Chapter 2

Working with categorical data

Creating and manipulating categorical data sets requires some skills and techniques in R beyond those ordinarily used for quantitative data. This chapter illustrates these for the main formats for categorical data: case form, frequency form and table form.

{ch:working}

TODO: DM: The chapter does not cover NA handling, although this is needed in some chapters. Maybe treat this in the also missing section on subsetting?

Categorical data can be represented as data sets in various formats: case form, frequency form, and table form. This chapter describes and illustrates the skills and techniques in R needed to input, create and manipulate R data objects to represent categorical data, and convert these from one form to another for the purposes of statistical analysis and visualization which are the subject of the remainder of the book.

As mentioned earlier, this book assumes that you have at least a basic knowledge of the R language and environment, including interacting with the R console (Rgui for Windows, R.app for Mac OS X) or some other editor/environment (e.g., R Studio), loading and using R functions in packages (e.g., library (vcd)) getting help for these from R (e.g., help (matrix)), etc. This chapter is therefore devoted to covering those topics beyond such basic skills needed in the book.¹

2.1 Working with R data: vectors, matrices, arrays and data frames

{sec:Rdata}

R has a wide variety of data structures for storing, manipulating and calculating with data. Among these, vectors, matrices, arrays and data frames are most important for the material in this book.

In R, a *vector* is a collection of values, like numbers, character strings, or logicals (TRUE, FALSE), and often correspond to a variable in some analysis. Matrices are rectangular arrays like a traditional table, composed of vectors in their columns or rows. Arrays add additional dimensions, so that, for example, a 3-way table can be represented as composed of rows, columns and layers. An important consideration is that the values in vectors, matrices and arrays must all be of the same *mode*, e.g., numbers or character strings. A *data frame* is a rectangular table, like a traditional data set in other statistical environments, and composed of rows and columns like a matrix, but allowing variables (columns) of different types. These data structures and the types of data they can contain

¹Some excellent introductory treatments of R are: Fox and Weisberg (2011, Chapter 2), ... Tom Short's *R Reference Card*, http://cran.us.r-project.org/doc/contrib/Short-refcard.pdf is a handy 4-page summary of the main functions. The web sites Quick-R http://www.statmethods.net/ and Cookbook for R http://www.cookbook-r.com/provide very helpful examples, organized by topics and tasks.

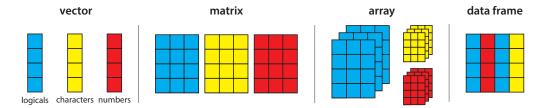


Figure 2.1: Principal data structures and data types in R. Colors represent different data types: numeric, character, logical.

are illustrated in Figure 2.1. A more general data structure is a *list*, a generic vector which can contain any other types of objects (including lists, allowing for *recursive* data structures). A data frame is basically a list of equally-sized vectors, each representing a column of the data frame.

TODO: Delete subsections on vectors, matrices and arrays?

2.1.1 Vectors

The simplest data structure in R is a *vector*, a one-dimensional collection of elements of the same type. An easy way to create a vector is with the c (), which combines its arguments. The following examples create and print vectors of length 4, containing numbers, character strings and logical values respectively:

```
> c(17, 20, 15, 40)
[1] 17 20 15 40
> c("female", "male", "female", "male")
[1] "female" "male" "female" "male"
> c(TRUE, TRUE, FALSE, FALSE)
[1] TRUE TRUE FALSE FALSE
```

To store these values in variables, R uses the assignment operator (<-) or equals sign (=). This creates a variable named on the left-hand side. An assignment doesn't print the result, but a bare expression does, so you can assign and print by surrounding the assignment with ().

```
> count <- c(17, 20, 15, 40)  # assign
> count  # print

[1] 17 20 15 40

> (sex <- c("female", "male", "female", "male"))  # both

[1] "female" "male" "female" "male"

> (passed <- c(TRUE, TRUE, FALSE, FALSE))

[1] TRUE TRUE FALSE FALSE</pre>
```

Other useful functions for creating vectors are:

• The : operator for generating consecutive integer sequences, e.g., 1:10 gives the integers 1 to

