Solution (a) (i) single Linkage

O we denote that d(i,j) is the distant between i and j

(2) $d(A,B) = \min \{d_{0,3}, d_{0,9}, d_{2,3}, d_{2,9}, d_{5,3}, d_{6,9}\}$ = $\min \{3,9,1,7,3,3\}$

= 1

 $d(A,C) = min\{do, 11, d_{2,11}, d_{5,11}\}$ = $min\{11, 9, 5\}$

= 5 d(B,C)=min\$d 3,11, d 9,11) = min \$ 8,23 = 2.

	A	В	
A	G		
В		D	
C	5	2	6

@1<2<5

So, the cluster A and chuster B nill be merged at the next iteration.

(2) Complete Cinkage

O we denote that d(i,j) is the distant between i and j

(2) d(A,B) = max fdo,3, do,9, dz,3, dz,9, d 6,3, d6,9)

= max 93,9,1,7,3,3}

= 9

 $d(A,C) = \max\{d_{0,11}, d_{2,11}, d_{5,11}\}$ = $\max\{11, 9, 5\}$

d(B,C)=max { d 3,11 , d 9,11 } = max { 8,2}

- 8

	Á	В	
A	O		
В	9	D	
C	[]	8	6

3 8c9c11

So, the cluster B and chuster C nill be merged at the next iteration.

(b) (i) we denote distant between samples and claster centroids as d(i,j), if [5,7,19,12], je(1,2)

Samples	5	[7	10	[12
C1=3	2	4	7	9
Cz = 13	8,	6	3	1
Assign	Cil	CI	CZ	CZ

So we assign \$5,7 to C, and assign \$(0,12) to C2

(2) new controids

(c)(i) O object: The mean squre error (MSE) of the projected data is minimized and the variance of the projected data is maximized. 3 To learn the best low-dimensional subspace for data projection 3 achieve: APPLY SVD to the data matrix. Select the unit weight vector Ut from the U matrix and calculate CVK xi)VK (ii) pcl is the eigenvector with the largest eigon value; it defines the direction along which the data show waximum variance All subsequent PCs are orthogonal to PCI and to each other each englaing the greatest remaining variance ciii) D Learning target: PCA is ansupervised Linear regre ssion is supervised. 2 Optimisation criterion: PCA max variance and min MSE; regression min residual variance of the responce

$$(dx) N_{k=1} = 4, N_{k=0} = 4$$

$$p(k=1) = p(k=0) = 0.5$$

$$p(a=1|k=0) = 0.5$$

$$p(b=1|k=0) = 0.5$$

$$p(b=1|k=0) = 0.5$$

$$p(c=0|k=1) = 0.5$$

$$p(c=0|k=0) = 0.2$$

$$(i) p(k=1|a=1,b=1,c=0)$$

$$= \frac{p(a=1,b=1,c=0)}{p(a=1,b=1,c=0)}$$

$$= \frac{p(a=1,b=1,c=0)}{p(a=1,b=1,c=0)}$$

$$= \frac{p(a=1,b=1,c=0)}{p(a=1,b=1,c=0)}$$

$$= \frac{0.5 \times 0.25 \times 0.5}{0.125}$$

$$= 0.25$$

$$(ii) p(k=0|a=1,b=1)$$

$$= \frac{p(o=1,b=1|k=0) p(k=0)}{p(a=1,b=1)}$$

$$= \frac{p(a=1|k=0) \times p(b=1|k=0) p(k=0)}{p(a=1,b=1)}$$

$$= \frac{0.5 \times 0.5}{0.25}$$

-0.5