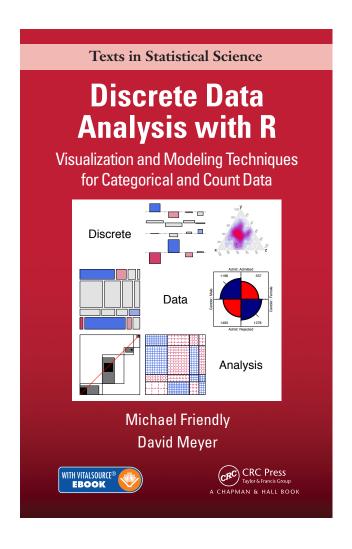
Discrete Data Analysis with R: Solutions and Hints to Exercises

February 5, 2016



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This document

This document is intended as an aid to instructors who wish to use *Discrete Data Analysis with R* in a course. It contains the text of the **Exercises** sections from all chapters, together with some solutions or hints for the various problems. Answers and commentary are indicated with the \bigstar symbol, and with text in this font.

All R code for the book, and other materials are available on the web site, http://ddar.datavis.ca.

For the most part, R code in answers indicates required packages with library() or require(). This document assumes, however, that the following packages are loaded: AER, car, effects, vcd, vcdExtra.

Chapter 1 Introduction

★ These questions are all conceptual, or based on judgment. No individual solutions are provided. In general, students should come up with some interesting examples related to the questions and explain why they consider them to be good or bad graphic or tabular displays.

Some other sources that students might consult are:

- The Gallery of Data Visualization, http://datavis.ca/gallery/. A categorized collection of some of the best and worst of statistical graphics.
- Junk Charts, http://junkcharts.typepad.com/, a blog by Kaiser Fung. There is also a list of related blogs on graphics and data visualization at http://junkcharts.typepad.com/junk_charts/other-graphics-blogs.html.
- Flowing Data, http://flowingdata.com/, by Nathan Yau. An eclectic collection of examples and blog posts encomposing a wide range from information visualization to statistical graphics.

Exercise 1.1 A web page, "The top ten worst graphs," http://www.biostat.wisc.edu/~kbroman/topten_worstgraphs/ by Karl Broman lists his picks for the worst graphs (and a table) that have appeared in the statistical and scientific literature. Each entry links to graph(s) and a brief discussion of what is wrong and how it could be improved.

- (a) Examine a number of recent issues of a scientific or statistical journal in which you have some interest. Find one or more examples of a graph or table that is a particularly bad use of display material to summarize and communicate research findings. Write a few sentences indicating how or why the display fails and how it could be improved.
- (b) Do the same task for some popular magazine or newspaper that uses data displays to supplement the text for some story. Again, write a few sentences describing why the display is bad and how it could be improved.

Exercise 1.2 As in the previous exercise, examine the literature in recent issues of some journal of interest to you. Find one or more examples of a graph or table that you feel does a *good* job of summarizing and communicating research findings.

- (a) Write a few sentences describing why you chose these displays.
- (b) Now take the role of a tough journal reviewer. Are there any features of the display that could be modified to make them more effective?

Exercise 1.3 Infographics are another form of visual displays, quite different from the data graphics featured in this book, but often based on some data or analysis. Do a Google image search for the topic "Global warming" to see a rich collection.

- (a) Find and study one or two images that attempt some visual explanation of causes and/or effects of global warming. Describe the main message in a sentence or two.
- (b) What visual and graphic features are used in these to convey the message?

Exercise 1.4 The Wikipedia web page en.wikipedia.org/wiki/Portal:Global_warming gives a few data-based graphics on the topic of global warming. Read the text and study the graphs.

- (a) Write a short figure title for each that would announce the conclusion to be drawn in a presentation graphic.
- (b) Write a figure caption for each that would explain what is shown and the important graphical details for a reader to understand.

Exercise 1.5 The R Graph Gallery, http://rgraphgallery.blogspot.com/, contains a large collection of examples of graphs in R, tagged by type or content, together with the R code to produce them. Explore this collection for the terms (a) association plot (b) bar chart (c) categorical data (d) fluctuation diagram (e) mosaic plot Find one or two you particularly like and write a few sentences saying why you do.

Chapter 2 Working with Categorical Data

Exercise 2.1 The packages vcd (Meyer et al., 2015) and vcdExtra (Friendly, 2015) contain many data sets with some examples of analysis and graphical display. The goal of this exercise is to familiarize yourself with these resources.

You can get a brief summary of these using the function datasets () from vcdExtra. Use the following to get a list of these with some characteristics and titles.

```
> ds <- datasets(package = c("vcd", "vcdExtra"))
> str(ds, vec.len = 2)

'data.frame': 75 obs. of 5 variables:
    $ Package: chr "vcd" "vcd" ...
    $ Item : chr "Arthritis" "Baseball" ...
    $ class : chr "data.frame" "data.frame" ...
    $ dim : chr "84x5" "322x25" ...
    $ Title : chr "Arthritis Treatment Data" "Baseball Data" ...
```

- (a) How many data sets are there altogether? How many are there in each package?
 - ★ nrow() gives the number of rows in a data frame. table() for a single variable gives the frequencies for each level.

```
> ds <- datasets(package=c("vcd", "vcdExtra"))
> nrow(ds)
[1] 75
> table(ds$Package)
    vcd vcdExtra
    33    42
```

- (b) Make a tabular display of the frequencies by Package and class.
 - ★ Use table (), but now for Package and class.

- (c) Choose one or two data sets from this list, and examine their help files (e.g., help (Arthritis) or ?Arthritis). You can use, e.g., example (Arthritis) to run the R code for a given example.
 - ★ Run the following types of commands:

```
> ?Arthritis  # Help Files
> ?Baseball  # Help Files
> example (Arthritis)  # Example Syntax/Analysis
> example (Baseball)  # Example Syntax/Analysis
```

Exercise 2.2 For each of the following data sets in the vcdExtra package, identify which are response variable(s) and which are explanatory. For factor variables, which are unordered (nominal) and which should be treated as ordered? Write a sentence or two describing substantitive questions of interest for analysis of the data. (*Hint*: use data(foo, package="vcdExtra") to load, and str(foo), help(foo) to examine data set foo.)

- (a) Abortion opinion data: Abortion
 - ★ Support_Abortion is the response, Sex and Status are binary, nominal explanatory variables. From help (Abortion), How does support for abortion depend on sex and status?

(b) Caesarian Births: Caesar

★ Infection is the response, Risk, Antibiotics and Planned are binary, nominal explanatory variables.

```
> data(Caesar, package="vcdExtra")
> str(Caesar)

table [1:3, 1:2, 1:2, 1:2] 0 1 17 0 1 1 11 17 30 4 ...
- attr(*, "dimnames")=List of 4
    ..$ Infection : chr [1:3] "Type 1" "Type 2" "None"
    ..$ Risk : chr [1:2] "Yes" "No"
    ..$ Antibiotics: chr [1:2] "Yes" "No"
    ..$ Planned : chr [1:2] "Yes" "No"
```

(c) Dayton Survey: DaytonSurvey

★ In DaytonSurvey, the variables cigarette, alcohol, and marijuana can all be treated as response variables. sex and race are potential explanatory variables. Potentially interesting questions are how each of the responses depend on sex and race, and how they vary jointly.

```
> data(DaytonSurvey, package="vcdExtra")
> str(DaytonSurvey)
```

(d) Minnesota High School Graduates: Hoyt

★ Status is the response, Rank, Occupation, and Sex are explanatory variables. Both Rank and Occupation are ordinal. How does Status vary with Rank, Occupation, and Sex?

```
> data(Hoyt, package="vcdExtra")
> str(Hoyt)
```

Exercise 2.3 The data set *UCBAdmissions* is a 3-way table of frequencies classified by Admit, Gender, and Dept.

(a) Find the total number of cases contained in this table.

★ For a table object, just use sum()

```
> data(UCBAdmissions)
> sum(UCBAdmissions)
[1] 4526
```

(b) For each department, find the total number of applicants.

★ Use margin.table(UCBAdmissions, 3) to find the marginal total for the third dimension (dept).

```
> margin.table(UCBAdmissions, 3)
Dept
A B C D E F
933 585 918 792 584 714
```

(c) For each department, find the overall proportion of applicants who were admitted.

 \star

```
> ucb.df <- as.data.frame(UCBAdmissions)
> abd <- xtabs(Freq ~ Dept + Admit, data=ucb.df)
> prop.table(abd, 1)

    Admit
Dept Admitted Rejected
    A 0.644159 0.355841
    B 0.632479 0.367521
    C 0.350763 0.649237
    D 0.339646 0.660354
    E 0.251712 0.748288
    F 0.064426 0.935574
```

(d) Construct a tabular display of department (rows) and gender (columns), showing the proportion of applicants in each cell who were admitted relative to the total applicants in that cell.

*

Exercise 2.4 The data set DanishWelfare in vcd gives a 4-way, $3 \times 4 \times 3 \times 5$ table as a data frame in frequency form, containing the variable Freq and four factors, Alcohol, Income, Status, and Urban. The variable Alcohol can be considered as the response variable, and the others as possible predictors.

- (a) Find the total number of cases represented in this table.
 - ★ This is a data set in the form of a frequency data.frame, so sum the Freq variable

```
> data("DanishWelfare", package="vcd")
> sum(DanishWelfare$Freq)
[1] 5144
```

- (b) In this form, the variables Alcohol and Income should arguably be considered *ordered* factors. Change them to make them ordered.
 - ★ Use ordered() or as.ordered() on the factor variable. str() will then show them as Ord.factor.

```
> levels(DanishWelfare$Alcohol)
[1] "<1" "1-2" ">2"

> DanishWelfare$Alcohol <- as.ordered(DanishWelfare$Alcohol)
> DanishWelfare$Income <- as.ordered(DanishWelfare$Income)
> str(DanishWelfare)

'data.frame': 180 obs. of 5 variables:
$ Freq : num 1 4 1 8 6 14 8 41 100 175 ...
$ Alcohol: Ord.factor w/ 3 levels "<1"<1-2"<">>2": 1 1 1 1 1 1 1 1 1 1 1 1 ...
$ Income : Ord.factor w/ 4 levels "0-50"<"50-100"<..: 1 1 1 1 1 1 1 1 1 1 ...
$ Status : Factor w/ 3 levels "Widow", "Married", ...: 1 1 1 1 2 2 2 2 2 2 ...
$ Urban : Factor w/ 5 levels "Copenhagen", "SubCopenhagen", ...: 1 2 3 4 5 1 2 3 4 5 ...</pre>
```

- (c) Convert this data frame to table form, DanishWelfare.tab, a 4-way array containing the frequencies with appropriate variable names and level names.
 - ★ Use xtabs() with Freq as the response.

```
> DanishWelfare.tab <-xtabs(Freq ~ ., data = DanishWelfare)
> str(DanishWelfare.tab)

xtabs [1:3, 1:4, 1:3, 1:5] 1 3 2 8 1 3 2 5 2 42 ...
- attr(*, "dimnames")=List of 4
    ..$ Alcohol: chr [1:3] "<1" "1-2" ">2"
    ..$ Income : chr [1:4] "0-50" "50-100" "100-150" ">150"
    ..$ Status : chr [1:3] "Widow" "Married" "Unmarried"
    ..$ Urban : chr [1:5] "Copenhagen" "SubCopenhagen" "LargeCity" "City" ...
- attr(*, "class")= chr [1:2] "xtabs" "table"
- attr(*, "call")= language xtabs(formula = Freq ~ ., data = DanishWelfare)
```

- (d) The variable Urban has 5 categories. Find the total frequencies in each of these. How would you collapse the table to have only two categories, City, Non-city?
 - ★ margin.table() handles the first part; collapse.table() is designed for the second part. It is arguable whether SubCopenhagen should be considered City or NonCity.

```
> margin.table(DanishWelfare.tab, 4)
Urban
   Copenhagen SubCopenhagen
                                  LargeCity
                                                                 Country
> DW2 <- vcdExtra::collapse.table(DanishWelfare.tab,
                                   Urban=c("City", "NonCity", "City", "City", "NonCity"))
> head(ftable(DW2))
                                   "Urban" "City" "NonCity"
 "Alcohol" "Income"
                      "Status"
 "<1"
           "0-50"
                      "Widow"
                                               1.0
                      "Married"
                                              155
                                                         183
                      "Unmarried"
                                               14
                                                          10
                      "Widow"
            "50-100"
                                               2.9
                      "Married"
                                              338
                      "Unmarried"
```

(e) Use structable() or ftable() to produce a pleasing flattened display of the frequencies in the 4-way table. Choose the variables used as row and column variables to make it easier to compare levels of Alcohol across the other factors.

*

Exercise 2.5 The data set *UKSoccer* in vcd gives the distributions of number of goals scored by the 20 teams in the 1995/96 season of the Premier League of the UK Football Association.

This two-way table classifies all $20 \times 19 = 380$ games by the joint outcome (Home, Away), the number of goals scored by the Home and Away teams. The value 4 in this table actually represents 4 or more goals.

(a) Verify that the total number of games represented in this table is 380.

*

```
> data("UKSoccer", package="vcd")
> sum(UKSoccer)
[1] 380
> margin.table(UKSoccer)
[1] 380
```

- (b) Find the marginal total of the number of goals scored by each of the home and away teams.
 - ★ Use margin.table() for each dimension:

```
> margin.table(UKSoccer, 1)
Home
    0     1     2     3     4
    76     142     90     45     27
> margin.table(UKSoccer, 2)
Away
    0     1     2     3     4
140     136     55     38     11
```

- (c) Express each of the marginal totals as proportions.
 - ★ Use prop.table() on the result of margin.table() for each dimension:

- (d) Comment on the distribution of the numbers of home-team and away-team goals. Is there any evidence that home teams score more goals on average?
 - ★ You could find the mean number of goals, weighted by their marginal frequencies. On average, home teams score about 0.4 more goals.

```
> weighted.mean(0:4, w=margin.table(UKSoccer,1))
[1] 1.4868
> weighted.mean(0:4, w=margin.table(UKSoccer,2))
[1] 1.0632
```

Graphically, you could also compare the marginal frequencies in a mosaic plot, or use agreementplot().

```
Goals
Team 0 1 2 3 4
home 76 142 90 45 27
away 140 136 55 38 11
> mosaic(margins, shade=TRUE)
```



Exercise 2.6 The one-way frequency table Saxony in VCd records the frequencies of families with 0, 1, 2, ... 12 male children, among 6115 families with 12 children. This data set is used extensively in Chapter 3.

```
> data("Saxony", package = "vcd")
> Saxony

nMales
0 1 2 3 4 5 6 7 8 9 10 11 12
3 24 104 286 670 1033 1343 1112 829 478 181 45 7
```

Another data set, <code>Geissler</code>, in the <code>vcdExtra</code> package, gives the complete tabulation of all combinations of <code>boys</code> and <code>girls</code> in families with a given total number of children (<code>size</code>). The task here is to create an equivalent table, <code>Saxony12</code> from the <code>Geissler</code> data.

```
> data("Geissler", package = "vcdExtra")
> str(Geissler)

'data.frame': 90 obs. of 4 variables:
$ boys : int 0 0 0 0 0 0 0 0 0 0 0 ...
$ girls: num 1 2 3 4 5 6 7 8 9 10 ...
$ size : num 1 2 3 4 5 6 7 8 9 10 ...
$ Freq : int 108719 42860 17395 7004 2839 1096 436 161 66 30 ...
```

(a) Use subset () to create a data frame, sax12 containing the Geissler observations in families with size==12.

★

```
> data("Saxony", package="vcd")
> data("Geissler", package="vcdExtra")
> sax12 <- subset(Geissler, size==12)</pre>
> sax12
     boys girls size Freq
12
         0
                  12
                         12
24
                            12
                                     24
                    11
                   10 12 104
9 12 286
8 12 670
45
                     8
54
           4
                            12 1033
```

```
69 6 6 12 1343

75 7 5 12 1112

80 8 4 12 829

84 9 3 12 478

87 10 2 12 181

89 11 1 12 45

90 12 0 12 7
```

(b) Select the columns for boys and Freq.

```
*
```

```
> sax12 <- subset(sax12, select=c("boys", "Freq"))
```

(c) Use xtabs () with a formula, Freq ~ boys, to create the one-way table.

```
*
```

```
> Saxony12<-xtabs(Freq~boys, data=sax12)
> Saxony12
boys
0  1  2  3  4  5  6  7  8  9  10  11  12
3  24  104  286  670  1033  1343  1112  829  478  181  45  7
```

(d) Do the same steps again to create a one-way table, Saxony11, containing similar frequencies for families of size==11.

```
*
```

```
> sax11 <- subset(Geissler, size==11, select = c("boys","Freq"))
> Saxony11 <- xtabs(Freq~boys, data=sax11)
> Saxony11
boys
0  1  2  3  4  5  6  7  8  9  10  11
8  72  275  837  1540 2161 2310 1801 1077  492  93  24
```

Exercise 2.7 * Interactive coding of table factors: Some statistical and graphical methods for contingency tables are implemented only for two-way tables, but can be extended to 3+-way tables by recoding the factors to interactive combinations along the rows and/or columns, in a way similar to what ftable() and structable() do for printed displays.

For the *UCBAdmissions* data, produce a two-way table object, UCB.tab2, that has the combinations of Admit and Gender as the rows, and Dept as its columns, to look like the result below:

```
Dept
Admit:Gender
                    Α
                        В
                             С
                                     Ε
                                         F
  Admitted:Female 89
                       17 202 131
                                    94
                                        24
  Admitted:Male
                  512 353 120 138
                                    53
                        8 391 244 299 317
  Rejected: Female 19
                  313 207 205 279 138 351
  Rejected: Male
```

(a) Try this the long way: convert UCBAdmissions to a data frame (as.data.frame()), manipulate the factors (e.g., interaction()), then convert back to a table (as.data.frame()).
★

(b) Try this the short way: both ftable() and structable() have as.matrix() methods that convert their result to a matrix.

Exercise 2.8 The data set VisualAcuity in vcd gives a $4 \times 4 \times 2$ table as a frequency data frame.

```
> data("VisualAcuity", package = "vcd")
> str(VisualAcuity)

'data.frame': 32 obs. of 4 variables:
$ Freq : num 1520 234 117 36 266 ...
$ right : Factor w/ 4 levels "1","2","3","4": 1 2 3 4 1 2 3 4 1 2 ...
$ left : Factor w/ 4 levels "1","2","3","4": 1 1 1 1 2 2 2 2 3 3 ...
$ gender: Factor w/ 2 levels "male","female": 2 2 2 2 2 2 2 2 2 ...
```

(a) From this, use xtabs () to create two 4×4 frequency tables, one for each gender.

 \star

(b) Use structable() to create a nicely organized tabular display.

+

```
> structable(right ~ left + gender, data = va.tab)
                            3
           right 1 2
left gender
                             72
    male
                  821 116
                                   43
                 1520 234 117
112 494 151
     female
                                   36
2
     male
    female
                  266 1512
                            362
                  85 145 583
124 432 1772
    male
                                 179
    female
    male
                   35
                        27
                              87
                                  331
   female
                       78 205
               66
                                 492
```

(c) Use $\mathtt{xtable}()$ to create a \mathtt{LMEX} or \mathtt{HTML} table.

```
> library(xtable)
> va.xtab <- xtable(va.tabm)
> print(va.xtab, type="html")
```

Chapter 3 Fitting and Graphing Discrete Distributions

Exercise 3.1 The Arbuthnot data in HistData (Friendly, 2014a) (Example 3.1) also contains the variable Ratio, giving the ratio of male to female births.

(a) Make a plot of Ratio over Year, similar to Figure 3.1. What features stand out? Which plot do you prefer to display the tendency for more male births?

 \star



The plot is similar to Figure 3.1 in the text. If it is easier to think in terms of probability of a male birth, plotting that directly may be preferable.

(b) Plot the total number of christenings, Males + Females or Total (in 000s) over time. What unusual features do you see?

```
> # total number of Christenings
> with(Arbuthnot, {
    Total= Males + Females
+ plot(Year, Total, type='b', ylab="Total Christenings (Male + Female)")
+ Arb.smooth <- loess.smooth(Year, Total)
+ lines(Arb.smooth$x, Arb.smooth$y, col="blue", lwd=2)
+ })</pre>
```



There was a large decline in births between 1640–1660, corresponding to years of plague in England.

Exercise 3.2 Use the graphical methods illustrated in Section 3.2 to plot a collection of geometric distributions for p = 0.2, 0.4, 0.6, 0.8, over a range of values of $k = 0, 1, \dots 10$.

(a) With xyplot(), try the different plot formats using points connected with lines, as in Figure 3.9, or using points and lines down to the origin, as in the panels of Figure 3.10.

```
> KL <- expand.grid(k = 0 : 10, p = c(0.2, 0.4, 0.6, 0.8))
> geom_df <- data.frame(KL, prob = dgeom(KL$k, KL$p))
> geom_df$p = factor(geom_df$p)
> library(lattice)
> mycol<-palette()[2:5]
> xyplot(prob ~ k | p , data = geom_df, type = c("b"),
+ pch = 16, lwd = 4, cex = 1.25,
+ xlab = list("Number of events (k)", cex = 1.25), layout = c(2,2),
+ ylab = list("Probability", cex = 1.25))
> xyplot(prob ~ k | p , data = geom_df, type = c("h", "p"),
+ pch = 16, lwd = 4, cex = 1.25,
+ xlab = list("Number of events (k)", cex = 1.25), layout = c(2,2),
+ ylab = list("Number of events (k)", cex = 1.25), layout = c(2,2),
+ ylab = list("Probability", cex = 1.25))
```



(b) Also with xyplot(), produce one version of a multi-line plot in a single panel that you think shows well how these distributions change with the probability p of success.

*



(c) Do the same in a multi-panel version, conditional on p.

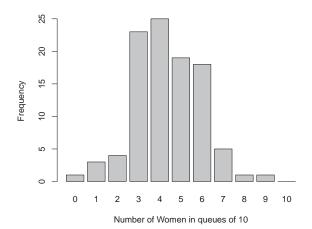
 \star



Exercise 3.3 Use the data set WomenOueue to:

(a) Produce plots analogous to those shown in Section 3.1 (some sort of bar graph of frequencies).

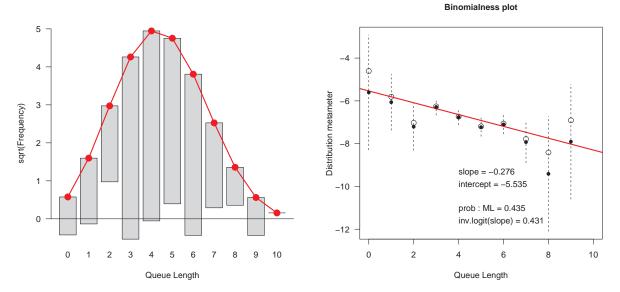
```
> data("WomenQueue", package = "vcd")
> barplot(WomenQueue, xlab="Number of Women in queues of 10", ylab= "Frequency")
```



(b) Check for goodness-of-fit to the binomial distribution using the goodfit () methods described in Section 3.3.2. \bigstar Note that with goodfit (), you should specify n=10 for the binomial distribution as the size parameter.

- (c) Make a reasonable plot showing departure from the binomial distribution.
 - ★ The simplest plot is the hanging rootogram. An alternative plot is a "binomialness" plot produced by distplot().

```
> plot(gf.women, xlab = "Queue Length")
> distplot(WomenQueue, type = "binomial", size=10, xlab = "Queue Length")
```



(d) Suggest some reasons why the number of women in queues of length 10 might depart from a binomial distribution, Bin(n = 10, p = 1/2).

*

- Perhaps women (or men) are more prevalent in these queues, so $p \neq 1/2$.
- · People often join lines in groups, so the observations are unlikely to be independent.

Exercise 3.4 Continue Example 3.13 on the distribution of male children in families in Saxony by fitting a binomial distribution, $Bin(n = 12, p = \frac{1}{2})$, specifying equal probability for boys and girls. [*Hint*: you need to specify both size and prob values for goodfit().]

(a) Carry out the GOF test for this fixed binomial distribution. What is the ratio of χ^2/df ? What do you conclude? \bigstar Note that you need to specify both n and p as fixed parameters here.

The binomial model fits very badly.

(b) Test the additional lack of fit for the model $Bin(n=12,p=\frac{1}{2})$ compared to the model $Bin(n=12,p=\hat{p})$ where \hat{p} is estimated from the data.

```
\star
```

This fits much better, but still not a good fit.

(c) Use the plot.gootfit() method to visualize these two models.



```
> plot(Saxony_gf, main = "Fit for p=0.5", xlab = "Number of Male Children (Out of 12)")
> plot(Saxony_gf2, main = "Fit for p=phat", xlab = "Number of Male Children (Out of 12)")
```

Fit for p=0.5

Fit for p=phat





Exercise 3.5 For the Federalist data, the examples in Section 3.3.1 and Section 3.3.2 showed the negative binomial to provide an acceptable fit. Compare this with the simpler special case of geometric distribution, corresponding to n = 1.

(a) Use goodfit () to fit the geometric distribution. [Hint: use type="nbinomial", but specify size=1 as a parameter.]

