

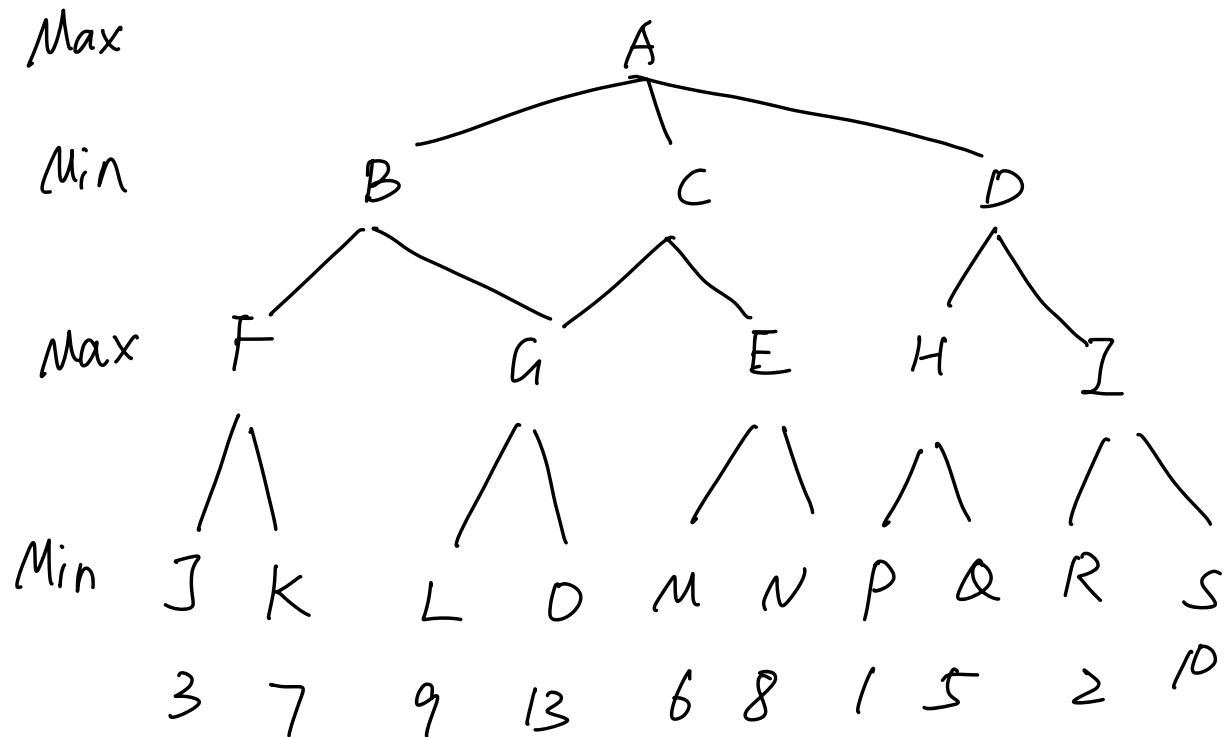
24-S1-Q2

(a) first \rightarrow Max

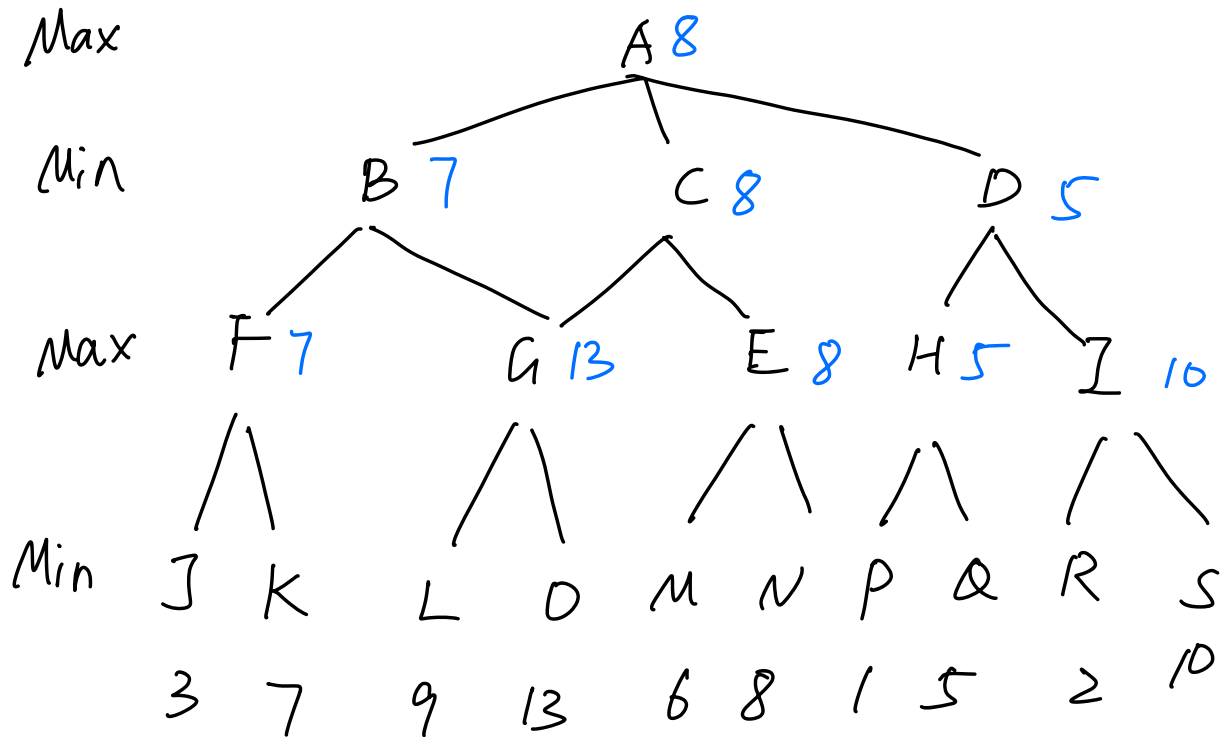
(i) $A \rightarrow B < D$?

