

23-S1-Q3

Q(a) state. ? p?

$$S = \{0, 1, 2\}$$

$$P_{00} = P\{B_k \geq 2\} = 1 - P\{B_k = 1\} - P\{B_k = 0\}$$

$$= 1 - \frac{e^{-0.1}(0.1)^1}{1!} - \frac{e^{-0.1}(0.1)^0}{0!} = 1 - 1.1e^{-0.1}$$

$$P_{01} = P(B_k = 1) = 0.1e^{-0.1}$$

$$P_{02} = P(B_k = 0) = e^{-0.1}$$

$$P_{10} = P(B_k \geq 2) = 1 - 1.1e^{-0.1}$$

$$P_{11} = P(B_k = 1) = 0.1e^{-0.1}$$

$$P_{12} = P(B_k = 0) = e^{-0.1}$$

$$P_{20} = 1 - 1.1e^{-0.1} \quad P = \begin{bmatrix} 1 - 1.1e^{-0.1} & 0.1e^{-0.1} & e^{-0.1} \\ 1 - 1.1e^{-0.1} & 0.1e^{-0.1} & e^{-0.1} \\ 1 - 1.1e^{-0.1} & 0.1e^{-0.1} & e^{-0.1} \end{bmatrix}$$

$$P_{21} = 0.1e^{-0.1}$$

$$P_{22} = e^{-0.1}$$

$$(b) E(T_0) = \frac{1}{1 - P_{00}} = \frac{1}{1.1e^{-0.1}} = 1.0047$$

$$E(T_1) = \frac{1}{1 - P_{11}} = \frac{1}{1 - 0.1e^{-0.1}} = 1.0995$$

$$E(T_2) = \frac{1}{1-p_{22}} = \frac{1}{1-e^{-0.1}} = 10.5083$$

$$\text{mean } E(T_i) = \frac{1}{3} [E(T_0) + E(T_1) + E(T_2)] = 4.2042$$

没有这种概念

state \geq stays longer than 0 and 1

No surprise

comment: $\lambda = 0.1$ is a small number

so the usage rate is low and
the replenishment policy reset the
number of spare bulks to 2 whenever

there is a shortfall

(c) independent of previous state

$$\pi_0 = 1 - 1.1e^{-0.1}$$

$$\pi_1 = 0.1e^{-0.1}$$

$$\pi_2 = e^{-0.1}$$

$$(d) P(U_{k+1} = 1) = \pi_1 = 0.1e^{-0.1}$$