$$2z-SI-Q4$$

$$Q(a)(i) k? \rightarrow deadbeaf control$$

$$\gamma(b+1) = [A-BK] \times (h)$$

$$[A-Bk] = \begin{bmatrix} 1 & 0 \\ -1 & 1 \end{bmatrix} - \begin{bmatrix} 1 \\ 1 \end{bmatrix} k$$

$$k = [01]Wc^{-1}c^{-1}c^{-1}(A)$$

$$Wc^{-1} = \begin{bmatrix} B & AB \end{bmatrix}^{-1} \qquad AB = \begin{bmatrix} -10 \\ -11 \end{bmatrix}$$

$$= \begin{bmatrix} 1 \\ 1 \end{bmatrix}$$

$$= \begin{bmatrix} 0 & 1 \\ -11 \end{bmatrix}$$

$$= \begin{bmatrix} 0 & 1 \\ -11 \end{bmatrix}$$

$$k = [01] \begin{bmatrix} 01 \\ 1-1 \end{bmatrix} \begin{bmatrix} 01 \\ 21 \end{bmatrix} = [1 - 1] \begin{bmatrix} 1 \\ -21 \end{bmatrix} = [3 - 1]$$

$$[A-Bk] = \begin{bmatrix} 1 & 0 \\ -11 \end{bmatrix} - \begin{bmatrix} 1 \\ 1 \end{bmatrix} \begin{bmatrix} 3 & -1 \end{bmatrix}$$

 $=\begin{bmatrix} -1 & 0 & 7 & -1 & 8 & -1$

$$= \begin{bmatrix} -2 & 1 \\ -4 & 2 \end{bmatrix}$$

$$= Q > 1 , [A - BK]^{2} = 0 , \pi(k) = [A - BK] \times (0)$$

$$[A - BK]^{2} = \begin{bmatrix} -2 & 1 \\ -4 & 2 \end{bmatrix} \begin{bmatrix} -2 & 1 \\ -4 & 2 \end{bmatrix} = \begin{bmatrix} 0 & 0 \\ 0 & 0 \end{bmatrix} \quad q = 2.$$
(ii) $\hat{\chi}_{i}(k)$ 是什么? 逐變到 意識的

$$\begin{bmatrix} \hat{x}_{1}(k) \\ \hat{x}_{2}(k) \end{bmatrix} = \begin{bmatrix} 1 \\ 0 \\ \end{bmatrix} \begin{bmatrix} x_{1}(k) \\ x_{2}(k) \end{bmatrix}$$

$$u(k) = -\hat{k} \begin{bmatrix} 1 \\ 0 \\ \end{bmatrix} \begin{bmatrix} x_{1}(k) \\ x_{2}(k) \end{bmatrix}$$

状态转移矩阵

$$2 \times \chi(k) = pw(k) \quad \text{lecture } 2 - 5 - p_4$$

$$\chi(k) = \begin{bmatrix} 1 & 1 \\ 0 & 1 \end{bmatrix}^{-1} \hat{\chi}(k)$$

$$p = \begin{bmatrix} 1 & 1 \\ 0 & 1 \end{bmatrix}^{-1} = \begin{bmatrix} 1 & -1 \\ 0 & 1 \end{bmatrix}$$

$$Aw = p^{-1}Ap = \begin{bmatrix} 1 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 \\ -1 & 1 \end{bmatrix}$$