(ii) left \rightarrow right $A - \beta$ pruning

(iii) not examined nodes



Solution (a) (i) ① compute result



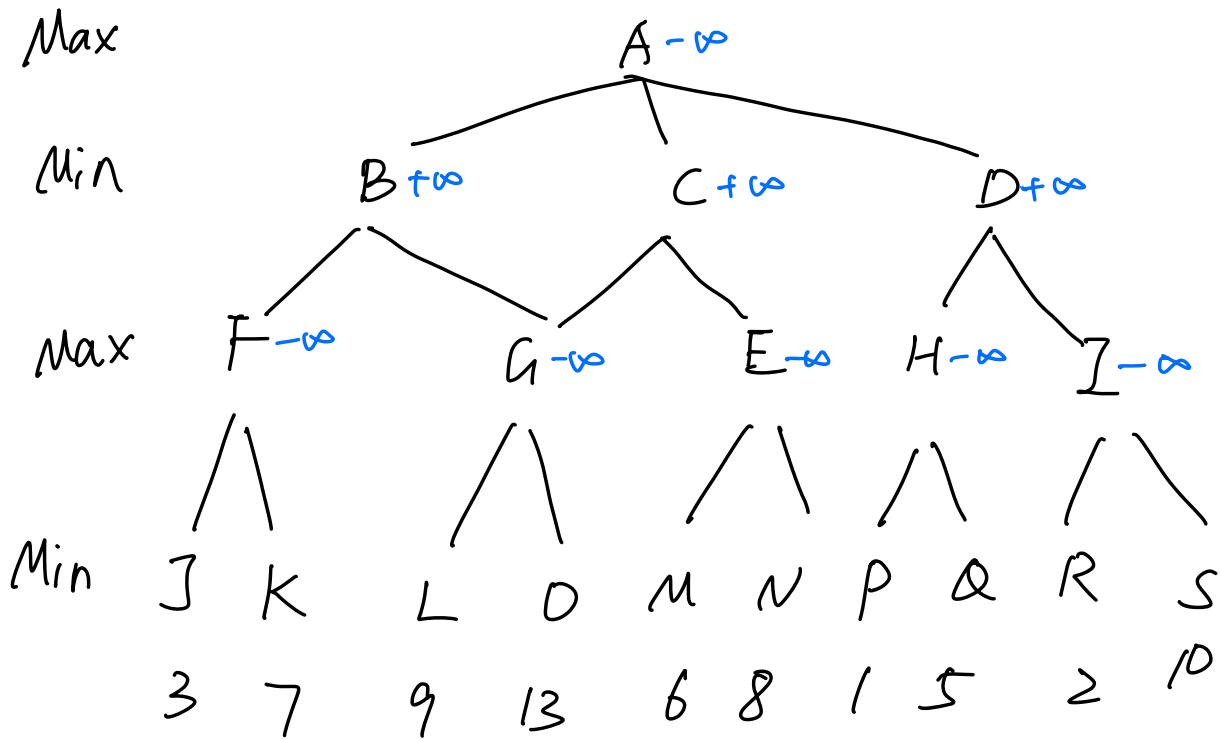
② the first player choose C

Since according to min-max algorithm
