Convolutional Neural Network (CNN) for Digital Radio Frequency Memory (DRFM) Jammers

by

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A thesis submitted to The Johns Hopkins University in conformity with the requirements for the degree of Master of Science.

Baltimore, Maryland

May, 2023

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Abstract

Radar electronic jammers are evolving from hostile nations thus becoming more complex and present serious issues when a radar system is trying to interrogate the actual targets of interest. Electronic jammers that present a serious challenge are in a class called Digital Radio Frequency Memory (DRFM). DRFM techniques work by generating coherent false targets to the radar receiver based on an intercepted pulse signal from the radar transmitter. This will position false targets either ahead or behind the actual radar target, thus masking the real target with false targets. The false targets can also be manipulated in amplitude, phase and frequency.

Traditional approaches to target detection and estimation for electronic jammers in general, rely on parametric modeling, that can fail because it violates the strict assumptions of classical signal processing algorithms. The result is substantial algorithm performance degradation. Furthermore parametric models to handle DRFM jammers are difficult to design and ineffective against an evolving DRFM technology. The key to identifying opportunities for improved electronic jammer protection and

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signal processing in radars is to use machine learning techniques to challenge the underlying assumptions of the standard parametric approach for the design and analysis of radar systems.

Convolutional Neural Networks (CNN) have gained popularity in the last few years with the advent of faster high performance computer systems which rely GPUs for the best computational performance. A CNN operates from a mathematical perspective and is used for non-trivial tasks such as image classification. CNN's have great performance while classifying images when they are very similar to the training dataset. However little work as been done in developing realistic radar models which are ignoring radar environmental and antenna effects thus providing inaccurate simulation training datasets and credibility. In addition, current public available research does not typically consider the five dimensions of a radar sensor, thus presenting an incomplete signal processing chain. From a first principles perspective the radar measures the following aspects of a signal target return: Range, azimuth, elevation, Doppler, and signal amplitude.

We propose to design a CNN that will use both temporal and spatial training datasets, where the radar signal processing with respect to DRFM jamming will be examined to identify and classify DRFM type jammers. The CNN will use raw uncompressed In-phase and Quadrature (IQ) time series data and range-doppler maps

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as inputs to classify if our ground based phased array radar system is being jammed

by DRFM false targets. A suitable network architecture and values for hyperparam-

eters are found by iterative experimental studies. The final classification accuracy

objective will be 95 percent or better. This achieved accuracy suggests that CNNs

can be used to detect radar DRFM jamming with good results and thus allowing a

radar system to decide on any further actions to mitigate a DRFM jammer attack.

Primary Reader and Advisor: Dr. David Shrug

Secondary Reader: Dr. Kurt Stein

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Dedication

Hello, here is some text without a meaning. This text should show what a printed text will look like at this place. If you read this text, you will get no information. Really? Is there no information? Is there a difference between this text and some nonsense like "Huardest gefburn"? Kjift – not at all! A blind text like this gives you information about the selected font, how the letters are written and an impression of the look. This text should contain all letters of the alphabet and it should be written in of the original language. There is no need for special content, but the length of words should match the language.

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Chapter 1

Introduction

1.1 Problem Overview

Ideally radar signal processing should be able to accurately and efficiently detect false or misleading targets of interest. The reality is that typical radar signal processing is ineffective against false targets produced by deceptive electronic jammers. Traditional approaches to target detection and track estimation for electronic countermeasures (ECM) in general, rely on parametric modeling, that can fail because it violates the strict assumptions of classical signal processing algorithms. ECM in general attempts to interfere or deceive the radar system with misleading electronic signals. This failure occurs because the misleading signals and the real targets are processed in the same way at the output of the analog-to-digital converter, thus the false targets and real targets are mixed together. The result is substantial algo-

rithm performance degradation in both target detection and track performance. The matched-filter (see section 2.3.3) which optimizes the SNR for detection processing has no knowledge of target identification, in fact false targets are passed through to the point of detection processing (see Figure 1.1), which then can pollute the tracker and further task scheduling of radar resources towards the misleading signals. We argue that if we can identify when and what type of deceptive jamming is occurring, then the radar can take steps to mitigate or cancel the ECM. We also propose to identify that we have misleading signals prior to processing the detections, thus saving the radar from unnecessary computing cycles to process the false targets and prevent overall algorithm performance degradation. Chapter 2 provides a discussion on radar concepts that hopes to make clear from a mathematics perspective and explanation that there are no clear rules on target deception.

We propose to use machine learning techniques to challenge the underlying assumptions of the standard parametric approach for the design and analysis of radar systems. Convolutional Neural Networks (CNN) have gained popularity in the last few years with the advent of faster high performance Graphics Processing Unit (GPU) computers. Current research demonstrates CNN as a sound approach for radar signal classification with more work to be done. We will show a Convolutional Neural Network (CNN) that will use spatial training datasets in the form of range-Doppler images to perform radar signal classification. The radar signal processing will then

be examined to identify different ECM classes. The goal is to show that ECM can be mitigated and thus improve overall radar performance operation and target recognition. We focus on a particular type of active ECM called Digital Radio Frequency Memory (DRFM). We choose to focus on the DRFM jammer because it's the most problematic ECM for radars to date.

Success is defined by the identification of an ECM, in this case a DRFM jammer and its type via the CNN model. The new CNN model is proposed to be part of the radar's signal processing chain. The DRFM jammer will fail to effect radar detection and tracking operations in the radar. Identification is the first step in mitigating the effects of ECM.

The status quo is the failure to identify false targets or interference is what we face today since DRFM is problematic for typical signal processing. The failure effects are as follows:

- Promotes sub-optional signal processing operation
- Degrades detection performance
- Hides the real targets, deceiving the Tracker

Figure 1.1: Radar Processing Chain with DRFM Jammer

This thesis proposes a novel CNN design exploring gradient descent approaches and cross-entropy loss functions in the application of image classification of radar targets. We put this in the categorically of machine learning. We cast this as an optimization problem where we are attempting to minimize (θ^*) over some loss function $L(\theta)$ to specifically solve an image classification problem.

1.2 Background

In recent years, the development of radar jamming technology is advancing and becoming more problematic for radar signal processing. Digital Radio Frequency

Memory (DRFM) is one of the emerging technologies in the area of active deceptive jamming that is becoming problematic for existing radar capability to keep pace. [1].

An active radar jamming system using DRFM as the central subsystem in the generation and detection of specific signal characteristics was patented by Richard Wiegand in 1985. [2] DRFM works by intercepting the transmitting radar's pulse and then storing in memory its pulse characteristics, thus matching the transmitted pulse. The matching of the transmitted pulse is troublesome because typical signal processing uses a matched filter approach to separate the detection signal from the noise which is dependent on the transmitted pulse. The DRFM will then radiate a signal with a time or doppler delay that will present a false target to the receiving radar. The false target is directed towards the radar main-lobe which makes this a hard problem since this will get processed as a real target detection. We generally define this as deceptive jamming.

Deceptive jamming is a very active field of study in the radar community within the last decade. Major efforts focus on the classification of the jamming signal which is where our interest lies. Various techniques have been studied such as the use of a likelihood generalized function to determine a false target produced by the jammer and a real target of interest. [3] [4] Likelihood methods are what is used in typical signal detection processing and rely on apriori information which needs to match the jammer. This approach falls short in the real world of jammer evolution.

More recently, machine learning techniques have been proposed which have founded

success in image recognition. [5] Machine learning was first conceived from the mathematical modeling of neural networks, which was published in 1943 by Walter Pitts and Warren McCulloch. Through the decades various applications and advancements have occurred. Most notably in 2006 with "deep learning" where Geoffrey Hinton developed algorithms that helped computers recognize different types of objects and text characters in pictures and videos. Also in 2010, ImageNet classification was conceived which dramatically improved the accuracy in machine learning and artificial intelligence image recognition. [6] In terms of radar jammer classification research since 2018 we note some of the relevant contributions which are as follows: A dense false target jamming recognition algorithm using Gabor time-frequency parameters extraction can represent the essential target and false target features based on time-frequency atomic decomposition theory and support vector machine (SVM) is proposed [7]. A decision tree algorithm is proposed to recognize jamming. [8] Another approach is a feature fusion algorithm based on Bayesian decision theory is applied to the recognition of radar deception jamming. These algorithms seems to rely on subject matter expert knowledge in terms of feature extraction and judgment. They do also appear to be ambiguous in areas and can lead to subjectivity, thus leading to problems in robustness and accuracy. There are other contributions [9] [10] [11] that seem well suited but require a large amount of computation resources because of the complexity of the feature extractions. This thesis will focus on image recognition and hopes to address some of the shortcomings in the past and current active research to make

contributions in both the radar and machine learning domains.

1.3 Thesis Overview

The remainder of the thesis is as follows:

- Chapter 2 A review of radar concepts that are essential to the test data generation and the problem space. We will consider a ground based phased array radar system and how we extract information from the radar signals which are then used to train our neural network.
- Chapter 3 A review of machine learning concepts. An introduction to the
 theory and optimization techniques and how that applies to neural networks.
 We will focus specifically on Convolutional Networks (CNN) and justify how
 that applies to our problem space to then propose our algorithms and solution
 approach.
- Chapter 4 An overview of the two simulation models, which are the Radar Model and the CNN Model will be presented in which we detail the theory, mathematics, and provide an overall model overview in terms of the software and hardware used.
- Chapter 5 The thesis results will be provided with an overview of the scenarios and experiments performed. The data analysis approach is defined and the

results are discussed.

• Chapter 6 - The findings and conclusions to the thesis are presented with the proposed future work.

Chapter 2

Radar Concepts

2.1 Overview

This chapter provides some basic radar concepts that help to support this thesis. We will consider for this thesis a phased array radar system and describe its basic signal processing capabilities and techniques. We will also introduce electronic jammers and the various techniques which are fundamental to the groundwork of this thesis. Most of the content is based on years of work-related experience in this field.

The chapter content is mostly supported by the standard references such as Skolnik and Richards which are well known and established throughout the radar community.

2.2 Phased Array Antenna

When we think of radar its common to picture the antenna in our minds. The antenna selection is a unique and important part of any radar. There are various types of antennas used in radar application. This thesis will incorporate and model a ground-based phased array radar system. We focus on using the phased array antenna since this is an antenna type used for the Ballistic Missile Defense System (BMDS) [12] in defense of the United States against ballistic missile threats from hostile nations. A phased array antenna system is typically made up of many transmit and receive (T/R) elements. The T/R element is typically housed within the same module and configured in some geometrical pattern. The AN/TPY-2 radar for example has over 25,000 T/R modules arranged in a rectangular pattern that has an array size of about 9.2 m^2 . The phased array steers the direction of the beams by electronic time-delay or phase shifting of the transmit/receive (T/R) elements. So there is no mechanical motion to direct the antenna towards its intended target of interest. Another feature of an antenna system to consider is how the beams are formed. There are two general approaches to beamforming, they are analog and digital.

Analog beamforming relies on a single electromagnetic signal as the input to each T/R module. This signal can be phase shifted and amplified which is done prior to the analog-to-digital converter (ADC). This has been the approach for the BMDS radars and is considered a cost-effective way of building phased array systems. It can only generate a single beam at a time and thus does not adapt very well to a changing

environment.

Digital beamforming converts the electromagnetic signal at each T/R module into two streams of digital data that are 90 degrees from each other in terms of sin and cos functions. This gives a complex sample at each element of the array. This allows for a digital signal earlier in the signal processing chain. Digital radars are quickly becoming more popular and cost effective since it allows the radar to not only adapt to various array configurations but provides more timely digital data and thus is part of the motivation for this thesis.