{fig:datatypes}

- 10. The seq() function is more general, taking the forms seq(from, to), seq(from, to, by=), and seq(from, to, length=) where the optional argument by specifies the interval between adjacent values and length gives the desired length of the result.
- The rep() function generates repeated sequences, replicating its first argument (which may be a vector) a given number of times, to a given length or each a given multiple.

```
> seq(10, 100, by = 10)  # give interval
[1] 10 20 30 40 50 60 70 80 90 100
> seq(0, 1, length = 11)  # give length
[1] 0.0 0.1 0.2 0.3 0.4 0.5 0.6 0.7 0.8 0.9 1.0
> (sex <- rep(c("female", "male"), times = 2))
[1] "female" "male" "female" "male"
> (sex <- rep(c("female", "male"), length.out = 4)) # same
[1] "female" "male" "female" "male"
> (passed <- rep(c(TRUE, FALSE), each = 2))
[1] TRUE TRUE FALSE FALSE</pre>
```

2.1.2 Matrices

A *matrix* is a two-dimensional array of elements of the same type composed in a rectangular array of rows and columns. Matrices can be created by the function matrix (values, nrow, ncol), which reshapes the elements in the first argument (values) to a matrix with nrow rows and ncol columns. By default, the elements are filled in columnwise, unless the optional argument byrow = TRUE is given.

The last example illustrates that the values in the first argument are recycled as necessary to fill the given number of rows and columns.

All matrices have a dimensions attribute, a vector of length two giving the number of rows and columns, retrieved with the function dim (). Labels for the rows and columns can be assigned using

dimnames (), 2 which takes a list of two vectors for the row names and column names respectively. To see the structure of a matrix (or any other R object) and its attributes, you can use the str() function, as shown in the example below.

```
> dim(matA)
[1] 2 4
> str(matA)
int [1:2, 1:4] 1 2 3 4 5 6 7 8
> dimnames(matA) <- list(c("M", "F"), LETTERS[1:4])
> matA

A B C D
M 1 3 5 7
F 2 4 6 8

> str(matA)
int [1:2, 1:4] 1 2 3 4 5 6 7 8
- attr(*, "dimnames")=List of 2
..$: chr [1:2] "M" "F"
..$: chr [1:4] "A" "B" "C" "D"
```

Additionally, names for the row and column *variables* themselves can also be assigned in the dimnames call by giving each dimension vector a name.

```
> dimnames(matA) <- list(sex = c("M", "F"), group = LETTERS[1:4])
> ## or: names(dimnames(matA)) <- c("Sex", "Group")
> matA

    group
sex A B C D
    M 1 3 5 7
    F 2 4 6 8

> str(matA)

int [1:2, 1:4] 1 2 3 4 5 6 7 8
    - attr(*, "dimnames")=List of 2
    ..$ sex : chr [1:2] "M" "F"
    ..$ group: chr [1:4] "A" "B" "C" "D"
```

(LETTERS is a predefined character vector of the 26 uppercase letters). Matrices can also be created or enlarged by "binding" vectors or matrices together by rows or columns:

- rbind(a, b, c) creates a matrix with the vectors a, b and c as its rows, recycling the elements as necessary to the length of the longest one.
- cbind (a, b, c) creates a matrix with the vectors a, b and c as its columns.
- rbind (mat, a, b, ...) and cbind (mat, a, b, ...) add additional rows (columns) to a matrix mat, recycling or subsetting the elements in the vectors to conform with the size of the matrix.

²The dimnames can also be specified as an optional argument to matrix().

```
> rbind(matA, c(10, 20))

A B C D
M 1 3 5 7
F 2 4 6 8
10 20 10 20
> cbind(matA, c(10, 20))

A B C D
M 1 3 5 7 10
F 2 4 6 8 20
```

Rows and columns can be swapped (transposed) using t ():

```
> t(matA)

sex
group M F
    A 1 2
    B 3 4
    C 5 6
    D 7 8
```

Finally, we note that basic computations involving matrices are performed *element-wise*:

```
> 2 * matA / 100

group
sex    A    B    C    D
M 0.02 0.06 0.10 0.14
F 0.04 0.08 0.12 0.16
```

Special operators and functions do exist for matrix operations, such as % *% for the matrix product.