 \star

```
> fdfit1 <- goodfit(Federalist, type = "binomial", par = list(size=6))</pre>
> fdfit1
Observed and fitted values for binomial distribution
with parameters estimated by `ML'
 count observed
                   fitted pearson residual
    0 156 1.3072e+02
                            2.21074
-3.39860
             63 9.6362e+01
            29 2.9597e+01
                                   -0.10972
                                  1.43139
5.31624
             8 4.8483e+00
            4 4.4673e-01
1 2.1954e-02
                                    6.60094
             1 4.4953e-04
                                  47.14399
> fdfit2 <- goodfit(Federalist, type = "nbinomial", par = list(size=1))</pre>
Observed and fitted values for nbinomial distribution
with parameters estimated by `ML with size fixed'
                   fitted pearson residual
 count observed
                            -0.172219
           156 158.16590
             63 62.68326
                                  0.040006
             29 24.84221
                                  0.834194
             8 9.84530
4 3.90182
                                 -0.588102
                                 0.049702
     4
                  1.54635
                                 -0.439353
                             -0.015044
                  0.61284
```

(b) Compare the negative binomial and the geometric models statistically, by a likelihood-ratio test of the difference between these two models.

 \star

(c) Compare the negative binomial and the geometric models visually by hanging rootograms or other methods.

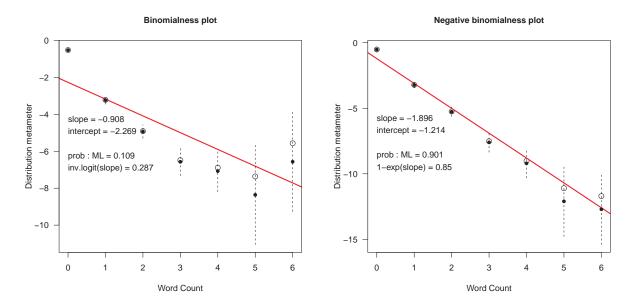
★ Hanging rootograms:

```
> plot(fdfit1)
> plot(fdfit2)
```



Distribution-ness plots:

```
> distplot(Federalist, type = "binomial", size=6, xlab = "Word Count")
> distplot(Federalist, type = "nbinomial", size=6, xlab = "Word Count")
```



Exercise 3.6 Mosteller and Wallace (1963, Table 2.4) give the frequencies, n_k , of counts $k = 0, 1, \ldots$ of other selected marker words in 247 blocks of text known to have been written by Alexander Hamilton. The data below show the occurrences of the word *upon*, that Hamilton used much more than did James Madison.

```
> count <- 0 : 5
> Freq <- c(129, 83, 20, 9, 5, 1)
```

- (a) Read these data into R and construct a one-way table of frequencies of counts or a matrix or data frame with frequencies in the first column and the corresponding counts in the second column, suitable for use with goodfit().
 - *\pmodfit() requires its first argument to be either a one-way table (from xtabs()), or a data.frame with frequencies in the *first* column and the corresponding counts in the second column. Both of the following forms will work.

(b) Fit and plot the Poisson model for these frequencies.

```
*
```

```
> (up0 <- goodfit(Upon, type="poisson"))</pre>
Observed and fitted values for poisson distribution
with parameters estimated by `ML'
             rved fitted pearson residual 129 121.61816 0.66937
                               0.66937
-0.34115
              83 86.16671
               20
                   30.52465
                                      -1.90494
                   7.20892
                                      0.66708
                    1.27688
                                        3.29481
                    0.18094
                                       1.75800
> summary(up0)
 Goodness-of-fit test for poisson distribution
X^2 df P(> X^2)
Likelihood Ratio 13.139 4 0.010617
> plot (up0)
```



(c) Fit and plot the negative binomial model for these frequencies.

```
*
```

```
83
                 73.89421
                                   1.059285
             20
                 28.41547
                                  -1.578705
                  9.25319
                                  -0.083233
                  2.74068
                                   1.364738
                  0.76332
                                   -0.036432
> summary (up1)
Goodness-of-fit test for nbinomial distribution
                    X^2 df P(> X^2)
Likelihood Ratio 6.0306 3 0.11013
> plot (up1)
```



(d) What do you conclude?

★ The negative binomial model fits better than the Poisson.

Exercise 3.7 The data frame *Geissler* in the vcdExtra package contains the complete data from Geissler's (1889) tabulation of family sex composition in Saxony. The table below gives the number of boys in families of size 11.

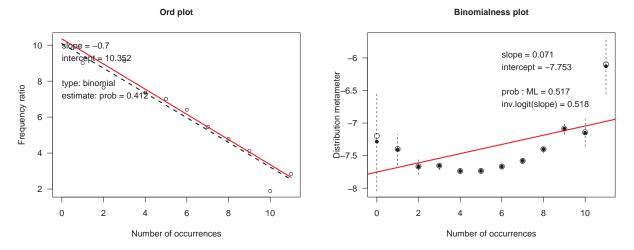
boys	0	1	2	3	4	5	6	7	8	9	10	11
Freq	8	72	275	837	1,540	2,161	2,310	1,801	1,077	492	93	24

- (a) Read these data into R.
 - ★ See Exercise 2.6, which calculates sax11 in the form of a data frame.
- (b) Following Example 3.13, use goodfit () to fit the binomial model and plot the results. Is there an indication that the binomial does not fit these data?
 ★ The binomial distribution fits badly, where the extremes are under-fitted, and the middle values are over-fitted.

```
> sax11.tab <- xtabs(Freq ~ boys, data=sax11)
> goodfit(sax11.tab, type="binomial", par=list(size=11))
Observed and fitted values for binomial distribution
with parameters estimated by `ML'
 count observed
                       fitted pearson residual
                       3.5616
                8
                                           2.3518
                    41.9479 224.5724
                                            4.6400
              275
                                           3.3650
             837 721.3629
1540 1544.7559
                                           4.3055
                                           -0.1210
             2161 2315.6023
2310 2479.3627
                                           -3.2128
                                           -3.4013
             1801 1896.2173
                                           -2.1866
      8
              1077 1015.1593
                                            1.9409
              492
                    362.3173
                                            6.8130
     10
               93
                      77.5881
                                            1.7497
                       7.5523
                                            5.9850
> summary(goodfit(sax11.tab, type="binomial", par=list(size=11)))
```

- (c) Diagnose the form of the distribution using the methods described in Section 3.4.
 - ★ The Ord plot indicates that the closest distribution according to its heuristics is the binomial; the binomialness distribution plot, however, shows this is not an acceptable model, as was also seen in the text for families of size 12.

```
> Ord_plot(sax11.tab)
> distplot(sax11.tab, type="binomial", size=11)
```



(d) Try fitting the negative binomial distribution, and use distplot () to diagnose whether the negative binomial is a reasonable fit. **TODO**: Something wrong here.

```
> goodfit(sax11.tab, type="nbinomial", par=list(size=11))
Observed and fitted values for nbinomial distribution with parameters estimated by `ML with size fixed' \,
 count observed
                    fitted pearson residual
                8
                   109.12
                                       -9.6801
               72
                    409.11
                                      -16.6667
              275 836.63
                                      -19.4171
              837 1235.67
                                      -11.3414
                                        1.7171
             1540 1474.07
             2161 1507.26
                                       16.8389
             2310 1369.95
                                       25.3981
             1801 1133.97
                                       19.8082
             1077
                   869.62
                                        7.0323
                   625.73
              492
                                       -5.3462
                   426.55
               93
                                      -16.1500
                                       -25.3999
```

Exercise 3.8 The data frame *Bundesliga* gives a similar data set to that for UK soccer scores (*UKSoccer*) examined in Example 3.9, but over a wide range of years. The following lines calculate a two-way table, BL1995, of home-team and away-team goals for the 306 games in the year 1995.

```
4 3 5 3 0 0 0 0
5 4 1 0 1 0 0 0
```

- (a) As in , find the one-way distributions of HomeGoals, AwayGoals, and TotalGoals = HomeGoals +
 - ★ There are several ways to do this, but as illustrated in the text for Example 3.9, create the one-way variables in a data.frame, and then use xtabs () to get their marginal distributions.

```
> BL.df <- as.data.frame(BL1995, stringsASFactors=FALSE)
> BL.df <- as.data.rrame(BL1995, strings)
BL.df <- within(BL.df, {
+ HomeGoals <- as.numeric(HomeGoals)
+ AwayGoals <- as.numeric(AwayGoals)
+ TotalGoals <- HomeGoals + AwayGoals
      # marginal distributions
> (BL.home <- xtabs(Freq ~ HomeGoals, data=BL.df))
HomeGoals

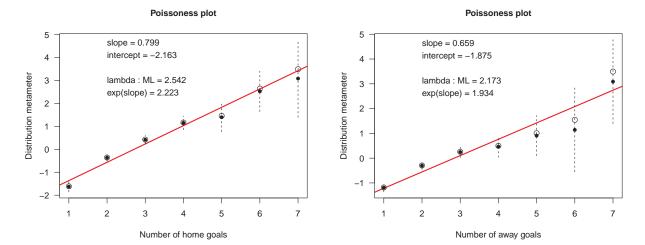
1 2 3 4 5 6 7
61 107 78 41 11 6 2
> (BL.away <- xtabs(Freq ~ AwayGoals, data=BL.df))</pre>
       2 3 4
 1 2 3 4 5 6 7
94 114 66 21 7 2 2
> (BL.total <- xtabs(Freq ~ TotalGoals, data=BL.df))
TotalGoals
2 3 4 5 6 7 8 9 10 11 12 13 14 26 35 98 62 39 29 10 4 2 1 0 0 0
```

- (b) Use goodfit () to fit and plot the Poisson distribution to each of these. Does the Poisson seem to provide a reasonable fit?
 ★ The Poisson distribution has a bad fit for all of these.

```
> summary(goodfit(BL.home))
Goodness-of-fit test for poisson distribution
                   X^2 df P(> X^2)
Likelihood Ratio 70.722 5 7.2516e-14
> summary(goodfit(BL.away))
Goodness-of-fit test for poisson distribution
                   X^2 df P(> X^2)
Likelihood Ratio 97.973 5 1.4131e-19
> summary(goodfit(BL.total))
Goodness-of-fit test for poisson distribution
                   X^2 df P(> X^2)
Likelihood Ratio 72.558 8 1.5185e-12
```

- (c) Use distplot () to assess fit of the Poisson distribution.
 - ★ The distribution plots for home goals looks better than that for away goals, which shows a systematic departure from the red line.

```
> distplot(BL.home, xlab="Number of home goals")
> distplot(BL.away, xlab="Number of away goals")
```



- (d) What circumstances of scoring goals in soccer might cause these distributions to deviate from Poisson distributions?
 - ★ The Poisson distribution relies on (a) independent events with (b) constant probabilities. The probability of scoring a goal is almost certainly not constant over all pairs of teams.

Exercise 3.9 * Repeat the exercise above, this time using the data for all years in which there was the standard number (306) of games, that is for Year>1965, tabulated as shown below.

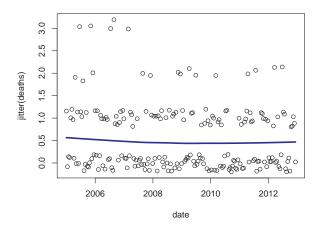
```
> BL <- xtabs(~ HomeGoals + AwayGoals, data = Bundesliga,
                subset = (Year > 1965))
> BL
          AwayGoals
HomeGoals
                                                                   9
                                                              8
                  590
            868
                        458
                              206
                                     88
                                           22
                                                        2
                                                                   0
                                                 12
            1049 1550
                        589
                              360
                                    121
                                           34
                                                  8
                                                        6
            1039
                        810
                                     95
                                           26
                                                                   0
             712
                  793
                        392
                              187
                                     43
                                            8
                                                                   0
                   388
                        245
                                     26
                                                                   0
             128
                  164
                        106
                               34
                                                              0
                                                                   0
                    63
                         38
                               10
                                                                   0
        8
                                                              0
                                                                   0
                     0
        10
        11
                     2
                           0
                                0
                                      0
                                                                   0
```

★ The steps are similar to those in the previous problem, but now there are more years, and the range of both home goals and away goals is larger.

Exercise 3.10 Using the data CyclingDeaths introduced in Example 3.6 and the one-way frequency table CyclingDeaths.tab = table (CyclingDeaths\$ deaths),

- (a) Make a sensible plot of the number of deaths over time. For extra credit, add a smoothed curve (e.g., using lines (lowess(...))).
 - ★ The number of deaths in a given fortnight are discrete, taking values 0:3. A barplot, using plot (deaths ~ date, type="h", data=CyclingDeaths) is one option. Perhaps slightly better is to jitter the number of deaths.

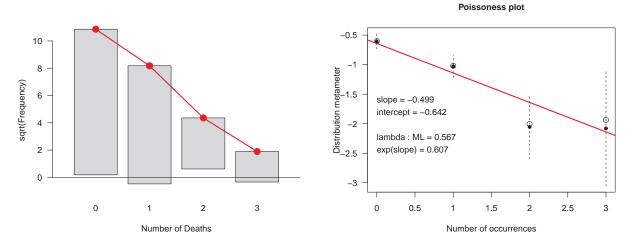
```
> data("CyclingDeaths", package="vcdExtra")
> CyclingDeaths.tab <- table(CyclingDeaths$deaths)
> plot(jitter(deaths) ~ date, data=CyclingDeaths)
> with(CyclingDeaths, {lines(lowess(date, deaths), lwd=3, col="blue")})
```



 $(b) \ \ Test \ the \ goodness \ of \ fit \ of \ the \ table \ \texttt{CyclingDeaths.tab} \ to \ a \ Poisson \ distribution \ statistically \ using \ \texttt{goodfit} \ () \ .$

(c) Continue this analysis using a ${\tt rootogram}$ () and ${\tt distplot}$ ().

```
> plot(gf, xlab="Number of Deaths")
> distplot(CyclingDeaths.tab)
```



(d) Write a one-paragraph summary of the results of these analyses and your conclusions.

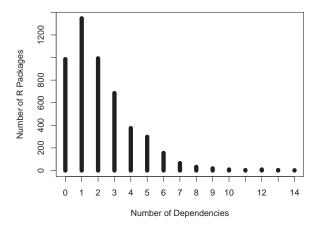
Exercise 3.11 * The one-way table, *Depends*, in vcdExtra and shown below gives the frequency distribution of the number of dependencies declared in 4,983 R packages maintained on the CRAN distribution network on January 17, 2014. That is, there were 986 packages that had no dependencies, 1,347 packages that depended on one other package, . . . up to 2 packages that depended on 14 other packages.

Depends	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14
# Pkgs	986	1,347	993	685	375	298	155	65	32	19	9	4	9	4	2

(a) Make a bar plot of this distribution.

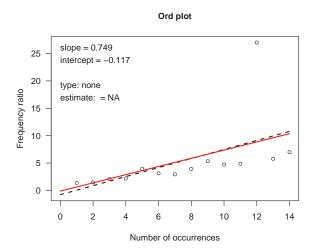
*

```
> data("Depends", package="vcdExtra")
> plot(Depends, xlab="Number of Dependencies", ylab="Number of R Packages", lwd=8)
```

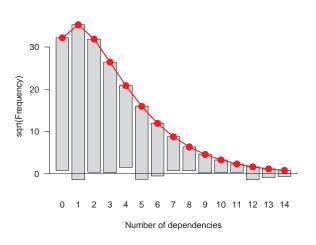


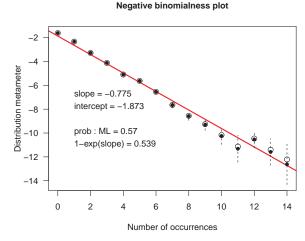
- (b) Use Ord_plot () to see if this method can diagnose the form of the distribution.
 - \bigstar This turns out to be a case where the Ord plot method, as implemented in Ord_plot () does not determine the form of the distribution. According to Table 3.11, the log series distribution is the only one with positive slope b and negative intercept a, but this requires a=-b.

> Ord_plot (Depends)



- (c) Try to fit a reasonable distribution to describe dependencies among R packages.
 - ★ Among the distributions described in Chapter 3 and implemented in the vcd package the negative binomial may be the best to try.





So, this does not fit well, particularly for the packages with many dependencies, but it is not altogether terrible. The remaining differences come from further heterogeneity for which we haven't got any covariates in the data set. For example, the age of the package would seem like a natural candidate: older packages probably have fewer dependencies.

Exercise 3.12 * How many years does it take to get into the baseball Hall of Fame? The Lahman (Friendly, 2014b) package provides a complete record of historical baseball statistics from 1871 to the present. One table, HallOfFame, records the history of players nominated to the Baseball Hall of Fame, and those eventually inducted. The table below, calculated in help (HallOfFame, package="Lahman"), records the distribution of the number of years taken (from first nomination) for the 109 players in the Hall of Fame to be inducted (1936–present). Note that years=0 does not, and cannot, occur in this table, so the distribution is restricted to positive counts. Such distributions are called *zero-truncated distributions*. Such distributions are like the ordinary ones, but with the probability of zero being zero. Thus the other probabilities are scaled up (i.e., divided by 1 - Pr(Y = 0)) so they sum to 1.

years	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
inducted	46	10	8	7	8	4	2	4	6	3	3	1	4	1	2

(a) For the Poisson distribution, show that the zero-truncated probability function can be expressed in the form

$$\Pr\{X = k \mid k > 0\} = \frac{1}{1 - e^{-\lambda}} \times \frac{e^{-\lambda} \lambda^k}{k!} \qquad k = 1, 2, \dots$$

★ The standard Poisson distribution has the probability mass function

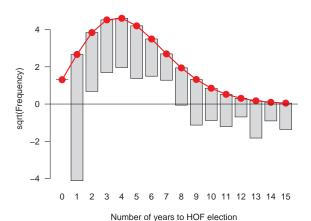
$$\Pr\{X = k\} = \frac{e^{-\lambda} \lambda^k}{k!} \quad k = 1, 2, \dots.$$

For this, $\Pr\{X=0\}=e^{-\lambda}$. The formula given in the problem scales the standard probability to account for zero-truncation, i.e., by the factor $\frac{1}{1-\Pr\{X=0\}}$.

(b) Show that the mean is $\lambda/(1 - \exp(-\lambda))$.

- (c) Enter these data into R as a one-way table, and use goodfit () to fit the standard Poisson distribution, as if you hadn't encountered the problem of zero truncation.
 - ★ The rootogram below shows why zero truncation needs to be taken into account.

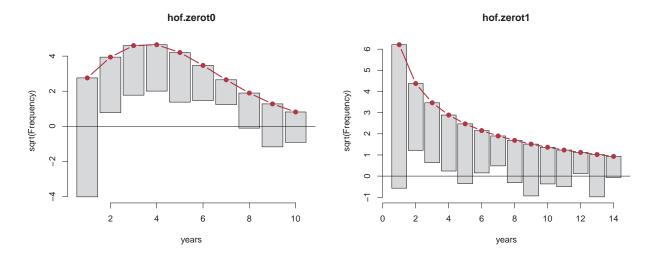
```
> years <- 1:15
> inducted <- c(46, 10, 8, 7, 8, 4, 2, 4, 6, 3, 3, 1, 4, 1, 2)
> HOF.df <- data.frame(years, inducted)
> HOF.tab <- xtabs(inducted ~ years, data=HOF.df)
> goodfit(HOF.tab)
Observed and fitted values for poisson distribution with parameters estimated by `ML' \,
                           fitted pearson residual
                      1.7081050
                  0
                                                -1.30694
                  46 7.0988218
                                               14.60056
                  10 14.7512214
                                                -1.23706
                  8 20.4351783
                                               -2.75082
                   7 21.2319627
                                                -3.08866
                  8 17.6478516
                                                -2.29660
                   4 12.2239706
                                               -2.35221
                  2 7.2574819
4 3.7702285
6 1.7409924
                                               -1.95157
       8
                                                0.11833
                                                3.22782
       9
                   3 0.7235500
     1.0
                                                2.67623
                   3 0.2733679
     11
                                                5.21498
                  1 0.0946756
4 0.0302668
                                                 2.94229
                                                22.81803
      14
                   1 0.0089848
                                                10.45503
     15
                   2 0.0024894
                                                34.54549
> summary(HOF.tab)
Number of cases in table: 109
Number of factors: 1
> plot(goodfit(HOF.tab), xlab='Number of years to HOF election')
```



Though not asked in the problem, the zero-truncated Poisson distribution can be fit using vglm() in the VGAM (Yee, 2015) package.

Models for count data, taking account of excess zeros or zero truncation are examined in more detail in Chapter 11. There, we use the countreg (Zeileis and Kleiber, 2014) package, that provides a zerotrunc() function for these problems. The zero truncated negative binomial provides a better fit than the zero truncated Poisson, but that is not great either.

```
> library(countreg)
> hof.zerot0 <- zerotrunc(years ~ 1, weights = inducted, data=HOF.df)
> hof.zerot1 <- zerotrunc(years ~ 1, weights = inducted, dist="negbin")
> countreg::rootogram(hof.zerot0)
> countreg::rootogram(hof.zerot1)
```



Chapter 4 Two-Way Contingency Tables

Exercise 4.1 The data set fat, created below, gives a 2×2 table recording the level of cholesterol in diet and the presence of symptoms of heart disease for a sample of 23 people.

(a) Use chisq.test (fat) to test for association between diet and disease. Is there any indication that this test may not be appropriate here?



(b) Use a fourfold display to test this association visually. Experiment with the different options for standardizing the margins, using the margin argument to fourfold(). What evidence is shown in different displays regarding whether the odds ratio differs significantly from 1?



(c) oddsratio(fat, log = FALSE) will give you a numerical answer. How does this compare to your visual impression from fourfold displays?



(d) With such a small sample, Fisher's exact test may be more reliable for statistical inference. Use fisher.test(fat), and compare these results to what you have observed before.



(e) Write a one-paragraph summary of your findings and conclusions for this data set.



Exercise 4.2 The data set Abortion in vcdExtra gives a $2 \times 2 \times 2$ table of opinions regarding abortion in relation to sex and status of the respondent. This table has the following structure:

```
> data("Abortion", package = "vcdExtra")
> str(Abortion)

table [1:2, 1:2, 1:2] 171 152 138 167 79 148 112 133
- attr(*, "dimnames")=List of 3
..$ Sex : chr [1:2] "Female" "Male"
..$ Status : chr [1:2] "Lo" "Hi"
..$ Support_Abortion: chr [1:2] "Yes" "No"
```

(a) Taking support for abortion as the outcome variable, produce fourfold displays showing the association with sex, stratified by status.

```
\star
```



(b) Do the same for the association of support for abortion with status, stratified by sex.

```
*
```

```
> Abortion3<-aperm(Abortion, c(2,3,1))
> fourfold(Abortion3)
```



(c) For each of the problems above, use oddsratio() to calculate the numerical values of the odds ratio, as stratified in the question.

```
\star
```

```
# Sex by support for abortion, stratified by status
> summary(oddsratio(Abortion2))
z test of coefficients:
4.18 2.9e-05
                                                 0.91
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
     # Status by support for abortion, stratified by sex
> summary(oddsratio(Abortion3))
z test of coefficients:
                  Estimate Std. Error z value Pr(>|z|) 0.563 0.186 3.03 0.0025
                  0.563
Lo:Hi/Yes:No|Female
Lo:Hi/Yes:No|Male
                    -0.201
                               0.164
                                       -1.23
                                              0.2199
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

- (d) Write a brief summary of how support for abortion depends on sex and status.
 - ★ Regardless of status, more women say no to abortion and more men say yes. Regardless of gender, more low status say no and more high status say yes.

Exercise 4.3 The *JobSat* table on income and job satisfaction created in Example 2.5 is contained in the vcdExtra package.

(a) Carry out a standard χ^2 test for association between income and job satisfaction. Is there any indication that this test might not be appropriate? Repeat this test using simulate.p.value = TRUE to obtain a Monte Carlo test that does not depend on large sample size. Does this change your conclusion?

 \star

(b) Both variables are ordinal, so CMH tests may be more powerful here. Carry out that analysis. What do you conclude?

 \star

Exercise 4.4 The Hospital data in vcd gives a 3×3 table relating the length of stay (in years) of 132 long-term schizophrenic patients in two London mental hospitals with the frequency of visits by family and friends.

(a) Carry out a χ^2 test for association between the two variables.

```
*
```

```
> data("Hospital", package="vcd")
> chisq.test(Hospital)

Pearson's Chi-squared test

data: Hospital
X-squared = 35.2, df = 4, p-value = 4.3e-07
```

(b) Use association () to compute association statistics. How would you describe the strength of association here?

 \star

By the contingency coefficient, there is moderately strong association between the length of stay long-term schizophrenic patients and the frequency of visits by family and friends.

(c) Produce an association plot for these data, with visit frequency as the vertical variable. Describe the pattern of the relation you see here.

```
\star
```

```
> assoc(Hospital, shade=TRUE)
Error in UseMethod("assoc", model): no applicable method for 'assoc' applied to an object of class
"table"
```

(d) Both variables can be considered ordinal, so CMHtest() may be useful here. Carry out that analysis. Do any of the tests lead to different conclusions?

