

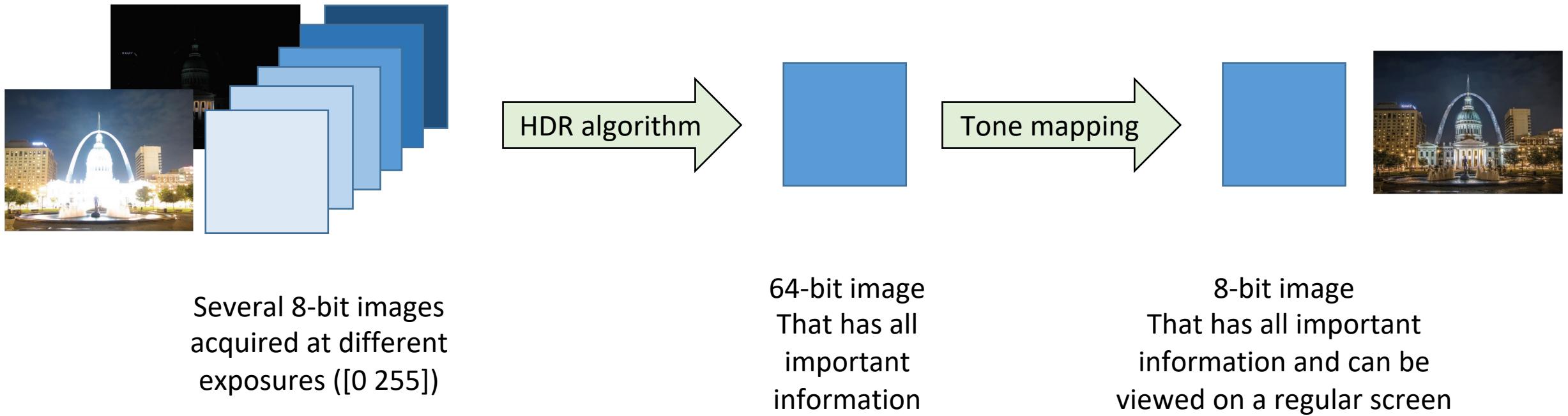


Problem Session 4

Topics

- High dynamic range images
 - Debevec's Method
 - Tone mapping
- SNR Calculations
 - Burst Imaging
 - Flutter Shutter