2.1.3 Arrays

Higher-dimensional arrays are less frequently encountered in traditional data analysis, but they are of great use for categorical data, where frequency tables of three or more variables can be naturally represented as arrays, with one dimension for each table variable.

The function array (values, dim) takes the elements in values and reshapes these into an array whose dimensions are given in the vector dim. The number of dimensions is the length of dim. As with matrices, the elements are filled in with the first dimension (rows) varying most rapidly, then by the second dimension (columns) and so on for all further dimensions, which can be considered as layers. A matrix is just the special case of an array with two dimensions.

```
> (arrayA <- array(1:16, dim = c(2, 4, 2))) # 2 rows, 4 columns, 2 layers
, , 1

[,1] [,2] [,3] [,4]
[1,] 1 3 5 7
[2,] 2 4 6 8

, , 2

[,1] [,2] [,3] [,4]
[1,] 9 11 13 15
[2,] 10 12 14 16</pre>
```

```
> str(arrayA)
int [1:2, 1:4, 1:2] 1 2 3 4 5 6 7 8 9 10 ...
> (arrayB <- array(1:16, dim = c(2, 8))) # 2 rows, 8 columns

[,1] [,2] [,3] [,4] [,5] [,6] [,7] [,8]
[1,] 1 3 5 7 9 11 13 15
[2,] 2 4 6 8 10 12 14 16

> str(arrayB)
int [1:2, 1:8] 1 2 3 4 5 6 7 8 9 10 ...
```

In the same way that we can assign labels to the rows, columns and variables in matrices, we can assign these attributes to dimnames (arrayA), or include this information in a dimnames argument to array().

```
> dimnames(arrayA) <- list(sex = c("M", "F"),</pre>
                           group = letters[1:4],
                           time = c("Pre", "Post"))
> arrayA
, , time = Pre
   group
sex a b c d
 M 1 3 5 7
  F 2 4 6 8
 , time = Post
   group
sex a b c d
 M 9 11 13 15
  F 10 12 14 16
> str(arrayA)
 int [1:2, 1:4, 1:2] 1 2 3 4 5 6 7 8 9 10 ...
 - attr(*, "dimnames")=List of 3
  ..$ sex : chr [1:2] "M" "F"
  ..$ group: chr [1:4] "a" "b" "c" "d"
 ..$ time : chr [1:2] "Pre" "Post"
```

Arrays in R can contain any single type of elements—numbers, character strings, logicals. R also has a variety of functions (e.g., table(), xtabs()) for creating and manipulating "table" objects, which are specialized forms of matrices and arrays containing integer frequencies in a contingency table. These are discussed in more detail below (Section 2.4.1).

2.1.4 data frames

{sec:data-frames}

Data frames are the most commonly used form of data in R and more general than matrices in that they can contain columns of different types. For statistical modeling, data frames play a special role, in that many modeling functions are designed to take a data frame as a data argument, and then find the variables mentioned within that data frame. Another distinguishing feature is that discrete variables (columns) like character strings ("M", "F") or integers (1, 2, 3) in data frames can be represented as *factor*s, which simplifies many statistical and graphical methods.

A data frame can be created using keyboard input with the data.frame() function, applied

to a list of objects, data.frame (a, b, c, ...), each of which can be a vector, matrix or another data frame, but typically all containing the same number of rows. This works roughly like cbind(), collecting the arguments as columns in the result.

The following example generates n=100 random observations on three discrete factor variables, A, B, sex, and a numeric variable, age. As constructed, all of these are statistically independent, since none depends on any of the others. The function sample() is used here to generate n random samples from the first argument allowing replacement (replace = TRUE). The rnorm()() function produces a vector of n normally distributed values with mean 30 and standard deviation 5. The call to set.seed() guarantees the reproducibility of the resulting data. Finally, all four variables are combined into the data frame mydata.

```
> set.seed(12345) # reproducibility
> n <- 100
> A <- factor(sample(c("a1", "a2"), n, replace = TRUE))
> B <- factor(sample(c("b1", "b2"), n, replace = TRUE))
> sex <- factor(sample(c("M", "F"), n, replace = TRUE))
> age <- round(rnorm(n, mean = 30, sd = 5))</pre>
> mydata <- data.frame(A, B, sex, age)
> head (mydata, 5)
   A B sex age
 a2 b1
  a2 b2
                33
            M 31
3 a2 b2
4 a2 b2
              26
5 al b2
            F 29
> str (mydata)
'data.frame': 100 obs. of 4 variables:
 $ A : Factor w/ 2 levels "a1", "a2": 2 2 2 2 1 1 1 2 2 2
 $ B : Factor w/ 2 levels "b1", "b2": 1 2 2 2 2 2 2 1 1 ...
$ sex: Factor w/ 2 levels "F", "M": 1 1 2 1 1 1 2 2 1 1 ...
 $ age: num 22 33 31 26 29 29 38 28 30 27 ..
```

