23 - S(-Qq
(a) (i)
$$k? \rightarrow Z_{12} = 0.9 \pm j0.1$$

Solwein: $k = [01]$ Wc $[-]$

$$d_0(z) = z^2$$

$$do(A) = A^2 = \begin{bmatrix} 4 - 1 \\ 2 & 0 \end{bmatrix}^2 = \begin{bmatrix} 14 & -47 \\ 8 & -2 \end{bmatrix}$$

$$W_{0} = \begin{bmatrix} C \\ CA \end{bmatrix} = \begin{bmatrix} 2 & 1 \\ 0 & -2 \end{bmatrix}$$

$$CA = \begin{bmatrix} 2 & 1 \end{bmatrix} \begin{bmatrix} 4 & -1 \\ 2 & 0 \end{bmatrix}$$

$$W_{0}^{-1} = \begin{bmatrix} \frac{1}{7} & \frac{1}{4} \\ \frac{5}{7} & -\frac{1}{7} \end{bmatrix} \in \begin{bmatrix} 0.1428 & 0.0714 \end{bmatrix} = \begin{bmatrix} 10 & -2 \end{bmatrix}$$

$$\begin{bmatrix} 0 = \begin{bmatrix} 14 & -4 \\ 8 & -2 \end{bmatrix} \begin{bmatrix} \frac{1}{7} & \frac{1}{4} \\ \frac{5}{7} & -\frac{1}{7} \end{bmatrix} \begin{bmatrix} 0 \\ 1 \end{bmatrix} = \begin{bmatrix} \frac{11}{7} \\ \frac{6}{7} \end{bmatrix} = \begin{bmatrix} 1.5714 \\ 0.8571 \end{bmatrix}$$

$$= \begin{bmatrix} \overline{z} - 4 & 1 \\ -2 & \overline{z} \end{bmatrix} + \begin{bmatrix} 1 \\ 0 \end{bmatrix} \begin{bmatrix} 2.2 & -0.59 \end{bmatrix}$$

$$Y(z) = \frac{1}{2} \frac{z^{2}+2}{z^{2}-1.8z+0.8z} \quad R(z)$$

$$\lim_{z \to A} y(z) = \lim_{z \to 1} (1-z^{1}) \quad Y(z)$$

$$= \lim_{z \to 1} (1-z^{1}) \quad \frac{z^{2}+2}{z^{2}-1.8z+0.8z} \quad \frac{1}{1-z^{-1}}$$

$$= \frac{4}{1-1.8+0.8z}$$

$$= 200 \quad kr$$

$$So \quad 200 \quad kr = 1 \quad kr = 0.005$$

$$(a) \quad (i) \quad (0: optimal \quad control \quad law \quad min \quad j \quad ?$$

$$So \quad (1i) \quad (0: optimal \quad control \quad law \quad min \quad j \quad ?$$

$$So \quad (1i) \quad (1i)$$

$$S = 45 + 1 - \frac{365^{2}}{95 + 5}$$

$$-35 = 1 - \frac{365^{2}}{75 + 5}$$

$$-35(95 + 5) = 95 + 5 - 365^{2}$$

$$365^{2} - 275^{2} - 155 - 95 - 5 = 0$$

$$95^{2} - 245 - 5 = 0$$

$$S_{12} = \frac{4 \pm \sqrt{21}}{3}$$

$$S_{1} = 2.8609$$

$$S_{2} = 2.8609$$

$$S_{3} = 2.8609$$

$$S_{4} = 2.8609$$

$$S_{5} = 2.8609$$

$$S_{5$$

(ii) $x(k+1) = 2x(k) - 3x0.5583 \times (k)$ $= 0.3251 \times (k)$ gince [0.3251|<1], x(k) converges to zero $for \qquad x(0) \neq 0$ So, the final value of x(k) = 0