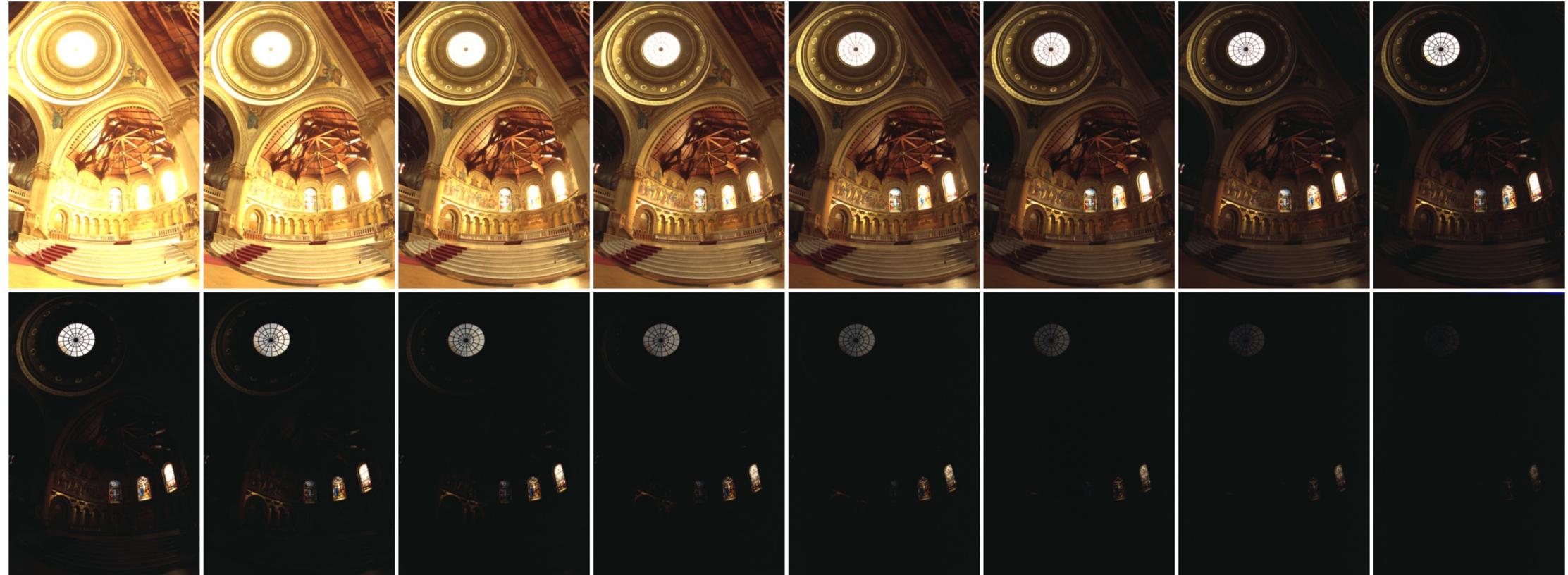
HDR & Tone mapping



Task 1: High dynamic range

(Debevec's method)

```
# Number of Images  
16  
# Filename 1/shutter_speed f/stop gain(db) ND_filters  
memorial0061.ppm 0.03125 8 0 0  
memorial0062.ppm 0.0625 8 0 0  
memorial0063.ppm 0.125 8 0 0  
memorial0064.ppm 0.25 8 0 0  
memorial0065.ppm 0.5 8 0 0  
memorial0066.ppm 1 8 0 0  
memorial0067.ppm 2 8 0 0  
memorial0068.ppm 4 8 0 0  
memorial0069.ppm 8 8 0 0  
memorial0070.ppm 16 8 0 0  
memorial0071.ppm 32 8 0 0  
memorial0072.ppm 64 8 0 0  
memorial0073.ppm 128 8 0 0  
memorial0074.ppm 256 8 0 0  
memorial0075.ppm 512 8 0 0  
memorial0076.ppm 1024 8 0 0
```



Task 1: High dynamic range

Linearize the images using gamma of 2.2



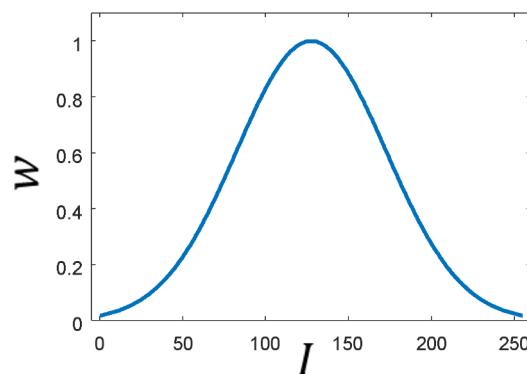
Task 1: High dynamic range image

Computing the weights: we want to give a higher weight to pixels that are close to the center of the dynamic range at each exposure k .

$$w_{k,ij} = \exp\left(-4 \frac{(I_{k,ij} - 0.5)^2}{0.5^2}\right)$$

Center of the dynamic range
(127.5 if pixels are [0,255])