```
> CMHtest (Hospital)

Cochran-Mantel-Haenszel Statistics for Visit frequency by Length of stay

AltHypothesis Chisq Df Prob

cor Nonzero correlation 29.1 1 6.74e-08

rmeans Row mean scores differ 34.4 2 3.40e-08

cmeans Col mean scores differ 29.6 2 3.72e-07

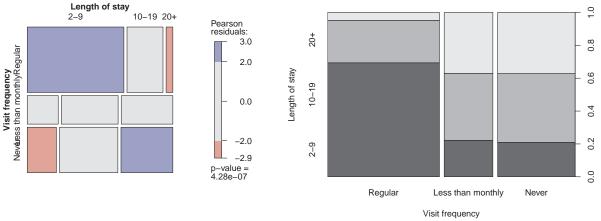
general General association 34.9 4 4.86e-07
```

The results of all four tests lead to the same conclusion that there is a significant association between the visit frequency and the length of stay. The test for non-zero correlation, trteating both variables as ordinal, has the largest ratio of χ^2/df .

Exercise 4.5 Continuing with the *Hospital* data:

(a) Try one or more of the following other functions for visualizing two-way contingency tables with this data: plot(), tile(), mosaic(), and spineplot(). [For all except spineplot(), it is useful to include the argument shade=TRUE].
★





(b) Comment on the differences among these displays for understanding the relation between visits and length of stay.

*

Exercise 4.6 The two-way table *Mammograms* in vcdExtra gives ratings on the severity of diagnosis of 110 mammograms by two raters.

(a) Assess the strength of agreement between the raters using Cohen's κ , both unweighted and weighted. \bigstar Both unweighted and weighted κ indicate substantial agreement. Fleiss-Cohen weights give greater weight to the "near-misses," so gives a larger value.

```
> Kappa (Mammograms)

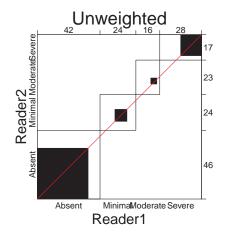
value ASE z Pr(>|z|)
Unweighted 0.371 0.0603 6.15 7.56e-10
Weighted 0.596 0.0492 12.11 8.90e-34

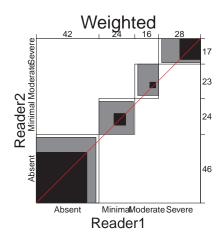
> Kappa (Mammograms, weights= "Fleiss-Cohen")

value ASE z Pr(>|z|)
Unweighted 0.371 0.0603 6.15 7.56e-10
Weighted 0.764 0.0400 19.12 1.67e-81
```

- (b) Use agreementplot() for a graphical display of agreement here.
 - \bigstar The default for agreementplot() shows the weighted display, so you can use weights=1 for the unweighted version.

```
> agreementplot (Mammograms, main="Unweighted", weights=1)
> agreementplot (Mammograms, main="Weighted")
```





- (c) Compare the Kappa measures with the results from assocstats(). What is a reasonable interpretation of each of these measures?
 - ★ The contingency coefficient and Cramer's V assess only association, so these could be large when there is little agreement. The values of these statistics are not directly comparable.

Exercise 4.7 Agresti and Winner (1997) gave the data in Table 4.1 on the ratings of 160 movies by the reviewers Gene Siskel and Roger Ebert for the period from April 1995 through September 1996. The rating categories were Con ("thumbs down"), Mixed, and Pro ("thumbs up").

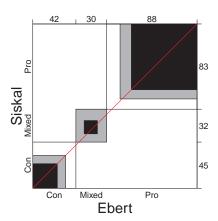
Table 4.1: Movie ratings by Siskel & Ebert, April 1995–September 1996. Source: Agresti and Winner (1997)

			Ebert		
		Con	Mixed	Pro	Total
	Con	24	8	13	45
Siskel	Mixed	8	13	11	32
	Pro	10	9	64	83
	Total	42	30	88	160

(a) Assess the strength of agreement between the raters using Cohen's κ , both unweighted and weighted.

- (b) Use agreementplot() for a graphical display of agreement here.
 - ★ The agreement plot shows that both Siskal and Ebert most commonly gave "thumbs up" ratings where they largely agreed. Their ratings differed most when one of them gave a Mixed rating.

```
> agreementplot (ratings)
```



(c) Assess the hypothesis that the ratings are *symmetric* around the main diagonal, using an appropriate χ^2 test. *Hint*: Symmetry for a square table T means that $t_{ij} = t_{ji}$ for $i \neq j$. The expected frequencies under the hypothesis of symmetry are the average of the off-diagonal cells, $E = (T + T^{\mathsf{T}})/2$.

```
> T <- (ratings + t(ratings))/2
> (Chisq <- sum((ratings - T)^2 / T))
[1] 0.5913
> df <- nrow(T) * (nrow(T) - 1) / 2
> pchisq(Chisq, df, lower.tail = FALSE)
[1] 0.89842
```

(d) Compare the results with the output of mcnemar.test().

```
> mcnemar.test(ratings)

McNemar's Chi-squared test

data: ratings
McNemar's chi-squared = 0.591, df = 3, p-value = 0.9
```

Exercise 4.8 For the *VisualAcuity* data set:

(a) Use the code shown in the text to create the table form, VA.tab.

```
> data("VisualAcuity", package = "vcd")
> VA <- xtabs(Freq ~ right + left + gender, data = VisualAcuity)
> dimnames(VA)[1:2] <- list(c("high", 2, 3, "low"))
> names(dimnames(VA))[1:2] <- paste(c("Right", "Left"), "eye grade")</pre>
```

(b) Perform the CMH tests for this table.



```
> CMHtest (VA)
$`gender:male
Cochran-Mantel-Haenszel Statistics for Right eye grade by Left eye grade
in stratum gender:male
                   AltHypothesis Chisq Df Prob
          Nonzero correlation 1555
rmeans Row mean scores differ 1556 3 cmeans Col mean scores differ 1557 3
                                                  0
                                                  0
general General association 3303 9
$`gender:female`
Cochran-Mantel-Haenszel Statistics for Right eye grade by Left eye grade
in stratum gender:female
                   AltHypothesis Chisq Df Prob
cor Nonzero correlation 3691 1
rmeans Row mean scores differ 3709 3
cmeans Col mean scores differ 3724 3
general General association 8096
```

- (c) Use the woolf_test() described in Section 4.3.2 to test whether the association between left and right eye acuity can be considered the same for men and women.
 - ★ The Woolf test gives no evidence that the association differs for men and women.

```
> woolf_test(VA)
Woolf-test on Homogeneity of Odds Ratios (no 3-Way assoc.)
data: VA
X-squared = 0.0892, df = 1, p-value = 0.77
```

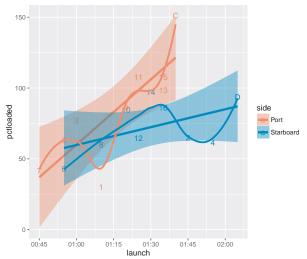
Exercise 4.9 The graph in Figure 4.23 may be misleading, in that it doesn't take into account of the differing capacities of the 18 life boats on the *Titanic*, given in the variable cap in the *Lifeboats* data.

(a) Calculate a new variable, pctloaded, as the percentage loaded relative to the boat capacity.



```
> Lifeboats$pctloaded <- with(Lifeboats, 100*total/cap)
```

- (b) Produce a plot similar to Figure 4.23, showing the changes over time in this measure.
 - ★ Boats on the port side began loading earlier, but were initally less than half full. Boats launched from the starbord side were more consistent over time. With percent loaded (0–100) as the response, a linear model is only a rough approximation.



Test a model allowing different slopes and intercepts for port and starboard sides:

```
> summary(lm(pctloaded ~ side * as.numeric(launch), data=Lifeboats))
Call:
lm(formula = pctloaded ~ side * as.numeric(launch), data = Lifeboats)
Residuals:

Min 1Q Median 3Q Max

-45.34 -11.78 0.34 11.46 29.61
                                       Max
Coefficients:
                                            Estimate Std. Error t value Pr(>|t|)
                                           4.67e+07 1.10e+07
-3.39e+07 1.48e+07
                                                                       4.24 0.00083 ***
-2.29 0.03800 *
(Intercept)
sideStarboard
                                           -3.39e+07
as.numeric(launch)
                                            2.56e-02
                                                          6.05e-03
                                                                        4.24
                                                                                 0.00083 ***
sideStarboard:as.numeric(launch) -1.86e-02
                                                          8.12e-03
                                                                        -2.29 0.03800 *
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Residual standard error: 20.2 on 14 degrees of freedom Multiple R-squared: 0.602, Adjusted R-squared: 0.517 F-statistic: 7.06 on 3 and 14 DF, p-value: 0.004
```

Chapter 5 Mosaic Displays for n-Way Tables

Exercise 5.1 The data set criminal in the package logmult (Bouchet-Valat, 2015) gives the 4×5 table below of the number of men aged 15–19 charged with a criminal case for whom charges were dropped in Denmark from 1955–1958.

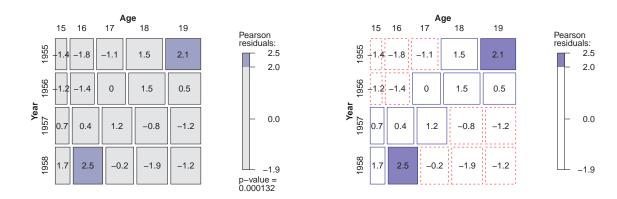
```
> data("criminal", package = "logmult")
> criminal

Age
Year    15    16    17    18    19
    1955    141    285    320    441    427
    1956    144    292    342    441    396
    1957    196    380    424    462    427
    1958    212    424    399    442    430
```

- (a) Use loglm() to test whether there is an association between Year and Age. Is there evidence that dropping of charges in relation to age changed over the years recorded here?
 - \bigstar There is a significant association between Year and Age, so the row profiles of proportions differ over year.

- (b) Use mosaic() with the option shade=TRUE to display the pattern of signs and magnitudes of the residuals. Compare this with the result of mosaic() using "Friendly shading," from the option gp=shading_Friendly. Describe verbally what you see in each regarding the pattern of association in this table.
 - ★ It is helpful here to display all the residual contributions to association in the mosaic display using labeling_residuals.

```
> mosaic(criminal, shade=TRUE,
+ labeling=labeling_residuals, suppress=0)
> mosaic(criminal, gp=shading_Friendly,
+ labeling=labeling_residuals, suppress=0)
```



Although only two residuals exceed the default $|r_{ij}| > 2$ threshold for shading, there is clearly a systematic association between year and age shown by the signs of the residuals.

The Friendly shading option here gives a better picture of the pattern of associations, showing positive and negative residuals in the diagonally opposite corners of the plot. See Exercise 6.2 for further analysis of this data.

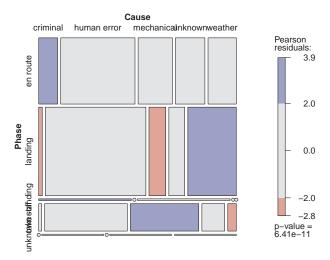
Exercise 5.2 The data set AirCrash in vcdExtra gives a database of all crashes of commercial airplanes between 1993-2015, classified by Phase of the flight and Cause of the crash. How can you best show is the nature of the association between these variables in a mosaic plot? Start by making a frequency table, aircrash.tab:

```
> data("AirCrash", package = "vcdExtra")
> aircrash.tab <- xtabs(~ Phase + Cause, data = AirCrash)</pre>
```

(a) Make a default mosaic display of the data with shade=TRUE and interpret the pattern of the high-frequency cells.



mosaic(aircrash.tab, shade=TRUE)



Four cells stand out as having greater than expected frequencies, if Phase and Cause were independent. Both take-off and en-route are positively associated with criminal activities. Crashes in landing are more associated with weather. It is difficult to interpret the unknown cells.

- (b) The default plot has overlapping labels due to the uneven marginal frequencies relative to the lengths of the category labels. Experiment with some of the labeling_args options (abbreviate, rot_labels, etc.) to see if you can make the plot more readable. Hint: a variety of these are illustrated in Section 4.1 of vignette("strucplot")
 - ★ Here are two alternatives that reduce the overplotting of labels:

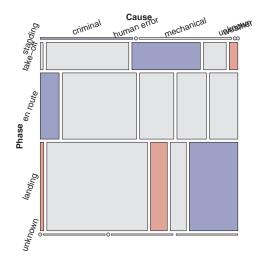
```
> mosaic(aircrash.tab, shade=TRUE, rot_labels=c(20,90,0,70), legend=FALSE)
> mosaic(aircrash.tab, shade=TRUE, alternate_labels=TRUE, legend=FALSE)
```





- (c) The levels of Phase and Cause are ordered alphabetically (because they are factors). Experiment with other orderings of the rows/columns to make interpretation clearer, e.g., ordering Phase temporally or ordering both factors by their marginal frequency.
 - ★ Ordering by Phase is slightly easier to interpret. Ordering both variables by marginal frequencies is also slightly better than the default, except that it leads to more overplotting of the labels.

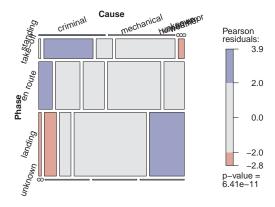
```
> # reorder Phase temporarally
> roworder <- c(3, 4, 1, 2, 5)
> mosaic(aircrash.tab[roworder,], shade=TRUE, rot_labels=c(20,90,0,70), legend=FALSE)
> 
> # marginal frequencies
> roworder <- order(rowSums(aircrash.tab))
> colorder <- order(colSums(aircrash.tab))
> mosaic(aircrash.tab[roworder, colorder], shade=TRUE, rot_labels=c(20,90,0,70), legend=FALSE)
```





The best general approach, as was illustrated in Figure 1.10, uses *effect ordering* to order the factors according to their associations. One easy method for this (Friendly and Kwan, 2003) is to order the factor levels according to their scores on the first dimension of a correspondence analysis solution as illustrated below. This maximizes an opposite corner pattern of the residuals.

```
0.051548 27.5 93.1 *******
0.012340 6.6 99.7 **
0.000562 0.3 100.0
 Total: 0.187452 100.0
> # reorder by CA coordinates on Dim 1
> revorder <- order(aircrash.ca$rowcoord[,"Dim1"])
> colorder <- order(aircrash.ca$colcoord[,"Dim1"])</pre>
> aircrash.tab[roworder, colorder]
Phase
            criminal mechanical unknown human error weather
                        2 0
24 8
  standing
  take-off
                                                          29
  en route
                                  29
                                                          63
                                            18
                                                         114
  landing
                                  0
                                                           1
                                            1
  unknown
> mosaic(aircrash.tab[roworder, colorder], shade=TRUE, rot_labels=c(20,90,0,70))
```



Exercise 5.3 The Lahman package contains comprehensive data on baseball statistics for Major League Baseball from 1871 through 2012. For all players, the *Master* table records the handedness of players, in terms of throwing (L, R) and batting (B, L, R), where B indicates "both." The table below was generated using the following code:

```
> library(Lahman)
> data("Master", package = "Lahman")
> basehands <- with(Master, table(throws, bats))</pre>
```

	Bats		
Throws	В	L	R
L	177	2640	527
R	924	1962	10442

- Use the code above, or else enter these data into a frequency table in R.
 - ★ These notes use a later version of the Lahman package (v. 4.0-1) with the code above, so the numbers used in the plots don't correspond to those in the table. The current version of the table is shown below.

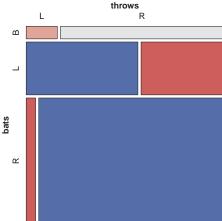
```
> bats
throws B L R
L 182 2742 550
R 956 2031 10814
```

• Construct mosaic displays showing the relation of batting and throwing handedness, split first by batting and then by throwing.

 \bigstar By default, a two-way contingency table is split first by the row variable, then by the column variable. So, to split the other way, you can use t () on the table argument.

```
> mosaic(basehands, shade=TRUE, labeling=labeling_residuals(), legend=FALSE)
> mosaic(t(basehands), direction=c("h", "v"), shade=TRUE, legend=FALSE)
```





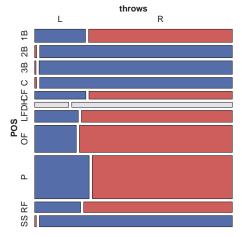
- From these displays, what can be said about players who throw with their left or right hands in terms of their batting handedness?
 - ★ Players who throw with their left or right hands are most likely to bat in the same way. From the values of the cell residuals, left handers are more likely to be uni-handers than righties.

Exercise 5.4 * A related analysis concerns differences in throwing handedness among baseball players according to the fielding position they play. The following code calculates such a frequency table.

```
> library(Lahman)
> MasterFielding <- data.frame(merge(Master, Fielding, by = "playerID"))
> throwPOS <- with(MasterFielding, table(POS, throws))</pre>
```

- (a) Make a mosaic display of throwing hand vs. fielding position.
 - ★ There is clearly a very strong association between throwing hand and fielding position. A peculiarity of the data is that designated hitters (DH) do not play a fielding position, but instead fill in for the pitcher in the batting order, so throwing hand is not really relevant here. This position might arguably be deleted from this analysis.

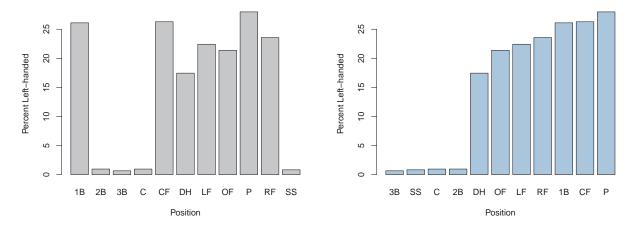
> mosaic(throwPOS, shade=TRUE, legend=FALSE)



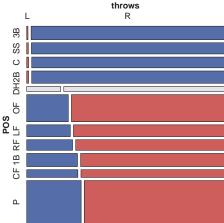
- (b) Calculate the percentage of players throwing left-handed by position. Make a sensible graph of this data.
 - ★ A barplot is simple and reasonable here. However, the levels of fielding position are ordered alphabetically, which makes interpretation harder. Sorting by pctLeft is better.

```
> pctLeft <- 100 * throwPOS[,1] / rowSums(throwPOS)
> pctLeft

   1B   2B   3B   C   CF   DH   LF   OF   P   RF   SS
26.100   0.955   0.650   0.952  26.284  17.449  22.419  21.385  27.984  23.571   0.818
> ord <- order(pctLeft)
> barplot(pctLeft, xlab="Position", ylab="Percent Left-handed")
> barplot(pctLeft[ord], xlab="Position", ylab="Percent Left-handed", col="lightblue")
```



- (c) Re-do the mosaic display with the positions sorted by percentage of left-handers.
 - > mosaic(throwPOS[ord,], shade=TRUE, legend=FALSE)



- (d) Is there anything you can say about positions that have very few left-handed players?
 - \bigstar All infield positions except for 1^{st} base have a very small percentage of players who throw left-handed. Given the marginal distributions of handeness and position, outfielders, pitchers and 1^{st} basemen are more likely to throw left-handed than if these variables were independent.

Exercise 5.5 For the Bartlett data described in Example 5.12, fit the model of no three-way association, H_4 in Table 5.2.

(a) Summarize the goodness of fit for this model, and compare to simpler models that omit one or more of the two-way terms.



(b) Use a mosaic-like display to show the lack of fit for this model.

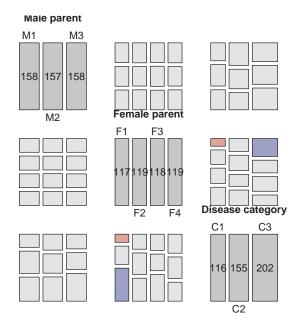


Exercise 5.6 Red core disease, caused by a fungus, is not something you want if you are a strawberry. The data set jansen.strawberry from the agridat (Wright, 2015) package gives a frequency data frame of counts of damage from this fungus from a field experiment reported by Jansen (1990). See the help file for details. The following lines create a $3 \times 4 \times 3$ table of crossings of 3 male parents with 4 (different) female parents, recording the number of plants in four blocks of 9 or 10 plants each showing red core disease in three ordered categories, C1, C2, or C3.

```
> data("jansen.strawberry", package = "agridat")
> levels(dat$male) <- paste0("M", 1:3)
> levels(dat$female) <- paste0("F", 1:4)</pre>
  jansen.tab <- xtabs(count ~ male + female + category, data = dat)</pre>
> names (dimnames (jansen.tab)) <- c("Male parent", "Female parent",
                                   "Disease category")
> ftable(jansen.tab)
                          Disease category C1 C2 C3
Male parent Female parent
                                           6 13 20
M1
            F1
                                           8 15 17
13 10 16
            F4
                                            8 21 11
M2
            F1
                                            5 13 21
                                           9 16 14
                                           16 9 15
                                           12 13 14
            F4
МЗ
                                            5 10 24
            F2
                                           13 12 15
                                            3 14 22
```

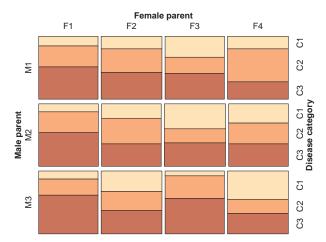
- (a) Use pairs (jansen.tab, shade=TRUE) to display the pairwise associations among the three variables. Describe how disease category appears to vary with male and female parent. Why is there no apparent association between male and female parent?
 - ★ This was a designed experiment, with male and female parents completely crossed to create 12 populations. Disease categories seem to be associated with female parents, with more serious disease (C3) more prevalent in parent F4.

```
> library(vcd)
> pairs(jansen.tab, shade=TRUE)
```

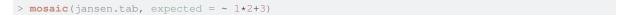


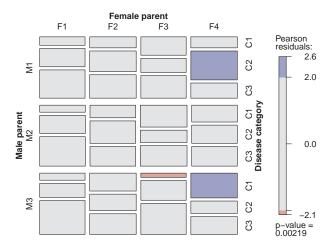
(b) As illustrated in Figure 5.6, use mosaic() to prepare a 3-way mosaic plot with the tiles colored in increasing shades of some color according to disease category. Describe the pattern of category C3 in relation to male and female parent. (Hint: the highlighting arguments are useful here.)

```
> cols <- c("moccasin", "lightsalmon1", "indianred")
> mosaic(jansen.tab, highlighting=3, highlighting_fill=cols)
```



(c) With category as the response variable, the minimal model for association is [MF][C], or $\sim 1 \pm 2 + 3$. Fit this model using loglm() and display the residuals from this model with mosaic(). Describe the pattern of lack of fit of this model.





Exercise 5.7 The data set caith in MASS (Ripley, 2015) gives another classic 4×5 table tabulating hair color and eye color, this for people in Caithness, Scotland, originally from Fisher (1940). The data is stored as a data frame of cell frequencies, whose rows are eye colors and whose columns are hair colors.

```
> data("caith", package = "MASS")
> caith
        fair red medium dark black
blue
         326 38
688 116
                     241 110
584 188
                           188
light
                                    4
medium
         343 84
                      909
                           412
                                   26
dark
          98
              48
                      403
                           681
                                   85
```

(a) The loglm() and mosaic() functions don't understand data in this format, so use Caith <- as.matrix(caith) to convert to array form. Examine the result, and use names (dimnames (Caith)) <-c() to assign appropriate names to the row and column dimensions.</p>
★

```
> Caith <- as.matrix(caith)
> dimnames(Caith)

[[1]]
[1] "blue" "light" "medium" "dark"

[[2]]
[1] "fair" "red" "medium" "dark" "black"
> names(dimnames(Caith)) <- c("Eye", "Hair")</pre>
```

(b) Fit the model of independence to the resulting matrix using loglm().

(c) Calculate and display the residuals for this model.

```
> residuals(caith.mod)
```

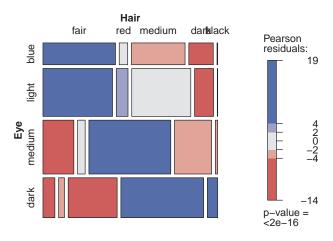
```
Hair

Eye fair red medium dark black
blue 8.63 -0.0193 -2.67 -6.00 -3.94
light 11.60 3.3125 -1.73 -12.19 -6.63
medium -6.56 -1.0691 7.40 -2.19 -2.20
dark -16.19 -2.7683 -5.41 16.28 8.46
```

(d) Create a mosaic display for this data.

*

```
> mosaic(Caith, shade=TRUE)
```



Exercise 5.8 The HairEyePlace data in VcdExtra gives similar data on hair color and eye color, for both Caithness and Aberdeen as a $4 \times 5 \times 2$ table.

(a) Prepare separate mosaic displays, one for each of Caithness and Aberdeen. Comment on any difference in the pattern of residuals.

 \star

(b) Construct conditional mosaic plots, using the formula ~ Hair + Eye | Place and both mosaic() and cotabplot(). It is probably more useful here to suppress the legend in these plots. Comment on the difference in what is shown in the two displays.

*

Exercise 5.9 Bertin (1983, pp. 30–31) used a 4-way table of frequencies of traffic accident victims in France in 1958 to illustrate his scheme for classifying data sets by numerous variables, each of which could have various types and could be assigned to various visual attributes. His data are contained in Accident in vcdExtra, a frequency data frame representing his $5 \times 2 \times 4 \times 2$ table of the variables age, result (died or injured), mode of transportation, and gender.

