

22-S1-Q2

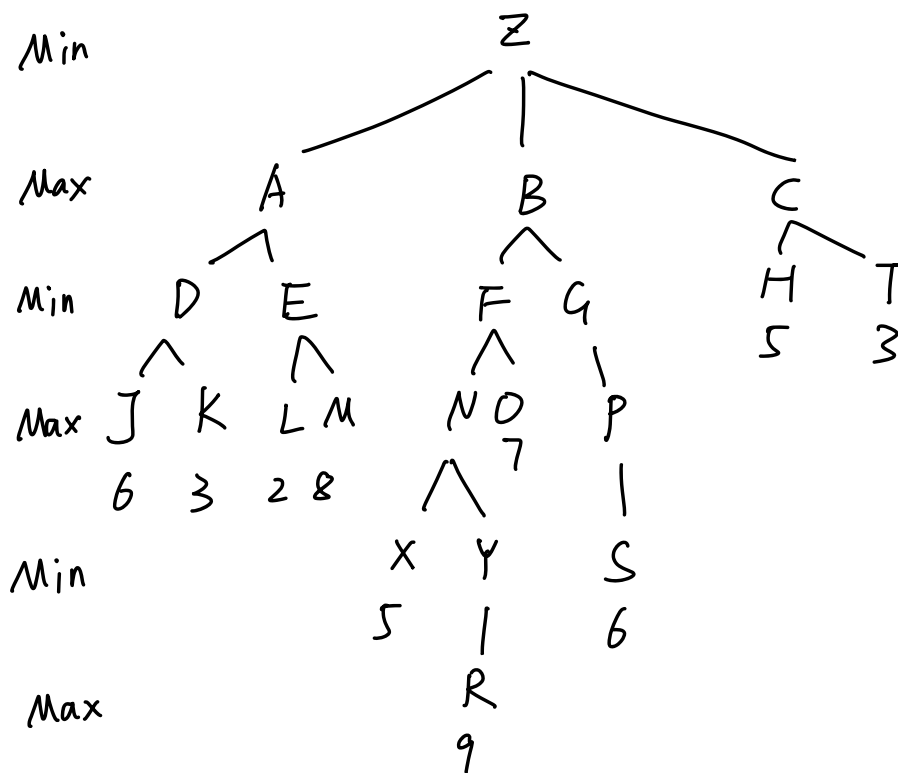
Q (a) first - min

(i) choose of ABC

(ii) left - to - right α β pruning

list no examined node

(iii) reduce computation cost in α - β
2 factors compare: min max



(b) 2-1-21 ReLU bias = 1.0 $\eta = 0.5$

(i) O_3 O_4 O_5 O_6 $\pi = (1, 0)$