2.3 Radar Signals and Detections

Radar signals in the form of electromagnetic energy is both transmitted and received respectively by the transmitter and receiver devices of a radar. A radar typically transmits a waveform modeled by the complex function

$$\bar{s}(t) = A(t)e^{i2\pi f_0(t) + \theta(t)}$$
 (2.1)

Where A(t) is the amplitude over time, f_0 is the carrier frequency of the pulsed waveform, and $\theta(t)$ is the phase component from $[0, \pi]$. This is also considered to be the complex envelop of a linear frequency modulated (LFM) waveform. The transmitted waveform or commonly known as a radar beam can be represented by a rectangular

envelop with a constant amplitude A(t) where τ is the pulse duration.

$$A(t) = \begin{cases} 1 : 0 \le t \le \tau \\ 0 : \text{otherwise} \end{cases}$$
 (2.2)

The LFM waveform which is Doppler tolerant and common for this type of radar will produce a linear sweep across a defined bandwidth β for a given pulsewidth τ is defined by

$$x(t) = \cos\left(\pi \frac{\beta}{\tau} t^2\right) \quad 0 \le t \le \tau$$
 (2.3)

The linear sweep in frequency naturally compresses the signal when processed which makes for excellent Doppler response, which is desired when using range-Doppler images. We do however point out that a large Doppler shift can produce undesired range-Doppler coupling that basically shifts the target inaccurately in range due to the increased target velocity. It will produce range and Doppler smearing (see Figure 2.5 Range-Bin Masking) which we do see in some of the generated range-Doppler images used in the CNN. We include this because its a real world effect. The plot below is from our radar MATLAB model and is using a representative set of parameters that generates our range-Doppler images that demonstrates the desired pulse compression.

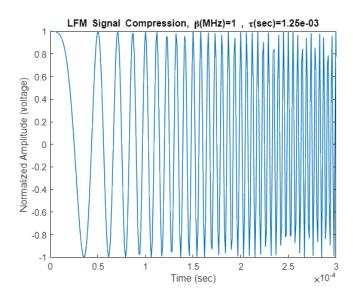


Figure 2.1: LFM Compression

2.3.1 Basic Radar Measurements

Mathematically we start with a dataset that contains digital samples called Inphase and Quadrature (IQ) data. The IQ is the result of converting an analog signal from the radar received signals to a complex number via an analog-to-digital converter processing computer chip. We assume an N-samples data set x[0], x[1], ...x[N-1]. The IQ for each sample in the data set is then a complex number defined by

$$e^{i2\pi ft} = \cos(2\pi ft) + i\sin(2\pi ft) \tag{2.4}$$

where f is the frequency in Hz, $cos(2\pi ft)$ represents the magnitude of the vector, inphase I component and $i \sin(2\pi ft)$ represents the phase, quadrature Q component.

We consider the IQ as a rotating vector in the complex plane. A radar is a five dimensional sensor and these dimensions are the origin of radar signal information that can be derived from the IQ data and the setup of the radar array. The five dimensions are as follows in no particular order: Doppler, range, azimuth, elevation, and amplitude.

Target Doppler
$$f_d = \frac{2v}{c} f_c = \frac{2v}{\lambda_t}$$
 (2.5)

Target Range
$$R = \frac{c\Delta t}{2} \tag{2.6}$$

Target Azimuth
$$\theta_{Az} = \Delta_{Az}/\Sigma$$
 (2.7)

Target Elevation
$$\theta_{El} = \Delta_{El}/\Sigma$$
 (2.8)

Target Amplitude
$$A_{dB} = 10 * log_{10} \left[\frac{I^2 + Q^2}{V_{FullScale}} \right]$$
 (2.9)

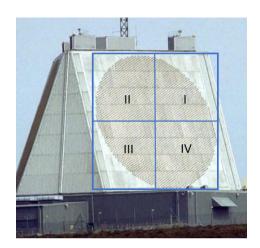


Figure 2.2: Monopulse Antenna Quadrants

The delta $(\Delta_{Az}, \Delta_{El})$ and summation (Σ) channels can be expressed by either

by the amplitude or phase measurements done at the antenna. Where segments I,II,III,IV split the antenna array face up to allow for monopulse measurements. For example, a target that impinges the radar at the origin (i.e. boresight) would calculate a difference of zero in the azimuth and elevation channels, since the amplitude or the phase is centered on the quadrant grid. This is considered a monopulse measurement since it only requires a single pulse to determine the target angle and signal strength.

$$\sum = (I + II + III + IV) \tag{2.10}$$

$$\Delta_{Az} = (I + IV) - (II + III) \tag{2.11}$$

$$\Delta_{El} = (I + II) - (III + IV) \tag{2.12}$$

2.3.2 Radar Signal Processing

Standard radar signal processing starts with and uses a generalized matched filter receiver. The input for the matched filter is the IQ data samples discussed in the previous section. We do note that the IQ gets filtered down to a baseband signal thus removing the carrier frequency and leaving the original baseband signal. The range-doppler maps are dependent on the matched filter output and serve as the primary inputs to our CNN. We will show how the matched filter transforms the output data. The figure below provides the primary components of a standard radar signal processing approach and where we will apply the CNN for image classification.

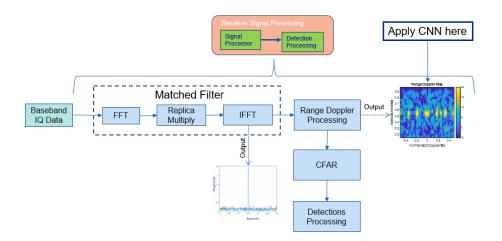


Figure 2.3: Standard Signal Processing Chain

2.3.3 Matched Filter

The matched filter is ubiquitous in radar signal processing and essential for detections processing, thus providing an essential signal processing step in the creation of the range-Doppler images. There is much documented about the matched filter, we cite Skolnik [13] as the reference which is preferred within the radar community. The matched filter attempts to optimize the signal-to-noise (SNR) of a detection in Gaussian noise. The replica or copy of the transmitted signal in our case the LFM waveform is used as a time-reversed and complex conjugate version of the transmitted signal to form the matched filter, which is then convolved with the received signal. We now provide the matched filter derivation to give mathematical reasoning to the range and frequency response of the received signal which makes up the range-Doppler images that are used as inputs to our CNN. We can express a matched filter in various

forms as the Fourier transform of the finite received signal s(t) at some time t, where we define a measured signal with noise as $s_i(t) = x_i(t) + n_i(t)$. Where i depends on the number of samples. The noise $n_i(t)$ is defined as a random process where its mean and auto-correlation functions are time invariant, thus the function $n_i(t)$ is defined as wide-sense stationary (WSS). Now we consider an impulse response h(t) with a Linear Time-Invariant (LTI) filter that takes our measured signal $s_i(t)$ and outputs an optimal filtered response $s_o(t) = x_o(t) + n_o(t)$. We now develop the equations for maximizing the signal to noise ratio (SNR). We first define the signal $s_o(t)$ and noise $n_o(t)$ outputs separately since we are interested in maximizing the ratio of these terms.

$$n_0(t) = n_i(t) * h(t) = \int_{-\infty}^{\infty} n_i(u)h(t-u)du$$
 (2.13)

$$s_0(t) = x_i(t) * h(t) = \int_{-\infty}^{\infty} x_i(u - t_0)h(t - u)du$$
 (2.14)

Now we need to express these equations in terms of signal and noise power. For noise power we assume an auto-correlation function since the input noise is band-limited and WSS. So then we write

$$N_{n_i(t)} = \left(\frac{\eta_0}{2}\right)\delta(t) \tag{2.15}$$

where $\left(\frac{\eta_0}{2}\right)$ is the constant noise source and $\delta(t)$ is the impluse signal or commonly referred to as the Dirac delta function. The auto-correlation in terms of the Fourier

transform of the output noise is

$$N_{n_o(t)} = \left(\frac{\eta_0}{2}\right) |H(f)|^2 \tag{2.16}$$

now expressing as the noise power we get

$$\sigma_{n_0}^2 = \left(\frac{\eta_0}{2}\right) \int_{-\infty}^{\infty} |H(f)|^2 df.$$
 (2.17)

For the signal power we assume a normalized signal power at the output of the matched filter Using Parseval's theorem [14] the total energy of some signal E_x is

$$E_{x_o} = |x_o(t)|^2. (2.18)$$

Taking Eq. (2.14) and applying a Fourier transform we get

$$S_0(f) = X_i(f)H(f)e^{i2\pi f t_0}$$
(2.19)

Integrating

$$s_0(t_0) = \int_{-\infty}^{\infty} X_i(f)H(f)e^{i2\pi f t_0} df$$
 (2.20)

Now apply Eq. (2.18) we get the signal power as

$$E_{x_o} = \left| \int_{-\infty}^{\infty} X_i(f) H(f) e^{i2\pi f t_0} df \right|^2$$
 (2.21)

Combing the signal and the noise as a ratio we get

$$SNR(t_0) = \frac{\left| \int_{-\infty}^{\infty} X_i(f) H(f) e^{i2\pi f t_0} df \right|^2}{\left(\frac{\eta_0}{2}\right) \int_{-\infty}^{\infty} |H(f)|^2 df}$$
(2.22)

The question to ask is what receiver frequency response H(f) will maximize the SNR. We assert that the optimum SNR at the output of the receiver matched filter is expressed in Eq. (2.22) when the numerator is at its maximum. To prove this we can use the Cauchy-Schwarz inequality to establish that we have a maximized SNR dependent on the receiver frequency response H(f). Applying the Cauchy-Schwartz inequality to Eq. (2.22) gives

$$SNR(t_0) = \frac{\left| \int_{-\infty}^{\infty} X_i(f) H(f) e^{i2\pi f t_0} df \right|^2}{\left(\frac{\eta_0}{2}\right) \int_{-\infty}^{\infty} |H(f)|^2 df} \le \frac{\int_{-\infty}^{\infty} |X_i(f)|^2 df |H(f)|^2 df}{\left(\frac{\eta_0}{2}\right) \int_{-\infty}^{\infty} |H(f)|^2 df}$$
(2.23)

$$\leq \frac{2\int_{-\infty}^{\infty} |X_i(f)|^2 df}{\eta_0} \tag{2.24}$$

Equality is assured if and only if $H(f) = \alpha X_i^*(f)^1$, where $X_i^*(f) = H(f)e^{i2\pi ft}$ and α

¹Starred transform which denotes a discrete time version of the Laplace transform

is some arbitrary constant. Thus the SNR is maximized when

$$h(f) = \alpha x_i^* (t_0 - t) \tag{2.25}$$

$$H(f) = \alpha X_i^*(f) e^{-i2\pi f t_0}$$
 (2.26)

Thus we can express the final SNR_{max} equation as

$$SNR_{max}(t_0) = \frac{2E_{x_i}}{\eta_0} \tag{2.27}$$

2.3.4 Detection Fundamentals

The detection itself is fairly straightforward, in which the power of the received signal with noise is compared to some threshold value. A detection is positively identified if the received signal power exceeds the threshold value. Thus the threshold value is critical to establishing detections. In general, the threshold value is a function of both the probability of false alarms and the probability of detections. A target is detected based on establishing a threshold at the output of the radar receiver. If the receiver output is large enough to exceed the threshold, a target is said to be present. The process also then must decide if this detection measurement represents the influence of a target or only signal interference. Statistical signal models are typically used. This then becomes a problem of statistical hypothesis testing.

A primary function of any radar system is the function of generating and process-

ing signal detections. The detection itself is binary, meaning it can be a real or false target of interest. A real target is the signal energy received by the radar receiver reflected from a real target of opportunity. A false target can be interference, random noise, or a jammer that is radiating noise or some deceptive signal towards the radar receiver. If its decided that we have a real target then further detection processing usually happens. A problem occurs when a false target can not determined and thus is considered a real target. The radar can be making up to a million of detection decisions per second. Since we are dealing with a large amount of data for detection decisions, a typical radar system targets can be best represented by statistical signal models. This has limitations since it assumes that the noise and interference levels are known. It also does not account for false targets that are deceptive, which thus appear as real targets when the statistical hypothesis testing is applied.