the first player is a Max player

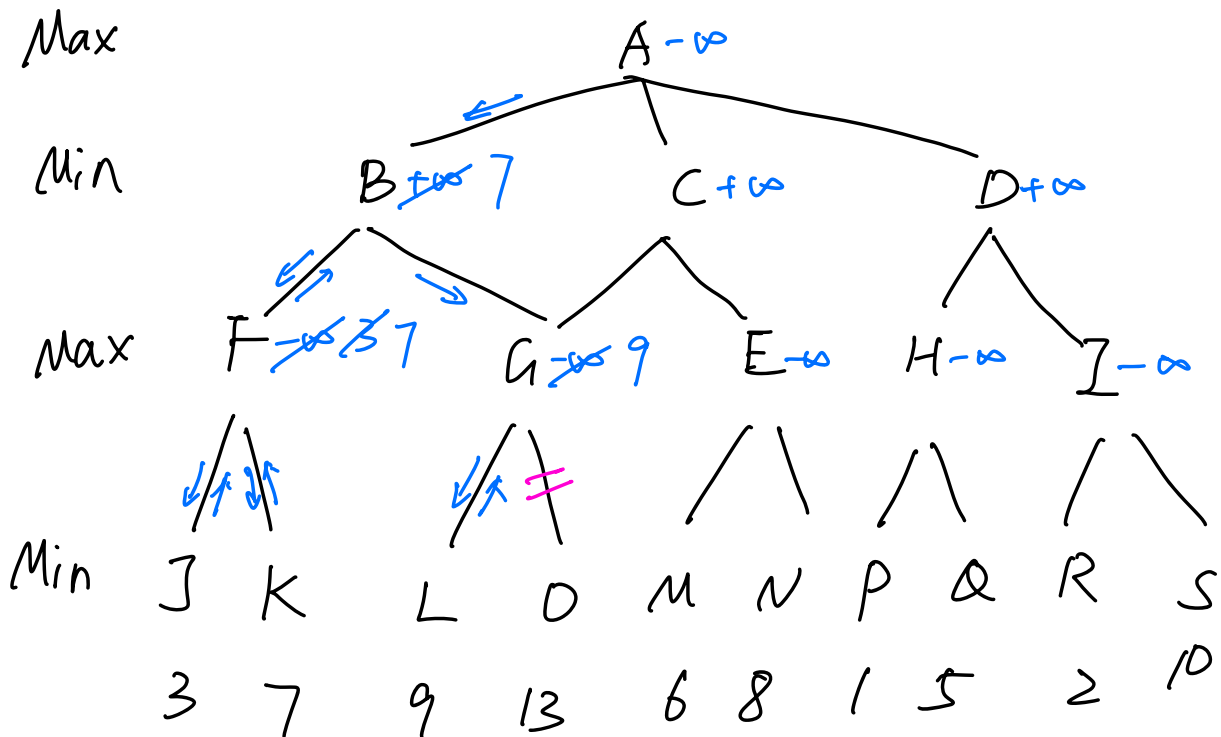
So he will choose the largest one

$8 > 7 > 5$, $C > B > D$, so he will choose
C

(ii) ① apply α - β pruning



②



$9 > 7$, prune.