```
> data("Accident", package = "vcdExtra")
> str(Accident, vec.len=2)

'data.frame': 80 obs. of 5 variables:
$ age : Ord.factor w/ 5 levels "0-9"<"10-19"<...: 5 5 5 5 5 ...
$ result: Factor w/ 2 levels "Died", "Injured": 1 1 1 1 1 ...
$ mode : Factor w/ 4 levels "4-Wheeled", "Bicycle",...: 4 4 2 2 3 ...
$ gender: Factor w/ 2 levels "Female", "Male": 2 1 2 1 2 ...
$ Freq : int 704 378 396 56 742 ...</pre>
```

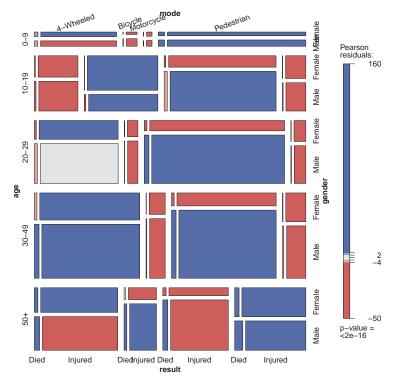
(a) Use loglm() to fit the model of mutual independence, Freq ~ age+mode+gender+result to this data set.
 ★ You can use loglm() directly on the frequency data frame, with Freq as the response:

Or, convert to an array first with xtabs ()

(b) Use mosaic() to produce an interpretable mosaic plot of the associations among all variables under the model of mutual independence. Try different orders of the variables in the mosaic. (*Hint*: the abbreviate component of the labeling_args argument to mosaic() will be useful to avoid some overlap of the category labels.)

★ In this data set, mode is arguably an ordered factor, and better results will come from reordering its levels, from Pedestrian to 4-Wheeled vehicle. The order of variables given in xtabs() gives a reasonable result. The label overlap can be avoided by rotating the labels for mode.

```
> Accident$mode <- ordered(Accident$mode,
+ levels=levels(Accident$mode)[c(4,2,3,1)])
> mosaic(accident.tab, shade=TRUE, rot_labels = c(20, 90, 00, 90))
```



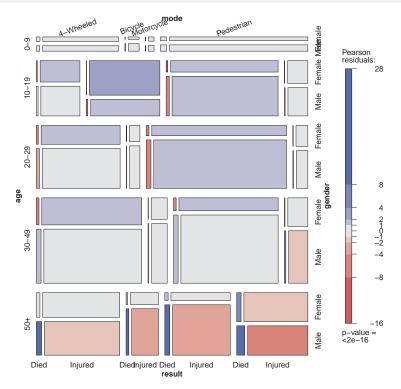
- (c) Treat result ("Died" vs. "Injured") as the response variable, and fit the model

 Freq ~ age*mode*gender + result that asserts independence of result from all others jointly.

 ★ This fits much better than the mutual independence model, but still has a terrible fit. There still remain important associations between result and the other variables
 - > loglm(Freq ~ age * mode * gender + result, data = Accident)

- (d) Construct a mosaic display for the residual associations in this model. Which combinations of the predictor factors are more likely to result in death?
 - ★ The largest postive residuals appear in the 50+ age group, where males are more likely to have died, regardless of mode. It can also be seen that in the 30-49 age group, more males die in bicycle and motorcycle accidents. Other permutations of the table variables or other displays like doubledecker plots can highlight other features.

```
> mosaic(accident.tab, expected = ~age * mode * gender + result,
+ shade=TRUE, rot_labels = c(20, 90, 00, 90),
+ gp_args=list(interpolate=c(1,2,4,8)))
```



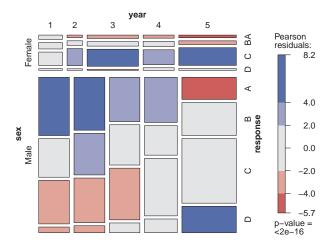
Exercise 5.10 The data set Vietnam in vcdExtra gives a $2 \times 5 \times 4$ contingency table in frequency form reflecting a survey of student opinion on the Vietnam War at the University of North Carolina in May 1967. The table variables are sex, year in school, and response, which has categories: (A) Defeat North Vietnam by widespread bombing and land invasion; (B) Maintain the present policy; (C) De-escalate military activity, stop bombing and begin negotiations; (D) Withdraw military forces immediately. How does the chosen response vary with sex and year?

```
> data("Vietnam", package = "vcdExtra")
> str(Vietnam)

'data.frame': 40 obs. of 4 variables:
$ sex : Factor w/ 2 levels "Female", "Male": 1 1 1 1 1 1 1 1 1 1 1 1 1 ...
$ year : int 1 1 1 1 2 2 2 2 3 3 ...
$ response: Factor w/ 4 levels "A", "B", "C", "D": 1 2 3 4 1 2 3 4 1 2 ...
$ Freq : int 13 19 40 5 5 9 33 3 22 29 ...
```

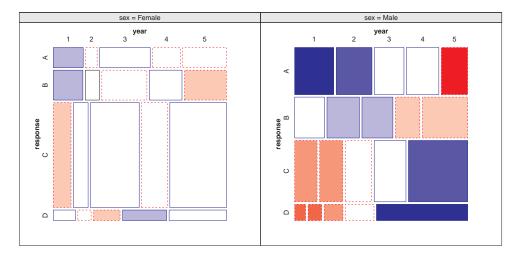
(a) With response (R) as the outcome variable and year (Y) and sex (S) as predictors, the minimal baseline loglinear model is the model of joint independence, [R][YS]. Fit this model, and display it in a mosaic plot.

★ The baseline model does not fit well, so response is associated with either year or sex or both. Note that when fitting with loglm() (or glm()), both mosaic(mod) and plot(mod) give the corresponding mosaic plot for a model object, mod.



- (b) Construct conditional mosaic plots of the response versus year separately for males and females. Describe the associations seen here
 - the associations seen here. \bigstar We use <code>cotabplot()</code> here, with the formula ~ response + year sex| to condition on sex. For males, there is a clear association between response and year, with 1st year students prefering the more military response A, and later-year students tending toward the more peaceful response D. For females, the association between response and year is weak, and does not show a coherent pattern.

```
> cotabplot(~ response + year | sex, data=vietnam.tab,
+ gp=shading_Friendly, gp_args=list(interpolate=1:4), legend=FALSE)
```



(c) Follow the methods shown in Example 5.10 to fit separate models of independence for the levels of sex, and

the model of conditional independence, $R \perp Y \mid S$. Verify that the decomposition of G^2 in Eqn. (5.6) holds for these models.

these models. \bigstar Splitting the data by sex, using apply () shows that the association between response and year is strongly significant for males, but not for females.

(d) Construct a useful 3-way mosaic plot of the data for the model of conditional independence.

 \star

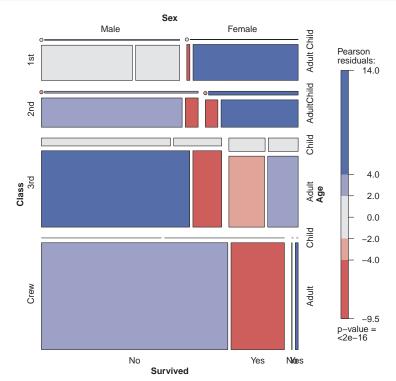
Exercise 5.11 Consider the models for 4-way tables shown in Table 5.3.

- (a) For each model, give an independence interpretation. For example, the model of mutual independence corresponds to $A \perp B \perp C \perp D$.
 - ★ The basic idea of the notation is that terms in separate []s are said to be independent under a given model. Variables within a [] term are allowed to be associated
 - mutual: [A] [B] [C] [D] $\leftrightarrow A \perp B \perp C \perp D$
 - joint: [ABC] [D] \leftrightarrow $(ABC) \perp D$
 - conditional: [AD] [BD] [CD] \leftrightarrow $(AD) \perp (BD) \perp (CD)$
 - markov (order 1): [AB] [BC] [CD] \leftrightarrow $(AB) \perp (BC) \perp (CD)$
 - markov (order 2): [ABC] [BCD] \leftrightarrow (ABC) \perp (BCD)
 - saturated: no independence relationship
- (b) Use the functions shown in the table together with loglin2formula() to print the corresponding model formulas for each.
 - ★ The model generating functions, mutual(), joint(), etc. provide a simple way to specify loglinear models for loglm() and mosaic().

```
> loglin2formula(mutual(4, factors=LETTERS[1:4]))
~A + B + C + D
> loglin2formula(joint(4, factors=LETTERS[1:4]))
~A:B:C + D
> loglin2formula(joint(4, factors=LETTERS[1:4], with=1))
~B:C:D + A
> loglin2formula(conditional(4, factors=LETTERS[1:4]))
~A:D + B:D + C:D
> loglin2formula(conditional(4, factors=LETTERS[1:4], with=1))
~B:A + C:A + D:A
> loglin2formula(markov(4, factors=LETTERS[1:4]))
~A:B + B:C + C:D
> loglin2formula(markov(4, factors=LETTERS[1:4], order=2))
~A:B:C + B:C:D
> loglin2formula(saturated(4, factors=LETTERS[1:4]))
~A:B:C:D
```

Exercise 5.12 The dataset *Titanic* classifies the 2,201 pasengers and crew of the *Titanic* by Class (1st, 2nd, 3rd, Crew), Sex, Age, and Survived. Treating Survived as the response variable,

(a) Fit and display a mosaic plot for the baseline model of joint independence, [CGA][S]. Describe the remaining pattern of associations.



- (b) Do the same for a "main effects" model that allows two-way associations between each of C, G, and A with S.
- (c) What three-way association term should be added to this model to allow for greater survival among women and children? Does this give an acceptable fit?
- (d) Test and display models that allow additional three-way associations until you obtain a reasonable fit.

Chapter 6 Correspondence Analysis

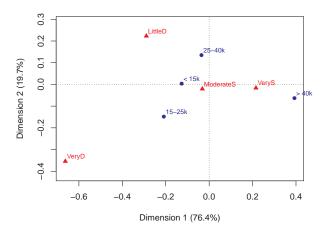
These solutions use an updated version of the ca package, v. 0.64 or greater. In particular, MCA plots are now simpler, using a new mcaplot() function, and lines can be added to MCA plots using multilines().

Exercise 6.1 The JobSat data in vcdExtra gives a 4×4 table recording job satisfaction in relation to income.

- (a) Carry out a simple correspondence analysis on this table. How much of the inertia is accounted for by a one-dimensional solution? How much by a two-dimensional solution?
 - ★ The 1D solution accounts for 76.4

(b) Plot the 2D CA solution. To what extent can you consider the association between job satisfaction and income "explained" by the ordinal nature of these variables?

```
> plot(jobsat.ca)
```



Job satisfaction is ordered as expected by its ordinal levels along Dimension 1. The levels of income in this plot do not appear to be ordered according to the quantitative levels they represent.

Exercise 6.2 Refer to Exercise 5.1 in Chapter 5. Carry out a simple correspondence analysis on the 4×5 table *criminal* from the logmult package.

(a) What percentages of the Pearson χ^2 for association are explained by the various dimensions?

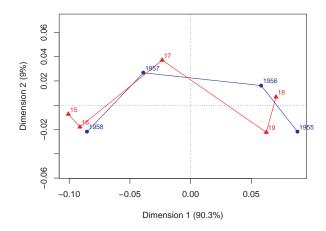
```
> data("criminal", package = "logmult")
> criminal.ca <- ca(criminal)
>  # just show the scree plot
> summary(criminal.ca, rows=FALSE, columns=FALSE)
Principal inertias (eigenvalues):
```

```
dim value % cum% scree plot
1 0.004939 90.3 90.3 **************
2 0.000491 9.0 99.3 **
3 3.8e-050 0.7 100.0
------
Total: 0.005468 100.0
```

(b) Plot the 2D correspondence analysis solution. Describe the pattern of association between year and age.

```
*
```

```
> plot(criminal.ca, lines=TRUE)
```



The category points for both year and age vary systematically over Dimension 1. There were more younger men in later years, and more older in earlier years.

Exercise 6.3 Refer to Exercise 5.2 for a description of the AirCrash data from the vcdExtra package. Carry out a simple correspondence analysis on the 5×5 table of Phase of the flight and Cause of the crash.

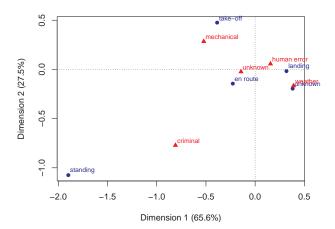
(a) What percentages of the Pearson χ^2 for association are explained by the various dimensions? \bigstar aircrash.tab was calculated in Exercise 5.2.

```
> aircrash.tab
Phase
           criminal human error mechanical unknown weather
  en route
                              63
                                          29
                                                  25
                 16
  landing
                  4
                             114
                                          19
                                                   18
                                                           55
  standing
                              2.9
                                          2.4
                                                    8
  take-off
                   0
  unknown
> aircrash.ca <- ca(aircrash.tab)</pre>
       # just show the scree
> summary(aircrash.ca, rows=FALSE, columns=FALSE)
Principal inertias (eigenvalues):
                        C11m%
 dim
        value
                               scree plot
                  65.6 65.6
        0.123002
                               *******
                  27.5 93.1
6.6 99.7
        0.051548
        0.012340
                               * *
                    0.3 100.0
        0.000562
Total: 0.187452 100.0
```

(b) Plot the 2D correspondence analysis solution. Describe the pattern of association between phase and cause. How would you interpret the dimensions?

```
\star
```

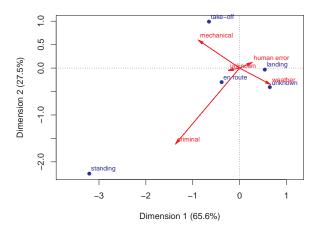
```
> plot (aircrash.ca)
```



Dimension 1 largely distinguishes standing from landing, where the main causes are human error and weather problems. Dimension 2 largely distinguishes standing from take-off, where mechanical problems are more prevalent.

(c) The default plot method uses map="symmetric" with points for both rows and columns. Try using map="symbiplot" with vectors (arrows=) for either rows or columns. (Read help(plot.ca) for a description of these options.)

```
★
> plot(aircrash.ca, map="symbiplot", arrows=c(FALSE, TRUE))
```



Exercise 6.4 The data set *caith* in MASS gives a classic table tabulating hair color and eye color of people in Caithness, Scotland, originally from Fisher (1940).

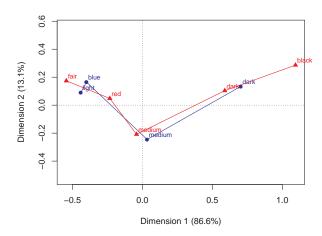
(a) Carry out a simple correspondence analysis on this table. How many dimensions seem necessary to account for most of the association in the table?

One could argue that a 1D solution is adequate here. The 2D solution is essentially complete.

(b) Plot the 2D solution. The interpretation of the first dimension should be obvious; is there any interpretation for the second dimension?

```
\star
```

```
> plot(caith.ca, lines=TRUE)
```



Dimension 1 is the obvious light–dark dimension for hair color and eye color (but not that blue and light eyes have quite similar positions). Dimension 2 could be called "extremes vs. middle", but in CA results with largely 1D association, this effect is common, often called the "horseshoe" or "arch" effect.

Exercise 6.5 The same data, plus a similar table for Aberdeen, are given as a three-way table as *HairEyePlace* in vcdExtra.

(a) Carry out a similar correspondence analysis to the last exercise for the data from Aberdeen. Comment on any differences in the placement of the category points.



(b) Analyze the three-way table, stacked to code hair color and place interactively, i.e., for the loglinear model [Hair Place][Eye]. What does this show?

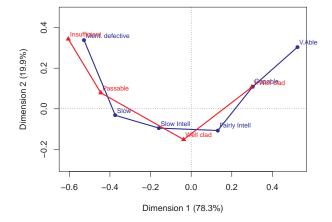


Exercise 6.6 The data set Gilby in vcdExtra gives a classic (but now politically incorrect) 6×4 table of English schoolboys classified according to their clothing and their teacher's rating of "dullness" (lack of intelligence).

(a) Compute and plot a correspondence analysis for this data. Write a brief description and interpretation of these results.

```
*
```

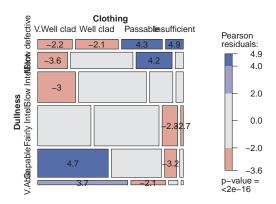
```
name
             mass
                   qlt
                          inr
                                      cor ctr
    Mntd
                         292
                                      707
                                           264
                                                   337
                                                       289 426
                   943
                         187
                                      936
                                          223
                                                   -32
2 3 4
    Slow
                                            75
                                                   -95
    SlwI
              236
                   938
                          85
                                 -159
                                      691
                                                       247
                                                            106
    FrlI
              310
                          88
                                 131
                                      601
                                            67
                                                  -107
                                                       398
                                                            176
5
                                                   109
                                                       115
             217
                  1000
                         223
                                 304 885 253
                                                            129
    Cpbl
                         125
                                          118
               34
                   990
                                 524
                                      740
                                                   304
                                                       250
                                                            157
Columns:
                                                   k=2 cor ctr
107 113 208
            mass
369
                                  k=1
    name
                   qlt
                          inr
                                      cor ctr
                                 299
1 2
    VWll
                         366
                                      886 414
                         106
                                                  -151 934 496
             435
                   989
                                       56
                                             8
    Wllc
3
                                 -445 946 383
    Pssb
             154
                   976
                         317
                                                    79
                                                             47
                                                   344 233 248
    Insf
               42
                   955
                         212
                                -605 722 195
```



The association between clothing and dullness is largely one dimensional, but there is a moderately large horseshoe effect. On Dimension 1, the categories of both variables are approximately equally spaced.

(b) Make an analogous mosaic plot of this table. Interpret this in relation to the correspondence analysis plot.

> mosaic(Gilby, shade=TRUE, labeling=labeling_residuals)



The mosaic nearly shows the opposite corner pattern associated with a unidimensional association of two ordered variables, but the largest residuals are not systematically confined to the diagonally opposite cells. The mosaic shows the marginal frequencies of dullness and the cell frequencies by the

area of the tiles, while this information is not available in the CA plot.

Exercise 6.7 For the mental health data analyzed in Example 6.2, construct a shaded sieve diagram and mosaic plot. Compare these with the correspondence analysis plot shown in Figure 6.2. What features of the data and the association between SES and mental health status are shown in each?

*

Exercise 6.8 Simulated data are often useful to help understand the connections between data, analysis methods, and associated graphic displays. Section 6.3.1 illustrated interactive coding in R, using a simulated 4-way table of counts of pets, classified by age, color, and sex, but with no associations because the counts had a constant Poisson mean, $\lambda = 15$.

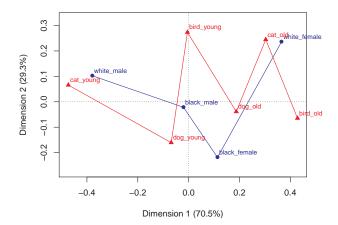
- (a) Re-do this example, but in the call to rpois(), specify a non-negative vector of Poisson means to create some associations among the table factors.
 - ★ First, create a data.frame of the factor levels. Then you can use these variables to create the Poisson means in a way that varies across some of the category combinations to create associations. Here we try to creates associations between Pet and Color (more black dogs than other combinations) and between Age and Sex (more young male pets). These cell means are then used in the call to rpois().

```
> dim <- c(3, 2, 2, 2)
/ dlm <- c(3, 2, 2, 2)
/ factors <- expand.grid(Pet=c("dog", "cat", "bird"),
/ Age=c("young", "old"),
/ Color=c("black", "white"),
/ Sex=c("male", "female"))</pre>
> means <-
+ with (factors, {
             ifelse(Pet=="dog", 10, 0) +
ifelse((Pet=="dog" & Color=="black"), 10, -10) +
             ifelse((Age=="young" & Sex=="male"), 5, -5)
> set.seed(1234)
> tab <- array(rpois(prod(dim), means), dim=dim)
> dimnames(tab) <- list(Pet=c("dog", "cat", "bird"),</pre>
                                   Age=c("young", "old"),
Color=c("black", "white"),
Sex=c("male", "female"))
> # stack
> as.matrix(ftable(Pet + Age ~ Color + Sex, tab))
                    Pet Age
Color_Sex
                      dog_young dog_old cat_young cat_old bird_young bird_old
  black_male
                            36
                                            30
                                                         16
                                                                      6
                                                                                        16
                                 30
                                                                         4
                                                                                                       5
   black_female
                                             25
   white_male
                                 22
                                                            18
   white_female
```

(b) Use CA methods to determine if and how the structure you created in the data appears in the results.

*

```
> library(ca)
> pets.ca <- ca(as.matrix(ftable(Pet + Age ~ Color + Sex, tab)))
> plot(pets.ca, lines=TRUE)
```



Exercise 6.9 The TV data was analyzed using CA in Example 6.4, ignoring the variable Time. Carry out analyses of the 3-way table, reducing the number of levels of Time to three hourly intervals as shown below.

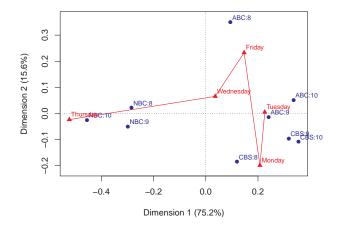
```
> data("TV", package="vcdExtra")
> # reduce number of levels of Time
> TV.df <- as.data.frame.table(TV)
> levels(TV.df$Time) <- rep(c("8", "9", "10"), c(4, 4, 3))
> TV3 <- xtabs(Freq ~ Day + Time + Network, TV.df)
> structable (Day ~ Network + Time, TV3)
                 Day Monday Tuesday Wednesday Thursday Friday
Network Time
                          536
ABC
                         1401
                                    1205
                                                              682
                                                                      907
                                   1044
                                                                       711
           10
                          910
                                                  668
                                                              349
CBS
          8
                         1167
                                                  550
                                                              680
                                                                       509
                                     646
           9
                          967
                                     959
                                                  409
                                                              385
                                                                      544
                                                                       426
           10
                          789
                                     798
                                                             270
                                                  324
NBC
                                    1090
                                                  512
                                                            1927
                          858
                                                                       823
           8
                                                                       590
                          946
                                     890
                                                  831
                                                            1858
          10
                          825
                                                  869
                                                            2101
```

(a) Use the stacking approach (Section 6.3) to perform a CA of the table with Network and Time coded interactively. You can create this using the as.matrix() method for a "structable" object.

```
> TV3S <- as.matrix(structable(Day ~ Network + Time, TV3), sep=":")
*
> TV3S.ca <-ca(TV3S)
> summary(TV3S.ca, rows=FALSE, columns=FALSE)
Principal inertias (eigenvalues):
 dim
        value
                        cum%
                               scree plot
                  75.2
        0.089629
                        75.2
 1
                               *******
                  15.6 90.8
7.5 98.3
1.7 100.0
        0.018576
                        90.8
                               ****
        0.008992
                               * *
        0.002001
 Total: 0.119198 100.0
```

- (b) What loglinear model is analyzed by this approach?
 - ★ The model is the joint independence model, [Day][Network Time], asserting that the frequencies of watching the combinations of networks in different time slots do not vary with day of the week.
- (c) Plot the 2D solution. Compare this to the CA plot of the two-way table in Figure 6.4.

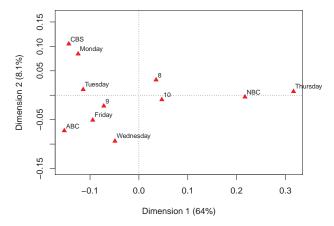
```
> plot(TV3S.ca, lines=c(FALSE, TRUE))
```



Overall, the plot is somewhat similar to that of Figure 6.4 except for the (arbitrary) reversal of Dimension 1. The category points for NBC cluster near Thursday, while those for ABC and CBS are at the other end of that dimension and Dimension 2 is related to the difference in viewership to those channels.

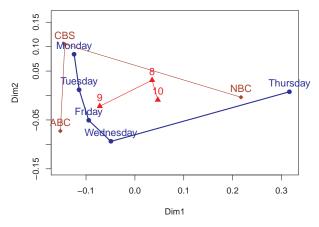
- (d) Carry out an MCA analysis using mjca() of the three-way table TV3. Plot the 2D solution, and compare this with both the CA plot and the solution for the stacked three-way table.
 - ★ The MCA analysis differs in that it includes all pairwise associations of Day, Time and Network rather than just the joint independence model analyzed by the stacking approach.

```
> TV3.mca <- mjca(TV3)
> plot(TV3.mca, collabels="level")
```



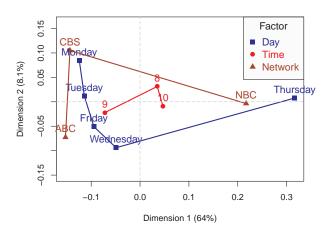
The default plot is somewhat difficult to read because the factor points s aren't distinguished by color or shape. A customized plot can be constructed as follows (as illustrated in the text, e.g., for Figure 6.10).