We propose a range-Doppler processing step to help identify false targets. There are radars today that produce range-Doppler data so this would be to exploit the available data. The range-Doppler data is the input for our CNN that will be used to detect false targets to mitigate the failure effects as follows:

- Sub-optional signal processing operation
- Detection efficiency
- Tracker deception by hiding the real target(s)

2.3.4.1 Detection Hypothesis and Optimization

The standard approach for target detection for any radar measurement depends on two hypothesis, in which one of the two hypothesis is assumed to be true. The radar measurement consists of either

- 1. The radar measurement contains only noise energy. No target is present.
- 2. The radar measurement is a combination of noise and target return energy. A target is present.

We regard this as a binary classification problem. Since we describe the signals statistically we consider the following probability density function (pdf) that describe the radar measurements to be tested under our two hypothesis (1.,2. from above).

$$p_x(\mathbf{x}|H_0) = \text{pdf of } \mathbf{x}$$
 given that the target was not present $p_x(\mathbf{x}|H_1) = \text{pdf of } \mathbf{x}$ given that the target was present

where \mathbf{x} is a column vector of N samples based on some x_n data such that

$$\mathbf{x} \equiv [x_0, x_1, x_2, ... x_{N-1}]'$$

This gives N-dimensional joint pdfs $p_x(x|H_0)$ and $p_x(x|H_1)$, used to consider the following probabilities for use cases which are figures of merit when describing detection

performance.

- 1. Probability of Detection (P_D) : A target is present and detected.
- 2. Probability of False Alarm (P_{FA}) : No target is present but a detection is identified.
- 3. Probability of a Missed Detection (P_M) : A target is present but there is no detection identified where $P_M = 1 P_D$.

The probability of detection and the probability of false alarm are of interest and can be expressed as integrals of joint probabilities over some region $\mathcal{R} = x : P(H_1|x) > l_0$, where l_0 is a threshold defined by $0 \le l_0 \le 1$.

$$P_D = \int_{\mathcal{R}} p_x(\mathbf{x}|H_1) dx \tag{2.28}$$

$$P_{FA} = \int_{\mathcal{R}} p_x(\mathbf{x}|H_0) dx \tag{2.29}$$

Based on the detection hypothesis we need a method to optimize our choice. Most radar detection processing use a Bayes optimization criteria that assigns a cost to a target being present or not present. In most radar systems a special case of the Bayes theorem called the Newman-Pearson (NP) detection criterion is the standard approach. [15] We now will develop the mathematics behind the NP theorem developing a variation to the Gibra explanation. [16]

Assume that the observation of a random variable whose probability density function (pdf) is $\mathcal{N}(\mu, \sigma^2)$ which is a Gaussian pdf with a mean μ and variance σ^2 . We now must determine if the mean is $\mu = 0$, (target not present: $\mathcal{N}[0,1]$) or $\mu = 1$, (target present: $\mathcal{N}[1,1]$). Now we can think of the μ as a hypothesis test such that

$$\mathcal{H}_0: \mu = 0$$
 (null hypothesis) (2.30)

$$\mathcal{H}_1: \mu = 1$$
 (alternative hypothesis) (2.31)

Now the problem is reduced to a binary hypothesis problem where we choose between the null or alternative hypothesis.

Theorem 1. (Neyman-Pearson) Given some probability of false alarm $P_{fa} = \gamma$ determine if a target is present \mathcal{H}_1 using a likelihood ratio function $L(\mathbf{x})$ if

$$L(\mathbf{x}) = \frac{p(\mathbf{x} : \mathcal{H}_1)}{p(\mathbf{x} : \mathcal{H}_0)} > \gamma$$
 (2.32)

where the threshold α is determined by

$$P_{fa} = \int_{x:L(x)>\alpha} p(\boldsymbol{x}:\mathcal{H}_{\prime}) dx = \gamma$$
 (2.33)

Proof. Let R be a critical region determined by the NP criteria, where the critical region given by Eq.(2.30) minimizes the error of Type II (false negative conclusion) for a large range of alternatives. Now suppose that the critical region R is not the

best choice for Type II error minimization. Now let R' be the better choice for Type II error minimization. We assume that both regions R, R' are of the same size α . We also introduce a probability of detection P_d where

$$P_d = (1 - P_{fa}) (2.34)$$

We now approach the proof assuming a minimized P_{fa} that provides a maximum P_d so we proceed in that way. We can use Lagrangian multipliers to maximize the P_d for some given P_{fa} . Using the Lagrangian we get

$$F = P_d + \lambda (P_{fa} - \gamma) \tag{2.35}$$

$$= \int_{R'} p(\mathbf{x} : \mathcal{H}_1) dx + \lambda \left(\int_{R'} p(\mathbf{x} : \mathcal{H}_0) dx - \gamma \right)$$
 (2.36)

$$= \int_{R'} \left[p(\mathbf{x} : \mathcal{H}_1) + \lambda p(\mathbf{x} : \mathcal{H}_0) \right] dx - \lambda \gamma \tag{2.37}$$

Now we consider two cases

case 1:
$$\int_{R'} \left[p(\mathbf{x} : \mathcal{H}_1) + \lambda p(\mathbf{x} : \mathcal{H}_0) \right] dx > 0$$
 (2.38)

case 2:
$$\int_{R'} \left[p(\mathbf{x} : \mathcal{H}_1) + \lambda p(\mathbf{x} : \mathcal{H}_0) \right] dx = 0$$
 (2.39)

For Case 1 to maximize F the integral is positive and \mathbf{x} is included in the region R'. For Case 2 when the integral $\int_{R'}(0) dx = 0$, \mathbf{x} can be found in both regions of R and R'.

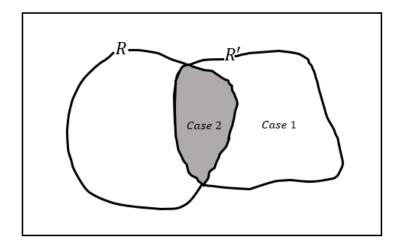


Figure 2.4: Diagram of Two Critcal Regions

We seek to determine the alternative hypothesis and if a target is present we state that

$$\frac{p(\mathbf{x}:\mathcal{H}_1)}{p(\mathbf{x}:\mathcal{H}_0)} > -\lambda \tag{2.40}$$

Given that the likelihood ratio is always positive and assuming that the pdf's are continuous Case 2 is not really required. We now see that $\lambda < 0$ must be true otherwise the likelihood ratio exceeds a negative value. So then we let $\alpha = -\lambda$ which gives

$$\frac{p(\mathbf{x}:\mathcal{H}_1)}{p(\mathbf{x}:\mathcal{H}_0)} > \alpha \tag{2.41}$$

where the threshold value $\alpha > 0$ is determined from the $P_f a = \gamma$.

2.3.4.2 Constant False Alarm Rate (CFAR) Detection

An approach for typical threshold detection processing was discussed in Detection Fundamentals, we now expand on this to include an approach where the noise and interference levels can be variable which is often the case with a real-world radar application. We desire an approach that will adapt to the changing interference and noise environment to establish a defined false alarm rate parameter over some given probability of detection. This concept is fundamental to the radar systems ability to maintain an acceptance false target threshold level. We desire to maintain a constant predictable false alarm rate, the detection threshold will increase or decrease in proportion to the noise power in the reference cells. The probability of false alarm is independent of the noise power. The probability distribution in detection of signals with noise follows a Rayleigh distribution. There are various forms of CFAR we will focus on what works best against typical noise jammers. Cell-averaging (CA)-CFAR is proven to be superior [17] for type of noise or target jamming and is the most widely used. This is considered an adaptive detection threshold technique that assumes that the probability density function of the noise is known. The CA-CFAR process flow is depicted in Figure 2.3. The output of the range-Doppler processing is the input to the square law detector (see Figure 2.2). Also worth noting is that this same input is also used for our CNN. We will argue that the CNN model approach will identify false targets more readily thus offering a better solution than the coventional CA-CFAR approach.

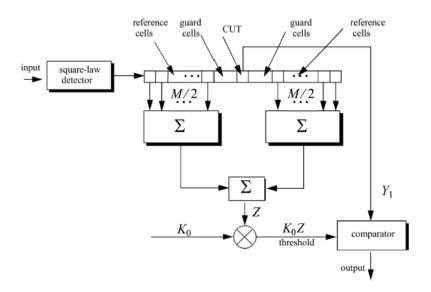


Figure 2.5: Conventional CA-CFAR diagram from B.R. Mahafza, Radar Systems Analysis and Design using MATLAB, 2nd Ed, 2005

The CUT is the cell-under-test. The guard cells provide support to inhibit the signal from leaking into the reference cells and distorting the noise estimate. The reference cells are made up of range and Doppler complex sample data which is also used to produce the range-Doppler images. In general the number of reference cells before and after the CUT is symmetric. We now will develop the (CA)-CFAR mathematics which closely follows Figure 2.3.

We start with a definition of the square-law detector threshold.

$$T_{sqLaw} = K_0 Z (2.42)$$

where the noise power estimate Z and scalar threshold K_0 is

$$Z = \sigma^2 = \frac{1}{M} \sum_{t=1}^{M} s_t \tag{2.43}$$

$$K_0 = -ln(P_{fa}) (2.44)$$

While we did provide an equation for P_{fa} in Eq. (2.29) we should expand more on the mathematical details to build a better intuition for the (CA)-CFAR. We consider a conditional P_{fa} which we average over all the K_0 threshold values such that

$$P_{fa}(K_0) = e^{-K_0/Z} (2.45)$$

We desire a P_{fa} that is independent of the noise power which is the overall objective of conventional CA-CFAR processing. So then, we define an unconditional probability as

$$P_{fa} = \int_0^\infty P_{fa}(K_0)f(z)dz \tag{2.46}$$

We then declare that if all the reference cells are Gaussian and not skewed (i.e. zero mean) with a σ^2 variance. Our noise estimate Z is considered a random variable with

a gamma probability distribution function where

$$f(z) = \frac{z^{(\frac{M}{2}-1)}e^{(\frac{-z}{2Z})}}{2^{\frac{M}{2}}Z^{M}\Gamma(\frac{M}{2})}, \quad z > 0.$$
 (2.47)

The function f(z) is the pdf of the threshold which follows Eq. (2.47) above, which now we define in terms of our scalar threshold K_0 therefore

$$f(z) = \frac{z^{(M-1)}e^{(\frac{-z}{2K_0Z})}}{(2K_0Z)^M\Gamma(M)}, \quad z \ge 0.$$
 (2.48)

Substituting f(z) into Eq. (2.46) and integrating we get the P_{fa} independent of the noise power.

$$P_{fa} = \frac{1}{(1+K_0)^M} \tag{2.49}$$

so then a detection is declared for the CUT at the output of the comparator when

$$Y_1 \ge T_{sqLaw}. (2.50)$$

Note that this is for a single pulse, a similar process can be followed for multiple pulses.

2.4 Electronic Jamming Techniques

Electronic jamming covers various techniques and spans many areas. We will focus on the area of *Deceptive Jamming*. We will look at a class of electronic jammers called smart jammers, commonly referred to as a deceptive jammers or DRFM jammers. Jammers in general are specifically employed to radiate interference via noise or signal towards the opposing radar thus jamming the opposing radar receiver. There are two types of methods for electronic jammers. They are noise and repeaters. Today's electronic countermeasure (ECM) equipment can work both as a deceptive and a noise jammer, while in the past these were two different classes of equipment. The aim of any ECM is to reduce the operational capability of a system. In our case, the system is a ground-based phased array radar.