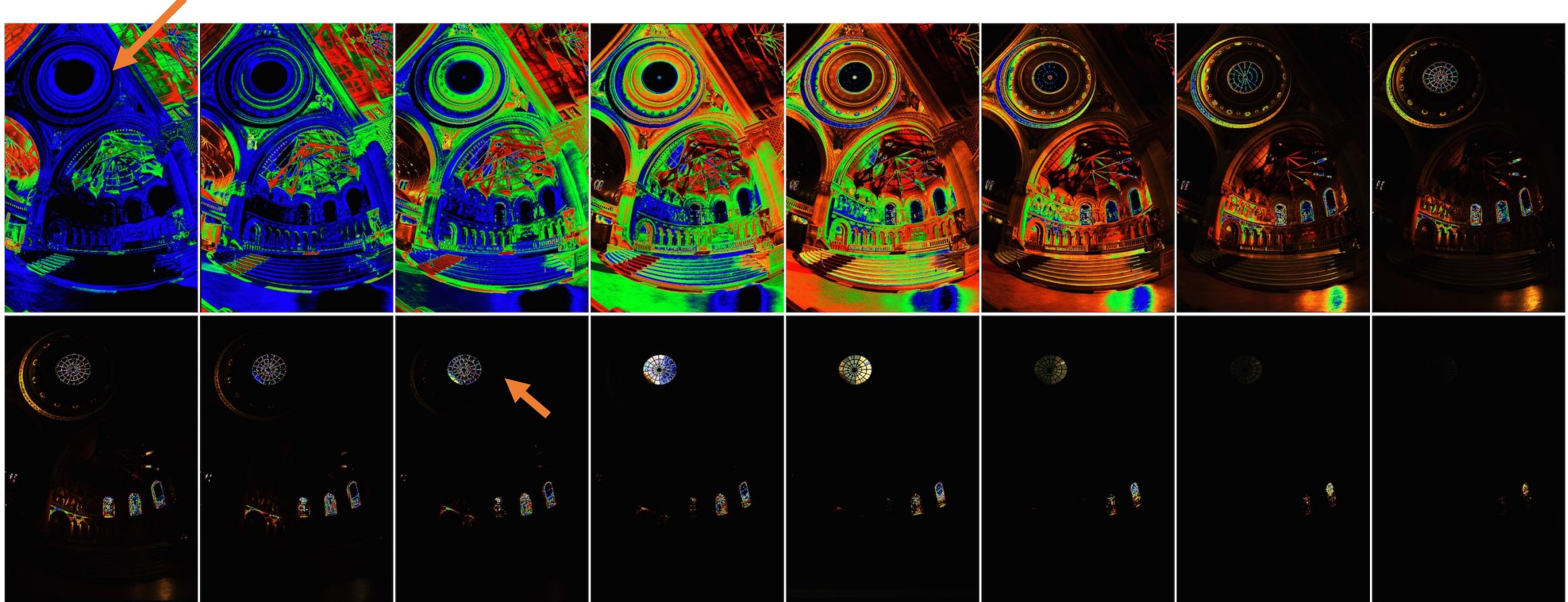
Linearized image
($\gamma=2.2$)



Compute this per color channel

Task 1: High dynamic range

Weights using Debevec's method (all 3 color channels)



Task 1: High dynamic range image

Find a good estimation, \hat{X} , for the “true image”, X , using an optimization problem:

Minimize the difference, in log scale, between your result, \hat{X} , at different exposures t_k and the acquired images at different exposures (I_{lin_k}). Multiplied by weight to indicate what's more important.

$$\underset{\hat{X}}{\text{minimize}} \quad 0 = \sum_k w_k (\log(I_{lin_k}) - \log(t_k \hat{X}))^2$$

Calculating the derivative of 0 , we get: hdr

$$\hat{X} = \exp \left(\frac{\sum_k w_k (\log(I_{lin_k}) - \log(t_k))}{\sum_k w_k} \right)$$

scale

Perceptually similar

Task 1: High dynamic range - Tonemapping

- After exp, scaling, cropping, try your own scaling+gamma correction
- Choose scale and gamma yourself, report chosen parameters and resulting image
 - Don't scale+shift to fill the range [0, 1], scale only

$$I_{HDR} = (s \times I_{HDR\ linear})^\gamma$$

- Also try Drago's tonemapping from opencv

```
# Normalize
hdr = np.exp(hdr / scale)
hdr *= 0.8371896/np.mean(hdr) # the mean of the image

# convert to 32 bit floating point
hdr = np.float32(hdr)

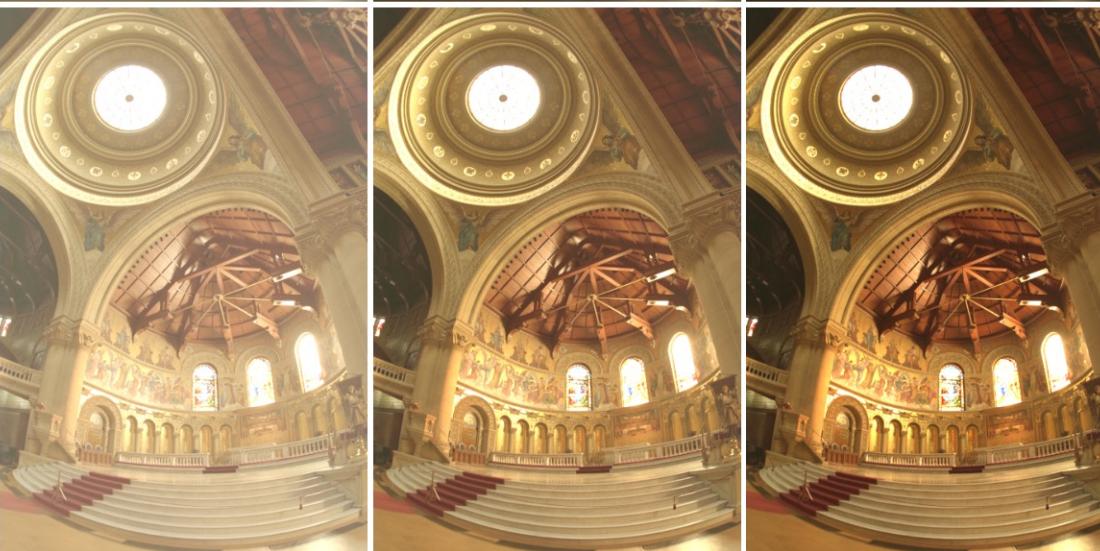
# crop boundary - image data here a
hdr = hdr[29:720, 19:480, :]
```