```
> res <- plot(TV3.mca, labels=0, pch='.', cex.lab=1.2)
> coords <- data.frame(res$cols, TV3.mca$factors)
> nlev <- rle(as.character(coords$factor))$lengths
> fact <- unique(as.character(coords$factor))
>
> cols <- c("blue", "red", "brown")
> lwd <- 2
> plot(Dim2 ~ Dim1, type='n', data=coords, asp=1)
> points(coords[,1:2], pch=rep(16:18, nlev), col=rep(cols, nlev), cex=1.2)
> text(coords[,1:2], labels=coords$level, col=rep(cols, nlev), pos=3, cex=1.2, xpd=TRUE)
> multilines(coords[, c("Dim1", "Dim2")], group=coords$factor, col=cols, lwd=lwd)
```



A similar plot can now be produced more simply using:

```
> mcaplot(TV3.mca, legend=TRUE)
```



Exercise 6.10 Refer to the MCA analysis of the *PreSex* data in Example 6.8. Use the stacking approach to analyze the stacked table with the combinations of premarital and extramarital sex in the rows and the combinations of gender and marital status in the columns. As suggested in the exercise above, you can use as .matrix (structable ()) to create the stacked table.

```
as.matrix(structable(PremaritalSex + ExtramaritalSex ~ Gender + Marital, PreSex), sep=":")
> presexS<-
> presexS
                    PremaritalSex:ExtramaritalSex
Gender: Marital Status Yes: Yes: No No: Yes No: No
      Women:Divorced
                                  54
                                         36
                                              214
      Women:Married
                                          4
                                               322
      Men:Divorced
                           28
                                  60
                                         17
                                                68
      Men:Married
```

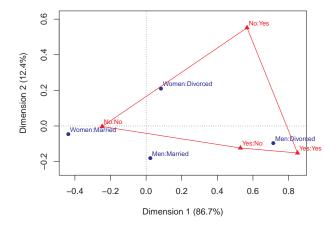
- (a) What loglinear model is analyzed by this approach? Which associations are included and which are excluded in this analysis?
 - ★ The model is that of independence between the combinations of the row variables and the column variables, i.e., [Pre Extra][Gender Marital]. The associations that remain indicate how the combinations of pre- and extra-marital sex are related to the the combinations of gender and marital status. The

- association between pre-marital sex and extra-marital sex is excluded, as is the association between gender and marital status.
- (b) Plot the 2D CA solution for this analysis. You might want to draw lines connecting some of the row points or column points to aid in interpretation.
 - ★ The 2D solution accounts for 99.1% of association between these sets of variables.

```
> presexS.ca <- ca(presexS)</pre>
> summary (presexS.ca)
Principal inertias (eigenvalues):
 dim
         value
                      오
                           cum%
                                   scree plot
                    86.7 86.7
         0.153126
         0.021929
                     12.4
                            99.1
                                    * * *
                     0.9 100.0
         0.001552
 Total: 0.176606 100.0
Rows:
    name
             mass
                    qlt
995
                          inr
                                  k=1 cor ctr
                                                    k=2 cor ctr
1
              310
                                   84
                                       138
                                             14
                                                    210 857 622
    WmnD
2
              343
                    995
                          376
                                  -437 984 427
                                                              34
    WmnM
                                                    -46 11
                    996
                                                    -97
    MnDv
              167
                          494
                                  715
                                       978
                                           558
4
                    878
                           39
    MnMr
              181
Columns:
                                                    k=2 cor ctr
-152 30 61
-124 51 122
552 486 817
             mass
58
                    qlt
979
                         inr
250
                                        cor ctr
948 274
    name
                                  850
    YsYs
              175
                                        937 320
2
                    989
                          296
                                  530
    YesN
3
                                  567
               59 1000
                          209
                                        514 124
    NoYs
              708 1000
                                 -247 1000 283
    NoNo
                          245
```

Here is one version of a plot, drawing lines connecting the pairs of Gender and Marital status.

```
> res <- plot(presexS.ca)
> # join pairs of column points
> lines(res$cols[1:2,], col="red")
> lines(res$cols[3:4,], col="red")
> lines(res$cols[c(1,3),], col="red")
> lines(res$cols[c(2,4),], col="red")
```



- (c) How does this analysis differ from the MCA analysis shown in Figure 6.10?
 - ★ The MCA analysis treats all four factors individually, analyzing all bivariate associations. The stacked approach here treats them in two sets, analyzing only the associations *between* sets.

Exercise 6.11 Refer to Exercise 5.10 for a description of the Vietnam data set in vcdExtra.

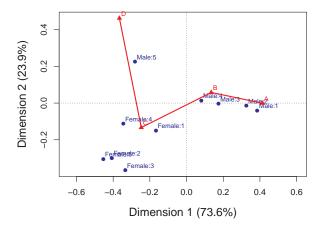
(a) Using the stacking approach, carry out a correspondence analysis corresponding to the loglinear model [R][YS], which asserts that the response is independent of the combinations of year and sex.

 \bigstar Two dimensions account for 97.5% of the association between response and the combinations of year and sex.

```
> data(Vietnam, package="vcdExtra")
> vietnam.tab <- xtabs (Freq ~ sex + year + response, data=Vietnam)
> vietnam.stacked <- as.matrix(structable(response ~ sex + year, vietnam.tab), sep=":")
> vietnam.ca <- ca(vietnam.stacked)</pre>
> summary(vietnam.ca, rows=FALSE, columns=FALSE)
Principal inertias (eigenvalues):
                   응
 dim
        value
                        cum%
                               scree plot
        0.085680 73.6 73.6
0.027881 23.9 97.5
 1
                               **********
                   2.5 100.0
        0.002854
Total: 0.116415 100.0
```

(b) Construct an informative 2D plot of the solution, and interpret in terms of how the response varies with year for males and females.

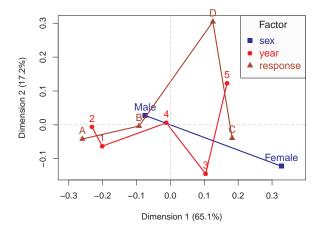
```
> plot(vietnam.ca, cex.lab=1.3, lines=c(FALSE, TRUE), lwd=2)
```



Dimension 1 corresponds to the ordering of the response categories, from the "dove" response D ("Withdraw military forces immediately") to the "hawk" response A ("Defeat North Vietnam by widespread bombing ..."). Males are ordered progressively from hawk to dove by their years in schools, with a big gap between year 4 and 5 (graduate students). Females cluster around response C ("De-escalate military activity ...") with no obvious trend over year in school.

- (c) Use mjca() to carry out an MCA on the three-way table. Make a useful plot of the solution and interpret in terms of the relationship of the response to year and sex.
 - ★ The MCA solution only accounts for 82.3% of the bivariate associations in 2D, and not much better in 3D.

```
> vietnam.mca <- mjca(vietnam.tab)</pre>
> summary (vietnam.mca, rows=FALSE, columns=FALSE)
Principal inertias (eigenvalues):
                   용
 dim
        value
                       cum%
                              scree plot
        0.028219 65.1
 1
                       65.1
                              *******
        0.007445
                  17.2
                       82.3
                              ****
        0.000380
                   0.9
                        83.2
 4
        1e-06000
                   0.0
                        83.2
 Total: 0.043317
> mcaplot(vietnam.mca, legend=TRUE)
```



The plot of the MCA solution is somewhat difficult to interpret, because neither the response categories nor year are ordered as one would expect. This turns out to be an example where MCA is not that useful, because the association of response and year is different for males and females— i.e., there is a three-way association in this table. MCA, however, only accounts for pairwise associations among the table variables.

Exercise 6.12 Refer to Exercise 5.9 for a description of the *Accident* data set in vcdExtra. The data set is in the form of a frequency data frame, so first convert to table form.

```
> accident.tab <- xtabs(Freq ~ age + result + mode + gender, data=Accident)
```

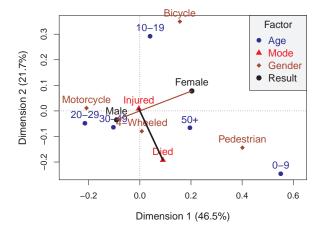
(a) Use mjca() to carry out an MCA on the four-way table accident.tab.

```
> accident.mca <- mjca(accident.tab)</pre>
> summary(accident.mca)
Principal inertias (eigenvalues):
        value
                                scree plot
        0.025429
                  46.5
                        46.5
        0.011848
                  21.7
                         68.1
        0.001889
                         71.6
                    0.9
        0.000491
                         72.5
 Total: 0.054700
Columns:
                                            k=1 cor ctr
                                                            k=2 cor ctr
                               qlt
672
                                    inr
                        mass
                name
             age:0-9
                                    107
                                            551 561 152
                                                           -246 111
                                                                     65
                         13
2
           age:10-19
                          49
                               678
                                     91
                                                            292 665 354
                                             40
                                                 1.3
                                           -215 747 102
           age:20-29
                               784
                                     8.5
                          56
                                                            -48
                                                                      11
4
           age:30-49
                          76
                               546
                                     75
                                           -103396
                                                      32
                                                            -63 149
                                                                      26
5
             age:50+
                                                            -67
                          56
                               687
                                     8.5
                                           196 616
                                                      84
                                                                 72.
                               515
515
                                                           -192 422
6
         result:Died
                          11
                                             90 92
                                                                      34
                                                 92
      result:Injured
                                             -4
                                                                422
                                     73
                                                            -80 228
8
      mode: 4-Wheeled |
                          81
                               230
                                              8
                                                      0
                                                                      43
                                            156 127
        mode:Bicycle
                          31
                               762
                                     98
                                                            349 635
10
     mode: Motorcycle
                          99
                               686
                                     70
                                           -209 684 170
                                                             11
11
     mode:Pedestrian
                           38
                               677
                                    100
                                            401 600
                                                    241
                                                           -144
12
       gender:Female
                               788
                                     77
                                            203 686 126
                                                             78 101
                               788
                                            -91 686
                                                            -35 101
```

The adjusted inertias indicate that a 2D solution accounts for only 68.1% of the pairwise associations. The qualities (qlt) of the factor levels indicate that the categories are only moderately well-represented in a 2D plot.

(b) Construct an informative 2D plot of the solution, and interpret in terms of how the variable result varies in relation to the other factors.

```
*
```



In the figure above, one interpretation of the dimensions is in terms of the age categories: Dimension 1 for young adults vs. old and young, Dimension 2 for teenage vs. the rest. In these terms, Dimension 1 shows associations among males, aged 20–49, riding a motorcycle or 4-wheeled vehicle and more likely to be injured, vs. females, either old or very young, as pedestrians and more likely to have died. Dimension 2 contrasts bicycle accidents involving youth aged 10–19 who are more likely to be just injured against the other categories.

Exercise 6.13 The *UCBAdmissions* data was featured in numerous examples in Chapter 4 (e.g., Example 4.11, Example 4.15) and Chapter 5 (e.g., Example 5.14, Example 5.18).

(a) Use mjca() to carry out an MCA on the three-way table UCBAdmissions.

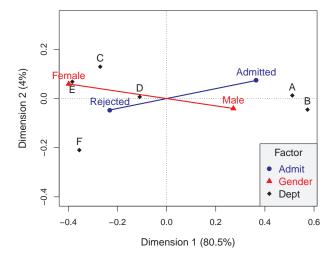


```
> ucb.mca <- mjca (UCBAdmissions)
> summary(ucb.mca)
Principal inertias (eigenvalues):
        value
                                scree plot
        0.114945
                   80.5
                        80.5
        0.005694
                   4.0
                         84.5
                   0.0
                         84.5
                         84.5
                    0.0
                         84.5
 Total: 0.142840
Columns:
                             qlt
911
                                          k=1 cor ctr
                                                           k=2 cor ctr
                       mass
                                   inr
                                                               36 123 |
36 78 |
                                          365 875 150
                                                           74
     Admit:Admitted
                        129
                                    93 |
                             911
                                    59
                        204
                                         -231 875
                                                   95
                                                           -47
     Admit:Rejected
                                    95 i
                        135
                             863
                                         -399 845 187
                                                           59
      Gender:Female |
                                                               19
                                                                   8.4
                        198
                                    6.5
                                          272 845 127
        Gender:Male
                             863
```

```
5
6
7
                                 838
                                       117
                                               512 837 156
               Dept:A
                                 829
                                       124
                                               573
                                                                 -45
                                                                           15
                            43
                                                    824 123
               Dept:B
                                                                 130 137
                                                                          199
               Dept:C
                                 731
                                       108
                                              -270
                                                    594
                                                         43
                            68
8 9
                                 832
                                       106
117
                                             -110 828
-384 787
                                                         6
55
               Dept:D
                            58
                                                                        3
                                                                            0
                                                                  69
                                                                      25
                                                                           35
                            43
               Dept:E
                                 812
                                                               -210 190 406
10
               Dept:F
                                 737
                                       116 |
                                             -355 547
```

(b) Plot the 2D MCA solution in a style similar to that shown in Figure 6.10 and Figure 6.11.

> **par** (op)



- (c) Interpret the plot. Is there some interpretation for the first dimension? What does the plot show about the relation of admission to the other factors?
 - ★ The first dimension largely corresponds to Admission, showing the overall association of Males more likely to be admitted, Females more likely to be rejected. Note that the departments, labeled A–F, were actually ordered by overall rate of admission, but this ordering does not appear along Dimension 1 in the plot.

Chapter 7 Logistic Regression Models

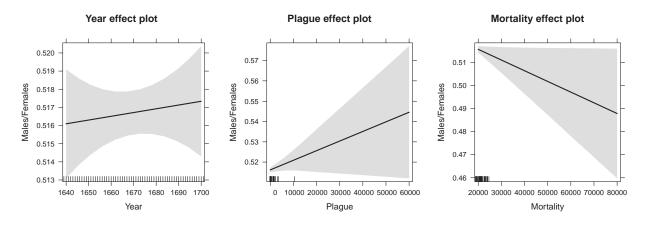
Exercise 7.1 Arbuthnot's data on the sex ratio of births in London was examined in Example 3.1. Use a binomial logistic regression model to assess whether the proportion of male births varied with the variables Year, Plague, and Mortality in the Arbuthnot data set. Produce effect plots for the terms in this model. What do you conclude?

★ For the binomial logistic model, use cbind (Males, Females) for the response variable in the model.

```
> data(Arbuthnot, package="HistData")
> arbuth.mod <- glm(cbind(Males, Females) ~ Year + Plague + Mortality,
                    data=Arbuthnot, family=binomial)
> summary (arbuth.mod)
Call:
glm(formula = cbind(Males, Females) ~ Year + Plague + Mortality,
    family = binomial, data = Arbuthnot)
Deviance Residuals:
  Min
            1Q Median
                                   Max
       -0.996
                -0.005
                         0.850
Coefficients:
             Estimate Std. Error z value Pr(>|z|)
(Intercept)
           -4.07e-02
                        3.09e-01
                                    -0.13
             8.28e-05
                        1.93e-04
                                    0.43
                                             0.668
Year
Plague
             1.91e-06
                        1.13e-06
                                    1.68
                                             0.093
                        9.26e-07
                                             0.045 *
Mortality
            -1.86e-06
                                    -2.01
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
(Dispersion parameter for binomial family taken to be 1)
    Null deviance: 169.74 on 81 degrees of freedom
Residual deviance: 156.31 on 78 degrees of freedom
AIC: 963.8
Number of Fisher Scoring iterations: 3
> LRstats (arbuth.mod)
Likelihood summary table:
           AIC BIC LR Chisq Df Pr(>Chisq)
arbuth.mod 964 973
                        156 78
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

The effects of Year and Plague are small and non-significant. The Male/Female proportion appears to decrease with increasing Mortality.

```
> library(effects)
> arbuth.eff <- allEffects(arbuth.mod)
> plot(arbuth.eff, ylab="Males/Females", rows=1, cols=3)
```



In the plots for Plague and Mortality, it is apparent that both are extremely skewed. One alternative is to represent these as log(Plague+1) and log(Mortality) in the model. Overall, these effects are quite small, but the main effects model arbuth.mod is better than the null model.

Exercise 7.2 For the Donner Party data in *Donner*, examine Grayson's 1990 claim that survival in the Donner Party was also mediated by the size of the family unit. This takes some care, because the family variable in the *Donner* data is a simplified grouping based on the person's name and known alliances among families from the historical record. Use the following code to compute a family.size variable from each individual's last name:

```
> data("Donner", package="vcdExtra")
> Donner$survived <-factor(Donner$survived, labels=c("no", "yes"))
> # use last name for family
> lname <-strsplit(rownames(Donner), ",")
> lname <-sapply(lname, function(x) x[[1]])
> Donner$family.size <-as.vector(table(lname)[lname])</pre>
```

(a) Choose one of the models (donner.mod4, donner.mod6) from Example 7.9 that include the interaction of age and sex and nonlinear terms in age. Fit a new model that adds a main effect of family.size. What do you conclude about Grayson's claim?

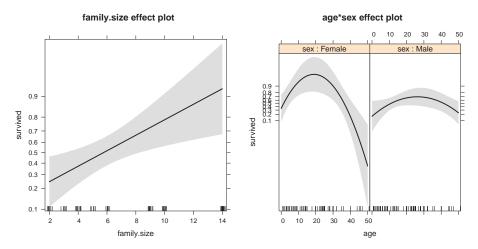
*

Family size seems to have an effect on survival.

(b) Produce an effect plot for this model.

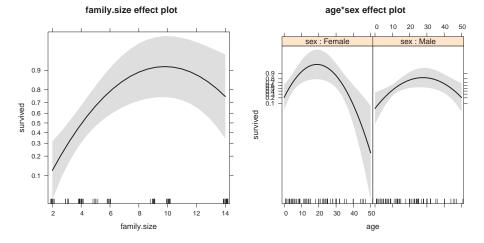
 \star

```
> library(effects)
> donner.eff4a <- allEffects(donner.mod4a, xlevels=list(age=seq(0,50,5)))
> plot(donner.eff4a, ticks=list(n=8))
```



(c) Continue, by examining whether the effect of family size can be taken as linear, or whether a nonlinear term should be added.

```
> Anova (donner.mod4b)
Analysis of Deviance Table (Type II tests)
Response: survived
                  LR Chisq Df Pr(>Chisq)
                    17.64
                               0.00015
poly(age, 2)
                     2.33
                              0.12688
poly(family.size, 2)
                    24.81
                               4.1e-06 ***
poly(age, 2):sex
                    12.25
                               0.00219 **
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
> donner.eff4b <- allEffects(donner.mod4b, xlevels=list(age=seq(0,50,5)))
> plot(donner.eff4b, ticks=list(n=8))
```



Exercise 7.3 Use component+residual plots (Section 7.5.3) to examine the additive model for the ICU data given by

(a) What do you conclude about the linearity of the (partial) relationship between age and death in this model?

 \star

(b) An alternative strategy is to allow some nonlinear relation for age in the model using a quadratic (or cubic) term like poly(age, 2) (or poly(age, 3)) in the model formula. Do these models provide evidence for a nonlinear effect of age on death in the ICU?

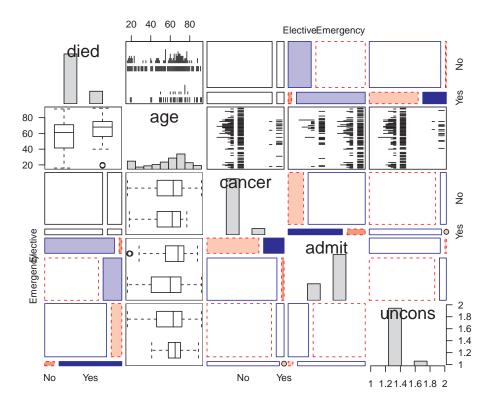


Exercise 7.4 Explore the use of other marginal and conditional plots to display the relationships among the variables predicting death in the ICU in the model icu.glm2. For example, you might begin with a marginal gpairs () plot showing all bivariate marginal relations, something like this:

```
> library(gpairs)
> gpairs(ICU[,c("died", "age", "cancer", "admit", "uncons")],
+ diag.pars=list(fontsize=16, hist.color="lightgray"),
+ mosaic.pars=list(gp=shading_Friendly,
+ gp_args=list(interpolate=1:4)))
```

★ First, begin with the gpairs () plot:

```
> library(gpairs)
> gpairs(ICU[,c("died", "age", "cancer", "admit", "uncons")],
+ diag.pars=list(fontsize=16, hist.color="lightgray"),
+ mosaic.pars=list(gp=shading_Friendly,
+ gp_args=list(interpolate=1:4)))
```



Exercise 7.5 The data set Caesar in VCdExtra gives a 3×2^3 frequency table classifying 251 women who gave birth by Caesarian section by Infection (three levels: none, Type 1, Type2) and Risk, whether Antibiotics were used, and whether the Caesarian section was Planned or not. Infection is a natural response variable. In this exercise, consider only the binary outcome of infection vs. no infection.

```
> data("Caesar", package="vcdExtra")
> Caesar.df <- as.data.frame(Caesar)
> Caesar.df$Infect <- as.numeric(Caesar.df$Infection %in%
+ c("Type 1", "Type 2"))</pre>
```

(a) Fit the main-effects logit model for the binary response Infect. Note that with the data in the form of a frequency data frame you will need to use weights=Freq in the call to glm(). (It might also be convenient to reorder the levels of the factors so that "No" is the baseline level for each.)

*

- (b) Use summary () or car (Fox and Weisberg, 2015)::Anova () to test the terms in this model.
 - ★ By both the Wald tests from summary() and the Type II LR tests from car::Anova all three factors have significant effects on the probability of infection.

```
> library(car)
> summary(caesar.glm)
Deviance Residuals:
          1Q Median
                            3Q
  Min
-6.747 -0.44\overline{3} 0.000 3.23\overline{4} 5.420
Coefficients:
               Estimate Std. Error z value Pr(>|z|)
(Intercept) -0.793 0.478 -1.66 0.097.
RiskYes 1.827 0.436 4.19 2.8e-05 ***
AntibioticsYes -3.001 0.459 -6.53 6.4e-11 ***
PlannedYes -0.906 0.408 -2.22 0.026 *
RiskYes
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
(Dispersion parameter for binomial family taken to be 1)
Null deviance: 300.85 on 16 degrees of freedom Residual deviance: 236.36 on 13 degrees of freedom
AIC: 244.4
Number of Fisher Scoring iterations: 6
> Anova (caesar.glm)
Analysis of Deviance Table (Type II tests)
Response: Infect
     LR Chisq Df Pr(>Chisq)
             20.6 1 5.8e-06 ***
56.5 1 5.7e-14 ***
5.2 1 0.022 *
Antibiotics
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
```

- (c) Interpret the coefficients in the fitted model in terms of their effect on the odds of infection.
 - ★ From the coefficients in the model given above, Risk factors increase the log odds of infection by 1.83; treatment with Antibiotics decreases the log odds by 3.0; a planned C-section descreases the log odds of infection by 0.91.

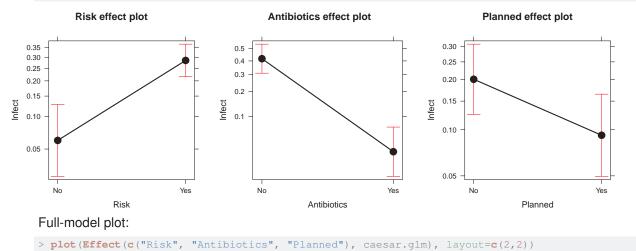
These effects can perhaps be more easily interpreted in terms of the odds ratios calculated below, that give the multiple of the odds for the Yes group compared to the No group. For example, Risk can be said to multiply the odds by 6.22; Antibiotics multiplies the odds by 0.05, or a decrease of 95%; a planned C-section multiplies the odds of infection by 0.40, a decrease of 60%.

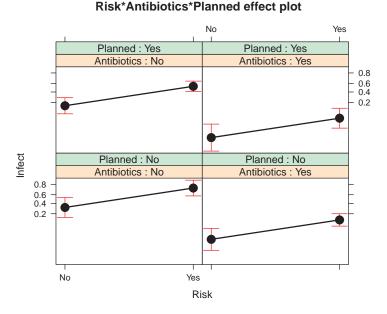
```
> exp(cbind(OddsRatio=coef(caesar.glm),
+ confint(caesar.glm)))

OddsRatio 2.5 % 97.5 %
(Intercept) 0.452263 0.170362 1.13401
RiskYes 6.215158 2.736586 15.35990
AntibioticsYes 0.049734 0.019257 0.11742
PlannedYes 0.403978 0.176257 0.88092
```

- (d) Make one or more effects plots for this model, showing separate terms, or their combinations.
 - ★ Two kinds of effect plots are useful here: alleffects(), that gives plots for each of the (main effect) terms in the model, and a full-model plot, showing predicted log odds of infection for all combinations of Risk, Antibiotics and Planned.

```
> library(effects)
> plot(allEffects(caesar.glm), rows=1, cols=3)
```

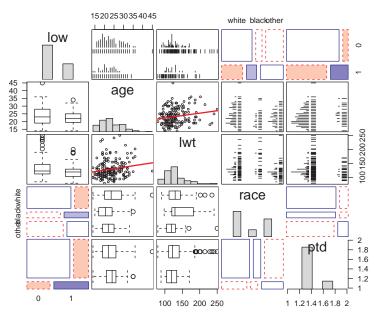




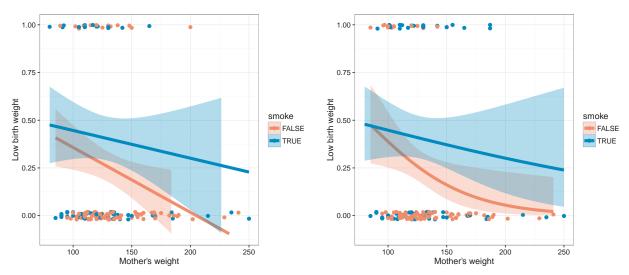
Exercise 7.6 The data set birthwt in the MASS package gives data on 189 babies born at Baystate Medical Center, Springfield, MA during 1986. The quantitative response is bwt (birth weight in grams), and this is also recorded as low, a binary variable corresponding to bwt < 2500 (2.5 Kg). The goal is to study how this varies with the available predictor variables. The variables are all recorded as numeric, so in R it may be helpful to convert some of these into factors and possibly collapse some low frequency categories. The code below is just an example of how you might do this for some variables.

```
> data("birthwt", package="MASS")
> birthwt <- within(birthwt, {
    low <- factor(low)
+    race <- factor(race, labels = c("white", "black", "other"))
+    ptd <- factor(ptl > 0)  # premature labors
+    ftv <- factor(ftv)  # physician visits
+    levels(ftv)[-(1:2)] <- "2+"
+    smoke <- factor(smoke>0)
+    ht <- factor(ht>0)
+    ui <- factor(ui>0)
+    })
```

- (a) Make some exploratory plots showing how low birth weight varies with each of the available predictors. In some cases, it will probably be helpful to add some sort of smoothed summary curves or lines.
 - ★ There are a wide variety of plots one could make for this data set. It is not unreasonable to start with a <code>gpairs()</code> plot for an overview. The first row and column shows the relations of low birth weight to the predictors. From this we can see that low birth weight (<code>low==1</code>) is associated with lower age, lower mother's weight (<code>lwt</code>), <code>race=="black"</code>, and previous premature labors (<code>ptd</code>).



