

Example: CoLa

```
Constraint loan approval01 {
  loan_approval_clerk.finished precedes loan_approval_supervisor.started
  Documentation: "Clerks must first approve a loan application, only then
are supervisors allowed to further handle the application (reason: cost
reduction)."
 Mandatory: yes
Constraint loan approval02 {
  after loan amount > 100000 [ loan approval.finished leads to
loan_approval_supervisor.started ]
 Documentation: "If the loan amount exceeds 100.000 EUR, then also a
supervisor must approve."
 Mandatory: yes
```

Example: LTL-SNL

```
Constraint loan approval01 {
  not loan_approval_supervisor.started until loan_approval_clerk.finished
 Documentation: "Clerks must first approve a loan application, only then
are supervisors allowed to further handle the application (reason: cost
reduction)."
 Mandatory: yes
Constraint loan approval02 {
  globally(loan amount > 100000 implies globally(loan approval.finished
implies finally loan approval supervisor.started)
  Documentation: "If the loan amount exceeds 100.000 EUR, then also a
supervisor must approve."
 Mandatory: yes
```

Example: TQL

```
Constraint loan approval01 {
  initial truth value: temporarily satisfied
  permanently satisfied: loan approval clerk.finished
  permanently violated: not loan approval supervisor.started until
loan approval clerk.finished
  Documentation: "[...]"
  Mandatory: yes
Constraint loan approval02 {
  initial truth value: temporarily satisfied
  temporarily satisfied: loan amount > 100000 leads-to every
loan_approval.finished leads to loan_approval_supervisor.started
  temporarily violated: loan amount > 100000 leads-to every
loan_approval.finished
  Documentation: "[...]"
  Mandatory: yes
```

CoLa Operators

- A leads-to B: Whenever A happens, B must happen eventually
 - [A] temporarily violated
 - [A, B] temporarily satisfied
 - [A, B, A] temporarily violated
 - [A, B, A, C] temporarily violated
 - [A, B, A, C, B] temporarily satisfied
- A precedes B: B is only allowed to happen if A already has happened
 - [C] temporarily satisfied
 - [C, A] permanently satisfied
 - [C, B] permanently violated
- A occurs
 - [C] temporarily violated
 - [C, A] permanently satisfied
- A never occurs
 - [C] temporarily satisfied
 - [C, A] permanently violated

CoLa

Operators and Scopes

- After C [A leads to B]
 - [A] temporarily satisfied
 - [A, C] temporarily satisfied
 - [A, C, B] temporarily satisfied
 - [A, C, B, A] temporarily violated
 - [A, C, B, A, B] temporarily satisfied
 - [A, C, B, A, B, A] temporarily violated
- Between C and D [A leads to B]
 - [A] temporarily satisfied
 - [A, C, E, A] temporarily satisfied
 - [A, C, E, A, D] permanently violated
- After C until D [A leads to B]
 - [A] temporarily satisfied
 - [A, C, E, A] temporarily violated
 - [A, C, E, A, D] permanently violated

LTL-SNL Operators

- globally p
 - p must always hold
- finally p
 - p must eventually hold
- next p
 - p must hold at the next state
- \blacksquare p₁ until p₂
 - \blacksquare p_1 must hold until p_2 holds
- p₁ weak-until p₂
 - p_1 must hold until p_2 holds or globally not p_1
- Boolean Logic Operators (not, and, or, implies)

LTL-SNL Operator Precedence

- finally, globally, next, not
- until
- weak-until
- and
- or
- implies

Strongest Binding

Weakest Binding

finally A implies not B or P until C (finally A) implies (((not B) or P) until C)

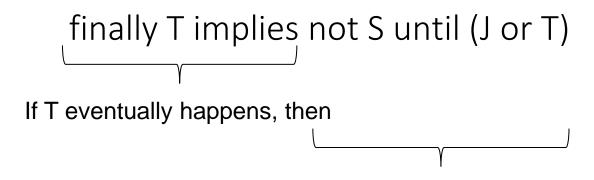
LTL-SNL Example 1

globally(A implies finally B)

Every time A happens, B must follow somewhere thereafter

- temporarily satisfied
 - [A, B]
 - **[**C]
 - [C, B]
 - [C, B, A, C, B]
- temporarily violated
 - [A, B, A]
 - [A, C]
 - [C, B, A]
 - [C, B, A, C, B, A]

LTL-SNL **Example 2**



As long as T has not occurred: temporarily satisfied As soon as T occurs for the first time:

- trace fulfills not S until (J or T) → permanently satisfied
 - [A, T]
 - [A, J, S, T]
- otherwise → permanently violated
 - [A, S, T]
 - [A, S, J, T]

S is not allowed to happen until J or T occurs

TQL **Operators**

- every e
 - fire for every occurrence of e
- not e
 - start as true and change to false once e fires
- not e₁ until e₂
 - becomes true if e_1 does not occur until e_2 occurs
- e_1 and e_2
 - becomes true when both become true
- \bullet e_1 or e_2
 - becomes true when at least one becomes true
- e_1 leads-to e_2
 - becomes true when e_2 is finally followed by e_2

TQL

Operator Precedence

- every, not
- until
- and
- or
- leads-to

Strongest Binding

Weakest Binding

A leads-to not C until B A leads-to ((not C) until B)

TQL Example 1

initial truth value: temporarily satisfied temporarily satisfied query: every(A leads-to B) temporarily violated query: every A

- temporarily satisfied
 - [A, B]
 - [C]
 - [C, B]
 - [C, B, A, C, B]
- temporarily violated
 - [A, B, A]
 - [A, C]
 - [C, B, A]
 - [C, B, A, C, B, A]

TQL Example 2

initial truth value: temporarily satisfied permanently violated query: not M and not Q until K leads-to M permanently satisfied query: not K until Q

- permanently violated
 - [A, K, A, M]
 - [A, K, A, Q, M]
- permanently satisfied
 - [A, Q]
- temporarily satisfied
 - [A]
 - [A, M, K, M]

TQL

Examples for operator *every*

- every(A leads-to B)
 - \blacksquare [A, B] \rightarrow fires
 - [A, B, B]
 - [A, B, B, A]
 - $[A, B, B, A, B] \rightarrow fires$
- A leads-to every B
 - \blacksquare [A, B] \rightarrow fires
 - \blacksquare [A, B, B] \rightarrow fires
- every(A leads-to not C and every(B))
 - $[A, B] \rightarrow fires$
 - [A, B, A, C, B]
 - $[A, B, A, C, B, A, B] \rightarrow fires$
 - $\blacksquare [A, B, A, C, B, A, B, B] \rightarrow \text{fires}$

Possible Truth Value Changes

