

知识点Z4.40

案例：二次抑制载波振幅调制接收系统

主要内容：

二次抑制载波振幅调制接收系统

基本要求：

了解二次抑制载波振幅调制接收系统的基本原理



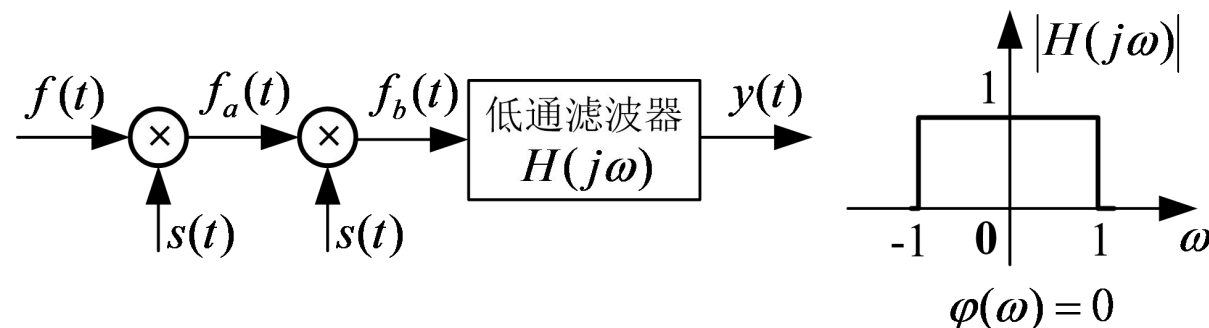
Z4.40* 案例：二次抑制载波振幅调制接收系统

例：如图二次抑制载波振幅调制接收系统，已知

输入信号： $f(t) = \frac{\sin t}{\pi t}, -\infty < t < \infty$

调制信号： $s(t) = \cos 500t, -\infty < t < \infty$

问：输出信号 $y(t)=?$



解： $y(t) = f(t) \times s(t) \times s(t) * h(t)$

$$Y(j\omega) = \left\{ \frac{1}{2\pi} \left[\frac{1}{2\pi} F(j\omega) * S(j\omega) \right] * S(j\omega) \right\} \cdot H(j\omega)$$