Rows, columns and individual values in a data frame can be manipulated in the same way than a matrix. Additionally, variables can be extracted using the \$ operator:

For real data sets, it is usually most convenient to read these into R from external files, and this is easiest using plain text (ASCII) files with one line per observation and fields separated by commas (or tabs), and with a first header line giving the variable names—called *comma-separated* or CSV format. If your data is in the form of Excel, SAS, SPSS or other file format, you can almost always export that data to CSV format first.³

³The foreign package contains specialized functions to *directly* read data stored by Minitab, SAS, SPSS, Stata, Systat

The function read.table() has many options to control the details of how the data are read and converted to variables in the data frame. Among these some important options are:

header indicates whether the first line contains variable names. The default is FALSE unless the first line contains one fewer field than the number of columns;

sep (default: "" meaning white space, i.e., one or more spaces, tabs or newlines) specifies the separator character between fields;

stringsAsFactors (default: TRUE) determines whether character string variables should be converted to factors;

na.strings (default: "NA") one or more strings which are interpreted as missing data values (NA);

For delimited files, read.csv() and read.delim() are convenient wrappers to read.table(), with default values sep="" respectively, and header=TRUE.

{ex:ch2-arth-csv}

EXAMPLE 2.1: Arthritis treatment

The file Arthritis.csv contains data in CSV format from Koch and Edwards (1988), representing a double-blind clinical trial investigating a new treatment for rheumatoid arthritis with 84 patients. The first ("header") line gives the variable names. Some of the lines in the file are shown below, with . . . representing omitted lines:

```
ID, Treatment, Sex, Age, Improved 57, Treated, Male, 27, Some 46, Treated, Male, 29, None 77, Treated, Male, 30, None 17, Treated, Male, 32, Marked ... 42, Placebo, Female, 66, None 15, Placebo, Female, 66, Some 71, Placebo, Female, 68, Some 1, Placebo, Female, 74, Marked
```

TODO: DM: Add this to vcd or vcdExtra.

We read this into R using read.table() as shown below:

Note that the character variables <code>Treatment</code>, <code>Sex</code> and <code>Improved</code> were converted to factors, and the levels of those variables were ordered <code>alphabetically</code>. This often doesn't matter much for binary variables, but here, the response variable, <code>Improved</code> has levels that should be considered <code>ordered</code>, as <code>"None"</code>, <code>"Some"</code>, <code>"Marked"</code>. We can correct this here by re-assigning <code>Arthritis\$Improved</code> using <code>ordered()</code>. The topic of re-ordering variables and levels in categorical data is considered in more detail in Section 2.3.

and other software. There are also a number of packages for reading (and writing) Excel spreadsheets directly (gdata, XLConnect, xlsx). The R manual, *R Data Import/Export* covers many other variations, including data in relational data bases.

Finally, we note that data frames can conveniently be edited using, e.g., fix (Arthritis).

 \triangle

2.2 Forms of categorical data: case form, frequency form and table form

{sec:forms}

As we saw in Chapter 1, categorical data can be represented as ordinary data sets in case form, but the discrete nature of factors or stratifying variables allows the same information to be represented more compactly in summarized form with a frequency variable for each cell of factor combinations, or in tables. Consequently, we sometimes find data created or presented in one form (e.g., a spreadsheet data set, a two-way table of frequencies) and want to input that into R. Once we have the data in R, it is often necessary to manipulate the data into some other form for the purposes of statistical analysis, visualizing results and our own presentation. It is useful to understand the three main forms of categorical data in R and how to work with them for our purposes.