Other plots can explore particular relationships with low birth weight more thoroughly. Here we just show some example plots using ggplot2 (Wickham and Chang, 2015) for the relationship between low and mother's weight (lwt) conditioned by smoking status.



- (b) Fit several logistic regression models predicting low birth weight from these predictors, with the goal of explaining this phenomenon adequately, yet simply.
 - ★ Here, we just start with the main effects model, then eliminate non-significant terms. A more general analysis could use MASS::stepAIC(), test for non-linear relations, and the presence of interaction effects.

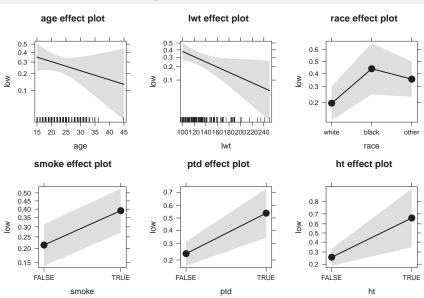
```
> # quick check on important effects
> bwt.mod0 <- glm(low ~ age + lwt + race + smoke + ptd + ht + ui + ftv,</pre>
                     data=birthwt, family = binomial)
> summary(bwt.mod0)
glm(formula = low ~ age + lwt + race + smoke + ptd + ht + ui +
ftv, family = binomial, data = birthwt)
Deviance Residuals:
         1Q Median
-0.807 -0.501
                                 3Q
   Min
                                         Max
                             0.884
-1.704
                                       2.215
Coefficients:
              Estimate Std. Error z value Pr(>|z|)
                            1.24471
0.03870
0.00708
(Intercept) 0.82302
                                                0.5085
                                        0.66
              -0.03723
                                         -0.96
age
                                                  0.3360
              -0.01565
                                        -2.21
7 w/t
                                                  0.0271
               1.19241
0.74068
                            0.53596
                                         2.22
raceblack
                                                  0.0261 *
                            0.46174
raceother
                                          1.60
                                                  0.1087
               0.75553
smokeTRUE
                             0.42502
                                          1.78
                                                  0.0755
ptdTRUE
               1.34376
                             0.48062
                                          2.80
                                                  0.0052 **
htTRUE
               1.91317
                             0.72074
                                          2.65
                                                  0.0079 **
uiTRUE
               0.68020
                             0.46434
                                          1.46
                                                  0.1430
ftv1
              -0.43638
                             0.47939
                                         -0.91
                                                  0.3627
               0.17901
                             0.45638
                                          0.39
                                                  0.6949
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
(Dispersion parameter for binomial family taken to be 1)
Null deviance: 234.67 on 188 degrees of freedom Residual deviance: 195.48 on 178 degrees of freedom
AIC: 217.5
Number of Fisher Scoring iterations: 4
> car::Anova(bwt.mod0)
Analysis of Deviance Table (Type II tests)
Response: low
       LR Chisq Df Pr(>Chisq)
                          0.3318
age
            0.94
            5.47
5.75
                          0.0193 *
1 wt.
                          0.0564 .
race
                          0.0737 .
smoke
            3.20
            8.11
                          0.0044 **
ptd
ht
            7.46
                          0.0063 **
```

```
2.11 1
ui
                    0.1463
          1.36
                2
                       0.5071
ftv
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
> # remove NS terms
> bwt.mod1 <- update(bwt.mod0, . ~ . - ui - ftv)</pre>
> Anova (bwt.mod1)
Analysis of Deviance Table (Type II tests)
Response: low
      LR Chisq Df Pr(>Chisq)
          1.33
                       0.2487
age
lwt
          5.40
                       0.0201
          6.24
                       0.0441 *
race
smoke
          4.62
                       0.0316
          8.73
                       0.0031 **
ptd
          6.46
                       0.0111 *
ht
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
> anova(bwt.mod1, bwt.mod0, test="Chisq")
Analysis of Deviance Table
Model 1: low ~ age + lwt + race + smoke + ptd + ht
Model 2: low ~ age + lwt + race + smoke + ptd + ht + ui + ftv
 Resid. Df Resid. Dev Df Deviance Pr(>Chi)
        181
                    199
                    196
```

(c) Use some graphical displays to convey your findings.

*

> plot(allEffects(bwt.mod1), ci.style="bands")



Exercise 7.7 Refer to Exercise 5.9 for a description of the Accident data. The interest here is to model the probability that an accident resulted in death rather than injury from the predictors age, mode, and gender. With glm(), and the data in the form of a frequency table, you can use the argument weight=Freq to take cell frequency into account.

- (a) Fit the main effects model, result == "Died" ~ age + mode + gender. Use car::Anova() to assess the model terms.
 - * For analysis using glm() it is useful to consider the ordering of factors for the interpretation of coefficients, contrasts and plots. In the Accident data, mode is an unordered factor, but it is probably more useful to reorder the levels to make Pedestrian the reference level.

- (b) Fit the model that allows all two-way interactions. Use anova() to test whether this model is significantly better than the main effects model.
 ★ In the all two-way model, all terms are significant and the addition of these terms is a significant
 - ★ In the all two-way model, all terms are significant and the addition of these terms is a significant improvement over the main effects model.

```
> acc.mod2 <- update(acc.mod1, . ~ .^2)</pre>
> Anova (acc.mod2)
Analysis of Deviance Table (Type II tests)
Response: result == "Died"
             LR Chisq Df Pr(>Chisq)
                 1101 4
136 3
419 1
                             < 2e-16 ***
age
                              < 2e-16 ***
mode
gender
                             < 2e-16 ***
age:mode
                  122 12
                             < 2e-16 ***
age:gender
                             1.6e-09 ***
                   47
                       4
mode:gender
                   22 3
                             6.7e-05 ***
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
> anova(acc.mod1, acc.mod2, test="Chisq")
Analysis of Deviance Table
Model 1: result == "Died" ~ age + mode + gender
Model 2: result == "Died" ~ age + mode + gender + age:mode + age:gender +
   mode:gender
  Resid. Df Resid. Dev Df Deviance Pr(>Chi)
          71
                   64599
2
          52
                   64384 19
                                  214 <2e-16 ***
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

- (c) Fit the model that also allows the three-way interaction of all factors. Does this offer any improvement over the two-way model?
 - ★ In the three-way model, the term age:mode:gender is not significant, and anova() shows that it does not improve the two-way model. Using LRstats(), the two-way model has the best AIC and BIC.

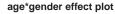
```
> acc.mod3 <- update(acc.mod1, . ~ .^3)</pre>
> Anova (acc.mod3)
Analysis of Deviance Table (Type II tests)
Response: result == "Died"
                LR Chisq Df Pr(>Chisq)
                    1101 4
                             < 2e-16 ***
mode
                     136
                                < 2e-16 ***
                     419 1
gender
                                < 2e-16 ***
age:mode
                     122 12
                                < 2e-16 ***
age:gender
                      47 4
22 3
                               1.6e-09 ***
                      22
mode:gender
                                6.7e-05 ***
age:mode:gender
                      13 12
                                  0.37
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
> anova(acc.mod1, acc.mod2, acc.mod3, test="Chisq")
Analysis of Deviance Table
Model 1: result == "Died" ~ age + mode + gender
Model 2: result == "Died" ~ age + mode + gender + age:mode + age:gender +
```

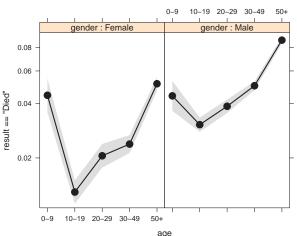
```
mode:gender
Model 3: result == "Died" ~ age + mode + gender + age:mode + age:gender +
   mode:gender + age:mode:gender
 Resid. Df Resid. Dev Df Deviance Pr(>Chi)
                64599
2
                 64384 19
                               214
                                     <2e-16 ***
                 64371 12
         40
                                1.3
                                       0.37
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
> LRstats(acc.mod1, acc.mod2, acc.mod3)
Likelihood summary table:
           AIC BIC LR Chisq Df Pr(>Chisq)
acc.mod1 64617 64638
                        64599 71
                                     <2e-16 ***
acc.mod2 64440 64507
                        64384 52
                                     <2e-16 ***
acc.mod3 64451 64547
                        64371 40
                                     <2e-16 ***
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

(d) Interpret the results of the analysis using effect plots for the two-way model, separately for each of the model terms. Describe verbally the nature of the age*gender effect. Which mode of transportation leads to greatest risk of death?

risk of death?
★ Controlling for mode, males and females have similar profiles, with the lowest probability of death in the 10–19 group, and highest in the 50+ age group.

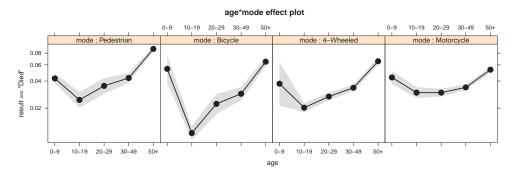
```
> plot(Effect(c("age", "gender"), acc.mod2), ci.style="bands")
```





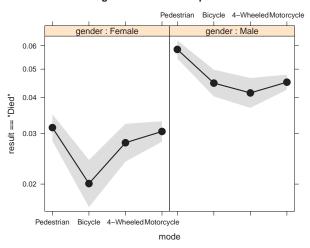
There are roughly similar profiles across age, with bicycle accidents showing the greatest differences among age groups.

> plot(Effect(c("age", "mode"), acc.mod2), ci.style="bands", layout=c(4,1))



```
> plot(Effect(c("gender", "mode"), acc.mod2), ci.style="bands")
```

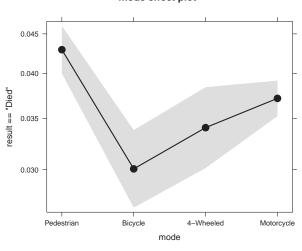
gender*mode effect plot



Overall, accidents involving motorcycles have the greatest probability of death, controlling for all other factors.

> plot(Effect("mode", acc.mod2), ci.style="bands")

mode effect plot



Chapter 8 Models for Polytomous Responses

Exercise 8.1 For the women's labor force participation data (Womenlf), the response variable, partic, can be treated as ordinal by using

```
> Womenlf$partic <- ordered(Womenlf$partic,
+ levels=c('not.work', 'parttime', 'fulltime'))</pre>
```

Use the methods in Section 8.1 to test whether the proportional odds model holds for these data.

★ We start fitting the proportional odds model using polr():

to see that region has no significant effect on the comparison of the different response categories; we will ignore it in the further analysis. Now, we try comparing the proportional and non-proportional odds models by refitting them using vglm():

The warnings indicate that the non-proportional odds model does not converge, leaving the object returned by vglm() without log-likelihood, and making impossible the comparison using lrtest():

```
> logLik(Wlf.npo)
[1] NaN
> VGAM::lrtest(Wlf.po, Wlf.npo)
Likelihood ratio test

Model 1: partic ~ hincome + children
Model 2: partic ~ hincome + children
#Df LogLik Df Chisq Pr(>Chisq)
1 522 -221
2 520 -2
```

It is, however, possible to fit a partial proportional odds model, relaxing the assumption for hincome:

```
> Wlf.ppo <- vglm(partic ~ hincome + children, data = Womenlf,
+ family = cumulative(parallel = FALSE ~ hincome))</pre>
```

The comparison with lrtest() now yields:

```
> VGAM::lrtest(Wlf.po, Wlf.ppo)
```

```
Likelihood ratio test

Model 1: partic ~ hincome + children

Model 2: partic ~ hincome + children

#Df LogLik Df Chisq Pr(>Chisq)

1 522 -221

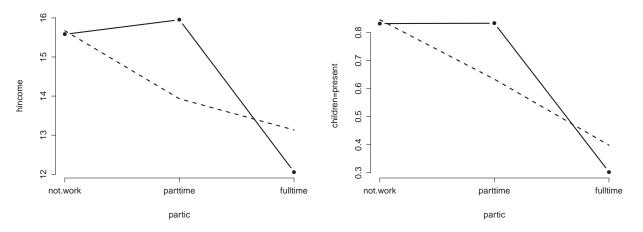
2 521 -219 -1 4.14 0.042 *

---

Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

showing that the partial proportional odds model is preferable to the proportional odds model. The graphical assessment using the method described in Section 8.1.4 provides further insights:

```
> library (rms)
> Wlf.po2 <- lrm (partic ~ hincome + children, data = Womenlf) > Wlf.po2
Logistic Regression Model
lrm(formula = partic ~ hincome + children, data = Womenlf)
                       Model Likelihood
                                             Discrimination
                                                                Rank Discrim.
                          Ratio Test
                                                  Indexes
                                                                   Indexes
                                                      0.236
                      LR chi2
not.work
               155
                      d.f.
                                             g
                                                       1.083
                                                                Dxy
                                                                         0.446
parttime
               42
                      Pr(> chi2) <0.0001
                                                       2.954
                                                                         0.461
                                                                gamma
                                             qr
                                                       0.236
 fulltime
               66
                                                                         0.253
                                                                tau-a
                                             qp
max |deriv| 4e-08
                                                       0.209
                                             Brier
                  Coef
                          S.E.
                                 Wald Z Pr(>|Z|)
                                  4.79
                   1.8520 0.3863
v>=parttime
                                         < 0.0001
                   0.9409 0.3699
                                  2.54
                                         0.0110
v>=fulltime
hincome
                  -0.0539 0.0195 -2.77
                                         0.0057
children=present -1.9720 0.2869 -6.87
                                         <0.0001
> plot.xmean.ordinaly(partic ~ hincome + children, data = Womenlf,
                       lwd=2, pch=16, subn=FALSE)
```



The mean values for hincome do indeed not follow the fitted ones under the proportional odds model. Also, the first two categories, not.work and parttime, are not well distinguished.

Exercise 8.2 The data set *housing* in the MASS package gives a $3 \times 3 \times 4 \times 2$ table in frequency form relating (a) satisfaction (Sat) of residents with their housing (High, Medium, Low), (b) perceived degree of influence (Infl) they have on the management of the property (High, Medium, Low), (c) Type of rental (Tower, Atrium, Apartment, Terrace), and (d) contact (Cont) residents have with other residents (Low, High). Consider satisfaction as the ordinal response variable.

(a) Fit the proportional odds model with additive (main) effects of housing type, influence in management, and contact with neighbors to this data. (Hint: Using polr(), with the data in frequency form, you need to use the weights argument to supply the Freq variable.)

★ All three factors have significant effects on satisfaction in this simple model.

```
> data("housing", package="MASS")
> str(housing)

'data.frame': 72 obs. of 5 variables:
    $ Sat : Ord.factor w/ 3 levels "Low"<"Medium"<...: 1 2 3 1 2 3 1 2 3 1 ...
    $ Infl: Factor w/ 3 levels "Low", "Medium",..: 1 1 1 2 2 2 3 3 3 1 ...
    $ Type: Factor w/ 4 levels "Tower", "Apartment",..: 1 1 1 1 1 1 1 1 1 2 ...
    $ Cont: Factor w/ 2 levels "Low", "High": 1 1 1 1 1 1 1 1 1 1 1 1 1 ...
    $ Freq: int 21 21 28 34 22 36 10 11 36 61 ...

> # proportional odds model
> library(MASS)
> PO.mod <- polr(Sat ~ Infl + Type + Cont, data=housing, weights=Freq)
> car::Anova(PO.mod)

Analysis of Deviance Table (Type II tests)

Response: Sat
    LR Chisq Df Pr(>Chisq)
Infl 108.2 2 < 2e-16 ***
Type 55.9 3 4.4e-12 ***
Cont 14.3 1 0.00016 ***

---
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1</pre>
```

Although not asked in the question, it is important to assess whether the proportional odds assumption hold statistically (using VGAM), following the methods described in Section 8.1.3, or graphically (using rms (Harrell, Jr., 2015)), following Section 8.1.4. Here, we illustrate the statistical test using vglm().

(b) Investigate whether any of the two-factor interactions among Infl, Type, and Cont add substantially to goodness of fit of this model. (Hint: use stepAIC(), with the scope formula ~ .^2 and direction="forward".) ★ Forward selection from the main effects model adds the interactions of Infl:Type and Type:Cont. That is, the effect of type of dwelling on satisfaction varies both with influence and contact with other residents.

```
> house.step <- stepAIC (PO.mod, scope = ~.^2, direction = "forward")
Start: AIC=3495.2
Sat ~ Infl + Type + Cont
           Df AIC
+ Infl:Type 6 3485
+ Type:Cont 3 3492
               3495
+ Infl:Cont 2 3499
Step: AIC=3484.6
Sat ~ Infl + Type + Cont + Infl:Type
               ATC
+ Type:Cont 3 3483
              3485
<none>
+ Infl:Cont 2 3489
Step: AIC=3482.7
Sat ~ Infl + Type + Cont + Infl:Type + Type:Cont
           Df AIC
              3483
<none>
+ Infl:Cont 2 3487
```

The result of stepAIC() includes an anova summary of the steps.

```
> house.step$anova
Stepwise Model Path
Analysis of Deviance Table
Initial Model:
Sat ~ Infl + Type + Cont
Final Model:
Sat ~ Infl + Type + Cont + Infl:Type + Type:Cont
           Step Df Deviance Resid. Df Resid. Dev
                               1673 3479.1 3495.1
1667 3456.6 3484.6
2 + Infl:Type 6 22.509
3 + Type:Cont 3 7.945
                                                3456.6 3484.6
> Anova (house.step)
Analysis of Deviance Table (Type II tests)
Response: Sat
            LR Chisq Df Pr(>Chisq)
                106.5 2 < 2e-16 ***

55.9 3 4.4e-12 ***

15.1 1 0.0001 ***

21.8 6 0.0013 **

7.9 3 0.0472 *
Infl
               106.5
Type
Infl:Type
Type:Cont
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

The next step, refitting the model chosen by <code>stepAIC()</code> is not strictly necessary (because that model was saved as <code>house.step</code>), but using the argument <code>Hess=TRUE</code> saves computation for some of the plots below.

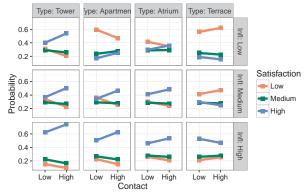
```
> PO.mod2 <- polr(formula = Sat ~ Infl + Type + Cont + Infl:Type + Type:Cont,
+ data = housing, Hess=TRUE, weights=Freq)
```

- (c) For your chosen model from the previous step, use the methods of Section 8.1.5 to plot the probabilities of the categories of satisfaction.
 - ★ A first step in plotting is to join the data with the predicted values.

Plotting predicted probabilities with ggplot2 is quite flexible, but requires that the data in fit.step be reshaped to long format.

Then, we can plot y = Probability against one factor as x, and use facet_grid() to show panels for the other factors as rows and columns. This gives what we call a "full-model plot."



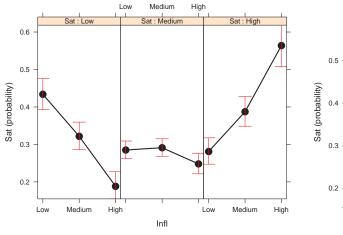


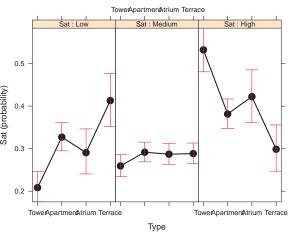
For ease of interpreting the model, effect plots give a more convenient visual summary. The model has 5 terms, and it is useful to plot them all; we only show selected terms here. Main effects of influence and type:

```
> plot(Effect("Infl", P0.mod2), main="Main Effect of Influence", layout=c(3,1))
> plot(Effect("Type", P0.mod2), main="Main Effect of Dwelling Type", layout=c(3,1))
```

Main Effect of Influence

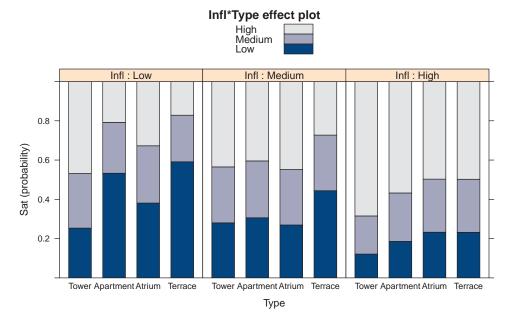
Main Effect of Dwelling Type





Interaction of influence and type:

```
> plot(Effect(c("Infl", "Type"), PO.mod2), style="stacked")
```



- (d) Write a brief summary of these analyses, interpreting *how* satisfaction with housing depends on the predictor variables.
 - ★ As Influence increases, high satisfaction also increases, low satisfaction decreases and medium satisfaction remains relatively constant. Dwelling type also has opposite effects on high and low satisfaction, with Tower dwellers being highest on high satisfaction and Terrace dwellers lowest. Again, medium satisfaction seems to be relatively static across dwelling type. High satisfaction also increases with high contact.

Exercise 8.3 The data TV on television viewing was analyzed using correspondence analysis in Example 6.4, ignoring the variable Time, and extended in Exercise 6.9. Treating Network as a three-level response variable, fit a generalized logit model (Section 8.3) to explain the variation in viewing in relation to Day and Time. The TV data is a three-way table, so you will need to convert it to a frequency data frame first.

```
> data("TV", package="vcdExtra")
> TV.df <- as.data.frame.table(TV)</pre>
```

(a) Fit the main-effects model, Network ~ Day + Time, with multinom(). Note that you will have to supply the weights argument because each row of TV.df represents the number of viewers in the Freq variable.

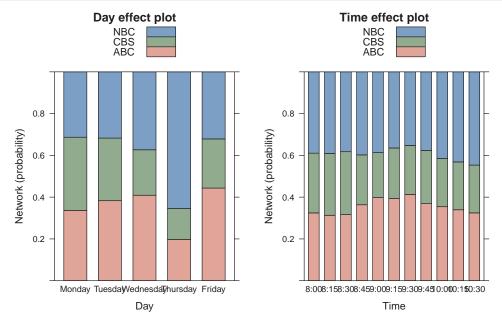
```
> library(nnet)
> tv.model = multinom(Network ~ Day + Time, data = TV.df,
                        weights = Freq, Hess = TRUE)
# weights: 48 (30 variable)
initial value 41318.808177
iter 10 value 38935.947713
iter 20 value 38818.222728
iter 30 value 38756.956301 final value 38752.186202
converged
> car::Anova(tv.model)
Analysis of Deviance Table (Type II tests)
Response: Network
     LR Chisq Df Pr(>Chisq)
                  <2e-16 ***
        3400 8
Time
          301 20
                       <2e-16 ***
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

Both Day and Time are clearly significant when comparing the Networks.

(b) Prepare an effects plot for the fitted probabilities in this model.

*

```
> library(effects)
> plot(allEffects(tv.model), style = "stacked")
```

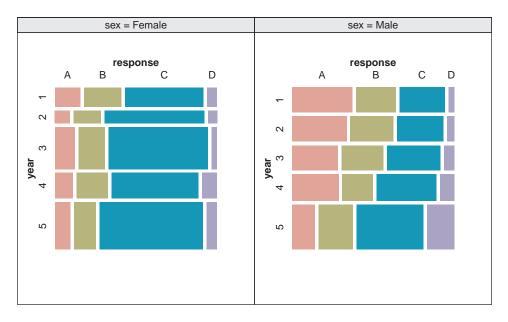


- (c) Interpret these results in comparison to the correspondence analysis in Example 6.4.
 - ★ The effect plots for Day clearly show a peak for NBC on Thursday, at the expense of the two other networks. ABC has most viewers on Tuesday and Wednesday, whereas CBS is the most popular Network on Monday. These results are consistent with the results from the correspondence analysis. Regarding time, ABC is most viewed from 8:45 to 9:30—after that, the viewing probability decreases in favor of NBC.

Exercise 8.4 * Refer to Exercise 5.10 for a description of the *Vietnam* data set in vcdExtra. The goal here is to fit models for the polytomous response variable in relation to year and sex.

- (a) Fit the proportional odds model to these data, allowing an interaction of year and sex.
 - ★ The Vietnam data is pretabulated; for a first explorative view, we transform it into tabular format, and use a conditional mosaicplot (with Marimekko shading) to get ideas on the structure.

