Solution

Justify: Yes, because it is defined for all real values oft and the function xxt) provides a specific value for everytime t in the real number domain, fulfilling the definition of a continuous-time signal or defined over a continuous range of time

@amplitude of continuous range of value or discrete values

可以直接用表格算

$$2\left\{e^{-2t}\operatorname{sin}\left(\frac{z}{z}t\right)+1\right\} \qquad \left|\begin{array}{c|c} 16. & \frac{\omega}{(s+a)^2+\omega^2} & e^{-at}\sin\omega t & \frac{e^{-akT}\sin\omega kT}{1-2e^{-aT}z^{-1}\cos\omega T+e^{-2aT}z^{-2}} \end{array}\right|$$

$$= \frac{z^{-1} \sin \frac{z}{z} T}{\left[-2z^{-1} \cos \frac{z}{z} T + z^{-2}\right]_{z=2e^{2}}} + \frac{1}{1-z^{-1}}$$

$$= \frac{z^{-1} \frac{\sqrt{z}}{z}}{\left[-2z^{-1} \frac{\sqrt{z}}{z} + \overline{z}^{2}\right]_{z=2e^{2}}} + \frac{1}{1-z^{-1}}$$

$$= \frac{\sqrt{2}}{2e} 2^{-1}$$

$$1 - \frac{\sqrt{2}}{e} 2^{-1} + \frac{1}{e^2} 2^{-2} + \frac{1}{1 - 2^{-1}}$$

the pole at 0.2601 ± j0.2601, I within the unit circle and with a possible exception of a simple pole at 2 = 1 fulfill the final Value Theorem

$$\lim_{k \to \infty} \chi(k) = \lim_{z \to 1} (1 - z^{-1}) \chi(z)$$

$$= \lim_{z \to 1} \frac{1 - 0.2602 z^{-1} - 0.1248 z^{-2}}{1 - 0.5203 z^{-1} + 0.1353 z^{-2}}$$

(b) Solve?
$$\lim_{z \to \infty} x(kT)$$
?

Solution

apply 2 transform
 $x(k+2) - x(k) = |(k)$
 $z^2 \ \chi(z) - z^2 \ \chi(z) - z \ \chi(1) - \chi(2) = 1 - z - 1$
 $|e + k = -2 \ \chi(0) - x(-2) = |(-2) \ = | \chi(0) = 0$
 $|e + k = -1 \ \chi(1) - \chi(-1) = |(-1) \ \Rightarrow \chi(1) = 0$
 $|e + k = -1 \ \chi(2) = \frac{1}{|-z^{-1}|}$
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$$\begin{cases}
 A + C = 0 \\
 B - 2C = 0
 \end{cases}
 = \frac{1}{2}$$
 $\begin{cases}
 A = -\frac{1}{4} \\
 B = \frac{1}{2}
 \end{cases}$
 $\begin{cases}
 C = \frac{1}{4}
 \end{cases}$

$$\frac{\chi(z)}{z} = \frac{-\frac{1}{4}}{z-1} + \frac{\frac{1}{z}}{(z-1)^2} + \frac{\frac{1}{4}}{z+1}$$

$$X(z) = -\frac{1}{4} \frac{1}{1-z^{-1}} + \frac{1}{z} \frac{z^{-1}}{(1-z^{-1})^{-1}} + \frac{1}{4} \frac{1}{1+z^{-1}}$$

apply inverse & transform # 3 #5 # 18

$$X(kT) = -\frac{1}{4}I(k) + \frac{1}{2}k + (-1)^{k} + \frac{1}{4}ik$$

$$X(S) = \frac{(S-1)(S_{J}-1)}{S}$$

the pole at Z=1, Z=-1, Z=1

z=- is not within the unit circle,

So it can't apply the Final value Theorem

$$X(kT) = -\frac{1}{4} ((k) + \frac{1}{2} k + (-1)^{k}$$