2.4.1 DRFM

The DRFM has the capability to intercept transmitting radar signals (see section 2.3 Radar Signals) through high speed digital sampling and then stores the samples in memory for later use. DRFM then uses a repeater technique that can modify and re-transmit the stored transmitted signal by adjusting the time or frequency. This results in a false target that is radiated to the opposing radar receiver thus deceiving the radar with a false target position. The deception or false target occurs because the radar echo radiation is matched to the opposing radar's receiver, thus resulting in

a false target detection. A DRFM-based repeater stores each received pulse enabling precise range and Doppler walk off. The DRFM can represent multiple false targets at once thus making it very problematic for typical radar detection processing. The DRFM can be launched from a decoy dispenser or towed behind a missile threat since it is small (55 mm diameter) and light-weight (1.1 kg) [18]



Figure 2.6: Hardware representation of an example DRFM object.

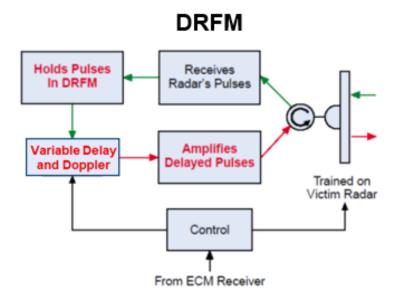


Figure 2.7: DRFM diagram from G. W. Stimson, Introduction to Airborne Radar, 2nd Ed, Scitech, 1998

We now will expand on the different types of DRFM jamming that will become the basis for our range-Doppler images and classes in our CNN. The example figures that follow are generated by our MATLAB Radar model.

2.4.1.1 No Jamming Single Target

We first consider the case where no jamming is present and there is a true intended target detection. Its important that we don't miss-classify a valid detection.

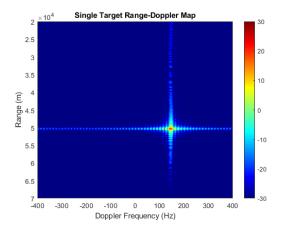


Figure 2.8: Single Target Detection

2.4.1.2 Range-Bin Masking

Range-bin masking obscures the target range by introducing a time-delayed Δt return signal back to the radar receiver which results in various false target detections lined up in the range dimension and centered about the true intended target Recall that target range is defined by $R = \frac{c\Delta t}{2}$

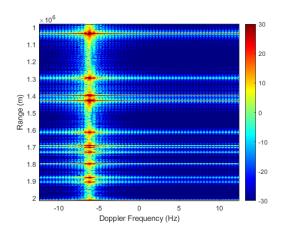


Figure 2.9: Range-Bin Masking

2.4.1.3 Doppler-Bin Masking

Doppler-bin masking obscures the target Doppler response by introducing a variety of slow-time phase modulated signals back to the radar receiver which effects the target velocity v and results in various false target detections lined up in the Doppler dimension and centered about the true intended target. Recall that $f_d = \frac{2v}{c} f_c = \frac{2v}{\lambda_t}$.

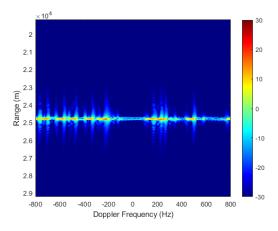


Figure 2.10: Doppler-Bin Masking

2.4.1.4 Combined Range-Doppler Masking

Multiple range and Doppler bins at once can be sent by a DRFM device.

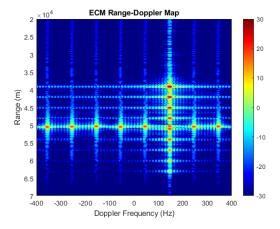


Figure 2.11: Combined Range-Doppler Masking

2.4.1.5 Random Masking

We also consider random false targets sent by a DRFM device.

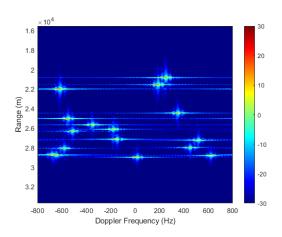


Figure 2.12: Random Masking

2.4.1.6 Interference Jamming

This DRFM will effectively hide the target in range for this example. This is considered interference since it appears as vertical lines in the range-Doppler image.

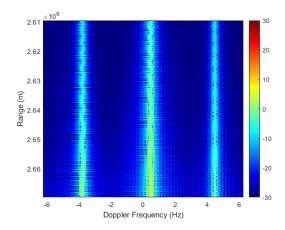


Figure 2.13: Interference Jamming

Chapter 3

Machine Learning

3.1 Basic Concepts

We are still in the age of information with the advent of bigger and faster computers we have been able to store and process more and more big data. An understanding of basic concepts and terminology of machine learning will be addressed here and thus provides a foundation for the material that follows. Arthur Samuel in 1959 popularized the term "Machine Learning" (ML) which is the field of study that gives computers the ability to learn without explicitly being programmed. Since ML is considered an algorithm technique this falls under the larger category of Artificial Intelligence (AI). We define AI as any technique that gives a machine or computer the ability to perform tasks in a way like humans. In order to perform ML we need to first consider a framework for development and testing. We will implement the

ML code using python which is common for most ML applications. We also will use a modern application programming interface (API) called PyTorch [19] as the deep learning framework. This choice was made after struggling with Tensor and Keras when trying to customize the ML code. The selection of PyTorch will also support the programming of any mathematical concepts that we develop. The training and execution will be done on graphics processing units (GPUs) which support parallel processing for faster code execution that we plan to benchmark for performance.

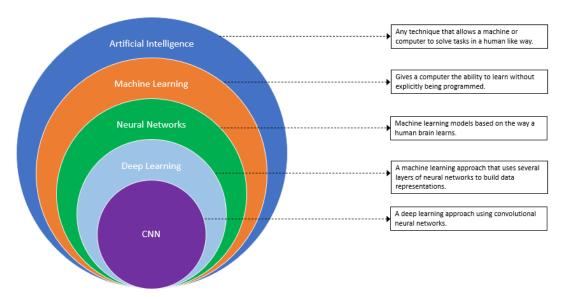


Figure 3.1: Artificial Intelligence

Recall that we are using machine learning techniques because electronic countermeasures (ECM) in general that rely on parametric modeling can fail because it violates the strict assumptions of classical signal processing algorithms. We propose to use supervised ML to label our datasets or images to then train our algorithms that will learn and predict the correct jammer classification. The reasons that follow

support the case for supervised ML:

- The problem of jammer classification is not a simple deterministic rules based solution solved by utilizing radar parameters. You can use supervised ML to effectively solve this problem.
- Radar range-Doppler images can manifest it many ways and thus is considered a large-scale problem. Supervised ML has been proven to be an effective approach for this type of problem. [20]

We realize that there is no ideal solution and using the George Box quote "all models are wrong, but some are useful". So we propose stacking simple models in a creative fashion to realize a deep learning architecture such as CNN. Fundamentally we are seeking reduced dimensionality of our data to extract the image features which in our case are the target detections. The image features that are prominent would be the range, Doppler, and the target signal strength with noise. We strive to develop a CNN that will recognize the patterns for the various DRFM jammer types described and illustrated in section 2.4.1., thus making the correct DRFM jammer type classification.

3.2 Hyperparameters

The selection and initial values of the parameters used in any machine learning problem is critical to understand to make the best use and choice for the problem

space. We research different approaches and make recommendations that propose modifications to fit our problem space. We also propose to explore particular areas of interest so as to not limit or constrain ourselves to any one aspect of machine learning. The chosen areas of focus are detailed in the subsections that follow. The typical processing sequence used in machine learning for CNN motivates our areas of interest and exploration. The notional diagram below depicts the CNN processing chain.

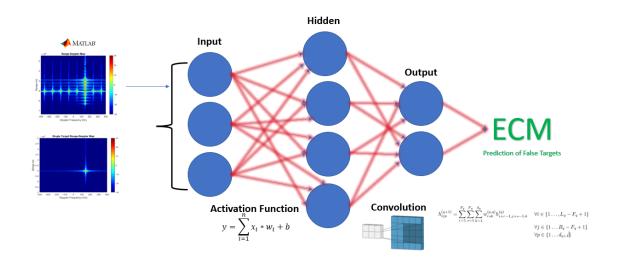


Figure 3.2: High-Level CNN Processing Chain

3.2.1 Hyperparameters Tuning

Hyperparameter tuning and machine learning in general is often done manually by hand in a trail and error approach which relies on the empirical results to guide the experimenter in the optimization of the hyperparameters. This can be very time

consuming to explore the hyperparameter space. There are two popular choices for a model and a brute force approach like Grid Search could be used by defining a search space over all the hyperparameters and going through every position in the grid which is not efficient. Random Search is the other approach where random values are chosen so there is the possibly of discovery but you could also miss important settings. So we must carefully define and constrain our model. We explore several key hyperparameters to optimize our tuning and results. A mathematical approach will be developed in this chapter so as to gain a more rigorous understanding for better informed choices when conducting our experiments.

Hyperparameter	Description	Value
Number of Filters	Used to map the activations from one layer to the next. The filter contains the trained weights and matches the kernel size.	[16,32,64,96]
Kernel Size	Generalized sliding dot product or convolution operation into higher dimensional spaces that are linearly separable. We convolve the filter(nxn kernel size) with the image.	[3,4,5]
Batch Size	Mini-batch size from our image dataset	[32-256]
Activation Function	Transforms our dot product summations into the final output feature vector.	ReLU with softmax
Number of Layers	The number of convolutional layers	[3-5]
Optimizer	Customized SGD (see section 3.3)	ALRM
Learning Rate	Quasi-Newton method (see section 3.3.1)	Trained automatically through ALRM
Momentum	Stochastic heavy ball method (see section 3.3.2)	Trained automatically through ALRM
Max Pooling	Creates a down-sampled feature map based on the largest segment of each feature map.	True or False
Dropout	Randomly discards nodes by setting them to zero. This helps to regularize which helps to prevent overfitting.	True or False

Figure 3.3: Hyperparameters (Place Holder)

3.2.2 Activation Function

The activation function is responsible for the output of a node, in our case a node is each pixel for our Range-Doppler image. Each image is a 32x32 square matrix so that is 1024 input nodes in total. The question answered here "Is this pixel useful or not?", if useful then that pixel gets activated "fired like in the brain" and considered important, in a sense it's like a mathematical filter or gate. The input to the activation function is the image matrix that has gone through convolution. In this case, we are seeking a non-linear activation function with a purpose to add non-linearity to the NN, without the activation function it would be linear by design because all the hidden layers will behave in the same way because the addition of two or more linear functions is linear. In modern neural networks, the default recommendation is to use the rectified linear unit or ReLu. [21] That however does not prelude us from gaining a mathematical perspective and selecting the proper activation function for this problem.

A nonlinear activation function f() sometimes called a transfer function [22] can be expressed as

$$y(x,w) = f\left(\sum_{k=1}^{N} w_k \phi_k(x)\right) = \mathbf{w}^T \phi(x)$$
(3.1)

Where N is the total number of parameters in the model. We now extend this function by making the basis functions $\phi_k(x)$ or features depend on N parameters, along with

adjusting the weighing coefficients w_k during the training of our CNN model. This then gives us a general neural network model that can be expressed as

$$a_k = \sum_{l=1}^{M} w_{kl} x_l + b_l \tag{3.2}$$

where b_0 is the bias constant and a_k is our activations. We now can use a transformation assuming a differentiable non-linear activation function $h_j = g(a_k)$ to then give the output of each activation.

$$a_i^{(1)} = \sum_{j=1}^{M} w_{ij}^{(1)} h_j + b_j^{(1)}$$
(3.3)

We use the notation $a_i^{(1,2,\dots)}$ to denote the layers of our network. There can be multiple layers which is common for CNNs. Written in matrix and vector form we get

$$\sum_{j=1}^{M} w_{ij}^{(1)} h_j + b_j = \begin{bmatrix}
w_{0,0}^{(1)} & w_{0,1}^{(1)} & \dots & w_{0,j}^{(1)} \\
w_{1,0}^{(1)} & w_{1,1}^{(1)} & \dots & w_{1,j}^{(1)} \\
\vdots & \vdots & \ddots & \vdots \\
w_{k,0}^{(1)} & w_{i,1}^{(1)} & \dots & w_{i,j}^{(1)}
\end{bmatrix} \begin{bmatrix} h_0 \\ h_1 \\ \vdots \\ h_j \end{bmatrix} + \begin{bmatrix} b_0 \\ b_1 \\ \vdots \\ b_j \end{bmatrix}$$
(3.4)

Written in a compact form we get

$$\mathbf{a}^{(1)} = f(\mathbf{W}^{(1)}\mathbf{h} + \mathbf{b}) \tag{3.5}$$

This now makes it convenient for writing a code block as this simply can be written for example in Python as a = relu(dot(w, h) + b) where relu is the rectified linear unit activation function.

