23-51-01 Q(a) 连? Z? o start 7=0.5 Solution

1) Yes, x(t) is a continuous-time signal because it is defined for all real values of t. The function r(e) provides a specific Value for every time t in the real number domain, fulfilling the definition

of a confinuous—time signal.

1 Too Sampling

according to the definition of & transform

$$\chi(z) = z \left[\pi(t)\right] = \sum_{k=0}^{\infty} \chi(k\tau) z^{-k}$$

= 100) = + X(05) Z -1 + X(1) Z -2 + X(1.5) Z -3 + ...

$$= |+2z^{-1}+z^{-2}+z^{-3}+\cdots$$
So $\sum_{k=2}^{\infty} z^{-k} = \frac{z^{-2}}{|-z^{-1}|}$

$$= \frac{(+2z^{-1})(-z^{-1})+z^{-2}}{|-z^{-1}|}$$

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$$= \frac{|-z^{-1}+zz^{-1}-zz^{-2}+z^{-2}|}{|-z^{-1}|}$$

$$= \frac{1+z^{-1}-z^{-2}}{|-z^{-1}|}$$
(b) Q: difference equation.

Solution apply z francform to
$$y(k+2)+(p-1)y(k+1)-py(k)=\delta(k-1)$$

$$z^{2}y(z)-z^{2}y(z)-zy(1)+(p-1)[zy(z)-zy(z)]-py(z)=z^{-1}$$
let $k=-2$, $y(z)+(p-1)y(z)-zy(z)-zy(z)=\delta(-z)$
So $y(z)=0$
let $k=-1$, $y(z)+(p-1)y(z)-zy(z)-zy(z)=z^{-1}$
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$$(2^{2}+\beta z-2-\beta)Y(z)=z^{-1}$$

$$Y(z)=\frac{z^{-1}}{z^{2}+(\beta-1)z-\beta}$$

$$\frac{Y(z)}{z}=\frac{1}{z^{2}(z-1)(z+\beta)}$$

A(Z-1)(Z+B)+BZ2(Z+B)+CZ2(Z-1) A(Z2+BZ-Z+B)+B(Z3+BZ2)+(&3-Z2)

$$\begin{cases} B+C = 0 \\ A+Bp-C=0 \\ Ae-A=0 \\ Ae=1 \end{cases} \begin{cases} A=1 \\ B=-\frac{1}{2} \\ C=\frac{1}{2} \\ B=-\frac{1}{2} \end{cases}$$

$$\begin{cases} B+C=0 \\ C=\frac{1}{2} \\ B=-\frac{1}{2} \end{cases}$$

$$\frac{Y(z)}{Z} = \frac{1}{z^2} + \frac{-\frac{1}{2}}{z^{-1}} + \frac{\frac{1}{2}}{z^{+1}}$$

$$Y(z) = z^{-1} - \frac{1}{z} \frac{1}{1-z^{-1}} + \frac{1}{2} \frac{1}{1+z^{-1}}$$

$$\frac{Y(3)}{Z} = \frac{1}{Z^{2}(Z-1)(Z+\beta)}$$

$$\frac{A}{Z} + \frac{B}{Z^{2}} + \frac{C}{Z-1} + \frac{D}{Z+\beta}$$

$$\frac{Z+\beta}{Z+\beta} + \frac{C}{Z-1} + \frac{D}{Z+\beta}$$

改进:试根法、救末

$$(AZ+B)(Z-1)(Z+\beta) + CZ^{2}(Z+\beta)+pZ^{2}(Z+\beta)$$

$$=(AZ+B)(Z^{2}+\beta Z-Z-\beta)+C(Z^{3}+\beta Z^{2})+p(Z^{3}-Z^{2})$$

$$=(AZ^{3}+A\beta Z^{2}-AZ^{2}-AZ^{2}-ABZ+BZ^{2}+BZ^{2}-BZ-BZ)$$

$$+C(Z^{3}+\beta Z^{2})+p(Z^{3}-Z^{2})$$

$$fron(4)$$
 $B=-\frac{1}{B}$

from (3)
$$A = \frac{B - B\beta}{\beta} = \frac{B(1-\beta)}{\beta} = \frac{1-\beta}{\beta^2} = \frac{\beta^2}{\beta^2}$$
from (1)

$$\frac{Y(2)}{Z} = \frac{A}{Z} + \frac{B}{Z^{2}} + \frac{C}{Z-1} + \frac{D}{Z+\beta}$$