Task 1: High dynamic range

Adjusting γ and s



$$s = 0.1$$



$$s = 1.0$$

$$\gamma = \frac{1}{5}$$

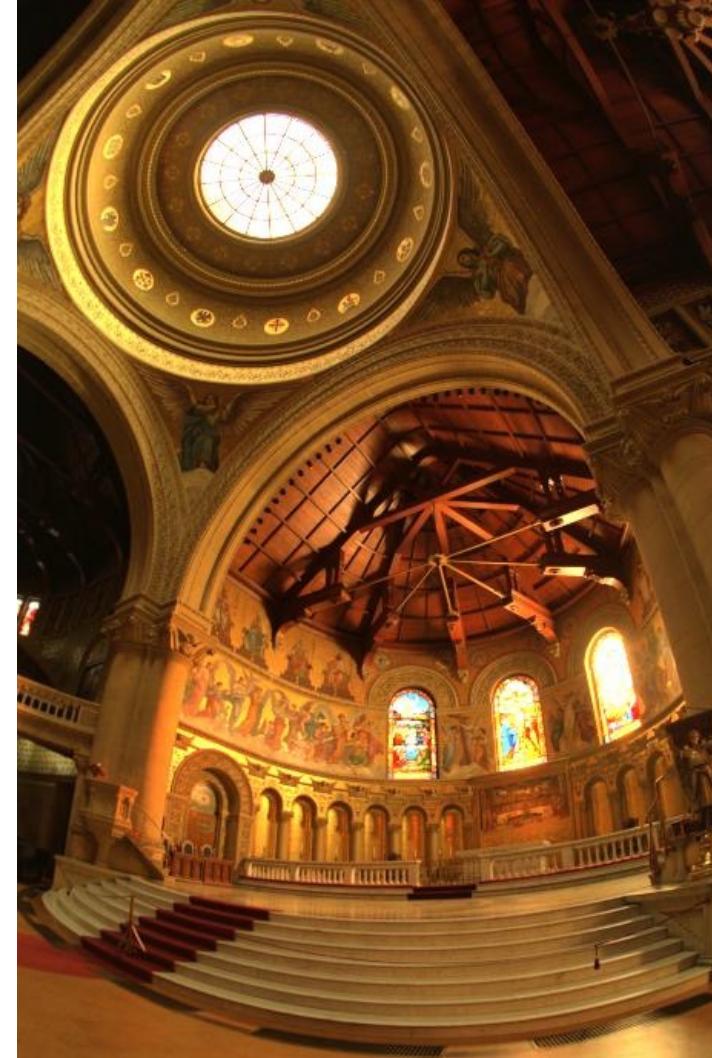
$$\gamma = \frac{1}{3}$$

$$\gamma = \frac{1}{2.2}$$

$$\gamma = 1/4$$

Task 1: High dynamic range

Generate a tonemapped image using
cv2.createTonemapDrago



Task 2/3: Denoising and SNR

- Read noise
 - Noise from heat in pixel hardware when image is captured
 - Signal-independent
 - Typically modelled as a **Gaussian distribution**
- Shot noise
 - Noise from statistics of light-pixel interactions
 - Signal-dependent
 - Typically modelled as a **Poisson distribution**

Task 2: Burst SNR calculations

$$SNR = \frac{\mu}{\sigma} = \frac{\text{mean number of photons}}{\text{standard deviation of noise}}$$

- Adding k signals of strength $\mu \Rightarrow$ mean becomes $k\mu$
- Scaling Gaussian/Poisson variable by $k \Rightarrow$ variance becomes $k^2\sigma^2$
- Adding independent Gaussian distributions
 - $G(\mu_1, \sigma_1^2) + G(\mu_2, \sigma_2^2) \sim G(\mu_1 + \mu_2, \underbrace{\sigma_1^2 + \sigma_2^2}_{\text{Variance} = (\text{standard deviation})^2})$
- Adding independent Poisson distributions
 - $Pois(\lambda_1) + Pois(\lambda_2) \sim Pois(\underbrace{\lambda_1 + \lambda_2}_{\text{Both mean and variance}})$
- Both signal and noise increase with the number of photons.
 - However, signal increases faster than noise!