Now that we have some mathematical insight into the activation function, we can precede with an approach for selecting the best activation function for the problem at hand which we consider as a categorical image classification. Since our problem involves multiple classifications we can eliminate any activation function that is binary or is susceptible to vanish gradients. So for example the binary activation functions like binary step and sign functions would not be useful. Functions such as tanh and sigmiod can saturate or cause vanishing gradients which is not what we want when filtering through data. We now define requirements for a good activation function for our image classification.

- Nonlinear activation function since we have a multi-layer network
- Differentiable and monotonic to allow back propagation
- Speed and accuracy
- Solve vanishing gradient or saturation problem

After conducting research ReLU seems to be the best choice, although we need to consider the negative values mapping to zero (i.e. dead neurons). ReLU is based on a cortex-inspired silicon circuit. [23] It has been demonstrated to improve the training of

deep neural networks for deep learning. [24] We define the ReLU function as follows:

$$f(\theta) = max(0, \theta) = \begin{cases} \theta : \theta \ge 0 \\ -\theta : \theta < 0 \end{cases}$$
(3.6)

$$f'(\theta) = \begin{cases} 1 : \theta > 0 \\ 0 : \theta < 0 \end{cases}$$

$$(3.7)$$

We note that ReLU is not differentiable at zero. We can arbitrarily assume when $\theta = 0$ that the differentiated value is zero. Also negative values result in a dead neuron since $f'(\theta) = 0$ for $\theta < 0$ such that no gradients flow back through the CNN processing chain. The consequence of pushing too many negative values through the processing chain is that our model will stop learning, since the activation is zero. To address this issue we can facilitate a slight curve or linear slope thus the negative values result in $f'(\theta) < 0$. Another approach is to lower the learning rate which we will explore in section 3.2.4.1.

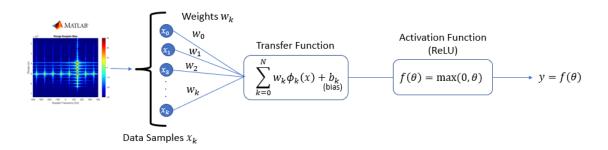


Figure 3.4: ReLU Data Flow

3.2.3 Loss Function

The function that we that we minimize or maximize over is typically called the objective function. Since we are minimizing over some objective function and extracting an error measurement, we will refer to this as the loss function. The loss function is used to evaluate the model predictions versus the truth or input data, so this is performed at the output layer or end of the neural network. The loss function acts as a guide to the optimizer which attempts to provide the correct direction towards the global minimum. The output is a scalar number that is used to minimize or maximize the model loss, which allows us to rank or compare candidate solutions. The question answered here is "How good or useful is my model at making predictions using a given set of parameters (i.e. weights and biases)?" Is it "To good to be true!" which is overfitting and not useful at all. Which loss function do we use? There are many different loss functions that can be used to provide error estimates for each set of parameter weights in a CNN. Cross-entropy is the default loss function to use for most multi-class classification problems. Cross-entropy measures the error between two probability distributions. We consider the predicted model and the true training probability distributions. We seek to minimize the cross-entropy between these two distributions. A nice feature of a cross-entropy approach is that it heavily penalizes wrong predictions that have a high confidence. We also propose a constraint of a symmetric loss. The claim is that we do not always expect clean data and thus must account for noisy data in our classification. It is also highly desirable to learn from

corrupted data since we expect this in real-world applications.

We define our loss model as

$$\mathcal{L}(X,\theta) = -\sum_{j=1}^{N} X_j log(\theta_j)$$
(3.8)

where X is random variable whose domain is our dataset of range-Doppler samples and θ between (0,1] is the predicted variable of interest. We apply a negative sign since the $log(\theta_j)$ is a negative value thus giving the positive probability that we desire. Since we have multiple classes we need a a function to keep track of the probabilities of each class. Since the output of $\mathcal{L}(X,\theta)$ is a vector of real numbers, we need a way to convert that to probabilities. The common approach is to use a softmax function which outputs a vector of sample values that sum up to a value of 1, which is generating the predicted probability distribution of the classes we define. Ideally the aim is to have the samples to be as close to unity as possible so then we have the highest probability of the correct classification. We define our softmax function as $p: \mathbb{R}^N \to [0,1]^N$ where $N \geq 1$ such that

$$p_i = \frac{e^{s_i}}{\sum_{j=1}^N e^{s_j}} \tag{3.9}$$

where i = 1, 2, ...N and $\mathbf{s} = [s_1, s_2, ...s_N] \in \mathbb{R}^N$

Using our logarithmic measure from Eq.(3.8) we now have our general equation for

the loss function.

$$-\sum_{i=1}^{N} \log \left(\frac{e^{s_i}}{\sum_{j=1}^{K} e^{s_j}} \right)$$
 (3.10)

3.2.4 Optimization

We define our problem as non-convex which fits for a stochastic gradient descent (SGD) based optimization approach. This implies that we seek an optimization that is not based on a direct calculation of the gradient. The SGD approach aligns with real world types of problems where analytical solutions are very few. We also confine our focus to mini-batch SGD which is the popular choice for training a CNN. Online training was considered but seems impractical to adjust the gradient after each forward and backwards pass of the data thus affecting overall performance. Using the mini-batch approach allows each subset of data to be trained with the gradient estimated at each step. The motivation is twofold. First we are not loading the data all at one time thus reducing the memory footprint. In our problem space that amounts to over (32x32x4000) 4 million data samples. Second we are updating the parameters more frequently with mini-batch by running numerous batches compared to a single batch. Therefore we reduce the probability of getting stuck in a local minima and increase the probability of finding a global minima. Compare this to a full batch that tends to get stuck in local minima thus not optimal for global solutions. [25] An additional consideration is the speeding up of the convergence. Learning rate and

momentum methods can be used to accelerate the solution convergence compared to default SGD. For optimization we will establish a customized SGD approach that fits our problem space of range-Doppler imaging classification. The overall goal of our optimization process is to fine-tune the model weights to include bias to therefore have an optimized model that makes the most correct predictions for the given image test data set.

3.2.4.1 Learning Rate and Momentum

Learning rates matter and its regard among practitioners to be the most important hyperparameter to tune. [26] [21] Too large a step and we diverge, too small of a step and we do not make progress. So if I'm really confident about the gradient then for example we can set the learning rate = 1.0 and take a confident large step forward. If its uncertain then a smaller step or learning rate is required but now it takes longer to converge to a global minima or worse get stuck in less desirable local minima. How do we make the optimal choice for the learning rate? There are two popular choices to consider they are learning rate schedulers and adaptive learning rate methods. We seek an adaptive method. Using an adaptive approach we hope to optimize the step size to avoid small local minima and thus converge faster and have more accurate learning models that seek a global minima. We propose to combine an adaptive learning rate and momentum so as not to concern the user with having to experiment with setting these hyperparameters to obtain the best results. Recent

activity in this area has motivated research in finding optimal solutions for these hyperparameters [27] [28] and thus is the foundation for a new algorithm that we name the Adaptive Learning Rate and Momentum (ALRM) method. Our high-level goals for this method are to reduce the computational complexity, faster convergence to a global minimum with auto tuning parameters that provide numerical stability, and easy implementation of the algorithms.

3.3 ALRM Method

We start with a default expression for SGD where θ_t is our model variable parameter of interest that are more precisely mathematical tensors which are estimated by our equation, X_t is a random variable and η_t is the adaptive learning rate we evaluate at each iteration using the training image data as input:

$$\theta_{t+1} = \theta_t - \eta_t \nabla \mathcal{L}(X_t, \theta_t) \tag{3.11}$$

Research points out a sensitivity to the learning rate for default SGD. [29] [30] So we propose an implicit SGD approach that reduces learning rate sensitivity and provides numerical stability. Implicit updates are simply evaluated at the next iteration (t+1) rather than the current iteration (t). We define this as implicit because we have θ_{t+1}

on both sides of the equation. So then we have

$$\theta_{t+1} = \theta_t - \eta_t \nabla \mathcal{L}(X_t, \theta_{t+1}) \tag{3.12}$$

Expanding on this implicit Eq.(3.12) to gain more intuition and motivate numerical stability [31], lets suppose a limit that approaches infinity for our model vector parameter θ such that

$$\lim_{n \to \infty} \theta_{t+1}^{(n)} \quad \text{where } n \in \mathbb{Z}^{0+}$$
 (3.13)

Now lets write out the sequence

$$\theta_{t+1}^{(1)} = \theta_t - \eta_t \nabla \mathcal{L}(X_t, \theta_t^{(0)})$$

$$\theta_{t+1}^{(2)} = \theta_t - \eta_t \nabla \mathcal{L}(X_t, \theta_{t+1}^{(1)})$$

...

$$\theta_{t+1}^{(\infty)} = \theta_t - \eta_t \nabla \mathcal{L}(X_t, \theta_{t+1}^{(\infty)}).$$

We can observe that the last term of the sequence above can be re-written as $\theta_{t+1} = \theta_t - \eta_t \nabla \mathcal{L}(X_t, \theta_{t+1})$ where we assume that the limit converges to a fixed point. We then have the implicit SGD we defined in Eq. (3.12). Therefore the implicit SGD is shown to be a repeated sequence or variant of the default expression for SGD. Its

easy to see that we are just updating the θ_t term until a fixed point or optimal solution is reached. This concept is related to the *self-consistency principle* in statistics. The term "self-consistency" was introduced in 1989 by Hastie and Stuetzle, where given a smooth curve or surface that each point is considered the mean of all points that project orthogonally onto it. We now provide mathematical argument for numerical stability by re-writing our implicit Eq.(3.12).

$$\theta_{t+1} = \theta_t - \eta_t \nabla \mathcal{L}(X_t, \theta_t),$$

$$\theta_t = \theta_{t+1} + \eta_t \nabla \mathcal{L}(X_t, \theta_t),$$

$$||\theta_t - \theta^*||^2 \ge ||\theta_{t+1} - \theta^*||^2 + 2\eta_t (\theta_{t+1} - \theta^*)^T \nabla \mathcal{L}(X_t, \theta_t),$$

$$||\theta_t - \theta^*||^2 \ge (1 + \eta_t \mu) ||\theta_{t+1} - \theta^*||^2 \quad \text{where } \mu > 0,$$

$$||\theta_{t+1} - \theta^*||^2 \le \frac{1}{(1 + \eta_t \mu)} ||\theta_t - \theta^*||^2.$$

This shows that $||\theta_{t+1} - \theta^*||^2$ has a high probability of contracting and thus providing the numerical stability that we desire.

A critical and important operation is finding the weighted averages of our function. So we define a finite-sum structure by minimizing over our loss function $\mathcal{L}(X,\theta)$ that is continuously differentiable over a dataset space called S where $\mathcal{L}(X,\theta)$ is defined by

$$\mathcal{L}(X,\theta): [S \subset \mathbb{R}^n \to \mathbb{R}]$$
 where n is the number of sample data points (3.14)

We consider an unconstrained optimization in which we seek the minimization of

$$\theta^* = \min_{\theta \in \mathbb{R}^n} \mathcal{L}(X, \theta) = \frac{1}{n} \sum_{t=1}^n \ell_t(X, \theta)$$
(3.15)

$$\approx \mathbb{E}[\ell(X,\theta)] \tag{3.16}$$

such that a sample data point θ^* is a local minimum if $\mathcal{L}(\theta^*) \leq \mathcal{L}(X,\theta) \forall \in S$. Furthermore we make the following assumptions for non-convex stochastic optimization which are typical for this type of problem.

