Problem 6.2

Ans:
$$E(T_0) = E(T_1) = E(T_2) = 1$$

$$P(n) = P^n = \begin{cases} P^2, & n \text{ even} \\ P, & n \text{ odd} \end{cases}$$

Problem 6.3

Ans: The steady-state probabilities of states 0, 1 and 2 are 0.4, 0.4 and 0.2 respectively.

Problem 9.4

Ans:
$$Q = \begin{bmatrix} -s & s & 0 \\ p & -(p+f) & f \\ (1-q)r & qr & -r \end{bmatrix}$$

Rate balance equations:

$$\pi_2(1 - q)r + \pi_1 p = \pi_0 s$$

$$\pi_0 s + q r \pi_2 = \pi_1 (p + f)$$

$$\pi_1 f = \pi_2 [qr + (1 - q)r]$$

$$\pi_0 + \pi_1 + \pi_2 = 1$$

$$\pi_0 = \frac{r[p + (1-q)f)]}{rp + rf(1-q) + rs + fs}$$

$$\pi_1 = \frac{rs}{rp + rf(1-q) + rs + fs}$$

$$\pi_2 = \frac{fs}{rp + rf(1-q) + rs + fs}$$

$$R = \pi_1 p = \frac{rsp}{rp + rf(1-q) + rs + fs}$$