

1. Constrained Optimization Problem 2. Free Optimization Problem

Recap of the Four Options

3. Constraint Satisfaction Problem

4. No Problem

constraints.

1)

2)

non-attacking.

Option 4

Below is a concise way to see why each of the four questions maps to either a **Constraint**

Satisfaction Problem or a Constrained Optimization Problem (and not to a "free

Thought about N-Queens problem types for 1m 44s

optimization" or "no problem"):

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- variables (for instance, optimizing a function f(x) over \mathbb{R} with no strict constraints).
- But N-Queens always imposes the constraint that queens must be placed on discrete board squares, plus we care about "non-attacking." Hence, none of these is truly "free" of
- Why not "No Problem" (Option 4)? Clearly, each question does pose a nontrivial problem.

Understanding CSP vs. Constrained Optimization

1. A Constraint Satisfaction Problem (CSP) requires all constraints to be satisfied exactly.

In the classic N-Queens, that means no two queens attack each other (i.e., 0 conflicts).

Or we have a cost/objective function we want to optimize (minimize or maximize),

Why not "Free Optimization Problem" (Option 2) in any of these?

A *free* optimization problem would have *no* real constraints beyond the bounds of the

2. A Constrained Optimization Problem (COP) arises when: We can tolerate partial satisfaction of constraints (e.g., "at least 7 non-attacking," rather than 8).

subject to various constraints.

Analysis of Each Question

"Find a configuration of 8 queens with at least 7 queens that are non-attacking."

We do not require a perfect (8/8) non-attacking solution; rather, we insist on at least 7

We are effectively relaxing the constraint and aiming to "optimize" (or at least to meet a

threshold) the number of non-attacking queens. Hence, this is a **Constrained Optimization Problem** (Option 1).

"Find a configuration of 8 queens where all the queens are non-attacking."

That is the textbook example of a **Constraint Satisfaction Problem** (Option 3).

This is the classical N-Queens requirement: all queens must be pairwise non-attacking.

There is no "maximize" or "minimize" objective here; the problem is simply "do not

This is not a pure "all-or-nothing" CSP (which would demand 8/8).

violate the (attack) constraints at all."

"Assume that you start off with a random configuration of 8 queens. You are allowed only one move for each queen and the extent of the movement of each queen should be minimized. Reposition the 8 queens such that the total number of steps moved is

3)

minimum and the number of non-conflicting queens is maximized." Here, there are two objectives under constraints:

Because we have explicit constraints on movement (one move per queen, must stay on

"Given a partial configuration of 4 queens in half the chess board, find the positions

of the remaining 4 queens whereby the number of non-conflicting queens is

the board, etc.) and an objective (or objectives) to optimize, this is a Constrained

1. Minimize total steps (sum of how far each queen moves).

2. Maximize the number of non-conflicting queens.

Optimization Problem (Option 1).

- 4)
 - maximized." We already have 4 queens placed (presumably immovable) and must place the
 - Again, that is an objective (maximize non-conflicting) under constraints (fixed squares for the first 4 queens, standard "no-attack" rules, limited board squares).

We want to maximize how many queens remain non-attacking once all 8 are on the

board (i.e., partial satisfaction is allowed if it's impossible to get 8/8 conflict-free).

Final "Best-Fit" Answers

Hence, this too is a **Constrained Optimization Problem** (Option 1).

Putting it all together:

1. Q1 (at least 7 non-attacking)

remaining 4.

- → Constrained Optimization Problem (Option 1) 2. **Q2** (all 8 non-attacking)
 - → Constraint Satisfaction Problem (Option 3)
- 3. Q3 (minimize total movement, maximize non-conflicts) → Constrained Optimization Problem (Option 1)
- 4. Q4 (complete partial configuration to maximize non-conflicts) → Constrained Optimization Problem (Option 1)
- **Short version** • Q1: X 3
 - Q2: 3 Q3: 1 • Q4:X(}

Because (2) "free optimization" and (4) "no problem" are not appropriate for any of these questions.

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