- Assumption 1: The stochastic gradient is uniformly bounded, for example, $\sup_t(||g^t||) \leq R$ with R > 0.
- Assumption 2: The SGD is an unbiased estimate, for example, $\mathbb{E}[\ell(X,\theta)] = \nabla \mathcal{L}(X,\theta_{t+1}).$
- Assumption 3: The gradient of \mathcal{L} is L-Lipschitz, for example, $||\nabla \mathcal{L}(x) \nabla \mathcal{L}(y) \leq L||x-y|| \text{ where } L > 0.$

3.3.1 Learning Rate Dynamic Adjustment

We propose using a Quasi-Newton method which is a well established approach to solve a non-convex optimization problem. This is based on Newton's method which is an alternative that assumes that the Hessian matrix is not available or practical since its computational complexity is $\mathcal{O}(n^3)$ to compute the Hessian matrix and its inverse.

So then the idea is to then approximate the Hessian (and it's inverse) matrix. We will start with the BFGS method which is named after the authors Broyden, Fletcher, Goldfarb, and Shanno and is considered a very effective Quasi-Newton method and its computational complexity $\mathcal{O}(n^2)$ is less expensive to compute and given by [32]:

$$B_{k+1} = B_k - \frac{1}{\mathbf{s}_k^T B_k \mathbf{s}_k} B_k \mathbf{s}_k \mathbf{s}_k^T B_k + \frac{1}{\mathbf{y}_k^T \mathbf{s}_k} \mathbf{y}_k \mathbf{y}_k^T$$
(3.17)

where

$$y_k = \nabla \mathcal{L}(\theta_{k+1}) - \nabla \mathcal{L}(\theta_k)$$
 and $s_k = \theta_{k+1} - \theta_k$.

The BFGS method provides positive-definite solutions so then we define B_k as the Hessian estimate which is a positive definite symmetric nxn matrix, furthermore the matrix B_{k+1} is guaranteed to be positive definite given B_k is also positive definite and we satisfy the curvature condition of $\mathbf{s}_k^T \mathbf{y}_k > 0$. There is still a performance concern if the rank of the matrix B_k is high. The optimization problem we are solving assumes to be unconstrained since we are required to solve for $\nabla \mathcal{L}(\theta_k)$ at each iteration. There are methods that we recommend to construct a sequence of lower rank matrices that have been proven to do a good job of approximating the Hessian matrix and thus provide the improved computational performance we seek. The limited-memory BFGS (L-BFGS) is that method [33]. So then we continue with

Eq. (3.16) and let us define S_k and Y_k by $(n \times k)$ matrices where

$$S_k \stackrel{\Delta}{=} [\mathbf{s}_0, \mathbf{s}_1, ..., \mathbf{s}_{k-1}] \tag{3.18}$$

$$Y_k \stackrel{\Delta}{=} [\mathbf{y}_0, \mathbf{y}_1, ..., \mathbf{y}_{k-1}] \tag{3.19}$$

Then let B_0 be a positive definite symmetric nxn matrix such that $s_i^T y_i > 0$ then using Eq. (3.16) we get a more compact form

$$B_{k} = B_{0} - [B_{0}S_{k} Y_{k}] \begin{bmatrix} S_{k}^{T}B_{0}S_{k} & L_{k} \\ L_{k}^{T} & -D_{k} \end{bmatrix}^{-1} \begin{bmatrix} S_{k}^{T}B_{0} \\ Y_{k}^{T} \end{bmatrix}$$
(3.20)

where D_k is the diagonal part and L_k the lower triangular part of the matrix we define as a symmetric $k \times k$ matrix

$$(L_k)_{i,j} = \begin{cases} s_{i-1}^T y_{j-1} & if \ i > j \\ 0 & otherwise. \end{cases}$$

$$(3.21)$$

We now take the compact form of the BFGS Eq. (3.19) and define as L-BFGS. Let $B_0 = \sigma I$ where I is an identity matrix and σ is a positive scale value. Substituting into Eq. (3.20) we then get

$$B_k = \sigma I - [\sigma S_k Y_k] \begin{bmatrix} S_k^T \sigma S_k & L_k \\ L_k^T & -D_k \end{bmatrix}^{-1} \begin{bmatrix} S_k^T \sigma \\ Y_k^T \end{bmatrix}$$
(3.22)

We now provide the inverse of the Hessian estimate H_k where $H_k = B_k^{-1}$, so then we simply get

$$H_{k+1} = \left(I - \frac{y_k s_k^T}{y_k^T s_k}\right) H_k \left(I - \frac{s_k y_k^T}{y_k s_k^T}\right) + \frac{y_k y_k^T}{y_k s_k^T}$$
(3.23)

Its important to point out that the main weakness we discovered of the L-BFGS method. If we have a Hessian matrix that contains a wide variance of eigenvalues, the solution tends to convergence more slowly due to the ill-conditioned problem. This approach is still favorable over a basic gradient descent since it has the property of always monotonically decreasing at each iteration unless the model parameter θ has arrived at a local or global minimum. Also keeping in mind one of our goals for ALRM is for easy implementation. Code libraries exist for the L-BFGS method through Tensorflow and SciPy, which aligns with our coding implementation strategy. We do however need to modify and extend the code to implement our ALRM method.

3.3.2 Momentum Dynamic Adjustment

The use of stochastic momentum with SGD is a popular choice and widely accepted which we will explore. In particular, we consider a stochastic heavy ball momentum with Polyak averaging or Polyak's momentum. [34] The motivation is to escape the local minima or saddle points which can inhibit the path to a global minimum. We did consider Nesterov momentum which is also a popular choice and is

an option in the popular Adam optimizer. Since we are using a finite sum structure recent papers have proved a possible divergence with Nesterov's approach. [35] [36]

First we assert that a weighted average of stochastic gradients will be preserved at each iteration through our sample data, commonly referred to as Polyak-Ruppert averaging. We also will concentrate on locating a second-order point assuming a smooth non-convex optimization by implicit SGD using a stochastic heavy ball method which we first establish by the heavy ball method which is defined by the following state transitions:

$$p_t = \nabla \mathcal{L}(X, \theta_{t+1}) \mid \nu_t p_{t+1} \tag{3.24}$$

$$\theta_{t+1} = \theta_t + \eta_t p_t \tag{3.25}$$

We can rewrite this as the iteration using our general Eq. (3.12) that we derived earlier.

$$\theta_{t+1} = \theta_t - \eta_t \nabla \ell_t(X, \theta_{t+1}) + \nu_t(\theta_{t+1} - \theta_t)$$
(3.26)

where the term $\nu_t(\theta_{t+1} - \theta_t)$ is referred to as momentum. Note that we replaced the true gradient $\nabla \mathcal{L}(\theta_{t+1})$ with our unbiased estimate gradient from assumption 2 where $\nabla \ell_t = \mathbb{E}[\ell(X, \theta)]$ to simply make this a stochastic heavy ball method. We now have a general Eq.(3.26) for the learning rate η_t combined with momentum ν_t .

3.3.3 Algorithms

The algorithms in this section are implemented in python using

Algorithm 1 ALRM, our new algorithm for SGD that incorporates adaptive methods for learning rate and momentum. Vector operation is element-by-element. Still in work...

```
Require: \nabla \ell_t(X, \theta_{t+1}): SGD loss function
Require: X: Random variable
Require: \theta: Model parameter weights

    ∨ Variable column vector of interest

Require: \epsilon: Convergence tolerance
Require: \eta: Learning rate
Require: \nu: Momentum
Require: m: Mini-batch size
Ensure: \epsilon > 0
 1: Input: A set of training data that consists of training vectors \{x_n\} where n=1
     \{1, 2, ..., N\}.
 2: function ALRM(a, b)
         for t = 0, ..., T do
 3:
              Choose m integers k_1, k_2, ..., k_m uniformly and independent from \{1, 2, 3, ..., N\}
 4:
              s_t \leftarrow \text{sample a mini-batch of set of training data using } m \text{ integers without replacement}
 5:
              while ||\nabla \ell(X, \theta_{t+1}) < \epsilon|| do
                                                                           6:
                                                     \triangleright \eta will be smaller by at most a factor of \beta
                  \eta \leftarrow \beta \cdot \eta
 7:
                  perform Quasi-Newton method
                                                                                      \triangleright See Algorithm 2
 8:
                  perform stochastic heavy-ball method
                                                                                      ⊳ See Algorithm 3
 9:
                  \theta_{t+1} \leftarrow \theta_t - \eta_t \nabla \ell_t(X, \theta_{t+1}) + \nu_t(\theta_{t+1} - \theta_t) \triangleright \text{Implicit SGD with } \eta \text{ and } \nu
10:
              end while
11:
             \theta_{\mathbf{t}+\mathbf{1}} \leftarrow \hat{\theta}_{\mathbf{t}}
12:
         end for
13:
         return \theta_{t+1}
14:
15: end function
```

Algorithm 2 Quasi-Newton Method based on L-BFGS, solve a non-linear optimization problem with an approximation of the Hessian matrix and its inverse. Still in work...

```
Require: \epsilon: Convergence tolerance
Require: \nabla \ell(\theta): Gradient loss function
Ensure: \epsilon > 0
 1: function L-BFGS(a, b)
         Choose an initial Hessian inverse H_t^0
                                                                                                    ⊳ cite
         p_k \leftarrow -H_t \nabla \ell(X, \theta_{t+1})
                                                                   \triangleright compute a search direction p_t
 3:
 4:
         x_{t+1} \leftarrow x_t + \eta_t p_t
                                                          \triangleright \eta satisfies the Wolfe conditions(cite)
         if t>m then
 5:
             \{s_{t-m}, y_{t-m}\}
                                                                               6:
         end if
 7:
         s_t \leftarrow x_{t+1} - x_t
                                                                                    8:
         y_t \leftarrow \nabla \ell(\theta_{t+1}) - \nabla \ell(\theta_t)

▷ save in memory

 9:
         t \leftarrow t + 1
10:
11:
         if \sim (converged || failed) then
             return inverse Hessain updated state
12:
         end if
13:
14: end function
```

Algorithm 3 Momentum Method, a stochastic heavy ball method based on Polyak momentum. Still in work...

```
Require: 0 \le \nu \le 1: Momentum

Require: 0 \le \eta \le 1: Learning rate (i.e. Step size)

1: function SHB(a,b)

2: for t = 0, ..., T do

3: \theta_{t+1} = \theta_t - \eta_t \nabla \ell_t(X, \theta_{t+1}) + \nu_t(\theta_{t+1} - \theta_t)

4: end for

5: return \nu

6: end function
```

Chapter 4

Models

4.1 Overview

Models rooted in the MATLAB and Python code base are used for conducting experiments to determine the goodness of our CNN model with the proposed ALRM method.

4.2 Radar Simulation Model

The radar model is implemented in MATLAB. The selection of MATLAB is based on several reasons. First, many professional radar engineers rely on MATLAB because of its rich and vetted radar functions along with the toolboxes which model radar systems and handle radar signal processing. Secondly, I have used MATLAB for

many years and I trust the software for modeling radar systems. To ensure the radar model does what we need the following requirements are established and followed.

4.2.1 Requirements

- 1. The radar testbed shall simulate the radar transmit and receiver operations.
- 2. The radar testbed shall model environmental effects.
- 3. The radar testbed shall model antenna effects.
- 4. The radar testbed shall provide a waveform model.
- 5. The radar testbed shall generate DRFM false targets.
- 6. The radar testbed shall generate real targets.
- 7. The radar testbed shall generate noise interference.
- 8. The radar testbed shall generate raw uncompressed IQ data.
- 9. The radar testbed shall perform signal processing on the IQ signal.
- 10. The radar testbed shall output range Doppler maps.