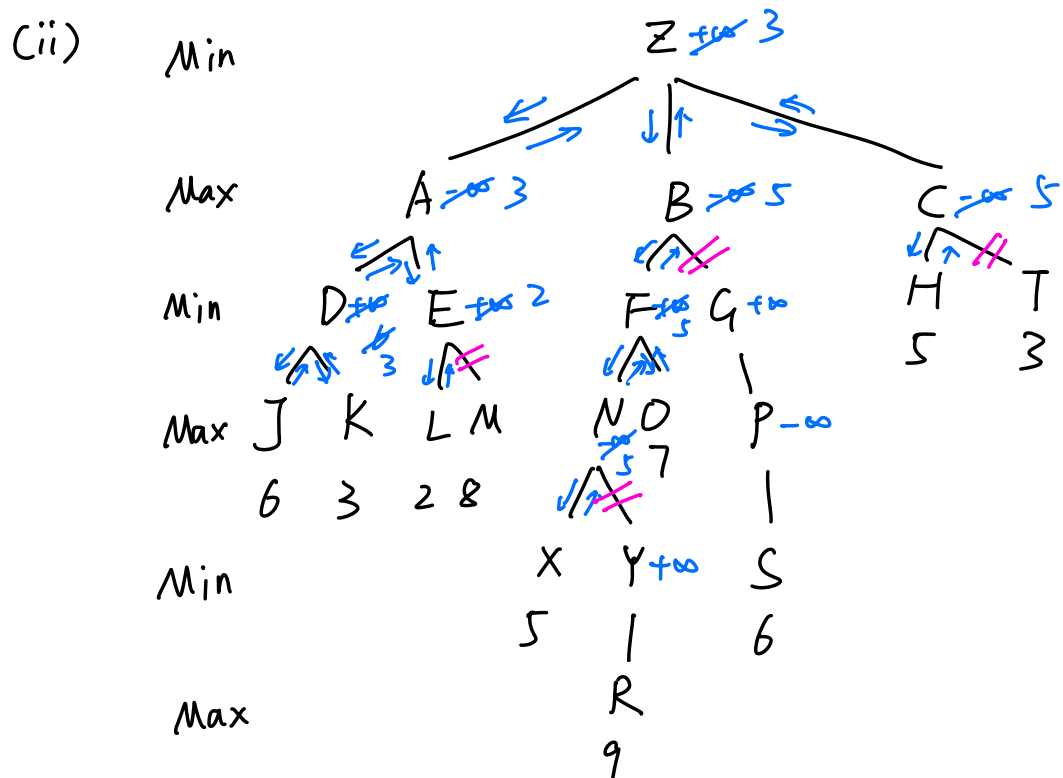
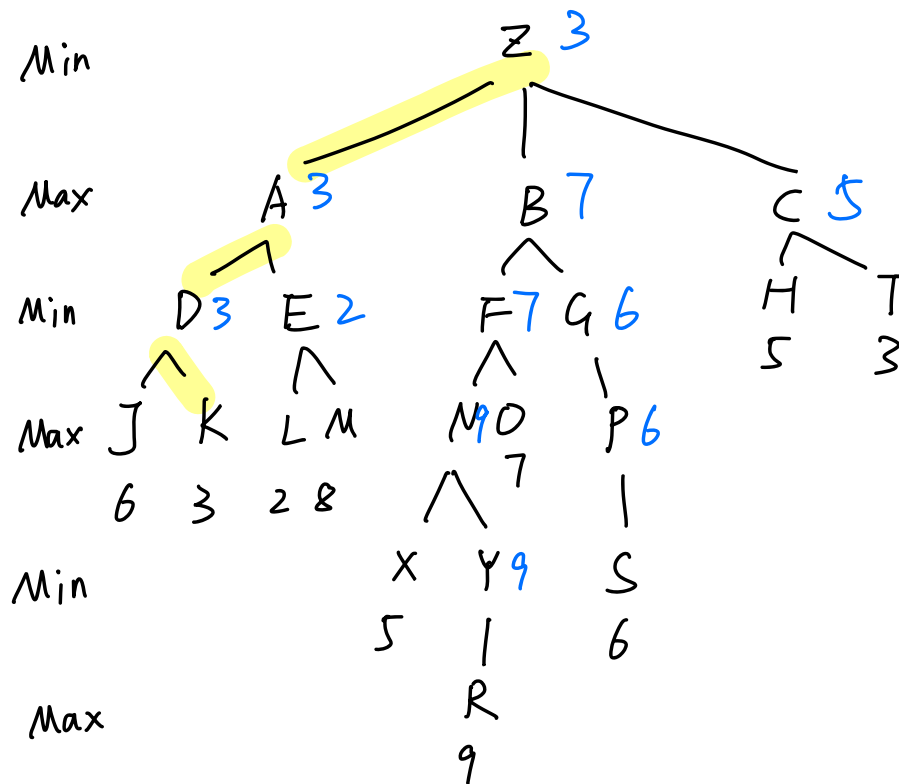
$t_6 = 0.8$

(ii) δ_{all}

(iii) $W_{5,bias}$

(iv) σ_6

Solution (i) MinMax : choose A



not examined node.

M Y R G P S T

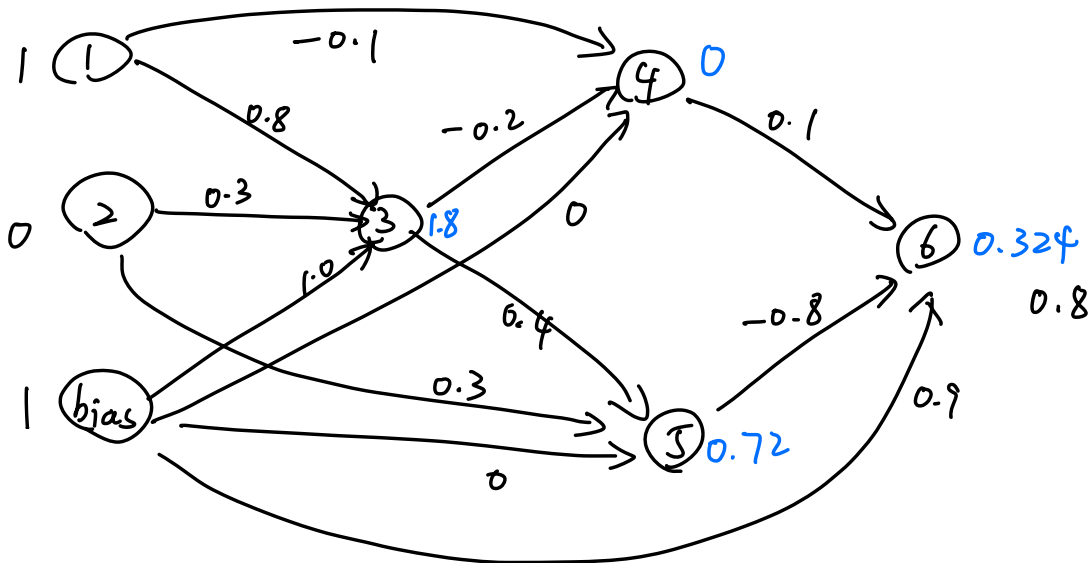
(iii) ① Pruning of irrelevant branches:

Once α or β crosses, entire subtrees can be skipped.

② Move ordering; If one finds either α very good for Max or very bad for Min move early, it tightens α or β sooner and prunes more aggressively

(b) c_1 O_3 O_4 O_5 O_6

①



$$\textcircled{2} \text{net}_3 = 0.8 \times 1 + 0.3 \times 0 + 1.0 \times 1$$

$$= 0.8 + 1$$

$$= 1.8$$

$$O_3 = \sigma(\text{net}_3) = 1.8$$

$$\textcircled{3} \text{net}_4 = -0.1 \times 1 - 0.2 \times 1.8 + 0 \times 1$$

$$= -0.46$$

$$O_4 = \sigma(\text{net}_4) = 0$$

$$\textcircled{4} \text{net}_5 = 0.4 \times 1.8 + 0.3 \times 0 + 0 \times 1$$

$$= 0.72$$

$$O_5 = \sigma(\text{net}_5) = 0.72$$

$$\textcircled{5} \text{net}_6 = 0.1 \times 0 - 0.8 \times 0.72 + 0.9 \times 1$$

$$= 0.324$$

$$O_6 = \sigma(\text{net}_6) = 0.324$$

(ii) δ

$$\textcircled{1} \sigma(x) = \max(0, x)$$

$$\sigma'(x) = \begin{cases} 1 & , x > 0 \\ 0 & , x < 0 \end{cases}$$

$$\textcircled{2} \delta_6 = \sigma'(\text{net}_6) (t_6 - o_6)$$

$$= 1 \times (0.8 - 0.324)$$

$$= 0.476$$

$$\textcircled{3} \delta_5 = \sigma'(\text{net}_5) \sum_k \delta_k w_{kj}$$

$$= 1 \times (\delta_6 \cdot w_{65})$$

$$= 0.476 \times (-0.8)$$

$$= -0.3808$$

$$\textcircled{4} \delta_4 = \sigma'(\text{net}_4) \delta_6 w_{64}$$

$$= 0$$

$$\textcircled{5} \delta_3 = 1 \times [\delta_4 \times (-0.2) + \delta_5 \times (0.4)]$$

$$= -0.3808 \times 0.4$$

$$= -0.15232$$

(iii) $w_{5, bias}$

$$\textcircled{1} \Delta w_{5, bias} = \eta \delta_5 o_{bias}$$

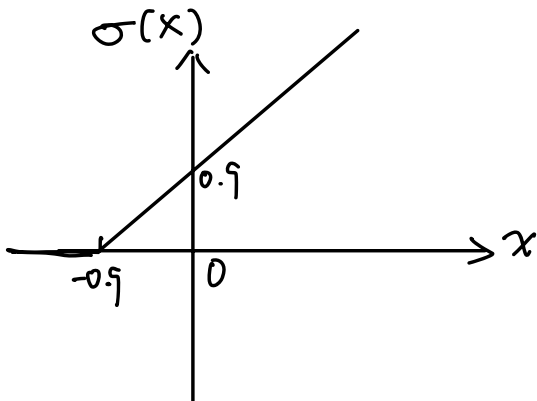
$$= 0.5 \times (-0.3808) \times 1$$

$$= -0.1904$$

$$\textcircled{2} w_{5, bias} = 1 - 0.1904$$

$$= 0.8096$$

(iv) $\sigma(x) = \max(0, x + 0.9)$



(c) (i) ① accuracy

TP	FN
FP	TN

300	200
250	9250

TP	FP
FN	TN

$$\text{accuracy} = \frac{TP + TN}{TP + FP + FN + TN} = \frac{300 + 9250}{10000} = 95.5\%$$

$$\text{② precision} = \frac{TP}{TP + FP} = \frac{300}{300 + 250} = 54.5454\%$$

$$\text{③ recall} = \frac{TP}{TP + FN} = \frac{300}{300 + 200} = 60\%$$

(ii)

① raise the recall.

② we must reduce the number of missed fake (FN)