$$g_2(t) \leftrightarrow 2Sa(\omega)$$

由对称性可知：

$$2Sa(t) \leftrightarrow 2\pi g_2(-\omega) = 2\pi g_2(\omega)$$

$$\frac{\sin t}{\pi t} = \frac{Sa(t)}{\pi} = f(t) \leftrightarrow g_2(\omega)$$

所以：

$$F(j\omega) = g_2(\omega)$$

调制信号：

$$s(t) = \cos 500t, -\infty < t < \infty$$

$$S(j\omega) = \pi[\delta(\omega + 500) + \delta(\omega - 500)]$$

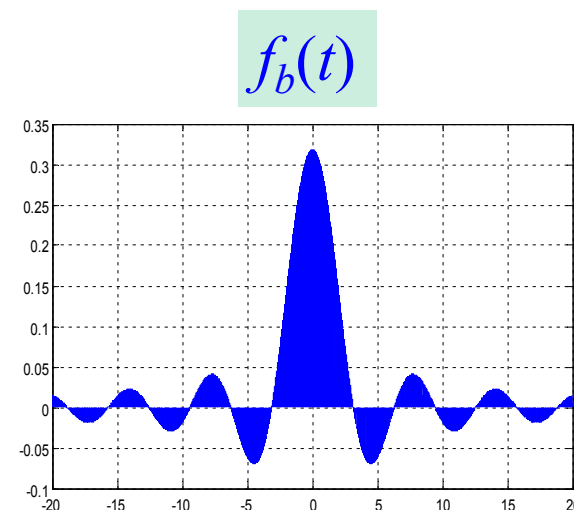
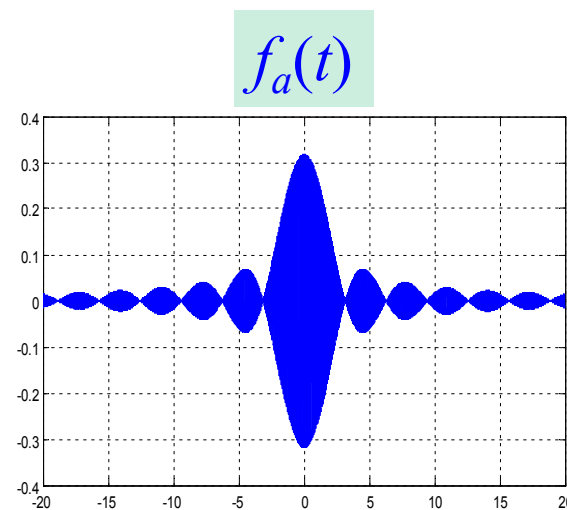
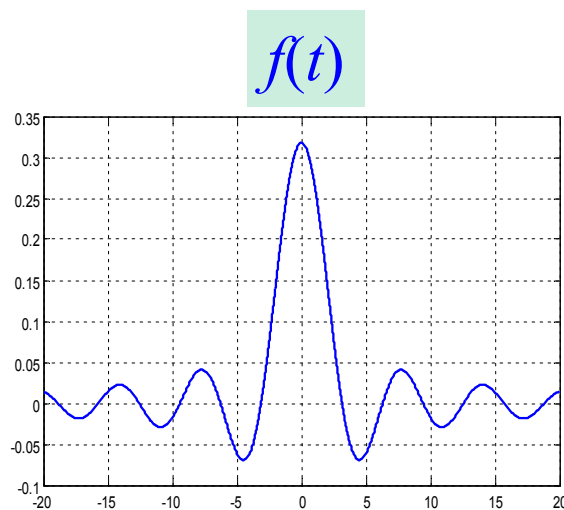
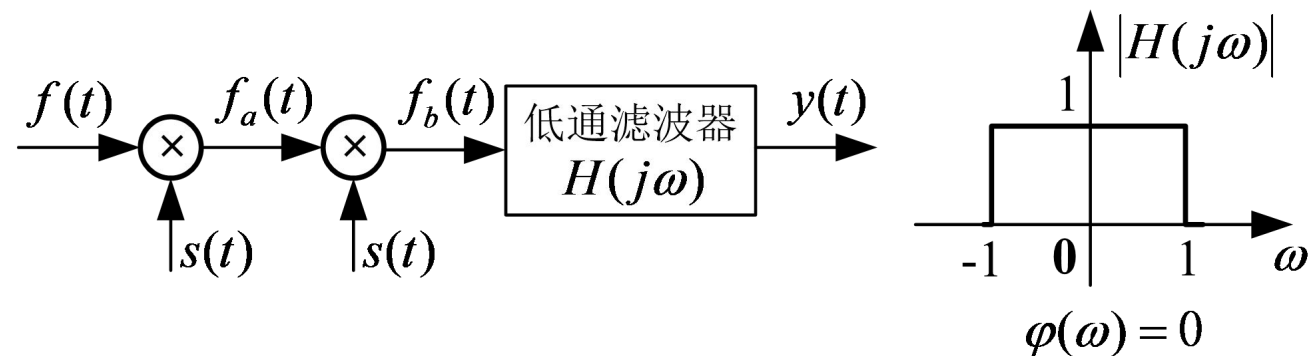


$$\begin{aligned} Y(j\omega) &= \left\{ \frac{1}{2\pi} \left[\frac{1}{2\pi} F(j\omega) * S(j\omega) \right] * S(j\omega) \right\} \cdot H(j\omega) \\ &= \frac{1}{4\pi^2} g_2(\omega) * \pi[\delta(\omega+500) + \delta(\omega-500)] * \pi[\delta(\omega+500) + \delta(\omega-500)] \cdot H(j\omega) \\ &= \frac{1}{4\pi^2} g_2(\omega) * \pi^2[\delta(\omega+1000) + 2\delta(\omega) + \delta(\omega-1000)] \cdot H(j\omega) \\ &= \frac{1}{4\pi^2} g_2(\omega) * \pi^2[\delta(\omega+1000) + 2\delta(\omega) + \delta(\omega-1000)] \cdot H(j\omega) \\ &= \frac{1}{4} g_2(\omega) * [\delta(\omega+1000) + 2\delta(\omega) + \delta(\omega-1000)] \cdot g_2(\omega) \\ &= \frac{1}{2} g_2(\omega) \end{aligned}$$

