典型的全连接层神经网络的输入和输出用x = [x1, x2, ···]表示。

, X100]7和y = [y1, y2, ···, y98]7。 在该层中应用线性激活函数,连接输入和输出的网络参数由大小为98×100的矩阵W =[Wij]和98维向量 θ =[θ1, θ1, ···] , θ98]T3. The inputs and outputs of a typical fully-connected layer of neural network are denoted

The inputs and outputs of a typical fully-connected layer of neural network are denoted by  $\mathbf{x} = [x_1, x_2, ..., x_{100}]^T$  and  $\mathbf{y} = [y_1, y_2, ..., y_{98}]^T$ . A linear activation function is applied in this layer and the network parameters to connect the inputs and outputs are given by a matrix  $\mathbf{W} = [w_{ij}]$  of size  $98 \times 100$  and a 98-dimensional vector  $\mathbf{\theta} = [\theta_1, \theta_1, ..., \theta_{98}]^T$ .

- (a) (i) Express the outputs in term of inputs in vector-matrix form and scalar form. 用向量矩阵形式和标量形式表示输入的输出。
  - (ii) Compute the numbers of trainable parameters, multiplications and summations required in this layer to compute the outputs from the inputs. 计算可训练参数的数量,这一层需要的乘法和求和来计算输入的输出。
  - (iii) What is the ratio of the number of outputs to the number of trainable parameters?

输出的数量与可训练参数的数量之比是多少?

(12 Marks)

将该层替换为卷积神经网络层,该层有20个可学习的过滤器,大小为3,具有可训练的参数,[] 这将生成20个输出特征映射,用[]表示。 在这一层中应用线性激活函数。

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- (b) Replace this layer by a convolutional neural network layer that has 20 learnable filters of size 3 with trainable parameters,  $\mathbf{w}^k = [w_{-1}^k, w_0^k, w_1^k]^T$  and  $\theta^k, 1 \le k \le 20$ . This generates 20 output feature maps, denoted by  $\mathbf{y}^k = [y_2^k, y_3^k, \dots, y_{99}^k]^T, 1 \le k \le 20$ . A linear activation function is applied in this layer.
  - (i) Express the outputs in term of inputs in scalar form. 用标量形式表示输入的输出。
- (ii) Compute the number of trainable parameters, multiplications and summations required in this layer to compute the outputs from the inputs. 计算可训练参数的数量,这一层需要的乘法和求和来计算输入的输出。
  - (iii) What is the ratio of the number of outputs to the number of trainable parameters?

输出的数量与可训练参数的数量之比是多少?

(13 Marks)

(a)(i) Q: vector - matrix form and scalar form input and output?

# scalar form

$$y_{i} = \frac{2}{2} w_{ij} x_{j} + 0i \qquad i = [,2,-9] \qquad \begin{bmatrix} 0.5 & 7.8 \\ 1.8 & 0.0 \\ 0.2 & 1.3 \end{bmatrix} \begin{bmatrix} 0.3 \\ 0 \\ 0.2 \end{bmatrix} + \begin{bmatrix} -1 \\ 1 \\ 0 \end{bmatrix} = \begin{bmatrix} 1.2 \\ 1.3 \\ 2.2 \end{bmatrix}$$

(ii) Q parameters? multiplications? summations?

#### Neural Networks and Deep CNN -- Neuron Model

In mathematical terms, we can describe the neuron as: 用版学本版。我们可以称种形式

$$u_k = \sum_{i=1}^p w_{kj} x_j \qquad y_k = f(u_k - \theta_k)$$

Where  $x_1, x_2, ..., x_p$  are the input signals,  $w_{k1}, w_{k2}, ..., w_{kp}$  are the synaptic weights of neuron k,  $u_k$  is the linear combiner output,  $\theta_k$  is the threshold, f(.) is the activation function and  $y_k$  is the neurons  $\theta_k$  is an external parameter, we can consider this parameter as an input variable: ०४६-०४४४४ स्थान

Then we have: 
$$x_0 = 1$$
,  $w_{k0} = -6$ 

#### Output after FC layer

$$= \begin{bmatrix} 0 & 3 & 7 & 8 \\ 1 & 8 & 0 & 0 \\ 0 & 8 & 1 & 0 \end{bmatrix} \begin{bmatrix} 0.3 \\ 0 \\ 0.2 \\ 0.1 \end{bmatrix} + \begin{bmatrix} -1 \\ 1 \\ 0 \end{bmatrix} = \begin{bmatrix} 1.2 \\ 1.3 \\ 2.2 \end{bmatrix}$$

## Solution

parameters: 98×100+98=9898

multiplications: 98×100 = 9800

summations: 98 x (99+1) =9800

### 助教回复

Here theta is the bias. Please note that in this questions theta is a 98 dimensional vector. While in the slides, theta is a scalar.

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Liii) 6: ratio

$$y_{i}^{(k)} = W_{-1}^{(k)} X_{i+1} + W_{0}^{(k)} X_{i} + W_{1}^{(k)} X_{i-1} + O^{(k)}$$

(b)(i) 
$$y_{i}^{(k)} = w_{-1} \times i_{-1} + w_{0}^{(k)} \times i_{1} + w_{1}^{(k)} \times i_{1} + o_{1}^{(k)}$$

$$z = 1/2$$
,  $z = 1/2$ 

(ii) parameters: 
$$20 \times (3+1) = 80$$
  
multiplications:  $3 \times 98 \times 20 = 5880$ 

(iii) 
$$Ratio = \frac{98 \times 20}{80} = 24.5$$

20分分数重十八个bias) 新兴乘3次,4897 共20个

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