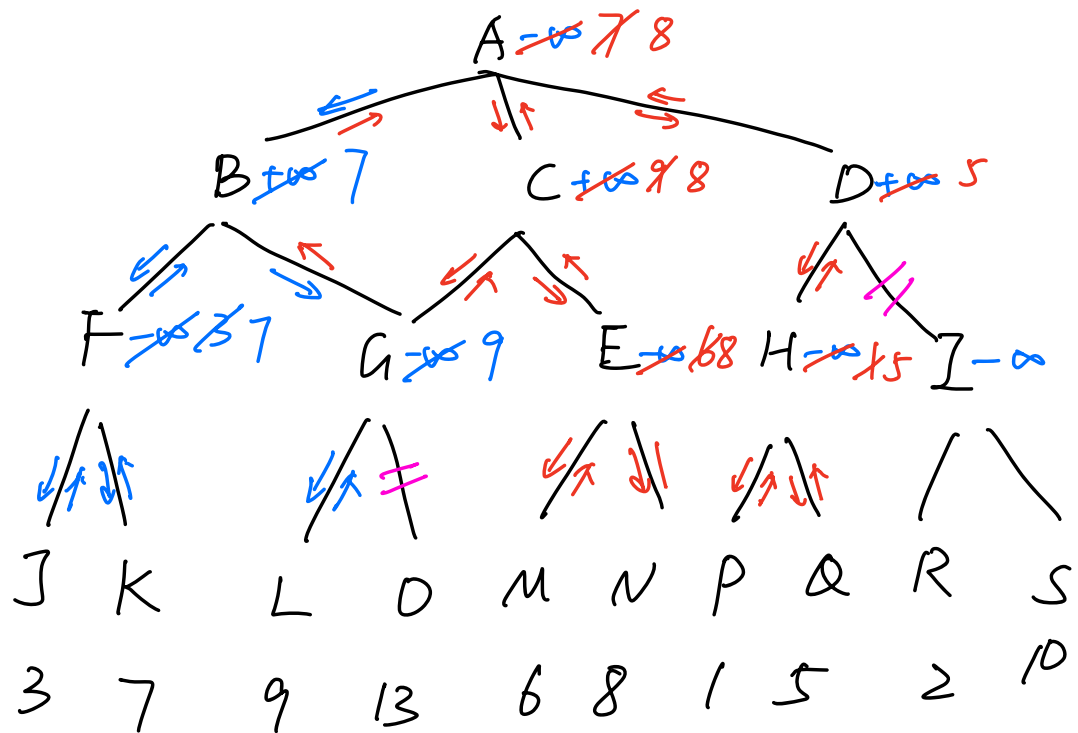
③

Max

Min

Max

Min

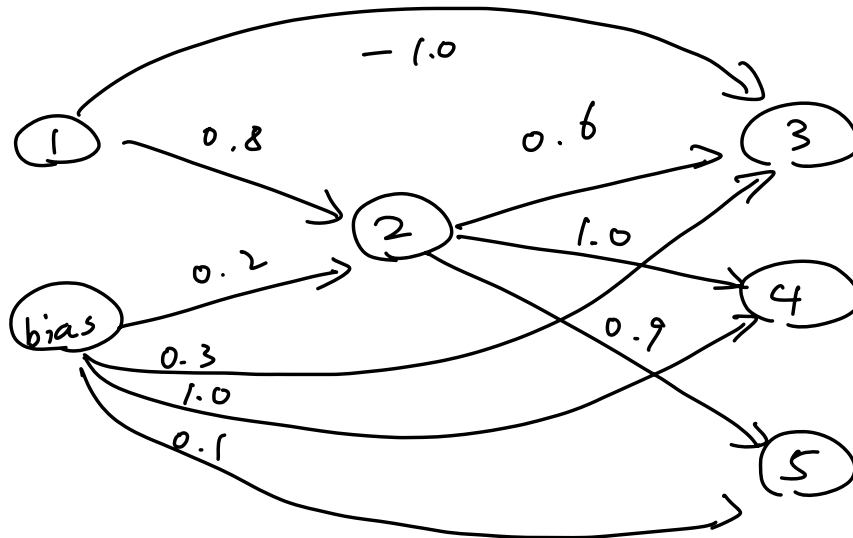


$5 < 8$ prune

(iii) not visited node.

O I R S

(b)