```
> library(vcdExtra)
> data(Vietnam)
> Vtn_tab = xtabs(Freq ~ ., data = Vietnam)
> cotabplot( ~ year + response | sex, data = Vtn_tab,
+ gp = shading_Marimekko(Vtn_tab[1,,]))
```



Whereas male students have a clear tendency to choose the more peaceful options A and B with higher study year (the mosaic plot suggests a linear relationship of <code>year</code> and <code>response</code>), the situation is less clear for female students—there seems to be a general tendency for response B (negotiations), independent from the study year.

The proportional odds model is fitted using polr(). Before, we make sure that the response is indeed treated as ordinal:

```
> library(MASS)
> Vietnam$response = ordered(Vietnam$response)
> Vtn_polr = polr(response ~ year * sex, data = Vietnam,
+ weights = Freq, Hess = TRUE)
> summary(Vtn_polr)
Call:
polr(formula = response ~ year * sex, data = Vietnam, weights = Freq,
    Hess = TRUE)
Coefficients:
               Value Std. Error t value
                       0.0548
              0.101
                                  1.84
-6.44
vear
             -1.437
                          0.2230
sexMale
                          0.0603
year:sexMale 0.233
                                     3.87
Intercepts:
Value Std. Error t value
A|B -1.353 0.206 -6.574
B|C -0.254 0.204 -1.244
C|D 2.188 0.210
Residual Deviance: 7757.06
AIC: 7769.06
> car::Anova(Vtn_polr)
Analysis of Deviance Table (Type II tests)
Response: response
         LR Chisq Df Pr(>Chisq)
vear
             166.5 1 < 2e-16 ***
                          2.1e-14 ***
              58.5
sex
                          0.00011 ***
year:sex
              15.0 1
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
```

Clearly, all terms are significant, including the interaction term with sex as expected from the mosaic plots.

(b) Is there evidence that the proportional odds assumption does not hold for this data set? Use the methods described in Section 8.1 to assess this.

★ We refit the model using vglm(), and compare it to the non-proportional odds model with lrtest():

The unconstrained model fits better than the proportional odds model—again as expected, since for women, the proportional odds assumption seems not be reasonable.

(c) Fit the multinomial logistic model, also allowing an interaction. Use car::Anova() to assess the model terms.

 \star

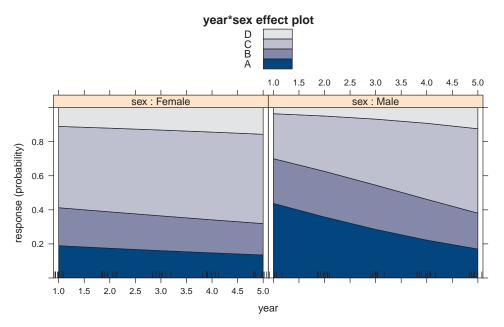
```
> library(nnet)
> library(car)
> Vtn_mtn = multinom(response ~ year * sex, data = Vietnam, weights = Freq)
# weights: 20 (12 variable)
initial value 4362.668354
iter 10 value 3927.047674
final value 3838.854903
converged
> summary(Vtn_mtn)
multinom(formula = response ~ year * sex, data = Vietnam, weights = Freq)
Coefficients:
  (Intercept)
                       year sexMale year:sexMale
                                      0.14692
     0.39288 -0.00051719 -0.97197
     1.14525 0.14751329 -1.88983
-1.31002 0.19089252 -2.00838
                                            0.17082
Std. Errors:
      tercept) year sexMale year:sexMale 0.39149 0.110209 0.41055 0.116272
  (Intercept)
                                  0.116272
      0.33686 0.093731 0.35726
                                      0.099851
      0.56775 0.150979 0.61640
                                      0.162177
Residual Deviance: 7677.7
AIC: 7701.7
> car::Anova(Vtn_mtn)
Analysis of Deviance Table (Type II tests)
Response: response
         LR Chisq Df Pr(>Chisq)
           175.9 3 <2e-16 ***
vear
             137.6 3
                           <2e-16 ***
sex
                           0.051.
vear:sex
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

All terms are again significant, alltough weakly so for the interaction term.

(d) Produce an effect plot for this model and describe the nature of the interaction.

*

```
> library(effects)
> plot(allEffects(Vtn_polr), style = "stacked")
```



The effect of year on response under the fitted model differentiates male and female students: Whereas the majority of female students prefer the more peaceful options in general (with a slight increase over the years), a majority of male students are in favor of more violent options as freshmen, but change their opinion dramatically during the studies so that the situation is reversed at the end. The model is consistent with the findings from the exploratory mosaic plot.

(e) Fit the simpler multinomial model in which there is no effect of year for females and the effect of year is linear for males (on the logit scale). Test whether this model is significantly worse than the general multinomial model with interaction.
 ★ To achieve this, we first construct an artificial variable yearMale, with non-zero entries only for

★ To achieve this, we first construct an artificial variable yearMale, with non-zero entries only formale students:

```
> Vietnam = within(Vietnam, yearMale <- year * (sex == "Male"))
> Vtn_mtn2 = multinom(response ~ sex + yearMale, data = Vietnam, weights = Freq)
# weights:
             16 (9 variable)
initial value 4362.668354
iter 10 value 3894.170452 final value 3841.568268
converged
> Anova (Vtn_mtn2)
Analysis of Deviance Table (Type II tests)
Response: response
          LR Chisq Df Pr(>Chisq)
                            <2e-16 ***
yearMale
                             <2e-16 ***
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
> anova (Vtn_mtn, Vtn_mtn2)
Likelihood ratio tests of Multinomial Models
Response: response
            Model Resid. df Resid. Dev
                                                        Df LR stat. Pr(Chi)
                                               Test
                                    7683.1
1 sex + yearMale
                          111
                                    7677.7 1 vs 2
                                                         3 5.4267 0.14309
      year * sex
```

The simpler model is not significant worse than the general model with interaction, and should therefore be preferred.

Chapter 9 Loglinear and Logit Models for Contingency Tables

Exercise 9.1 Consider the data set DaytonSurvey (described in Example 2.6), giving results of a survey of use of alcohol (A), cigarettes (C), and marijuana (M) among high school seniors. For this exercise, ignore the variables sex and race, by working with the marginal table Dayton. ACM, a $2 \times 2 \times 2$ table in frequency data frame form.

(a) Use loglm() to fit the model of mutual independence, [A][C][M].

 \star

(b) Prepare mosaic display(s) for associations among these variables. Give a verbal description of the association between cigarette and alcohol use.

 \star

(c) Use fourfold() to produce fourfold plots for each pair of variables, AC, AM, and CM, stratified by the remaining one. Describe these associations verbally.

 \star

Exercise 9.2 Continue the analysis of the *DaytonSurvey* data by fitting the following models:

(a) Joint independence, [AC][M]

 \star

(b) Conditional independence, [AM][CM]

 \star

(c) Homogeneous association, [AC][AM][CM]

*

(d) Prepare a table giving the goodness-of-fit tests for these models, as well as the model of mutual independence, [A][C][M], and the saturated model, [ACM]. *Hint*: anova() and LRstats() are useful here. Which model appears to give the most reasonable fit?

*

Exercise 9.3 The data set Caesar in vcdExtra gives a 3×2^3 frequency table classifying 251 women who gave birth by Caesarian section by Infection (three levels: none, Type 1, Type2) and Risk, whether Antibiotics were used, and whether the Caesarian section was Planned or not. Infection is a natural response variable, but the table has quite a few zeros.

(a) Use structable () and mosaic () to see the locations of the zero cells in this table.

 \star

(b) Use loglm() to fit the baseline model [I][RAP]. Is there any problem due to zero cells indicated in the output?

 \star

(c) For the purpose of this excercise, treat all the zero cells as *sampling zeros* by adding 0.5 to all cells, e.g., Caesar1 <- Caesar + 0.5. Refit the baseline model.

*

(d) Now fit a "main effects" model [IR][IA][IP][RAP] that allows associations of Infection with each of the predictors.

*

Exercise 9.4 The Detergent in vcdExtra gives a $2^3 \times 3$ table classifying a sample of 1,008 consumers according to their preference for (a) expressed Preference for Brand "X" or Brand "M" in a blind trial, (b) Temperature of laundry water used, (c) previous use ($\texttt{M_user}$) of detergent Brand "M," and (d) the softness ($\texttt{Water_softness}$) of the laundry water used.

(a) Make some mosaic displays to visualize the associations among the table variables. Try using different orderings of the table variables to make associations related to Preference more apparent.

*

- (b) Use a doubledecker() plot to visualize how Preference relates to the other factors.
 - \star
- (c) Use loglm() to fit the baseline model [P][TMW] for Preference as the response variable. Use a mosaic display to visualize the lack of fit for this model.
 - \star

Chapter 10 Extending Loglinear Models

Exercise 10.1 Example 10.5 presented an analysis of the data on visual acuity for the subset of women in the VisualAcuity data. Carry out a parallel analysis of the models fit there for the men in this data set, given by:

```
> data("VisualAcuity", package="vcd")
> men <- subset(VisualAcuity, gender=="male", select=-gender)</pre>
```

★ Fit the independence, quasi-independence, symmetry, and quasi-symmetry models for the data men. These require the gnm (Turner and Firth, 2014) package. It is convenient to use update() to add terms to a model.

```
> library(gnm)
> indep <- glm(Freq ~ right + left, data = men, family=poisson)
> quasi <- update(indep, . ~ . + Diag(right, left))
> symm <- glm(Freq ~ Symm(right, left),
+ data = men, family = poisson)
> qsymm <- update(symm, . ~ right + left + .)</pre>
```

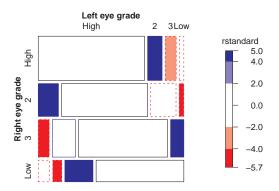
Nested models can be compared using anova() and all models can be compared using LRstats(). Note that unlike the data for women, the symmetry model is preferred over quasi-symmetry by AIC and BIC.

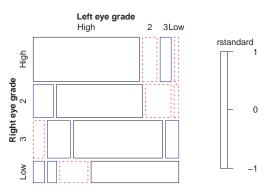
```
> anova(indep, quasi, qsymm, test="Chisq")
Analysis of Deviance Table
Model 1: Freq ~ right + left
Model 2: Freq ~ right + left + Diag(right, left)
Model 3: Freq ~ right + left + Symm(right, left)
  Resid. Df Resid. Dev Df Deviance Pr(>Chi)
                   2781
                                     2701 <2e-16 ***
79 <2e-16 ***
                      81
                            4
                                   2701
                           2
3
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
    # test of marginal homogeneity
> anova (symm, qsymm, test="Chisq")
Analysis of Deviance Table
Model 1: Freq ~ Symm(right, left)
Model 2: Freq ~ right + left + Symm(right, left)
  Resid. Df Resid. Dev Df Deviance Pr(>Chi)
                  4.77
      6
                     1.09 3
                                  3.68
> # model summaries, with AIC and BIC
> models <- glmlist(indep, quasi, symm, qsymm)</pre>
> vcdExtra::LRstats(models)
Likelihood summary table:
        AIC BIC LR Chisq Df Pr(>Chisq)
indep 2901 2906 2781 9 < 2e-16 *** quasi 208 217 81 5 6.6e-16 ***
                       81 5 6
quasi 208 217
symm 131 138
                                    0.57
qsymm 133 143
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

As in the text, it is useful to display some of these using mosaic displays like Figure 10.8.

Quasi-Independence (men)

Quasi-Symmetry (men)





Exercise 10.2 Table 10.1 gives a 4×4 table of opinions about premarital sex and whether methods of birth control should be made available to teenagers aged 14–16, from the 1991 General Social Survey (Agresti, 2013, Table 10.3). Both variables are ordinal, and their grades are represented by the case of the row and column labels.

Table 10.1: Opinions about premarital sex and availability of teenage birth control. Source: Agresti (2013, Table 10.3).

Premarital sex	Birth control			
	DISAGREE	disagree	agree	AGREE
WRONG	81	68	60	38
Wrong	24	26	29	14
wrong	18	41	74	42
OK	36	57	161	157

- (a) Fit the independence model to these data using loglm() or glm().
 - ★ First, enter the data into a matrix and assign row and column labels (dimnames ()).

```
> birthcontrol <- matrix(c(</pre>
  81, 68, 60, 38,
24, 26, 29, 14,
18, 41, 74, 42,
36, 57, 161, 157), 4, 4, byrow=TRUE)
> dimnames(birthcontrol) <-</pre>
         > birthcontrol
      birthcontrol
presex DISAGREE disagree agree AGREE
  WRONG
              81
                       68
                             60
                                   38
                             29
74
  Wrong
              24
                       26
                                   14
  wrong
              18
                       41
                                   42
                       57
                            161
```

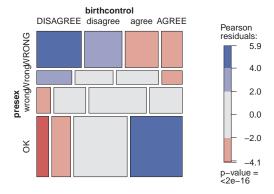
loglm() can handle the data in matrix form.

glm() requires that the data be converted to a data frame, but is much more capable in the results it gives.

```
> birthcontrol.df <- as.data.frame(as.table(birthcontrol))</pre>
> birth.indep <- glm(Freq ~ presex + birthcontrol,
+ data = birthcontrol.df, family = poisson)</pre>
> summary(birth.indep)
Call:
glm(formula = Freq ~ presex + birthcontrol, family = poisson, data = birthcontrol.df)
Deviance Residuals:
Min 1Q Median 3Q Max
-4.547 -2.582 0.067 1.652 5.258
                                        Max
Coefficients:
                         Estimate Std. Error z value Pr(>|z|)
                                                 38.95 < 2e-16 ***
-8.03 9.8e-16 ***
(Intercept)
                         3.7474 0.0962
presexWrong
                          -0.9768
                                       0.1217
                                                  -3.49 0.00049 ***
6.32 2.5e-10 ***
1.76 0.07861 .
7.35 2.0e-13 ***
presexwrong
                          -0.3446
                                        0.0988
presexOK
                           0.5092
                                        0.0805
birthcontroldisagree
                           0.1886
                                        0.1072
birthcontrolagree
                         0.7118
                                      0.0968
                                                   4.50 6.7e-06 ***
birthcontrolAGREE
                          0.4565
                                      0.1014
Signif. codes: 0 '*** 0.001 '** 0.01 '*' 0.05 '.' 0.1 ' ' 1
(Dispersion parameter for poisson family taken to be 1)
Null deviance: 431.08 on 15 degrees of freedom Residual deviance: 127.65 on 9 degrees of freedom
Number of Fisher Scoring iterations: 5
> anova(birth.indep)
Analysis of Deviance Table
Model: poisson, link: log
Response: Freq
Terms added sequentially (first to last)
               Df Deviance Resid. Df Resid. Dev
                                      15
presex
                      236.3
                                      12
                                                 195
birthcontrol 3 67.1
                                                 128
```

(b) Make a mosaic display showing departure from independence and describe verbally the pattern of association. ★ Those who believe that premarital sex is wrong disagree that birth control should be made available to teenagers, in relation to the strength of their opinion about premarital sex. Only those who believe that premarital sex is OK support birth control for teenagers.

```
> mosaic(birthcontrol, shade=TRUE)
```



- (c) Treating the categories as equally spaced, fit the $L \times L$ model of uniform association, as in Section 10.1. Test the difference against the independence model with a likelihood-ratio test.
 - \bigstar The $L \times L$ model fits appreciably better than the independence model, for a "cost" of only one extra parameter in the model.

```
> library(gnm)
> linlin <- gnm (Freq ~ presex + birthcontrol +
                        as.numeric(presex) * as.numeric(birthcontrol),
                 data=birthcontrol.df, family=poisson)
> anova(birth.indep, linlin, test="Chisq")
Analysis of Deviance Table
Model 1: Freq ~ presex + birthcontrol
Model 2: Freq ~ presex + birthcontrol + as.numeric(presex) + as.numeric(birthcontrol) +
    as.numeric(presex):as.numeric(birthcontrol)
  Resid. Df Resid. Dev Df Deviance Pr(>Chi)
          9
                127.7
2
           8
                   11.5
                         1
                                 116 <2e-16 ***
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

(d) Fit the RC(1) model with gnm(), and test the difference of this against the model of uniform association.
 ★ The L × L model and the RC(1) model both fit well, but the former, with only one parameter for association, is deemed best by AIC and BIC.

```
> RC <- qnm (Freq ~ presex + birthcontrol + Mult (presex, birthcontrol),
+ data=birthcontrol.df, family=poisson, verbose=FALSE)
> anova(linlin, RC, test="Chisq")
Analysis of Deviance Table
Model 1: Freq ~ presex + birthcontrol + as.numeric(presex) + as.numeric(birthcontrol) +
    as.numeric(presex):as.numeric(birthcontrol)
Model 2: Freq ~ presex + birthcontrol + Mult(presex, birthcontrol)
 Resid. Df Resid. Dev Df Deviance Pr(>Chi)
         8
               11.53
                   7.14
   # compare all models
> LRstats(birth.indep, linlin, RC)
Likelihood summary table:

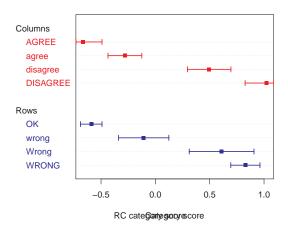
AIC BIC LR Chisq Df Pr(>Chisq)
                        127.7 9
11.5 8
birth.indep 232 238
                                      <2e-16
linlin
           118 124
                                      0.17
            122 131
                          7.1 4
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

(e) Write a brief summary of these results, including plots useful for explaining the relationships in this data set.
 ★ Essentially, the association of attitudes toward premarital sex and birth control is that of two ordinal variables: the more one disagrees with premarital sex, the less one is likely to support birth control

for teenagers. The uniform association model, linlin, is the most parsimonious, assuming that the categories of presex and birthcontrol are equally spaced. From the coefficient for the $L \times L$, one can say that each step toward viewing premarital sex as OK multiplies the odds of agreement with birth control by 1.33, an increase of 33%.

The logmult package also fits the RC(1) model and provides a useful plot of the category scores together with confidence intervals via its plot() method. From this it can be seen that there is little reason to question that the category scores are equally spaced, except possibly for the WRONG and Wrong categories of presex.

```
> library(logmult)
> rc1 <- rc(birthcontrol, verbose=FALSE, weighting="marginal", se="jackknife")
Computing jackknife standard errors...
> plot(rc1, pch=15, conf=.95)
> title(xlab="RC category score")
```



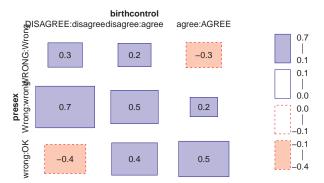
Exercise 10.3 For the data on attitudes toward birth control in Table 10.1,

- (a) Calculate and plot the observed local log odds ratios.
 - ★ The (log) odds ratios give the log odds of a 1-step change in attitude toward birth control for a 1-step change in the attitude toward premarital sex. Note that the mean of these values is similar to the common log odds ratio fit by the model of uniform association.

```
> (LOR <- loddsratio(birthcontrol))</pre>
log odds ratios for presex and birthcontrol
             birthcontrol
presex
              DISAGREE: disagree disagree: agree agree: AGREE
                                                  -0.27148
  WRONG: Wrong
                                       0.23436
                        0.25498
 Wrong:wrong
                        0.74316
                                        0.48129
                                                    0.16184
                        -0.36367
                                        0.44786
  wrong:OK
                                                     0.54124
> exp(mean(as.matrix(LOR)))
[1] 1.2811
```

A simple plot of these is a tile() plot, showing how the odds rations change systematically in each row, decreasing in the first two rows, but increasing in the last row. This is similar to the corrplot() shown in Figure 10.2 in the text.

```
> tile(LOR)
```



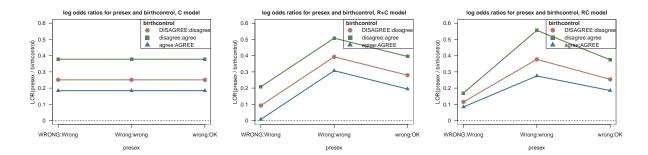
(b) Also fit the R, C, and R+C models.

```
*
```

```
> Rscore <- as.numeric(birthcontrol.df$presex)
> Cscore <- as.numeric(birthcontrol.df$birthcontrol)</pre>
> # row effects model (mental)
> roweff <- glm(Freq ~ presex + birthcontrol +
                         presex:Cscore,
                   family = poisson, data = birthcontrol.df)
 coleff <- glm(Freq ~ presex + birthcontrol +</pre>
                   Rscore:birthcontrol,
family = poisson, data = birthcontrol.df)
> RplusC <- glm(Freq ~ presex + birthcontrol +
+ Rscore:birthcontrol + presex:Cscore,</pre>
                   family = poisson, data = birthcontrol.df)
> LRstats (birth.indep, roweff, coleff, RplusC, linlin)
Likelihood summary table:
            AIC BIC LR Chisq Df Pr(>Chisq)
                               9
birth.indep 232 238
                         127.7
             120 128
                                6
roweff
                                         0.15
                           9.1
coleff
             120 128
                                6
                                         0.17
RplusC
             122 131
                           6.9
                                         0.14
            118 124
                          11.5 8
linlin
                                         0.17
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

- (c) Use the method described in Section 10.1.2 to visualize the structure of fitted local log odds ratios implied by each of these models, together with the RC(1) model.
 - ★ Here is a simple function to extract the fitted values from a given model, calculate the log odds ratios, and plot them.

Using this, we plot the C, R+C, and RC(1) models below in the style shown in Figure 10.4 in the text. These plots show quite clearly how these models differ in the structure of their fitted log odds ratios.



Exercise 10.4 The data set gss8590 in logmult gives a $4\times5\times4$ table of education levels and occupational categories for the four combinations of gender and race from the General Social Surveys, 1985–1990, as reported by Wong (2001, Table 2). Wong (2010, Table 2.3B) later used the subset pertaining to women to illustrate RC(2) models. This data is created below as Women.tab, correcting an inconsistency to conform with the 2010 table.

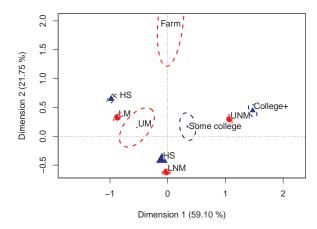
```
> data("gss8590", package="logmult")
> Women.tab <- margin.table(gss8590[,,c("White Women", "Black Women")], 1:2)
> Women.tab[2,4] <- 49
> colnames(Women.tab)[5] <- "Farm"</pre>
```

- (a) Fit the independence model, and also the RC(1) and RC(2) models using rc() with marginal weights, as illustrated in Example 10.4. Summarize these statistical tests in a table.
 - ★ Only the RC2 model fits here.

```
> Women.df <- as.data.frame(as.table(Women.tab))</pre>
> indep <- glm(Freq ~ Education + Occupation,
              data = Women.df, family = poisson)
> library(logmult)
> RC1 <- rc(Women.tab, verbose=FALSE, weighting="marginal", se="jackknife")
Computing jackknife standard errors...
> RC2 <- rc(Women.tab, verbose=FALSE, weighting="marginal", se="jackknife", nd=2)
Computing jackknife standard errors...
> LRstats(indep, RC1, RC2)
Likelihood summary table:
       AIC BIC LR Chisq Df Pr(>Chisq)
indep 1506 1514
                    1373 12
                                <2e-16
RC1
       269
           283
                     125
                                <2e-16 ***
RC2
       153
           171
                                  0.74
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
```

- (b) Plot the solution for the RC(2) model with 68% confidence ellipses. What verbal labels would you use for the two dimensions?
 ★ Dimension 1 most clearly corresponds to Education, ordered from low (< HS) to high (College).
 - ★ Dimension 1 most clearly corresponds to Education, ordered from low (< HS) to high (College). Dimension 2 largely reflects the Occupation categories, with Farm being most different from the others.

```
> plot(RC2, conf=0.68, cex=1.5)
```



- (c) Is there any indication that a simpler model, using integer scores for the row (Education) or column (Occupation) categories, or both, might suffice? If so, fit the analogous column effects, row effects, or $L \times L$ model, and compare with the models fit in part (a).
 - ★ Given that the RC(1) model does not fit very well here, there is little chance that a simpler model using integer scores would be adequate.

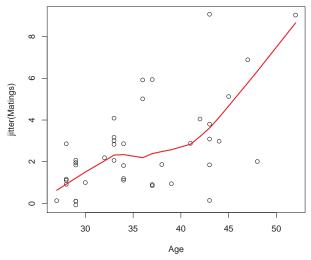
Chapter 11 Generalized Linear Models for Count Data

Exercise 11.1 Poole (1989) studied the mating behavior of elephants over 8 years in Amboseli National Park, Kenya. A focal aspect of the study concerned the mating success of males in relation to age, since larger males tend to be more successful in mating. Her data were used by Ramsey and Schafer (2002, Chapter 22) as a case study, and are contained in the Sleuth2 (Ramsey et al., 2012) package (Ramsey et al., 2012) as case 2201.