4.2.2 Data Generation

The main objective of the radar simulation model is to produce realistic range-Doppler images used as input to our CNN model. The images are 32x32 in size, which

represents the spatial location and 256 grayscale values that range from (0:black to 255:white) for each pixel in the image. While color images with a size of 656x875x3 could have been used and visually look more appealing it introduces another dimension. The extra dimensional increases computational complexity, along with the higher resolution. This is not needed since we are interested in the intensity of each pixel value, therefore grayscale works just fine, which we down-sampled the images to a size of 256x256 in grayscale. It is important to point out that the input layer has a depth of 1, but later layers through convolution still have a 2D spatial representation but include a depth that corresponds to the number of features (not number of channels, like grayscale=1 and RGB=3), thus the convolutional layer outputs are 3D. Several different image sizes were visually inspected. The sizes ranged from 16x16 up to 256x256. The selection of 32x32 with 1024 numerical values should have enough resolution to by used the CNN and produce reasonable results. It also aligns with our CIFAR-10 baseline dataset in terms of the matrix size. Too much resolution just introduces computational overhead and does not really improve results. We also constrain our range-Doppler images to square matrices which allows for useful linear algebra operations such as calculating the determinant, eigenvalues, eigenvectors, and singular value decomposition (SVD). Since the range-Doppler images are dominated mostly with Gaussian noise the matrices are also dense and thus mostly non-zero.

4.3 CNN Model

The central objective of our CNN model is best depicted below in the notional Figure 4.2 as to how our image classification experiments will work. The idea is to reduce the image dimensionality in layers as shown to obtain a final output feature vector that is made up of a prediction of the defined classes. Strictly speaking this is the output of the softmax function defined in Eq. (3.9).

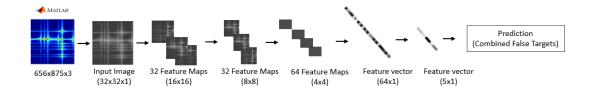


Figure 4.1: CNN Feature Map Flow

The learning style will be to map the images to the output which is a supervised learning technique. This technique allows us to provide labels and categorize the images into unique classes. We provided an overview of the DRFM classes starting in section 2.4.1.1.

4.3.1 Architecture

There are many different types of CNN's and architectures to exploit. While its easy to understand the choice of the final output (i.e. number of classes) the

structure preceding and its path is complex. We did explore hyperparameters that help us along the path and in some respects create a path through SGD. There is still the problem and decision of how many layers, the number of nodes in each layer and how to connect it all together. They are guidelines and research that suggests various architectures but there appears to be no widely accepted architecture for image classification. In other words its not an exact science. We put this in the bucket of the "no free lunch" (NFL) theorem. [37] Essentially the NFL theorem states that there is no single learning solution that is "one size fits all" on the path to the best architecture for image classification. Just because something works well on one type of problem does not guarantee ideal transfer to problems of a different type, which is often the case. So the best we can hope for is that our CNN model works in a relatively restricted set of problems. So faced with which CNN architecture is the best, what to do? The conventional approach is to experiment with different architectures and choose the one that is the best on your validation or test data set. We will extend this idea to consider perhaps a combination of architectures. This is still at best an empirical approach to the best solution.

We first make a general assumption for the CNN architecture. Since the input range-Doppler images are square (32x32) we assume the CNN architecture to be symmetric, so both dimensions have the same value for all variables. Otherwise if the architecture or the images are asymmetric then we would have to calculate the attributes for the feature map at each dimension.

We begin by breaking the CNN architecture into the following hyperparameters table and then propose an empirical method to find the best set of hyperparameter values. Mentioned in section 3.2.1 Grid Search and Random Search can be used but have their drawbacks. So we propose to make informed constraints on the hyperparameters, such that it limits our choices in the best way. We realize that this approach is not optimal so we will try and precede with caution.

Hyperparameter	Description	Value				
Number of Filters	Used to map the activations from one layer to the next. The filter contains the trained weights and matches the kernel size.	[16,32,64,96]				
Kernel Size	Generalized sliding dot product or convolution operation into higher dimensional spaces that are linearly separable. We convolve the filter(nxn kernel size) with the image.	[3,4,5]				
Batch Size	Mini-batch size from our image dataset	[32-256]				
Activation Function	Transforms our dot product summations into the final output feature vector. $ \begin{tabular}{ll} \hline \end{tabular} $	ReLU with softmax				
Number of Layers	The number of convolutional layers	[3-5]				
Optimizer	Customized SGD (see section 3.3)	ALRM				
Learning Rate	Quasi-Newton method (see section 3.3.1)	Trained automatically through ALRM				
Momentum	Stochastic heavy ball method (see section 3.3.2)	Trained automatically through ALRM				
Max Pooling	Creates a down-sampled feature map based on the largest segment of each feature map.	True or False				
Dropout	Randomly discards nodes by setting them to zero. This helps to regularize which helps to prevent overfitting.	True or False				

Table 4.1: Hyperparameters

To constrain our choices in the best way we propose a ResNet architecture approach which was proposed in 2015 by Microsoft Research. The ResNet NN allows us to train more layers by skipping over layers. It also has been tested extensively on known datasets such as CIFAR-10. So then there are established ResNet archi-

tectures for selection. These come with defined kernel sizes, number of convolutional layers, max and average pooling thus significantly reducing the hyperparamters to test. ResNet architectures work by not computing through each layer in a stack which is the conventional approach. Instead a residual mapping function $\mathcal{F}(\mathbf{x})$ is used to fit the layers. In principle, there is a desired sub mapping that we define as $\mathcal{H}(\mathbf{x})$ where $\mathcal{F}(\mathbf{x}) := \mathcal{H}(\mathbf{x}) - \mathbf{x}$. This then is mapped into $\mathcal{F}(\mathbf{x}) + \mathbf{x}$ The Figure 4.3 depicts this concept.

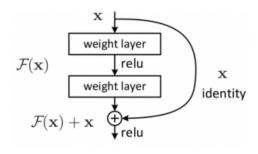


Figure 4.2: ResNet Residual Block

This is often refereed to as skip connections that perform an identity mapping function that allows us to skip over the layers and use deeper neural networks without the computational cost of stacked layers. Below is a table of ResNet architectures that we will test over

layer name	output size	18-layer	34-layer	50-layer	101-layer	152-layer							
conv1	112×112	7×7, 64, stride 2											
		3×3 max pool, stride 2											
conv2_x	56×56	$\left[\begin{array}{c}3\times3,64\\3\times3,64\end{array}\right]\times2$	$\left[\begin{array}{c} 3\times3,64\\ 3\times3,64 \end{array}\right]\times3$	$\begin{bmatrix} 1 \times 1, 64 \\ 3 \times 3, 64 \\ 1 \times 1, 256 \end{bmatrix} \times 3$	$\begin{bmatrix} 1 \times 1, 64 \\ 3 \times 3, 64 \\ 1 \times 1, 256 \end{bmatrix} \times 3$	$\begin{bmatrix} 1 \times 1, 64 \\ 3 \times 3, 64 \\ 1 \times 1, 256 \end{bmatrix} \times 3$							
conv3_x	28×28	$\left[\begin{array}{c} 3\times3, 128\\ 3\times3, 128 \end{array}\right] \times 2$	$\left[\begin{array}{c} 3\times3, 128\\ 3\times3, 128 \end{array}\right] \times 4$	$\begin{bmatrix} 1 \times 1, 128 \\ 3 \times 3, 128 \\ 1 \times 1, 512 \end{bmatrix} \times 4$	$\begin{bmatrix} 1 \times 1, 128 \\ 3 \times 3, 128 \\ 1 \times 1, 512 \end{bmatrix} \times 4$	$\begin{bmatrix} 1 \times 1, 128 \\ 3 \times 3, 128 \\ 1 \times 1, 512 \end{bmatrix} \times 8$							
conv4_x	14×14	$\left[\begin{array}{c} 3\times3,256\\ 3\times3,256 \end{array}\right]\times2$	$\left[\begin{array}{c} 3\times3,256\\ 3\times3,256 \end{array}\right]\times6$	$\begin{bmatrix} 1 \times 1, 256 \\ 3 \times 3, 256 \\ 1 \times 1, 1024 \end{bmatrix} \times 6$	$\begin{bmatrix} 1 \times 1, 256 \\ 3 \times 3, 256 \\ 1 \times 1, 1024 \end{bmatrix} \times 23$	$\begin{bmatrix} 1 \times 1, 256 \\ 3 \times 3, 256 \\ 1 \times 1, 1024 \end{bmatrix} \times 36$							
conv5_x	7×7	$\left[\begin{array}{c}3\times3,512\\3\times3,512\end{array}\right]\times2$	$\left[\begin{array}{c}3\times3,512\\3\times3,512\end{array}\right]\times3$	$\begin{bmatrix} 1 \times 1, 512 \\ 3 \times 3, 512 \\ 1 \times 1, 2048 \end{bmatrix} \times 3$	$\begin{bmatrix} 1 \times 1, 512 \\ 3 \times 3, 512 \\ 1 \times 1, 2048 \end{bmatrix} \times 3$	$\begin{bmatrix} 1 \times 1, 512 \\ 3 \times 3, 512 \\ 1 \times 1, 2048 \end{bmatrix} \times 3$							
	1×1	average pool, 1000-d fc, softmax											
FL	OPs	1.8×10^{9}	3.6×10^{9}	7.6×10^{9}	11.3×10 ⁹								

Figure 4.3: ResNet Architectures (add ResNet9)

Show an expanded view of the architecture once its been selected. Here is an example of ResNet34.

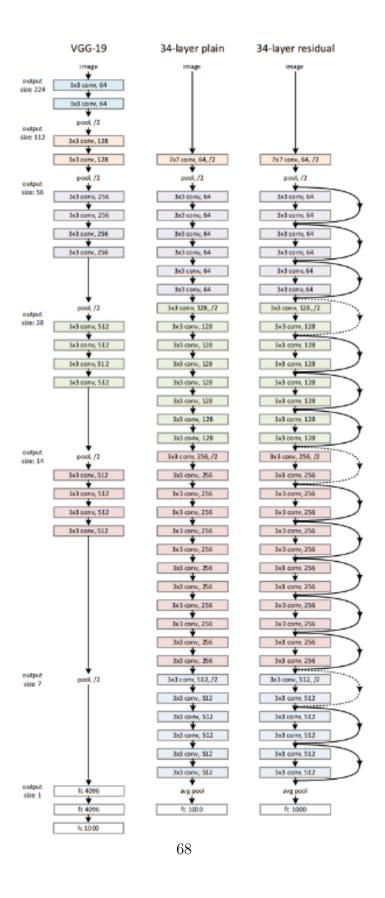


Figure 4.4: ResNet34 Architecture

Chapter 5

Experiments and Results

5.1 Methodology

To initiate the experiment testing we will start with an established CIFAR-10 image dataset which is a typical choice for CNN practitioners. The idea is to baseline with a known good data source. This also addresses several machine learning challenges that are important in running these experiments.

- 1. Poor data quality leads to garbage-in then garbage-out.
- 2. Variety of sample images for classification, so its not too simple.
- 3. Lack of data, the CIFAR-10 dataset has 80 million tiny images dataset and consists of 60,000 32x32 color images containing one of 10 object classes, with 6000 images per class.

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4. Good representative data, so as to not bias the CNN model.

We iterate through the ResNet architectures in Table 5.2 while varying the number of "Epochs" or cycles through the datasets. We propose to start with a small number of 10 and increase until the model loss is no longer trending down towards minimal error or starts to overfit. To help with overfit we adapt a regularization method using L1 ($||x_1||$) and L2 ($||x_2||$) norms. Which are defined as

$$||x_1|| = \sum |x_i| \tag{5.1}$$

$$||x_1|| = \sum |x_i|$$
 (5.1)
 $||x_2|| = \sqrt{\sum x_i^2}$

Notionally we depict an overfit and a good fit in Figure 5.1 below

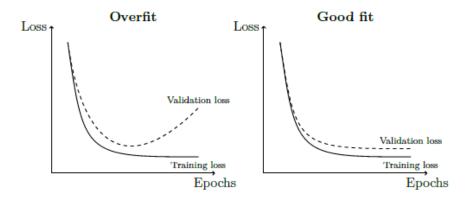


Figure 5.1: Model Fitting

We then select the best ResNet candidate based on the following metrics.

