23-51-01 Q(a) 连? Z? o start 7=0.5 Solution

1) Yes, x(t) is a continuous-time signal because it is defined for all real values of t. The function r(e) provides a specific Value for every time t in the real number domain, fulfilling the definition

of a confinuous—time signal.

1 Too Sampling

according to the definition of & transform

$$\chi(z) = z \left[\pi(t)\right] = \sum_{k=0}^{\infty} \chi(k\tau) z^{-k}$$

= $\chi(0) = \frac{1}{2} + \chi(0.5) = \frac{1}{2} + \chi(1) = \frac{1}{2} + \chi(1.5) = \frac{1}{2} + \cdots$

$$= |+2z^{-1}+z^{-2}+z^{-3}+\cdots$$
So $\sum_{k=2}^{\infty} z^{-k} = \frac{z^{-2}}{|-z^{-1}|}$

$$= \frac{(+2z^{-1})(-z^{-1})+z^{-2}}{|-z^{-1}|}$$

$$= \frac{(+2z^{-1})(-z^{-1})+z^{-2}}{|-z^{-1}|}$$

$$= \frac{|-z^{-1}+zz^{-1}-zz^{-2}+z^{-2}|}{|-z^{-1}|}$$

$$= \frac{1+z^{-1}-z^{-2}}{|-z^{-1}|}$$
(b) Q: difference equation.

Solution apply z francform to
$$y(k+2)+(p-1)y(k+1)-py(k)=\delta(k-1)$$

$$z^{2}y(z)-z^{2}y(z)-zy(1)+(p-1)[zy(z)-zy(z)]-py(z)=z^{-1}$$
let $k=-2$, $y(z)+(p-1)y(z)-zy(z)-zy(z)=\delta(-z)$
So $y(z)=0$
let $k=-1$, $y(z)+(p-1)y(z)-zy(z)-zy(z)=z^{-1}$
So $y(z)=0$
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$$(z^{2}+\beta z-z-\beta)Y(z)=z^{4}$$

$$Y(z)=\frac{z^{4}}{z^{2}+(\beta-1)z-\beta}$$

$$\frac{Y(3)}{Z} = \frac{1}{Z^2(Z-1)(Z+\beta)}$$

$$(B+C)^{2} + (A+B\beta-C)^{2} + (A\beta-A)^{2} + A\beta$$

$$\begin{cases} B+C = 0 \\ A+Bp-C=0 \\ Ap-A=0 \\ Ap=1 \end{cases} \begin{cases} B-C=0 \\ C=\frac{1}{2} \\ P=1 \end{cases} \begin{cases} B+C=0 \\ C=0 \\ B=-\frac{1}{2} \end{cases}$$

$$\frac{Y(2)}{Z} = \frac{1}{Z^2} + \frac{-\frac{1}{2}}{Z-1} + \frac{\frac{1}{2}}{Z+1}$$

$$Y(z) = z^{-1} - \frac{1}{z} \frac{1}{1-z^{-1}} + \frac{1}{z} \frac{1}{1+z^{-1}}$$

$$\frac{Z}{Z} = \frac{Z^{2}(Z-1)(Z+\beta)}{Z+2} + \frac{C}{Z-1} + \frac{P}{Z+\beta}$$

$$\frac{Z+\beta}{Z+\beta} = \frac{C}{Z-1} + \frac{P}{Z+\beta}$$

$$(AZ+B)(Z-1)(Z+B) + CZ^{2}(Z+B)+D(Z^{2}(Z+B))$$

$$A\beta - A+B+C\beta - D=0 \quad (2) \quad B=-\frac{1}{2}$$

$$A\beta + B\beta - B = 0 \qquad (3)$$

$$\begin{array}{c|c}
C = \overline{1+\beta} \\
C = \overline{1+\beta}
\end{array}$$

from (3)
$$A = \frac{B - B\beta}{\beta} = \frac{B(1-\beta)}{\beta} = \frac{1-\beta}{\beta^2} = \frac{\beta^2}{\beta^2}$$

