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On recognizing words that are squares for the shuffle product

The shuffle  $u \sqcup v$  of words u and v over alphabet A is the finite set of all words obtainable from merging the words u and v from left to right, but choosing the next symbol arbitrarily from u or v. The shuffle of two words u and v is the language  $u \sqcup v$  consisting of all words  $u_1v_1u_2v_2\ldots u_kv_k$ , where  $k \geq 0$  and the  $u_i$  and the  $v_i$  are the words such that  $u = u_1u_2\ldots u_k$  and  $v = v_1v_2\ldots v_k$ . It is well-known that it can be tested in polynomial-time whether or not  $u \in v_1 \sqcup v_2$  for given words u,  $v_1$  and  $v_2$  [J.-C. Spehner, Le Calcul Rapide des Mélanges de Deux Mots, TCS, 1986]. In this talk we consider the problem of determining whether or not a word u is a square for the shuffle product (i.e, there exists v such that  $u \in v \sqcup v$ ). Our approach is to represent words as linear graphs in which deciding whether or not a given word is a square for the shuffle product reduces to computing some constrained perfect matching. We shall also extend our approach to some related problems and propose future lines of research.