$$\begin{aligned}
&= \begin{bmatrix} 0 & 1 \\ -1 & 2 \end{bmatrix} \\
&= \begin{bmatrix} 0 & 1 \\ -1 & 2 \end{bmatrix} \\
&= \begin{bmatrix} 0 & 1 \\ -1 & 2 \end{bmatrix} \\
&= \begin{bmatrix} 0 & 1 \\ -1 & 2 \end{bmatrix} \\
&= \begin{bmatrix} 0 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & -1 \\ 0 & 1 \end{bmatrix} = \begin{bmatrix} 2 \\ 1 \end{bmatrix} \\
&= \begin{bmatrix} 0 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & -1 \\ 0 & 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 \end{bmatrix} \\
&= \begin{bmatrix} 0 & 1 \\ -1 & 2 \end{bmatrix} \hat{X}(k) + \begin{bmatrix} 1 \\ 1 \end{bmatrix} u(k) \\
&= \begin{bmatrix} 0 & 1 \\ -1 & 2 \end{bmatrix} \hat{X}(k) + \begin{bmatrix} 1 \\ 1 \end{bmatrix} u(k) \\
&= \begin{bmatrix} 0 & 1 \\ 1 & 2 \end{bmatrix} \hat{X}(k) + \begin{bmatrix} 1 \\ 1 & 2 \end{bmatrix} u(k) \\
&= \begin{bmatrix} 0 & 1 \\ 1 & 2 \end{bmatrix} \hat{X}(k) + \begin{bmatrix} 1 \\ 1 & 2 \end{bmatrix} \hat{X}(k) \\
&= \begin{bmatrix} 0 & 1 \\ 1 & 2 \end{bmatrix} \hat{X}(k) + \begin{bmatrix} 0 & 1 \\ 1 & 2 \end{bmatrix} \hat{X}(k) \\
&= \begin{bmatrix} 0 & 1 \\ 1 & 2 \end{bmatrix} \hat{X}(k) + \begin{bmatrix} 0 & 1 \\ 1 & 2 \end{bmatrix} \hat{X}(k) \\
&= \begin{bmatrix} 0 & 1 \\ 1 & 2 \end{bmatrix} \hat{X}(k) + \begin{bmatrix} 0 & 1 \\ 1 & 2 \end{bmatrix} \hat{X}(k) \\
&= \begin{bmatrix} 0 & 1 \\ 1 & 2 \end{bmatrix} \hat{X}(k) + \begin{bmatrix} 0 & 1 \\ 1 & 2 \end{bmatrix} \hat{X}(k) \hat{X}(k) + \begin{bmatrix} 0 & 1 \\ 1 & 2 \end{bmatrix} \hat{X}(k) \hat{X}(k$$

$$= [1 -2][-1 2]$$

$$= [3 -4]$$

Solution
$$\Im(k+1) = A\overline{X}(k) + Bu(k) + L_o(y(k) - C\overline{X}(k))$$

$$y(k) = C \times (k)$$

$$ZX(Z) = (A-LoC)\overline{X}(Z)+BU(Z)+LoCX(Z)$$

$$\frac{\overline{X(2)}}{U(2)} = \frac{B + L_0 C (2Z - A)^{-1} B}{ZI - A + L_0 C}$$

CC) optimal feel back gains minimize
$$J$$
obtain values of u*(k) as a function of x(0)

E=01,

Solution $A = 5$ $B = 1$ $N = 3$ $0 = 8$ $r = 1$

initialize $S(3) = 0$

let $K = 2$ $K(2) = (1 \times 0 \times 1 + 1)^{-1} \times 1 \times 0 \times 5 = 0$
 $S(2) = [S - K(2)]^T \times 0 \times [S - K(2)] + K(2) + 8$
 $= 8$

let $K = 1$ $K(1) = (1 \times 8 \times 1 + 1)^{-1} \times 1 \times 8 \times 5$
 $= \frac{40}{9} = 4.4444$
 $S(1) = (S - 1 \times \frac{40}{9}) \times 8 \times (S - 1 \times \frac{40}{9}) + (\frac{40}{9})^2 + 8$
 $= \frac{272}{7} = 30.2222$

let $K = 0$ $K(0) = (\frac{272}{9} + 1)^{-1} \times \frac{272}{9} \times 5$
 $= \frac{1360}{281} = 4.8399$
 $S(0) = (S - \frac{1360}{281})^2 \times \frac{272}{9} + (\frac{1360}{281})^2 + 8$
 $= \frac{9048}{281} = 32.1993$
 $U^*(0) = -K(0) \times (0) = -\frac{1360}{281} \times (0) = -4.8399 \times (0)$

$$x''(1) = Ax(6) + Bu'(0) = 5x(6) + u'(0)$$

$$= \frac{45}{281} \times (6)$$

$$= 0.160 | x(6)$$

$$x''(1) = -k(1) \times (1) = -\frac{44}{9} \times \frac{45}{281} \times (6)$$

$$= -\frac{220}{281} \times (6)$$

$$= -0.7829 \times (6)$$

$$x''(2) = 5x(1) + u''(1)$$

$$= \left(5 \times \frac{45}{281} - \frac{220}{281}\right) \times (6)$$

$$= \frac{5}{281} \times (6)$$

$$= 0.01 779 \times (6)$$

$$u''(2) = -k(2) \times (2) = 0$$
Summary $u''(0) = -4.8399 \times (6)$

$$u''(1) = -0.7829 \times (6)$$

(パ(2) = 0