ReLU : hidden and output
output bias = 1.0

learning rate $\eta = 0.5$

$$\text{error} : E = \frac{1}{2} \sum_k (t_k - o_k)^2$$

↓
target
output

↓
actual
output

$$\text{net}_j = \sum_i (w_{ji} \cdot o_i)$$

↓
input

↓
include bias

$$o_j = \sigma(\text{net}_j)$$

↓
output

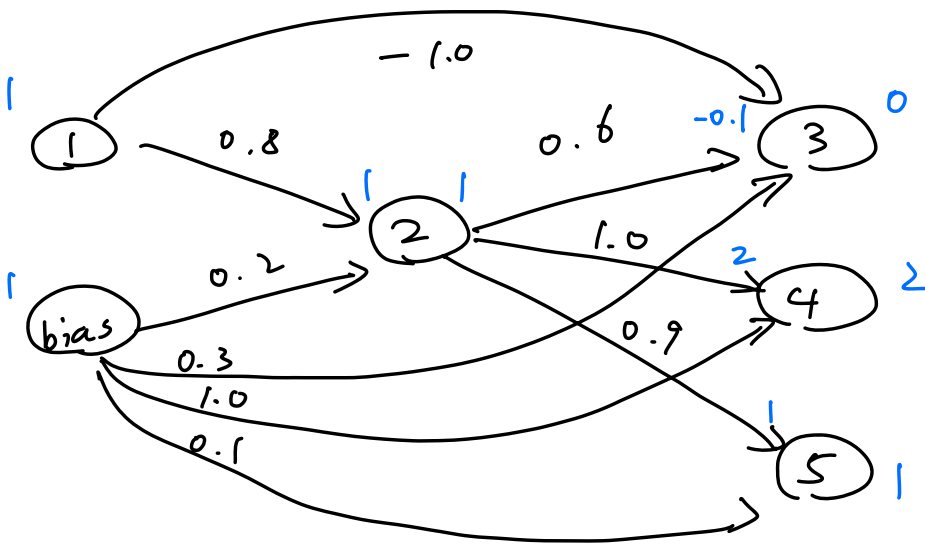
Backpropagation

Q (i) $x = (1, 0) \rightarrow t (0.1, 0.9, 0.1)$
 actual output. at 2, 3, 4, 5

(ii) error

(iii) bias of unit 2. \rightarrow adjust

Solution (i) ① Forward-pass outputs



$$x_1 = 1 \quad \text{bias} = 1$$

$$\textcircled{2} \text{ net}_2 = 0.8x_1 + 0.2x_{\text{bias}} = 1$$

$$O_2 = \text{ReLU}(\text{net}_2) = \text{ReLU}(1) = 1$$

$$\textcircled{3} \text{ net}_3 = (-1) \times 1 + 0.6 \times 1 + 0.3 \times 1 = -0.1$$

$$O_3 = \text{ReLU}(\text{net}_3) = \text{ReLU}(-0.1) = 0$$

$$\textcircled{4} \text{net}_4 = 1 \times 1 + 1 \times 1 = 2$$

$$O_4 = \text{ReLU}(\text{net}_4) = \text{ReLU}(2) = 2$$

$$\textcircled{5} \text{net}_5 = 0.9 \times 1 + 0.1 \times 1 = 1$$

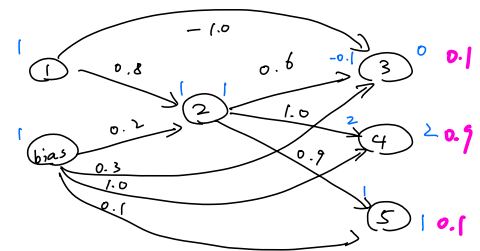
$$O_5 = \text{ReLU}(\text{net}_5) = \text{ReLU}(1) = 1$$

$$\textcircled{6} \text{ All in all, } O_2 = 1, O_3 = 0, O_4 = 2, O_5 = 1$$

$$\begin{aligned} \textcircled{\text{ii}} \textcircled{1} \delta_3 &= \frac{1}{2} (t_3 - O_3)^2 \\ &= \frac{1}{2} (0.1 - 0)^2 \\ &= 0.005 \end{aligned}$$

$$\begin{aligned} \textcircled{2} \delta_4 &= \frac{1}{2} \times (0.9 - 2)^2 \\ &= 0.605 \end{aligned}$$

$$\begin{aligned} \textcircled{3} \delta_5 &= \frac{1}{2} \times (0.1 - 1)^2 \\ &= 0.405 \end{aligned}$$



$$\begin{aligned} \textcircled{4} \delta_2 &= \sigma'(\text{net}_2) \sum_k \delta_k w_{k2} \\ &= 0.005 \times 0.6 + 0.605 \times 1 + 0.405 \times 0.9 \\ &= 0.9725 \end{aligned}$$

⑤ All in All

| | |
|------------|--------|
| δ_2 | 0.9725 |
| δ_3 | 0.005 |
| δ_4 | 0.605 |
| δ_5 | 0.405 |

$$(iii) \delta w_{2,bias} = \eta \delta_2 O_{bias}$$

$$= 0.5 \times 0.9725 \times 1$$

$$= 0.48625$$

$$w_{2,bias} = 0.2 + 0.48625$$

$$= 0.68625$$