4.2.2.4 Example
$$Q 3^{d} - 2^{d+1} + 1$$

$$d = 6$$

Solution of counting possible item subsets

non-empty subsets of a set with differ

2d-1

Deneral proof using induction

general proof using induction

to d=0

2°=1

the formula holds

- (2) Assume d=k formula holds.
- (3) d= K+1

I take any of the 2k subsets from the first k elements.

2, add the new (ktl)the lement to each of these 2k subsets forming another 2k new

- 3. Thus, the total number of subjects for d = k+1 is $2^{k} + 2^{k} = 2^{k+1}$
- (4) So A set with delemets has 2d subsets.
- 2) S contains at least two elements

in 2 -2 ways

Similary, we can use induction to proof.

eg. $S = \{a, b\}$ |S| = 2 $2^2 - 2 = 2$

 $X = \{a,b\}$ $Y = \emptyset$ X $a \qquad b \qquad \checkmark$ $b \qquad a \qquad \checkmark$ $\emptyset \qquad \{a,b\} \qquad X$

3 Total Rule Count computation

Summing ovel all possible subset size k

Finomial Theorem = TRA ZE

(a+b) d = ≥(d) ad-k jk

we can proof by induction

$$\frac{d}{Z} \binom{d}{k} 2^{k} = (1+2)^{d} = 3^{d}$$

$$\frac{d}{Z} \binom{d}{k} 2^{k} = 3^{d} - \binom{d}{0} 2^{0} - \binom{d}{0} 2^{0}$$

$$= 3^{d} - (-2)^{d}$$

(3) Take the second part $\frac{d}{\sum_{k=2}^{d} {k \choose k}} = 2^{d} - 1 - d$

Pue to bisnomial identity = $\frac{1}{2} \frac{1}{2} \frac{1}{2}$

$$G = \frac{d}{2} (x)^{2k} - \frac{d}{2} (x)^{2k}$$

$$= 3^{d} - 1 - 2d - 2x(2^{d} - 1 - d)$$

$$= 3^{d} - (-2d - 2^{d+1} + 2 + 2d)$$

$$= 3^{d} - 2^{d+1} + 1$$

$$\Im S_{0}$$

$$3^{6}-2^{6+1}+1=3^{6}-2^{7}+1=602$$