2.2.1 Case form

Categorical data in case form are simply data frames, with one or more discrete classifying variables or response variables, most conveniently represented as factors or ordered factors. In case form, the data set can also contain numeric variables (covariates or other response variables), that cannot be accommodated in other forms.

As with any data frame, X, you can access or compute with its attributes using nrow(X) for the number of observations, ncol(X) for the number of variables, names(X) or colnames(X) for the variable names and so forth.

{ex:ch2-arth}

EXAMPLE 2.2: Arthritis treatment

The Arthritis data is available in case form in the VCd package. There are two explanatory factors: Treatment and Sex. Age is a numeric covariate, and Improved is the response—an ordered factor, with levels "None" < "Some" < "Marked". Excluding Age, we would have a $2 \times 2 \times 3$ contingency table for Treatment, Sex and Improved.

```
> data(Arthritis, package = "vcd") # load the data
> names(Arthritis)
                     # show the variables
              "Treatment" "Sex"
                                                "Improved"
                      # show the structure
'data.frame': 84 obs. of 5 variables:
$ ID : int 57 46 77 17 36 23 75 39 33 55 ...
27 29 30 32 46 58 59 59 63 63
           : int
$ Improved : Ord.factor w/ 3 levels "None"<"Some"<..: 2 1 1 3 3 3 1 3 1 1 ...
> head(Arthritis, 5)
                      # first 5 observations, same as Arthritis[1:5,]
 ID Treatment
              Sex Age Improved
      Treated Male 27
                          Some
      Treated Male
                          None
 77
      Treated Male 30
                          None
      Treated Male
                   32
                        Marked
     Treated Male 46
                       Marked
```

2.2.2 Frequency form

Data in frequency form is also a data frame, containing one or more discrete factor variables and a frequency variable (often called Freq or count) representing the number of basic observations in that cell.

This is an alternative representation of a table form data set considered below. In frequency form, the number of cells in the equivalent table is nrow(X), and the total number of observations is the sum of the frequency variable, sum(X\$Freq), sum(X[,"Freq"]) or a similar expression.

{ex:ch2-GSS}

EXAMPLE 2.3: General social survey

For small frequency tables, it is often convenient to enter them in frequency form using expand.grid() for the factors and c() to list the counts in a vector. The example below, from Agresti (2002) gives results for the 1991 General Social Survey, with respondents classified by sex and party identification. As a table, the data look like this:

| | | party | |
|--------|-----|-------|-----|
| sex | dem | indep | rep |
| female | 279 | 73 | 225 |
| male | 165 | 47 | 191 |

We use expand.grid() to create a 6×2 matrix containing the combinations of sex and party with the levels for sex given first, so that this varies most rapidly. Then, input the frequencies in the table by columns from left to right, and combine these two results with data.frame().

```
> tmp
    sex party
1 female dem
         dem
   male
  female indep
   male indep
 female rep
   male rep
> GSS <- data.frame(tmp, count = c(279, 165, 73, 47, 225, 191))
    sex party count
1 female
         dem
   male
          dem
               165
3 female indep
                7.3
   male indep
                47
               225
5 female rep
   male
         rep
> names (GSS)
           "party" "count"
[1] "sex"
> str(GSS)
'data.frame': 6 obs. of 3 variables:
 $ sex : Factor w/ 2 levels "female", "male": 1 2 1 2 1 2
 $ party: Factor w/ 3 levels "dem", "indep", ..: 1 1 2 2 3 3
 $ count: num 279 165 73 47 225 191
```

```
> sum(GSS$count)
[1] 980
```

The last line above shows that there are 980 cases represented in the frequency table.

Δ

2.2.3 Table form

Table form data is represented as a matrix, array or table object whose elements are the frequencies in an n-way table. The number of dimensions of the table is the length, length (dim(X)), of its dim (or dimnames) attribute, and the sizes of the dimensions in the table are the elements of dim(X). The total number of observations represented is the sum of all the frequencies, sum(X).