所以：

$$y(t) = \frac{\sin t}{2\pi t} = \frac{\text{Sa}(t)}{2\pi} = \frac{1}{2} f(t)$$

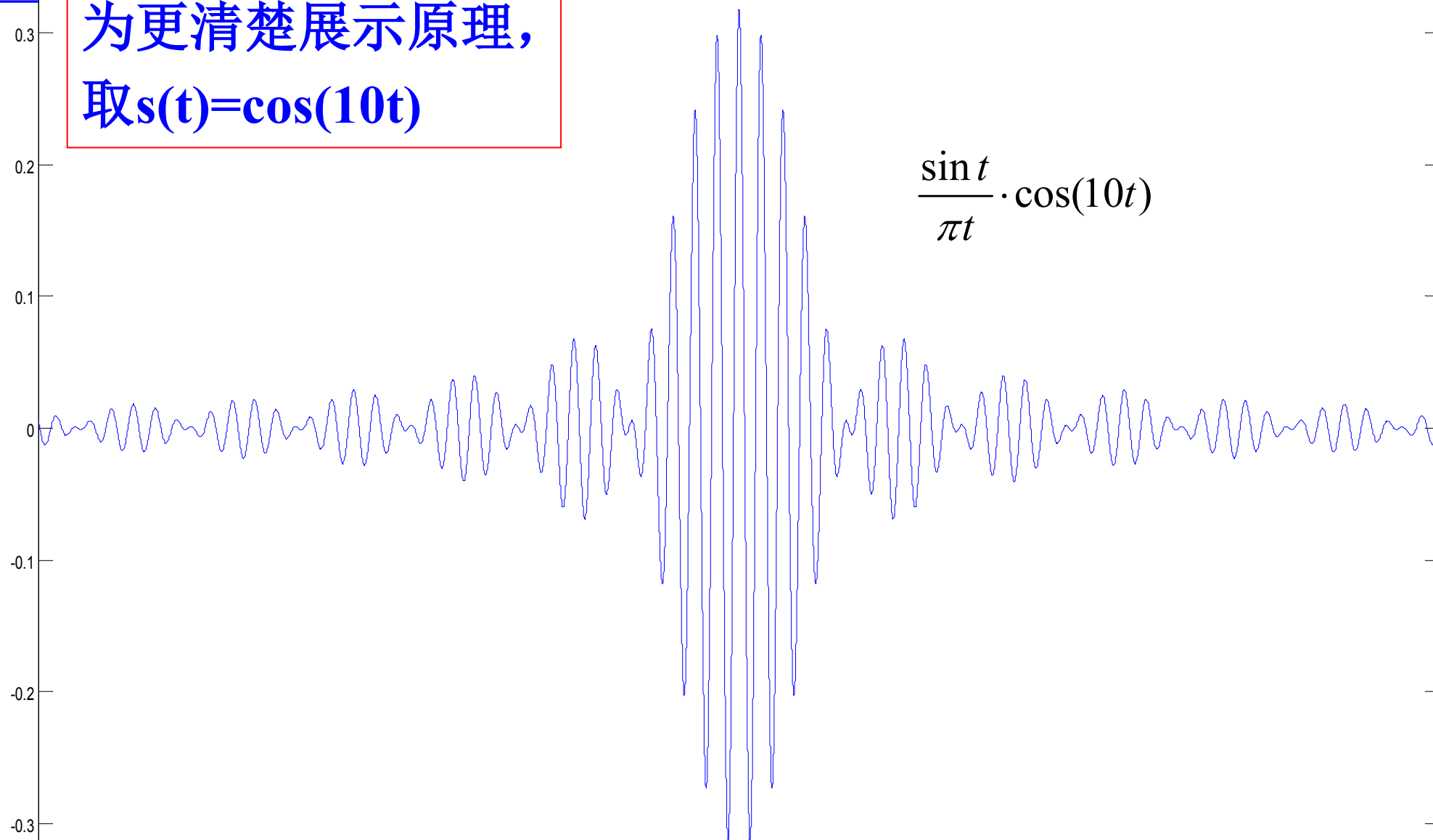




思考：各信号的频谱图？



为更清楚展示原理，
取 $s(t)=\cos(10t)$



0.4
0.3
0.2
0.1
0
-0.1
-0.2
-0.3

$$\frac{\sin t}{\pi t} \cdot \cos(10t) \cdot \cos(10t)$$

