- 1. Our car is travelling at a constant velocity of 30 m/s when we spot a priceless painting on the road 100 m in front of us! We apply the brakes, giving our car an acceleration of -5 m/s^2 .
 - Putting our initial position as 0 m and the position of the painting as 100 m, find our position when the car comes to a stop (i.e., when velocity is 0). Did we save the painting?

$$a(t) = -5$$

$$v(t) = -5t + v_0$$

$$= -5t + 30$$

$$x(t) = -2.5t^2 + 30t + x_0$$

$$= -2.5t^2 + 30t$$

The car comes to a stop when v(t) = 0.

$$0 = v(t)$$
$$0 = -5t + 30$$
$$t = 6$$

We need to know if we hit the painting (which is at position 100). We calculate the car's position when it stops.

$$x(t) = -2.5t^2 + 30t$$
$$x(6) = 90$$

We stopped at position 90, so we saved the painting!

2. We are designing a car, and we need to ensure that it has a stopping distance of 50 m when traveling at a speed of 25 m/s. How much acceleration must the brakes be designed to provide?

$$a(t) = -A$$

$$v(t) = -At + v_0$$

$$= -At + 25$$

$$x(t) = -\frac{A}{2}t^2 + 25t + x_0$$

$$= -\frac{A}{2}t^2 + 25t$$

We need to find the time t when the velocity is zero.

$$0 = v(t)$$
$$0 = -At + 25$$
$$t = \frac{25}{A}$$

Our car stops at time $t = \frac{25}{A}$. We need to see how far it goes.

$$x(t) = -\frac{A}{2}t^2 + 25t$$

$$x\left(\frac{25}{A}\right) = -\frac{A}{2}\left(\frac{25}{A}\right)^2 + 25\left(\frac{25}{A}\right)$$

$$= \frac{625}{2A}$$

So our stopping distance is $\frac{652}{2A}$. On the other hand, we need our stopping distance to be 50 m. Equate, and solve for A.

$$50 = \frac{625}{A}$$
$$A = 6.25$$

We need our brakes to be able to apply -6.25 m/s^2 of acceleration.

3. Our car has brakes that can provide -6 m/s^2 acceleration. Find the stopping distance as a function of velocity, and find the velocity at which the stopping distance becomes 100 m (give your answer in m/s and correct to 2 decimal places).