Task 3: Flutter Shutter

You're asked to compare the SNR of two imaging setups:

- Consumer camera in everyday use
- sCMOS in microscopy

At different acquisition modes:

- Flutter shutter
- Burst

Calculate the SNR and discuss your results.

Task 3: SNR calculations

Consumer camera in everyday conditions:

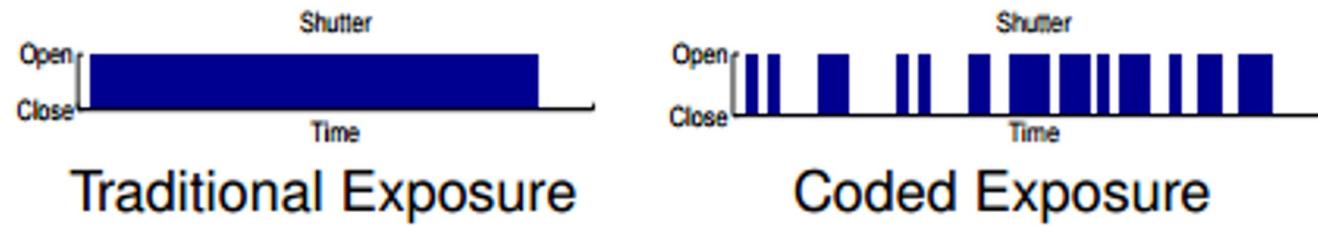
- Lots of photons (low shot noise)
- Room temperature (high read noise)

sCMOS microscope sensor in controlled conditions:

- Few photons (high shot noise)
- Cooled sensor (low read noise)

Task 3: SNR calculations

Flutter shutter: temporally modulated aperture pattern. Used, for example, for better motion deblurring (see “*Coded Exposure Photography: Motion Deblurring using Fluttered Shutter*”, Raskar et al.). The result is a single image.



Burst: acquires multiple short-exposure images. (for this problem, assume no delay between exposures)

Tradeoff: Number of exposures vs. number of photons

Task 3: SNR calculations

For each of the four cases, calculate:

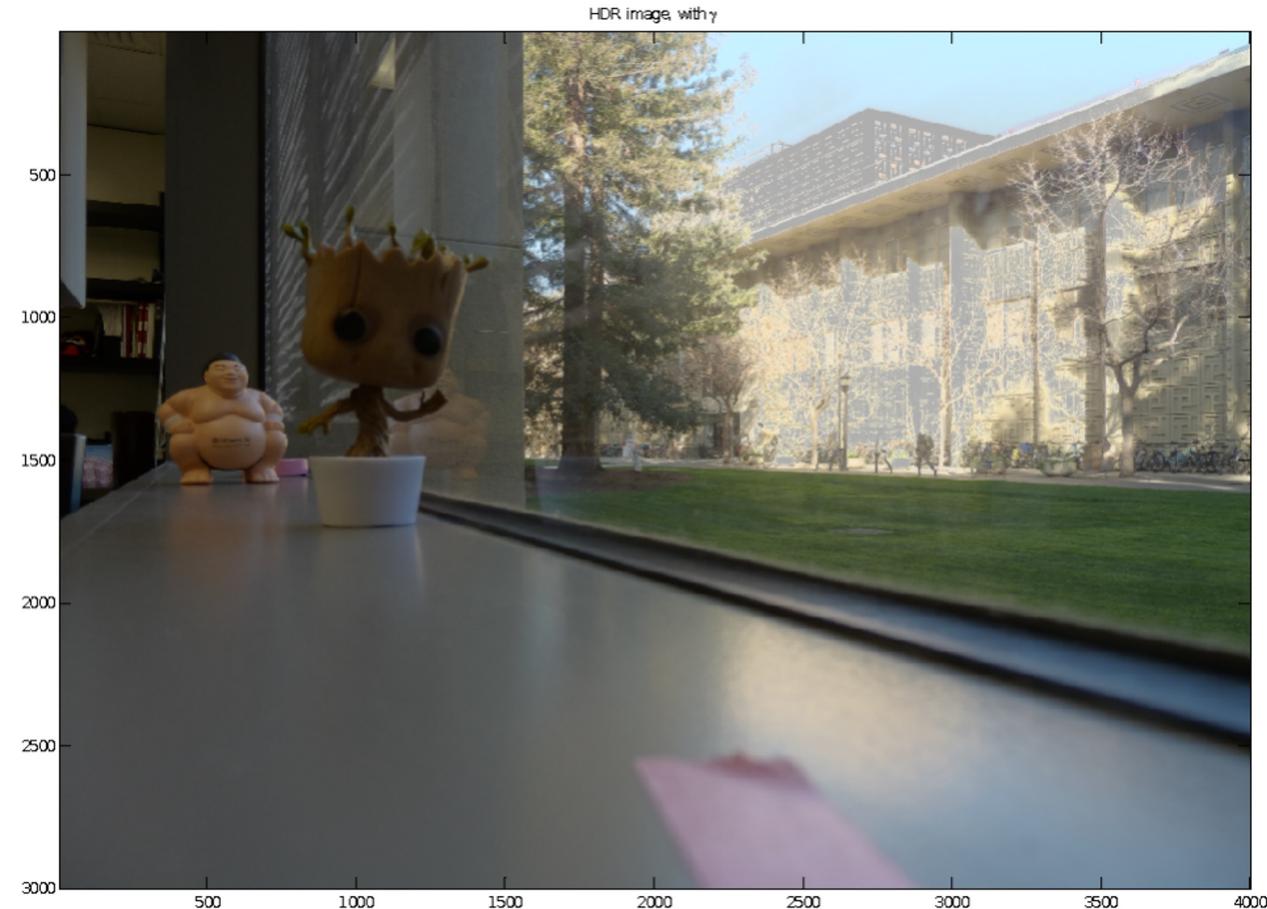
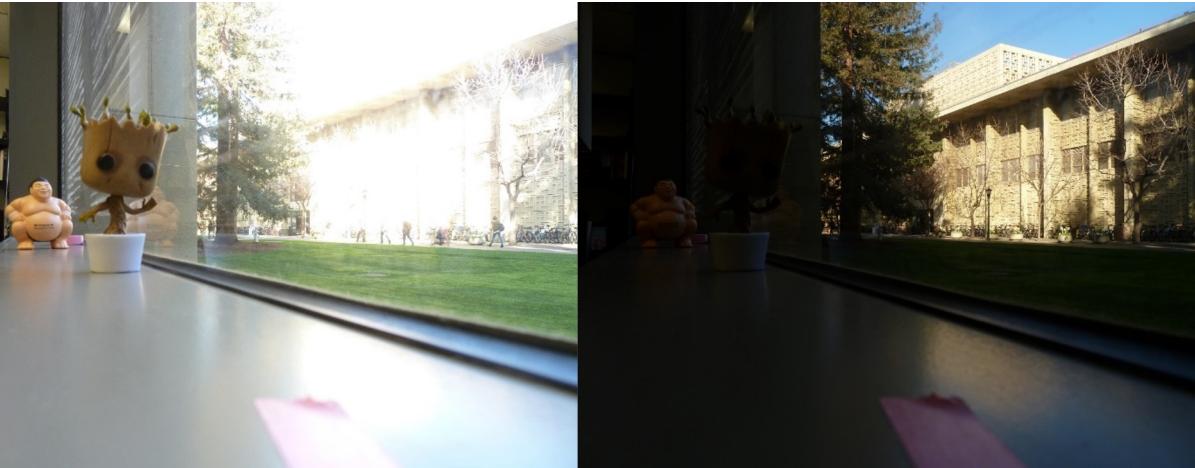
- The average number of photons (the signal)
- The standard deviation of the noise
- and divide them

Don't forget to describe your results and conclusions.

Intuitively, what general behavior do you expect?

Bonus: your own HDR image

Around ~10 images with different exposures



Have a nice weekend!

And good luck with the homework!



Stanford Memorial Church (HDR) <https://www.flickr.com/photos/scottloftesness/4334766965>