$$Y(2) = \frac{1-\beta}{\beta^{2}} - \frac{1}{\beta} Z^{-1} + \frac{1}{1+\beta} \frac{1}{1-Z-1} - \frac{1}{\beta^{2}(\beta+1)} \frac{1}{1+\beta Z^{-1}}$$

$$Y(k) = \frac{1-\beta}{\beta^{2}} S_{0}(k) - \frac{1}{\beta} S_{0}(k-1) + \frac{1}{1+\beta} I(k) - \frac{1}{\beta^{2}(\beta+1)} (-\beta)^{k}.$$

$$Y(k) = \begin{cases} \frac{1-\beta}{\beta^{2}} + \frac{1}{1+\beta} - \frac{(-\beta)^{k}}{\beta^{2}(\beta+1)} & k=0 \\ -\frac{1}{\beta} + \frac{1}{1+\beta} - \frac{(-\beta)^{k}}{\beta^{2}(\beta+1)} & k=1 \end{cases} \quad Y(1) = 0$$

$$Y(2) = 0$$

$$y(k) = \begin{cases} 0 & k=0,1,2 \\ \frac{1}{1+\beta} - \frac{(-\beta)^k}{\beta^2(\beta+1)} & k \ge 2 \end{cases}$$

$$k \ge 2 \qquad k = 3, 4,5;$$
(c) $\beta \Rightarrow y(k)$ convergence?

Solution

Then $|\beta| < 1$, $k \Rightarrow \infty$, $(-\beta)^k \Rightarrow 0$

$$y(k) \Rightarrow \frac{1}{1+\beta} \quad |\beta| < 1$$
, $k \Rightarrow \infty$, $(-\beta)^k \Rightarrow 0$

$$y(k) \Rightarrow \frac{1}{1+\beta} \quad |\beta| < 1$$
The Final Value Theorem applies
all soles of $y(2)$ lie in side the unit

all poles of Y(2) lie in side the unit circlue, with the possible exception of a simple pole at Z=1

Verification: limy(2)=lim(1-2-)Y(2)= 1

From Z=1

So confirm theorem acceptable.

(2) When [p+2] | = | (-p) k oscillates between ±1

y(k) doesn't converge, it oscillates

The Final value Theorem does not apply

when $\beta = -1$ $\frac{1}{1+\beta} - \frac{(-\beta)^k}{\beta^2(\beta+1)} = \frac{\beta^2 - 1}{\beta^2(1+\beta)} = \frac{(\beta+1)(\beta-1)}{\beta^2(1+\beta)}$

 $= \frac{\beta - 1}{\beta^2} = \frac{-2}{1} = -2$ $(-\beta)^k \text{ grows without bound}$ $y(b) \text{ diverges as } k \to \infty$ The Final value Theorem does not apply

关于(a) & transform 编思考,前面用定义主的&-transform 现在试用表求,

Solution

$$= \frac{1}{1-Z^{-1}} + \frac{Z^{-1} \sin z T}{1-2 Z^{-1} \cos z T + Z^{-2}} \qquad T = \frac{1}{z}$$

查不出来用定义

结论:分段用定义

不会外

关于23-01-6 对ABCD的优化:试银法

Solution

$$= \frac{A}{2} + \frac{B}{2^2} + \frac{C}{2-1} + \frac{D}{2+\beta}$$

 $A = (2-1)(8+\beta) + B(2-1)(2+\beta) + C = (2+\beta) + D = (2-1) = 1$ 由于等式过于复杂,所以可以采用 i式 根法

ABCD对于EER都成立,所以代入已值中ABCD

$$02=0, -\beta\beta = 1 \implies \beta = -\frac{1}{\beta}$$

①
$$Z = | , (\beta+1)(=| => C = \frac{1}{\beta+1})$$

$$(32 = -\beta, \beta^{2}(-\beta-1)) = 1 = D = \frac{-1}{\beta^{2}(\beta+1)}$$

●考虑 ≥3 项 汞A

$$AZ^{3} + CZ^{3} + DZ^{3} = (A + C + D)Z^{3}$$

=>
$$A = -C - D = -\frac{1}{\beta+1} + \frac{1}{\beta^2(\beta+1)}$$

$$=\frac{1-\beta^2}{\beta^2(\beta+1)}$$

$$= \frac{(1-\beta)(1+\beta)}{\beta^2(\beta+1)}$$

$$= \frac{1-\beta}{\beta^2}$$