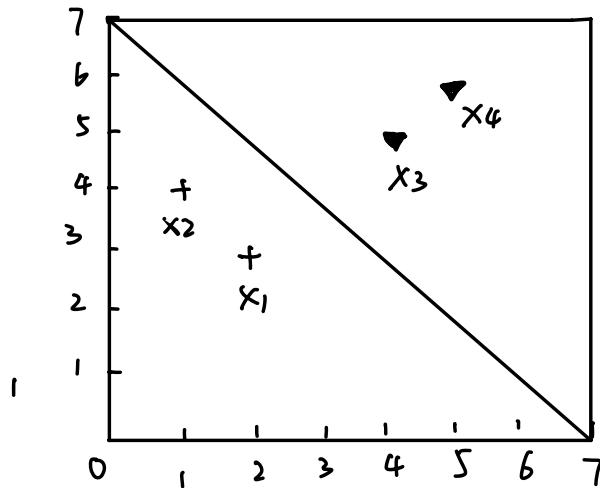


22-S1-03

Q: (a) SVM

(i) decision boundary



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② we denote $x_1(2,3)$ $x_2(1,4)$ $x_3(4,5)$ $x_4(5,6)$

we consider x_1, x_2, x_3 are support vector

we have $\lambda_1, \lambda_2, \lambda_3 \neq 0$

$$\sum_{i=1}^N \lambda_i y_i = 0$$

$$\lambda_1 + \lambda_2 - \lambda_3 = 0$$

$$w = \sum_{i=1}^N \lambda_i y_i x_i$$

$$\begin{pmatrix} w_1 \\ w_2 \end{pmatrix} = \lambda_1 \begin{pmatrix} 2 \\ 3 \end{pmatrix} + \lambda_2 \begin{pmatrix} 1 \\ 4 \end{pmatrix} - \lambda_3 \begin{pmatrix} 4 \\ 5 \end{pmatrix}$$

$$(w_1, w_2) \begin{pmatrix} 2 \\ 3 \end{pmatrix} + b = 1 \quad (1)$$

$$(w_1 w_2) \begin{pmatrix} 1 \\ 4 \end{pmatrix} + b = 1 \quad (2)$$

$$(w_1 w_2) \begin{pmatrix} 4 \\ 5 \end{pmatrix} + b = -1 \quad (3)$$

$$(1)(2)(3) \rightarrow w = \begin{pmatrix} -\frac{1}{2} \\ -\frac{1}{2} \end{pmatrix} \quad b = \frac{7}{2}$$

$$-\frac{1}{2}x_1 - \frac{1}{2}x_2 + \frac{7}{2} = 0$$

$$x_1 + x_2 = 7$$

$$d = \frac{2}{\|w\|} = \frac{2}{\sqrt{\frac{1}{4} + \frac{1}{4}}} = 4\sqrt{2}$$

③ The linear decision boundary leads to max margin because SVM selects the hyperplane that max the distance between itself and the support vectors.

This is achieved by min $\|w\|$ resulting the widest margin, $\frac{2}{\|w\|}$

(ii) Support vector : $x_1(2,3)$ $x_2(1,4)$ $x_3(4,5)$

Reason ① They satisfy the Karush-Kuhn-Tucker condition $\alpha_i > 0$

② Removing or moving any one of them would

change the optimal hyper-plane.

Relocating x_1 would not.

(b) (i) ① sharing parameters slashing memory

② much lower risk of over-fitting

③ retaining the receptive-field hierarchy

(ii) ① Prevents Overfitting: By randomly omitting neurons, the network cannot rely too heavily on specific features, forcing it to learn more robust and generalized representations

② Acts as an Ensemble Method: During training, different sub-networks are trained due to the randomness of dropped neurons

③ method: the outputs should be multiple $(1-p)$

ciii) Data augmentation

- ① Data augmentation increases the diversity of training data, helping the model generalize better without reducing complexity
- ② Early stopping and dropout both reduce model capacity, so they trade variance for higher bias