23-SI-Q2
Q: 
$$V = 98 \text{ cm}^3$$
  $L = 2H$  closed. \$10/cm\$

(a) Q: leagh  $x_1$  breadth  $x_2$  cost  $z = ?$ 

Solution  $z = lox[2x(x_1x_2 + 0.4x_1^2 + 0.4x_1x_2)]$  of the subject to  $v = x_1 \cdot x_2 \cdot \frac{x_1}{25} = 0.4x_1^2 x_2 = 98$ 

Where  $z = 20 \times (1.4x_1 \cdot x_2 + 0.4x_1^2)$ 

$$= 28x_1x_2 + 8x_1^2$$

$$x_1^2 x_2 = 245$$

$$x_1x_2 > 0$$

So  $z = 28x_1x_2 + 8x_1^2$ 

$$x_1x_2 > 0$$

(b) apply lagrange multipliers

Solution  $v = x_1^2 x_2 - 245$ 

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(b) apply lagrange multipliers

Solution  $v = x_1^2 x_2 - 245$ 

$$x_1 \cdot x_2 > 0$$

(c)  $v = x_1^2 x_2 - 245$ 

$$v = x_1^2 x_2 - 245$$

$$\begin{cases} \frac{\partial L}{\partial x_{1}} = 28 X_{2} + 16 X_{1} + 2 \lambda X_{1} X_{2} = 0 & (1) \\ \frac{\partial L}{\partial x_{2}} = 28 X_{1} + \lambda X_{1}^{2} = 0 & (2) \\ \frac{\partial L}{\partial \lambda} = 3 X_{1}^{2} X_{2} - 245 = 0 & (3) \end{cases}$$

$$from (3) \quad X_{1} = -28 \quad \Rightarrow \quad X_{1} = -\frac{28}{\lambda} \quad \Rightarrow \quad \lambda = \frac{-28}{X_{1}}$$

$$from (3) \quad X_{1} = \frac{245}{X_{1}^{2}} = \frac{245}{X_{1}^{2}} = \frac{5}{16} \lambda \quad \text{into (1) get}$$

$$from (1) \quad 22x \frac{1}{16} \lambda^{2} + 16(-\frac{28}{\lambda}) + 2\lambda (-\frac{28}{\lambda}) \frac{1}{16} \lambda^{2} = 0$$

$$\frac{27}{4} \lambda^{2} - \frac{448}{\lambda} - \frac{25}{\lambda} \lambda^{2} = 0 \quad 4 X_{1}^{3} = 245$$

$$\lambda_{1,2} = \frac{5 \pm 3 \sqrt{145}}{5} \quad \times \lambda_{1} = 7.5405$$

$$\lambda_{1} = 8.1250 \quad \lambda_{2} = -6.2250$$

$$-8.75 \lambda^{3} = 448$$
  
 $\lambda^{3} = -51.2$   
 $\lambda = -3.7133$ 

$$\pi_{1} = -\frac{28}{\lambda} = 7.5405$$

$$\pi_{2} = \frac{5}{16} \lambda^{2} = 4.3087$$

$$\cos \xi = 28x_{1}x_{2} + 8x_{1}^{2} = 1364.6284$$

So 
$$\chi_1 = 7.5405$$
  
 $\chi_2 = 4.3089$   
 $\chi = -3.7133$   
min cost  $z = 1364.6284$ 

Test of Optimum

let 
$$h(x) = x_1^2 x_2 - 245 = 0$$
 $\frac{\partial h(x)}{\partial x_1} = 2x_1 x_2$ 
 $\frac{\partial h(x)}{\partial x_2} = x_1^2$ 
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 $\frac{\partial h(x)}{\partial x_1} = x_$ 

$$\nabla x^{2} = \begin{bmatrix} \frac{3}{2} \\ \frac{3}{2} \\ \frac{3}{2} \\ \frac{3}{2} \end{bmatrix}$$

$$\frac{3L}{3x_{1}} = 28x_{2} + 16x_{1} + 2\lambda x_{1} \times 2 = 0 \qquad x_{1} = 7.5405$$

$$\frac{3L}{3x_{1}} = 28x_{1} + \lambda x_{1}^{2} = 0 \qquad x_{2} = 4.3089$$

$$\frac{3L}{3x_{2}} = 28x_{1} + \lambda x_{1}^{2} = 0 \qquad \lambda = -3.7133$$

$$\frac{3L}{3x_{1}} = 16 + 2\lambda \times 2 = -16$$

$$\frac{3L}{3x_{1}} = 28 + 2\lambda x_{1} = -28$$

$$\frac{3L}{3x_{1}} = 28 + 2\lambda x_{1} = -28$$

$$\frac{3L}{3x_{1}} = 0 \qquad x_{1} = -16 < 0$$

$$\nabla x_{1} = -16 < 0$$

$$\nabla x_{2} = -16 < 0$$

$$A_{2} = 0 - 28^{2} < 0$$
So  $\nabla x_{1} = 0 = 0$ 

$$x_{2} = 0 - 28^{2} < 0$$
So  $\nabla x_{1} = 0 = 0$ 

$$x_{1} = -16 < 0$$

$$x_{2} = 0 - 28^{2} < 0$$

$$x_{3} = 0 = 0$$

$$x_{4} = -16 < 0$$

$$x_{5} = 0 = 0$$

$$x_{1} = -16 < 0$$

$$x_{2} = 0 - 28^{2} < 0$$

$$x_{3} = 0 = 0$$

$$x_{4} = 0 = 0$$

$$x_{5} = 0$$

$$x$$

So the Z isn't optimal minimum ref > 3. understand > 2

Solution

$$SV = -0.05 \times 98 = -4.9 \text{ cm}^3$$
  
 $V_{new} = 98-4.9 = 93.1 \text{ cm}^3$   
 $N_{ew} = 98-4.9 = 93.1 \text{ cm}^3$   
 $N_{ew} = 232.71 = 232.71$   
 $Constrain change  $B = 232.71 - 240 = -12.25$   
 $V_{new} = V_{ord} - DB \lambda$   
 $V_{new} = V_{ord} - DB \lambda$$