For convenience, rename this to elephants, and study the relation between Age (at the beginning of the study) and number of successful Matings for the 41 adult male elephants observed over the course of this study, ranging in age from 27–52.

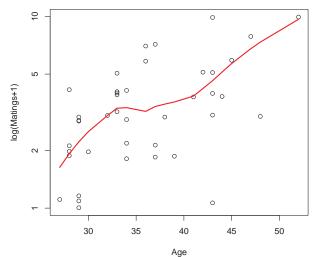
- (a) Create some exploratory plots of Matings against Age in the styles illustrated in this chapter. To do this successfully, you will have to account for the fact that Matings has a range of only 0–9, and use some smoothing methods to show the trend.
 - ★ The simplest plot just jitters the number of matings, and draws a smoothed lowess curve.

```
> with(elephants, {
+          plot(jitter(Matings) ~ Age)
+          lines(lowess(Age, Matings), lwd=2, col="red")}
+          )
```

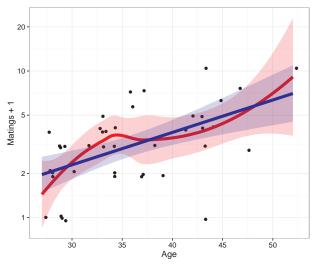


- (b) Repeat (a) above, but now plotting log (Matings+1) against Age to approximate a Poisson regression with a log link and avoid problems with the zero counts.
 - ★ As noted in the text, you can use log="y", but then the Y variable should be used as Y+1 to avoid problems with 0 counts.

```
> with(elephants, {
+          plot(jitter(Matings+1) ~ Age, log="y", ylab="log(Matings+1)")
+          lines(lowess(Age, Matings+1), lwd=2, col="red")}
+          )
```



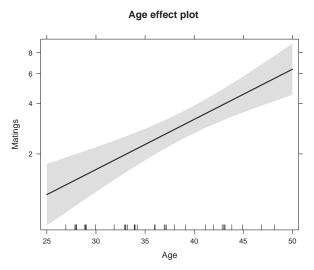
ggplot2 makes it easy to make a similar plot, and to also overlay the fit of a linear model. This also shows error bands for the loess and linear fits.



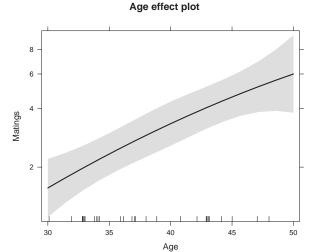
- (c) Fit a linear Poisson regression model for Matings against Age. Interpret the fitted model *verbally* from a graph of predicted number of matings and/or from the model coefficients. (*Hint*: Using Age-27 will make the intercept directly interpretable.)
 - \bigstar Age-27 shifts the value of intercept to the minimum value in the data. In a model formula, use I (Age-27). The coefficient for Age then relates to increments in log(Matings); expontiating the coefficient give the multiple of Matings for a unit change in Age.

Thus, at Age 27, these elephants have a predicted 1.31 matings. For each additional year, matings

are expected to be multiplied by 1.07, an increase of 7%. Perhaps the best way to visualize the model predictions are through an effect plot.



- (d) Check for nonlinearity in the relationship by using the term poly (Age, 2) in a new model. What do you conclude?
 ★ There is little evidence for nonlinearity, as evidenced by a test of the quadratic model in Age, or by
 - ★ There is little evidence for nonlinearity, as evidenced by a test of the quadratic model in Age, or by a plot of the predicted values under this model.



- (e) Assess whether there is any evidence of overdispersion in these data by fitting analogous quasi-Poisson and negative-binomial models.
 - \bigstar The simple way to assess overdispersion is via <code>dispersiontest()</code>, which is not significant here. A more careful answer would fit and compare the overdispersed models suggested.

Exercise 11.2 The data set *quine* in MASS gives data on absenteeism from schools in rural New South Wales, Australia. 146 children were classified by ethnic background (Eth), age (Age, a factor), Sex, and Learner status (Lrn), and the number of days absent (Days) from school in a particular school year was recorded.

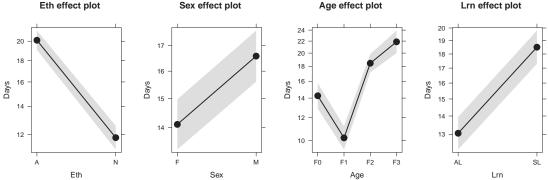
- (a) Fit the all main-effects model in the Poisson family and examine the tests of these effects using summary () and car::Anova(). Are there any terms that should be dropped according to these tests?
 - ★ For such a factorial design, a useful first step is to examine the sample sizes in the cells of this 4-way classification. The table below shows that the design is very unbalanced, and that there are no slow learners (SL) in age F3.

Age here corresponds to "Form", or grade in school, arguably an ordered factor, so we make it so. The Poisson model Anova() shows that all terms are significant. summary() shows that the effects of Age have significant linear, quadratic and cubic trends.

```
> data("quine", package="MASS")
> quine$Age <- ordered(quine$Age)
> quine.mod1 <- glm(Days ~ ., data=quine, family=poisson)</pre>
> Anova (quine.mod1)
Analysis of Deviance Table (Type II tests)
Response: Davs
    LR Chisq Df Pr(>Chisq)
Eth
      166.8 1 < 2e-16 ***
14.4 1 0.00015 ***
Sex
       168.3 3 < 2e-16 ***
45.8 1 1.3e-11 ***
Age
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
> summary(quine.mod1)
glm(formula = Days ~ ., family = poisson, data = quine)
Deviance Residuals:
  Min 1Q Median
-6.81 -3.06 -1.12
                                 3Q
                                         Max
                               1.82
                                         9.91
 -6.81
Coefficients:
             Estimate Std. Error z value Pr(>|z|)
              2.8033 0.0434 64.55 < 2e-16 ***
-0.5336 0.0419 -12.74 < 2e-16 ***
EthN
                            0.0425 3.80 0.00015 ***
0.0471 8.90 < 2e-16 ***
0.0497 5.06 4.1e-07 ***
0.0410 -7.34 2.1e-13 ***
SexM
                0.1616
Age.L
                0.4192
                0.2519
Age.Q
Age.C
               -0.3013
                                        6.70 2.0e-11 ***
               0.3489
                             0.0520
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
(Dispersion parameter for poisson family taken to be 1)
    Null deviance: 2073.5 on 145 degrees of freedom
```

```
Residual deviance: 1696.7 on 139 degrees of freedom
AIC: 2299
Number of Fisher Scoring iterations: 5
```

Although not asked in the question, a careful analysis will try to understand the fitted model, e.g., via an effect plot.



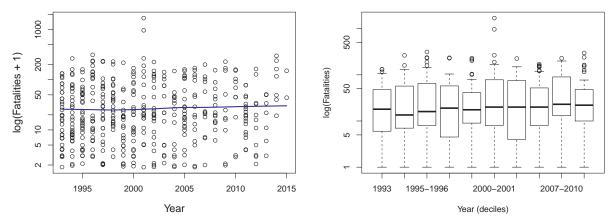
- (b) Re-fit this model as a quasi-Poisson model. Is there evidence of overdispersion? Test for overdispersion formally, using dispersiontest() from AER (Kleiber and Zeileis, 2015).
 - \bigstar dispersiontest () reveals very substantial overdispersion, with variance approximately $\widehat{\phi}=13.2$ times the mean under this model.

(c) Carry out the same significance tests and explain why the results differ from those for the Poisson model. \bigstar The Anova () tests for the quasi-Poisson model quine.modlq show that only ethnicity and age have significant effects, learner status nearly so. Relative to the standard Poisson model, the coefficients are the same, but the standard errors have been adjusted by a factor of $\hat{\phi}^{-1/2}=0.28$

```
> Anova (quine.mod1q)
Analysis of Deviance Table (Type II tests)
Response: Days
    LR Chisq Df Pr(>Chisq)
Eth
                   0.00037
       12.67
        1.09
                   0.29560
Sex
                   0.00513 **
Age
       12.78
                   0.06218 .
Lrn
Signif. codes: 0 '*** 0.001 '** 0.01 '*' 0.05 '.' 0.1 ' ' 1
> coeftest(quine.modlq)
z test of coefficients:
            Estimate Std. Error z value Pr(>|z|)
(Intercept)
                           0.158
                                  17.79
              2.803
                           0.152
              -0.534
                                   -3.51
                                          0.00045 ***
EthN
SexM
               0.419
                           0.171
                                    2.45
                                          0.01418
Age.L
Age.Q
               0.252
                           0.181
                                    1.40
                                          0.16288
                                          0.04297
Age.C
              -0.301
                           0.149
                                   -2.02
LrnSL
               0.349
                           0.189
                                    1.85
                                          0.06463 .
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

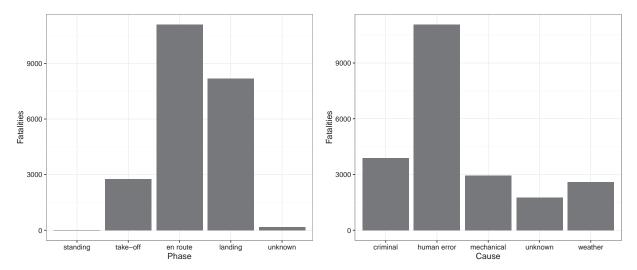
Exercise 11.3 The data set *AirCrash* in vcdExtra was analyzed in Exercise 5.2 and Exercise 6.3 in relation to the Phase of the flight and Cause of the crash. Additional variables include the number of Fatalities and Year. How does Fatalities depend on the other variables?

- (a) Use the methods of this chapter to make some exploratory plots relating fatalities to each of the predictors.
 - ★ Both Phase and Cause are unordered factors, whose levels are ordered lexically. For graphics and analysis it is useful to reorder Phase in temporal order. Plots of the total number fatalities over Year, in either jittered scatterplot or boxplot form show no overall trend. (Other plots, not shown here, indicate that the number of crashes has decreased over time.) As in the text, we plot these on a log scale.



Plots of fatalities against the factors can be done in a variety of forms. Here we use ggplot2 for bar charts. Note the use of <code>geom_bar(aes(weight=Fatalities))</code>, so that the height of each bar is proportional to the number of fatalities; otherwise, it would just show the number of crashes.

```
> ggplot(AirCrash, aes(Phase)) + geom_bar(aes(weight=Fatalities)) +
+     ylab("Fatalities") + theme_bw()
> ggplot(AirCrash, aes(Cause)) + geom_bar(aes(weight=Fatalities)) +
+     ylab("Fatalities") + theme_bw()
```

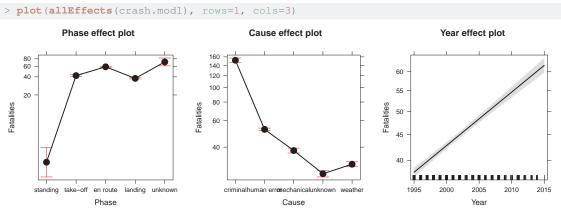


(b) Fit a main effects poisson regression model for Fatalities, and make effects plots to visualize the model. Which phases and causes result in the largest number of fatalities?

*

```
> crash.mod1 <- glm(Fatalities ~ Phase + Cause + Year,
                   data=AirCrash, family=poisson)
> Anova (crash.mod1)
Analysis of Deviance Table (Type II tests)
Response: Fatalities
      LR Chisq Df Pr(>Chisq)
Phase
          1586 4
                      <2e-16 ***
Cause
          5004
               4
                      <2e-16 ***
Year
           436
                      <2e-16 ***
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
```

From the marginal plots for part (a), it appears that most fatalities occur en route or on landing, and the primary cause is human error. However, an effects plot for the main effects model, where other factors are controlled in a given panel, tells a different story: Unknown phase rises to the top, and the greatest cause is criminal activity. The plot for Year is slightly misleading, because the range is relatively small compared to the other panels. This can be avoided by setting ylim=log(c(1,180)) in the plot.



- (c) A linear effect of Year might not be appropriate for these data. Try using a natural spline term, ns (Year, df) to achieve a better, more adequate model.
 - \bigstar A careful analysis would investigate the tradeoff between goodness-of-fit and parsimony in the choice of degrees of freedom. Here we just illustrate the use of ns (Year, 3), allowing 3 df for the Year effect. This fits significantly better than the linear model in Year.

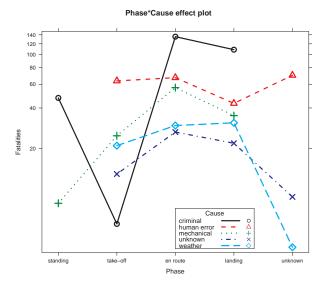
```
> library(splines)
> crash.mod2 <- glm(Fatalities ~ Phase + Cause + ns(Year, 3),
+ data=AirCrash, family=poisson)</pre>
```

- (d) Use a model-building tool like add1 () or MASS::stepAIC() to investigate whether there are important two-way interactions among the factors and your chosen effect for Year.
 - ★ We don't show a complete analysis here. add1() just looks at each of the two-way interaction terms and reports that adding each one, separately, would decrease the deviance and AIC, resulting in a better-fitting model. stepAIC() eventually includes all three two-way terms.

```
> add1(crash.mod2, scope= ~.^2, test="Chisq")
Single term additions
Fatalities ~ Phase + Cause + ns(Year, 3)
        Df Deviance AIC LRT Pr(>Chi)
30724 32862
Phase:Cause 11
                          29959 32119 765
30395 32554 329
                                              <2e-16 ***
Phase:ns(Year, 3) 11
Cause:ns(Year, 3) 12
                                              <2e-16 ***
                          28626 30788 2098
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
> # refit the stepAIC final model
> crash.modAIC <- update(crash.mod2, .~. + Phase:Cause + Phase:ns(Year, 3) + Cause:ns(Year, 3))</pre>
> Anova (crash.modAIC)
Analysis of Deviance Table (Type II tests)
Response: Fatalities
                 LR Chisq Df Pr(>Chisq)
                        703 4 <2e-16 ***
Phase
                       4654
                                    <2e-16 ***
Cause
ns(Year, 3)
                        480 3
                                    <2e-16 ***
                        426 8
194 8
Phase:Cause
                                    <2e-16 ***
Phase:ns(Year, 3)
                                    <2e-16 ***
                       2049 12
Cause:ns(Year, 3)
                                     <2e-16 ***
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

- (e) Visualize and interpret your final model and write a brief summary to answer the question posed.
 - ★ The number of fatalities in air crashes depends in a complex way on the combinations of Phase, Cause and Year. We illustrate this below with an effect plot for the interaction of Phase and Cause, the interpretation of which just entails trying to describe the patterns in the plot.

```
> plot(Effect(c("Phase", "Cause"), crash.modAIC),
+ multiline=TRUE, lwd=3, key.args=list(x=0.5, y=0.2))
```



Exercise 11.4 Male double-crested cormorants use advertising behavior to attract females for breeding. The *Cormorants* data set in vcdExtra gives some results from a study by Meagan Mc Rae (2015) on counts of advertising males observed two or three times a week at six stations in a tree-nesting colony for an entire breeding season. The number of advertising birds was counted and these observations were classified by characteristics of the trees and nests. The goal was to determine how this behavior varies temporally over the season and spatially over observation stations, as well as with characteristics of nesting sites. The response variable is count and other predictors are shown below. See help(Cormorants, package="vcdExtra") for further details.

```
> data("Cormorants", package = "vcdExtra")
> car::some (Cormorants)
      category week station
                                nest height
                                               density tree_health count
4
           Pre
                                                           healthy
                          C1 partial
                                        high
                                                   few
           Pre
34
                          В1
                                                   few
                                                              dead
                                 no
                                        high
143
                                                               dead
           Pre
                          В2
                                   no
                                         mid
                                                   few
155 Incubation
                          C2
                                   no
                                         mid
                                                   few
                                                              dead
160 Incubation
                          C2 partial
                                        high
                                                   few
                                                           healthy
175 Incubation
                             partial
                                        high
                                                   few
                                                              dead
240 Incubation
                                   no
                                         mid moderate
                                                              dead
250 Incubation
                          C4
                                        high
                   6
                                                   few
                                                              dead
                                   no
314 Incubation
                          В2
                                                   few
                                                           healthy
                                   no
                                         mid
340
          <NA>
                          В1
                                        hiah
                                                   few
                                                              dead
```

- (a) Using the methods illustrated in this chapter, make some exploratory plots of the number of advertising birds against week in the breeding season, perhaps stratified by another predictor, like tree height, nest condition, or observation station. To see anything reasonable, you should plot count on a log (or square root) scale, jitter the points, and add smoothed curves. The variable category breaks the weeks into portions of the breeding season, so adding vertical lines separating those will be helpful for interpretation.
 - ★ Here we use ggplot2 to plot count against week, stratified by height and nest. The plot for height shows that counts of advertising birds increase with height in the tree and rise over week at the end of the pre-breeding portion of the season.

```
+ scale y_log10 (breaks=c(1,2,5,10)) +
+ geom_vline(xintercept=c(4.5, 9.5)) +

height low mid high

low mid high

solution in the intercept of the intercept of
```

(b) Fit a main-effects Poisson GLM to these data and test the terms using Anova () from the car package.

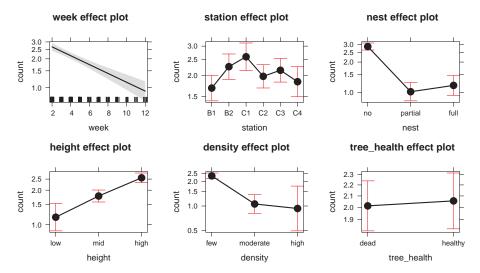
★ All terms except tree_health show significant main effects.

```
> fit1 <-glm(count \sim week + station + nest + height + density + tree_health, data=Cormorants,
       family = poisson)
> library(car)
> Anova (fit1)
Analysis of Deviance Table (Type II tests)
Response: count
             LR Chisq Df Pr(>Chisq)
62.8 1 2.3e-15 ***
14.1 5 0.015 *
week
station
                              < 2e-16 ***
                 137.8 2
48.0 2
nest
                              3.8e-11 ***
height
                              5.5e-11 ***
0.792
                  47.3 2
0.1 1
density
tree_health
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

(c) Interpret this model using an effects plot.

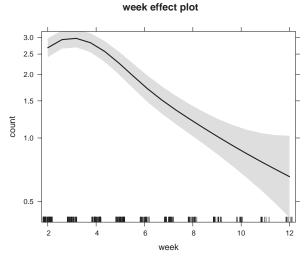
★ According to the linear model, counts (a) decrease over weeks in the seasons; (b) are greatest with no nests; (c) increase with height in the tree and (d) are greatest when the density is low.

```
> library(effects)
> plot(allEffects(fit1))
```



- (d) Investigate whether the effect of week should be treated as linear in the model. You could try using a polynomial term like poly (week, degree) or perhaps better, using a natural spline term like ns (week, df) from the splines package.
 - ★ Here we drop tree_health and use a natural spline with 3 degrees of freedom for week to allow a moderate departure from linearity, roughly comparable to a cubic term poly (week, 3) in complexity. The effect plot for week shows a pronounced rise over the early weeks, followed by a steady decline over the rest of the season.

```
> library(splines)
> fit2 <-glm(count ~ ns(week,3) + station + nest + height + density , data=Cormorants, + family = poisson)
> Anova (fit2)
Analysis of Deviance Table (Type II tests)
             LR Chisq Df Pr(>Chisq)
ns(week, 3)
                 98.8
                             < 2e-16
station
                 17.5
                              0.0036 **
nest
                             < 2e-16
                 59.2
height
                             1.4e-13 ***
density
                             2.6e-11 ***
Signif. codes:
                 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
> plot(Effect("week", fit2))
```



A more thorough analysis would investigate whether there are important interactions among the model terms. The model below checks whether there are interactions of week with any of the other factors.

The conclusion is no.

(e) Test this model for overdispersion, using either a quasipoisson family or dispersiontest() in AER. ★ Using dispersiontest() on the fit1 and fit2 models shows significant overdispersion for the former, but not for the latter. This illustrates that the test for overdispersion assumes that the model is correctly specified.

```
> require (AER)
> dispersiontest(fit1)
Overdispersion test
data: fit1
z = 1.79, p-value = 0.036
alternative hypothesis: true dispersion is greater than 1
sample estimates:
dispersion
    1.3713
> dispersiontest(fit2)
Overdispersion test
data: fit2
z = 1.19, p-value = 0.12
alternative hypothesis: true dispersion is greater than 1
sample estimates:
dispersion
 1.1782
```

Exercise 11.5 For the *CodParasites* data, recode the area variable as an ordered factor as suggested in footnote 13. Test the hypotheses that prevalence and intensity of cod parasites is linearly related to area.



Exercise 11.6 In Example 11.10, we ignored other potential predictors in the *CodParasites* data: depth, weight, length, sex, stage, and age. Use some of the graphical methods shown in this case study to assess whether any of these are related to prevalence and intensity.



Exercise 11.7 The analysis of the *PhdPubs* data in the examples in this chapter were purposely left incomplete, going only as far as the negative binomial model.

(a) Fit the zero-inflated and hurdle models to this data set, considering whether the count component should be Poisson or negative-binomial, and whether the zero model should use all predictors or only a subset. Describe your conclusions from this analysis in a few sentences.



(b) Using the methods illustrated in this chapter, create some graphs summarizing the predicted counts and probabilities of zero counts for one of these models.

 \star

(c) For your chosen model, use some of the diagnostic plots of residuals and other measures shown in Section 11.6 to determine if your model solves any of the problems noted in Example 11.17 and Example 11.18, and whether there are any problems that remain.



Exercise 11.8 In Example 11.19 we used a simple analysis of $\log(y+1)$ for the multivariate responses in the *NMES1988* data using a classical MLM (Eqn. (11.16)) as a rough approximation of a multivariate Poisson model. The HE plot in Figure 11.40 was given as a visual summary, but did not show the data. Examine why the MLM is not appropriate statistically for these data, as follows:

(a) Calculate residuals for the model nmes.mlm using

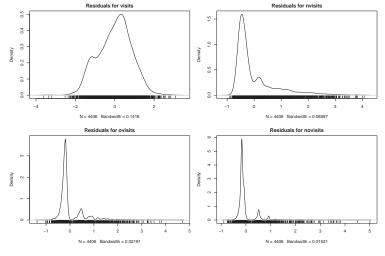
```
> resids <- residuals(nmes.mlm, type="deviance")</pre>
```

★ This just copies the code from the text to fit the model and calculate the residuals:

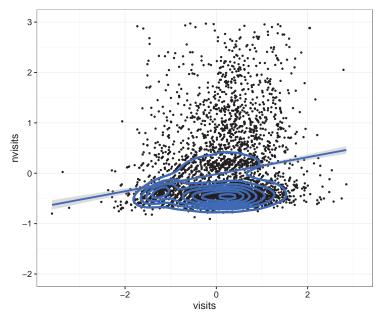
```
> data("NMES1988", package="AER")
> nmes2 <- NMES1988[, c(1:4, 6:8, 13, 15, 18)]
> clog <- function(x) log(x+1)
> nmes.mlm <- lm(clog(cbind(visits, nvisits, ovisits, novisits)) ~ ., data=nmes2)
> resids <- residuals(nmes.mlm, type="deviance")</pre>
```

- (b) Make univariate density plots of these residuals to show their univariate distributions. These should be approximately normal under the MLM. What do you conclude?
 - ★ There are a variety of ways to produce density plots in R, but the simplest for this question is just to use <code>density()</code> with default settings. The residuals for <code>visits</code> are reasonably symmetric. All the others are quite positively skewed.

```
> op <- par(mfrow=c(2,2), mar=c(5,4,2,1)+0.1)
> plot(density(resids[,1]), main = "Residuals for visits")
> rug(resids[,1])
>
> plot(density(resids[,2]), main = "Residuals for nvisits")
> rug(resids[,2])
>
> plot(density(resids[,3]), main = "Residuals for ovisits")
> rug(resids[,3])
> plot(density(resids[,4]), main = "Residuals for novisits")
> rug(resids[,4])
> par(op)
```

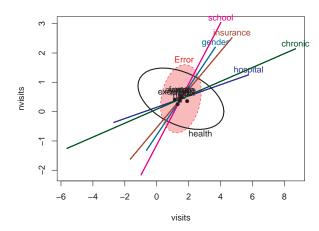


- (c) Make some bivariate plots of these residuals. Under the MLM, each should be bivariate normal with elliptical contours and linear regressions. Add 2D density contours (kde2d(), or geom_density2d() in ggplot2) and some smoothed curve. What do you conclude?
 - ★ Here is just one example for the first two variables, visits, and nvisits. The bivariate distribution is very far from bivariate normal, largely because nvisits is so positively skewed. All other pairs of the residuals would be worse.



The overall conclusion is that, while Figure 11.40 in the text gives a useful overall summary of the relationship among the multivariate resonses, it should only be considered as a rough approximation. For comparison, the plot above corresponds to the error ellipse in the (2,1) panel of Figure 11.40, shown in red in the plot below.

```
> library(heplots)
> heplot(nmes.mlm, variables=1:2, fill=c(TRUE, FALSE))
```



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