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Metrics	Description	Python Code
Bias	Error rate of the training data	
	Compares the known training label to the predicted label and provides	
Correct Predictions	a summation of correct predictions.	(predicted==train_labels).sum() or (predicted==test_labels).sum()
	Cross entropy loss with softmax from CNN with applied penalty during	
Cross Entropy Loss	forward propagation using a wrapped tensor and known labels.	cross_entropy(outputs,labels)+l1_penalty+l2_penalty
	Wrapped tensor <variable()> from the forward propagation of the</variable()>	
	neural network that also maintains the gradient function for back	
Outputs	propagation which allows the gradient calculation using the chain rule.	net(Variable(train_images)) or net(Variable(test_images))
Overfit		
	Returns the maximum value of all elements in the tensor. In this case,	
	for the max value in each row it provides the label prediction given its	
Predictions	column position.	torch.max(outputs.data,1)
	Percent accuaracy based on the number of correct predictions from the	
Test Accuracy	total inputs	torch.div(100*correct, total, rounding_mode='trunc')
	Scalar size of the number of images mapped to an	
Total Inputs	assigned label.	train_labels.size(0) or test_labels.size(0)
	Percent accuaracy based on the number of correct predictions from the	
Training Accuracy	total inputs	torch.div(100*correct, total, rounding_mode='trunc')
Training Time	Total training time	(time.time() - start_time)
	The difference between the error rate of training data	
Variance	and testing data	

Table 5.1: Metrics (Place Holder)

Using the selected ResNet candidate we now more runs varying the batch size. We propose testing batch sizes of 8, 16, 32, 64, 128, and 256, which provides a good range of batch sizes. We then follow with experiments using the range-Doppler images produced by our radar simulation model using the same approach. The selection process will be based on the metrics which are captured in the Experiment Results section 5.2.1.

5.2 Experiments

Test Case	Architecture	Dataset	Optimizer	Epochs	Batch Size
CIFAR-10_01	ResNet9	CIFAR-10	ALRM	variable	32
CIFAR-10_02	ResNet18	CIFAR-10	ALRM	variable	32
CIFAR-10_03	ResNet34	CIFAR-10	ALRM	variable	32
CIFAR-10_04	ResNet50	CIFAR-10	ALRM	variable	32
CIFAR-10_05	ResNet101	CIFAR-10	ALRM	variable	32
CIFAR-10_06	ResNet152	CIFAR-10	ALRM	variable	32
CIFAR-10_07	ResNet-xx	CIFAR-10	ALRM	variable	8
CIFAR-10_08	ResNet-xx	CIFAR-10	ALRM	variable	16
CIFAR-10_09	ResNet-xx	CIFAR-10	ALRM	variable	64
CIFAR-10_10	ResNet-xx	CIFAR-10	ALRM	variable	128
CIFAR-10_11	ResNet-xx	CIFAR-10	ALRM	variable	256
RD_01	ResNet9	RD Images	ALRM	variable	32
RD_02	ResNet18	RD Images	ALRM	variable	32
RD_03	ResNet34	RD Images	ALRM	variable	32
RD_04	ResNet50	RD Images	ALRM	variable	32
RD_05	ResNet101	RD Images	ALRM	variable	32
RD_06	ResNet152	RD Images	ALRM	variable	32
RD_07	ResNet-xx	RD Images	ALRM	variable	8
RD_08	ResNet-xx	RD Images	ALRM	variable	16
RD_09	ResNet-xx	RD Images	ALRM	variable	64
RD_10	ResNet-xx	RD Images	ALRM	variable	128
RD_11	ResNet-xx	RD Images	ALRM	variable	256

Table 5.2: Experiments

5.2.1 Experiment Results (Section in work)

Test Case	Architecture	Dataset	Optimizer	Epochs	Batch Size	Training Accuarcy	Test Accuracy	Bias	Variance	Overfit	Training time
CIFAR-10_01	ResNet9	CIFAR-10	ALRM		32						
CIFAR-10_02	ResNet18	CIFAR-10	ALRM		32						
CIFAR-10_03	ResNet34	CIFAR-10	ALRM		32						
CIFAR-10_04	ResNet50	CIFAR-10	ALRM		32						
CIFAR-10_05	ResNet101	CIFAR-10	ALRM		32						
CIFAR-10_06	ResNet152	CIFAR-10	ALRM		32						
CIFAR-10_07	ResNet-xx	CIFAR-10	ALRM		8						
CIFAR-10_08	ResNet-xx	CIFAR-10	ALRM		16						
CIFAR-10_09	ResNet-xx	CIFAR-10	ALRM		64						
CIFAR-10_10	ResNet-xx	CIFAR-10	ALRM		128						
CIFAR-10_11	ResNet-xx	CIFAR-10	ALRM		256						
RD_01	ResNet9	RD Images	ALRM		32						
RD_02	ResNet18	RD Images	ALRM		32						
RD_03	ResNet34	RD Images	ALRM		32						
RD_04	ResNet50	RD Images	ALRM		32						
RD_05	ResNet101	RD Images	ALRM		32						
RD_06	ResNet152	RD Images	ALRM		32						
RD_07	ResNet-xx	RD Images	ALRM		8						
RD_08	ResNet-xx	RD Images	ALRM		16						
RD_09	ResNet-xx	RD Images	ALRM		64						
RD_10	ResNet-xx	RD Images	ALRM		128						
RD_11	ResNet-xx	RD Images	ALRM		256						

Figure 5.2: Experiment Measurements

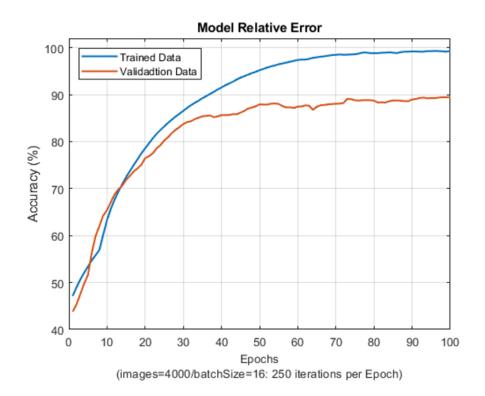


Figure 5.3: Model Relative Error (Place Holder)

5.3 Conclusion

We summarize our main conclusions based on the research and body of work produced in this thesis. Our findings are based on evidence to support any claims made. The contributions are both to the fields of radar and machine learning.

5.3.1 Findings and Contributions (Section in work)

Findings

Where is your evidence to support findings that you made in this thesis?

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What are some interesting findings or things that were surprising? What challenges did you encounter? Where you able to overcome? What did this thesis highlight? Any trades performed? Any limitations or design constraints?

Contributions

What are the important and main contributions to the fields of radar and machine learning? Include performance....

- Radar simulation
- Data Collection
- CNN Model
- Data analysis and Interpretation
- Reviewer contributions

5.3.2 Future Work

- Apply to an actual real-world system. IRAD funding has been secured by my
 work place to continue development of these concepts and methods for ECM
 identification.
- Identification of false targets is proven successful. Move towards methods that prohibit false targets from detections processing in the receiver signal processing

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chain. Methods such as null steering, adaptive beamforming, waveform diversity, frequency hopping are techniques used by the radar community that could be expanded and exploited by using ML.

- Separating the real targets from the false targets is a real challenge since real along with false targets are appearing in the main-lobe of the beam and thus should be considered. The main-lobe of a radar beam is like a sinc function where $y(t) = \frac{\sin(\pi t)}{\pi t}$ and $-\infty < t < \infty$. The detection decision is typically done by hypothesis testing using a Bayes optimization which determines the optimal choice between our hypotheses. In this case, I'm considering a multihypothesis approach for TBD features. We could try a particle filter approach which is a recursive, Bayesian state estimator that uses discrete particles to approximate the posterior distribution of the estimated state.
- Dive further into the mathematical theory behind ML to open up the black box.

Chapter 6

Appendix A - Source Code

6.1 MATLAB Source Code

The MATLAB source code that follows is used for the radar simulation that generates the IQ data and Range-Doppler images which serve as inputs into the CNN model.

CHAPTER 6. APPENDIX A - SOURCE CODE

```
function [opts,M] = getParameters(filename,type)
% DESCRIPTION: This function defines the parameters for the phasedArrayRadar
\% simulation. There are two types of structures defined which are for the
% target and the radar.
% INPUTS: filename: string (Excel spreadsheet file)
          type: string (types - 'radar' or 'targets')
% EXAMPLE: [~,tgt] = getParameters(tgtFile,"targets");
         [~,radar] = getParameters(radarFile,"radar");
% See Also: phasedArrayRadar.m
opts = detectImportOptions(filename);
preview(filename,opts)
M = readmatrix(filename,opts);
switch type
    case "targets"
        target = struct;
        target.id = M(:,1);
        target.pos = M(:,2);
        target.vel = M(:,3);
        target.rcs = M(:,4);
        target.type = M(:,5);
        target.pw = M(:,6);
        M = target;
    case "radar"
        radar = struct;
        radar.pwEnum = M(:,1);
        radar.pw = M(:,2);
        radar.duty = M(:,3);
        radar.fc = M(:,4);
        radar.pri = M(:,5);
        radar.prf = M(:,6);
        radar.fs = M(:,7);
        radar.wb = M(:,8);
        radar.nPulses = M(:,9);
        radar.nDoppler = M(:,10);
        radar.peakPwr = M(:,11);
        radar.txGain = M(:,12);
        radar.rxGain = M(:,13);
        radar.noiseFigure = M(:,14);
        radar.minTgtRng = M(:,15);
        radar.maxTgtRng = M(:,16);
        radar.minVel = M(:,17);
        radar.maxVel = M(:,18);
        radar.deltaVel = M(:,19);
        radar.deltaRange = M(:,20);
        M = radar;
    otherwise
        disp("Invalid type use 'radar' or 'targets'.")
end
end
```

Figure 6.1: getParameters.m

Chapter 7

Appendix B - Parameters

PulseWidth (secs)	Duty %	Frequency (Hz)	PRF (Hz)	Sampling Rate (Hz)	Wideband	#Pulses	#Doppler	peakPwr (Watts)	txGain (dB)	rxGain (dB)	noiseFigure (dB)	minTgtRng (m)	maxTgtRng (m)	minVel (m/s)	maxVel (m/s)
1.00E-02	0.25	9.5E+09	25	5.0E+05	0	64	64	450000	50	50	1.00E-04	2.00E+06	3.00E+06	10	250
5.00E-03	0.25	9.5E+09	50	1.0E+06	0	64	64	450000	50	50	1.00E-04	1.00E+06	2.00E+06	10	350
2.50E-03	0.25	9.5E+09	100	1.0E+06	0	64	64	450000	50	50	1.00E-04	550000	1000000	10	500
1.25E-03	0.25	9.0E+09	200	1.0E+06	0	64	64	450000	50	50	1.00E-04	270000	550000	100	1000
6.25E-04	0.25	9.0E+09	400	1.0E+06	0	64	64	450000	50	50	1.00E-05	135000	270000	100	1000
3.13E-04	0.25	9.0E+09	800	1.0E+06	1	64	64	450000	50	50	1.00E-04	65000	135000	100	1000
1.56E-04	0.25	9.0E+09	1600	1.0E+06	1	64	64	450000	50	50	1.00E-04	30000	65000	100	1000
7.81E-05	0.25	9.0E+09	3200	1.0E+07	1	64	64	450000	50	50	1.00E-04	20000	30000	100	1000

Table 7.1: Radar Parameters

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Vita

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