- 4. In an image application, the input feature maps of spatial size $P \times Q$ with C channels and the output feature maps of spatial size $P \times Q$ with D channels of a layer of neural network are expressed as $x_{i,j,k}$, $1 \le i \le P$, $1 \le j \le Q$, $1 \le k \le C$, and $y_{i,j,k}$, $1 \le i \le P$, $1 \le j \le Q$, $1 \le k \le D$, respectively.
 - (a) Express the output feature maps $y_{i,j,k}$ in terms of the input feature maps $x_{i,j,k}$ via the scalar network parameters of a layer of fully connected neural network. What is the number of learnable parameters?

(5 Marks)

(b) Express the output feature maps in terms of the input feature maps via the scalar network parameters of a layer of spatial convolutional neural network of filter size 3 × 3. What is the number of learnable parameters?

(5 Marks)

(c) Express the output feature maps in terms of the input feature maps via the scalar network parameters of a layer of spatial convolutional neural network of filter size 1 × 1. What is the number of learnable parameters?

(5 Marks)

(d) If we use a single index for the 2D spatial position to express the input and output feature maps by $x_{i,k}$, $1 \le i \le PQ$, $1 \le k \le C$, and $y_{i,k}$, $1 \le i \le PQ$, $1 \le k \le D$, respectively, reexpress the answer to part (c) without using the bias. What is the number of learnable parameters?

(5 Marks)

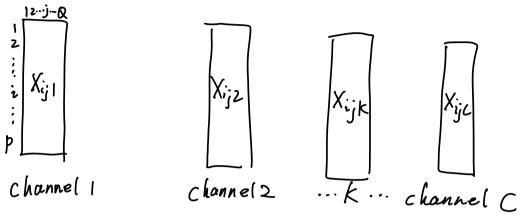
(e) Arrange all $x_{i,k}$ in part (d) into a $PQ \times C$ matrix, X, and arrange all $y_{i,k}$ in part (d) into a $PQ \times D$ matrix, Y. Re-express the answer to part (d) in the matrix format X and Y. (Note that $PQ \times C$ matrix has PQ rows and C columns.) What can you conclude about the relation between a convolutional neural network and a Transformer?

(5 Marks)

[Hint for Question 4: If inputs and outputs of a layer of network are expressed as x_i , $1 \le i \le P$ and y_i , $1 \le i \le Q$, respectively, the outputs of a layer of fully connected neural network can be expressed in terms of the inputs as $y_i = \sum_{l=1}^P w_{l,i} x_l + b_i$, $1 \le i \le Q$, where $w_{l,i}$, b_i are the scalar parameters called the weights and biases of the network, respectively.]

2z-52-Q4(a)Q: Xijk > Gijk? parameters?

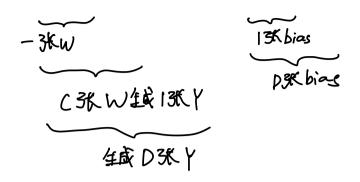
Solution ① understand $\begin{vmatrix} 12-j-Q \\ 2 \end{vmatrix}$



$$X_{ij,k} \Rightarrow y_{i,j,k}$$
 full connect

 P
 $A \times + P = P Y$
 $y_{ij,k}$
 $y_{ij,k}$

$$y_{ijk} = \sum_{l=1}^{C} \sum_{m=1}^{P} \sum_{n=1}^{P} W_{mnlk} X_{ijl} + b_{ijk} (1 \le k \le D)$$
parameters $P \times P \times C \times D + P \times Q \times D$



Cb) CNN?

$$\int_{V_{i,j,k}} \frac{1}{2} \sum_{u=-1}^{2} \sum_{v=-1}^{2} \sum_{v=-1}^$$

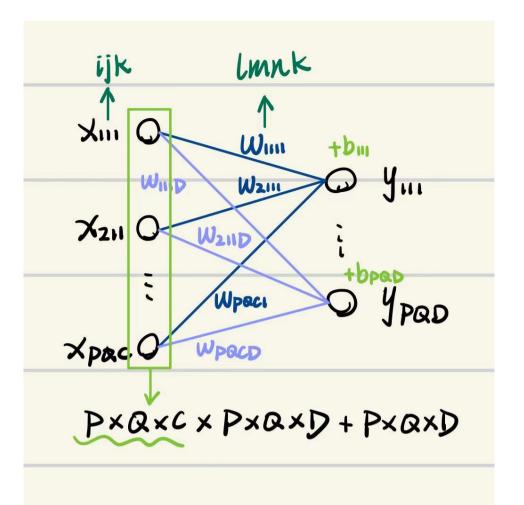
Pexw X po por matrix multiplications to process input

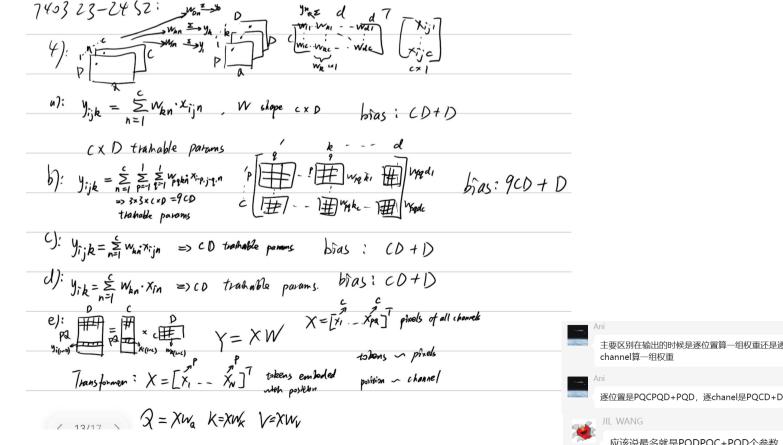
EY=XW shows the CNN perform a linear transformation on the input features at each spatial position, identical across all position.

It is similar to the linear layers

where in Transformer, where input

are transformed via weight matrices





比这个少的都是简化或者共享了参数

应该说最多就是PQDPQC+PQD个参数