$$22-SI-QI$$

(1) Q: h(x,y) =? 2spatial properties?

Solution

 $0 g(x,y) = f(x,y) *h(x,y)$ 

(3) 
$$h(x,y) = 4\delta(x,y)$$
  

$$- \delta(x-1,y) - \delta(x+1,y) - \delta(x,y-1) - \delta(x,y+1)$$

$$h(x,y) = \begin{cases} 4 & (x,y) = (0,0) \\ -1 & (x,y) = (\pm 1,0) \text{ or } (0,\pm 1) \\ 0 & \text{otherwise} \end{cases}$$

O spatial properties

1. High - Pass filtering: The filter emphasizes regions with high spatial frequency content (edges) by computing the difference between a pixel and its neighbors

2. Spatial Localization: The filter is localized affecting only a pixel and its immediate neighbors due to the non-zero co efficients being limited to the contral pixel and its four direct reighbors (b)  $H(u,v) = \frac{1}{mn} \sum_{x=0}^{m-1} \sum_{y=0}^{n-1} f(x,y) e^{-j2\pi (\frac{ux}{m} + \frac{vy}{n})}$  $= \frac{1}{3 \times 3} \sum_{X=-1}^{1} \frac{1}{2^{2}} f(x,y) e^{-\int_{1}^{2} \frac{2^{2}}{3} (ux + v^{2}y)}$  $= \frac{1}{9} \left[ f(0,0) e^{0} + f(1,0) e^{-j\frac{\pi}{3}u} + f(-1,0) e^{-j\frac{\pi}{3}u} \right]$  $+f(0,1)e^{-\frac{2}{3}v}+f(0,-1)e^{j\frac{2}{3}v}$  $= \frac{1}{9} \left[ 4 - e^{-j\frac{2\pi}{3}u} - e^{j\frac{2\pi}{3}u} - e^{-j\frac{2\pi}{3}u} - e^{j\frac{2\pi}{3}u} \right]$  $=\frac{1}{9}\left[4-(e^{-j\frac{2}{3}u}+e^{j\frac{2}{3}u})-(e^{-j\frac{2}{3}u}+e^{j\frac{2}{3}u})\right]$  $= \frac{1}{9} \left[ 4 - 2\cos\frac{2z}{3}u - 2\cos\frac{2z}{3}v \right]$ 

(c)

0	0	0	0	0	0	0	0	0
0	0	<b>6</b>	Ø'		<b>9</b>		0	0
0	<b>6</b>	<b>1</b>	<b>3</b>			P		0
0	<b>(3)</b>	<b>3</b>	(J)°	P	P°	<b>P</b>	<b>B</b> '	0
0	<b>9</b> '	<b>P</b>	ذ	(P)°		<b>P</b>	(P)	0
0	Ø	Đ'	<b>⊘</b> °	ذ				0
0	Ø '	B	(F)	<b>®</b>		P)	<b>B</b>	0
0	0	<b>1</b>	<b>®</b> ′	<b>Ø</b> '	<b>6</b>	<b>6</b> )	0	0
0	0	0	0	0	0	0	0	0

edge detection: as it suppresses uniform region and enhances areas with significant intensity changes.