$$fron(2) \qquad A\beta - A + \beta + C\beta - D = 0$$

$$\frac{1-\beta}{\beta} - \frac{1-\beta}{\beta^2} - \frac{1}{\beta} + C\beta - D = 0$$

$$\frac{1-\beta}{\beta} - \frac{1-\beta}{\beta^2} - \frac{1}{\beta} + C\beta - D = 0$$

$$C\beta - D = \frac{\beta^2 + 1 - \beta}{\beta^2} \qquad (6)$$

$$CJJ+(6) \quad (17\beta) \quad C = \frac{\beta - 1}{\beta^2} - \frac{\beta}{\beta^2} - \frac{1}{\beta^2} = \frac{\beta^2 - 1 - \beta^2}{\beta^2}$$

$$fron(5) \quad D = \frac{\beta - 1}{\beta^2} - C = \frac{\beta - 1}{\beta^2} - \frac{1}{\beta^2} = \frac{\beta^2 - 1 - \beta^2}{\beta^2 (\beta + \beta)}$$

$$So \quad D = \frac{-1}{\beta^2 (\beta + \beta)}$$

$$\frac{Y(2)}{Z} = \frac{A}{Z} + \frac{B}{Z^2} + \frac{C}{Z^{-1}} + \frac{D}{Z^{-1}\beta}$$

$$\frac{Y(2)}{Z} = \frac{1-\beta}{\beta^2} - \frac{1}{\beta} Z^{-1} + \frac{1}{1+\beta} \frac{1}{1-Z^{-1}} - \frac{1}{\beta^2 (\beta + 1)} \frac{1}{1+\beta Z^{-1}}$$

$$Y(k) = \frac{1-\beta}{\beta^2} S_0(k) - \frac{1}{\beta} S_0(k-1) + \frac{1}{1+\beta} \frac{1}{1+\beta} - \frac{1}{\beta^2 (\beta + 1)}$$

$$\frac{1}{\beta^2 (\beta + 1)} \frac{1}{1+\beta} - \frac{(-\beta)^k}{\beta^2 (\beta + 1)} \qquad k = 0$$

$$-\frac{1}{\beta} + \frac{1}{1+\beta} - \frac{(-\beta)^k}{\beta^2 (\beta + 1)} \qquad k = 1$$

$$\frac{1}{(+\beta)} = \frac{(-\beta)^k}{\beta^2(\beta+1)} \qquad k \ge 2$$
(c) $\beta \to y(\beta)$ convergence?

Solution

① When $|\beta| < 1$, $k \Rightarrow p$, $(-\beta)^k \Rightarrow 0$
 $y(\beta) \to \frac{1}{|+\beta|} \qquad |E| = 1 \qquad |E| = |-\beta| = |\beta| < 1$

The Final Value Theorem applies

all poles of $Y(B)$ lie in side the unit circlue, with the possible exception of a simple pole at $Z = 1$

Verification: $\lim_{k \to \infty} y(k) = \lim_{k \to \infty} (1-2^{-k}) Y(k) = \frac{1}{\beta+1}$

so confirm theorem acceptable.

② When $|\beta| = 1 \qquad (-\beta)^k$ oscillates between ± 1
 $y(k)$ doesn't converge, it oscillates

The Final value Theorem does not apply

3 When $|\beta| > 1$, $(-\beta)^k$ grows without bound y(b) diverges as $k > \infty$ The Final value Theorem does not apply

关于(a) & transform 编思考,前面用定义主的&-transform 现在试用表求,

Solution

$$= \frac{1}{1-Z^{-1}} + \frac{Z^{-1} \sin z T}{1-2 Z^{-1} \cos z T + Z^{-2}} \qquad T = \frac{1}{z}$$

查不出来用定义

结论:分段用定义

区[1]= 1 1-2-1 +>0.8 连续用查表

不会外

$$=\frac{1}{z}$$

