix} dt \\
&\int_{0}^{T} 8e^{-t} - 8e^{-\lambda t} dt \\
&= 8 \int_{0}^{T} e^{-t} dt - 8 \int_{0}^{T} e^{-\lambda t} dt \\
&= 8 \left(-e^{-t} \right) \Big|_{0}^{T} - 8 \left(-\frac{1}{2}e^{-\lambda t} \right) \Big|_{0}^{T} \\
&= -8 \left(e^{-T} - 1 \right) + 4 \left(e^{-\lambda t} - 1 \right) \\
&= -8 e^{-T} + 4e^{-\lambda t} + 4 \int_{0}^{T} -8e^{-t} + 16 \int_{0}^{T} e^{-\lambda t} dt & = 88 \left(e^{-T} - 1 \right) + 16 \left(\frac{1}{2} e^{-\lambda t} \right) \Big|_{0}^{T} \\
&= -8e^{-T} - 8 e^{-\lambda t} + 16 \int_{0}^{T} e^{-\lambda t} dt & = 88 \left(e^{-T} - 1 \right) - 8 \left(e^{-\lambda t} - 1 \right) \\
&= -8e^{-T} - 8e^{-\lambda t} + 4e^{-\lambda t} + 4e^{-$$

$$\int_{0}^{2e^{-t}-e^{-2t}} e^{-\frac{t}{2}e^{-2t}} e^{-\frac{t}{2}e^{-2t}}$$

$$CA = [1 -1][-4 -6] = [4 7]$$

(ii) unobservable?

$$Y(k+1) = \begin{bmatrix} 0 & 1 \\ -4 & -6 \end{bmatrix} Y(k) + \begin{bmatrix} 0 \\ 1 \end{bmatrix} [-k_1 - k_2] Y(k) + \begin{bmatrix} 2 \\ 2 \end{bmatrix} r(k)$$

$$= \left(\begin{bmatrix} 0 & 1 \\ -4 & -6 \end{bmatrix} + \begin{bmatrix} 0 & 0 \\ -k_1 & -k_2 \end{bmatrix}\right) \times (k) + \begin{bmatrix} 0 \\ 1 \end{bmatrix} r(k)$$

$$= \begin{bmatrix} 0 & 1 \\ -4-k_1 & -6-k_2 \end{bmatrix} \times (k) + \begin{bmatrix} 2 \\ 2 \end{bmatrix} r(k)$$

$$k = (0.2^{2} \times 2.6477 + 6)^{-1} \times 0.2 \times 2.6479 \times 0.8$$

$$= 0.06939$$

$$u(k) = -0.06939 \times (k)$$

$$\pi(k+1) = \left[0.8 + 0.2 \times (-0.06937)\right] \times (k)$$

$$= 0.7861 \times (k)$$