{ex:ch2-hec}

EXAMPLE 2.4: Hair color and eye color

A classic data set on frequencies of hair color, eye color and sex is given in table form in HairEyeColor in the datasets package, reporting the frequencies of these categories for 592 students in a statistics course.

```
> data(HairEyeColor, package = "datasets") # load the data
> str(HairEyeColor)
                                   # show the structure
 table [1:4, 1:4, 1:2] 32 53 10 3 11 50 10 30 10 25 ...
 - attr(*, "dimnames")=List of 3
  ..$ Hair: chr [1:4] "Black" "Brown" "Red" "Blond"
  ..$ Eye : chr [1:4] "Brown" "Blue" "Hazel" "Green"
  ..$ Sex : chr [1:2] "Male" "Female"
> dim(HairEyeColor)
                                    # table dimension sizes
[1] 4 4 2
> dimnames (HairEyeColor)
                                    # variable and level names
[1] "Black" "Brown" "Red"
                            "Blond"
[1] "Brown" "Blue" "Hazel" "Green"
$Sex
[1] "Male"
             "Female"
> sum(HairEyeColor)
                                    # number of cases
[1] 592
```

Three-way (and higher-way) tables can be printed in a more convenient form using structable () and ftable () as described below in Section 2.5. \triangle

Tables are often created from raw data in case form or frequency form using the functions table() and xtabs() described in Section 2.4.1. For smallish frequency tables that are already in tabular form, you can enter the frequencies in a matrix, and then assign dimnames and other attributes.

To illustrate, we create the GSS data as a table below, entering the values in the table by rows (byrow=TRUE), as they appear in printed form.

```
> GSS.tab <- matrix(c(279, 73, 225,

+ 165, 47, 191),

+ nrow = 2, ncol = 3, byrow = TRUE)

> dimnames(GSS.tab) <- list(sex = c("female", "male"),

+ party = c("dem", "indep", "rep"))

> GSS.tab

party
sex dem indep rep
female 279 73 225
male 165 47 191
```

GSS.tab is a matrix, not an object of class("table"), and some functions are happier with tables than matrices.⁴ You should therefore coerce it to a table with as.table(),

```
> GSS.tab <- as.table(GSS.tab)
> str(GSS.tab)

table [1:2, 1:3] 279 165 73 47 225 191
- attr(*, "dimnames")=List of 2
..$ sex : chr [1:2] "female" "male"
..$ party: chr [1:3] "dem" "indep" "rep"
```

{ex:jobsat1}

EXAMPLE 2.5: Job satisfaction

Here is another similar example, entering data on job satisfaction classified by income and level of satisfaction from a 4×4 table given by Agresti (2002, Table 2.8, p. 57).

```
> ## A 4 x 4 table Agresti (2002, Table 2.8, p. 57) Job Satisfaction
> JobSat <- matrix(c(1, 2, 1, 0,
                      3, 3, 6, 1,
10, 10, 14, 9,
6, 7, 12, 11),
                     nrow = 4, ncol = 4)
> dimnames(JobSat) <-</pre>
    list(income = c("< 15k", "15-25k", "25-40k", "> 40k"),
         satisfaction = c("VeryD", "LittleD", "ModerateS", "VeryS"))
> JobSat <- as.table(JobSat)</pre>
> JobSat.
        satisfaction
income VeryD LittleD ModerateS VeryS
  < 15k
                    3 10
              2
                      3
                                10
  15-25k
  25-40k
              1
                       6
                                14
                                       12
 > 40k
```

Δ

2.3 Ordered factors and reordered tables

{sec:ordered}

As we saw above (Example 2.1), the levels of factor variables in data frames (case form or frequency form) can be re-ordered (and the variables declared as ordered factors) using ordered (). As well, the order of the factor values themselves can be rearranged by sorting the data frame using sort (). However, in table form, the values of the table factors are ordered by their position in the table.

⁴There are quite a few functions in R with specialized methods for "table" objects. For example, plot (GSS.tab) gives a mosaic plot and barchart (GSS.tab) gives a divided bar chart.

Thus in the JobSat data, both income and satisfaction represent ordered factors, and the *positions* of the values in the rows and columns reflects their ordered nature, but only implicitly.

Yet, for analysis or graphing, there are occasions when you need *numeric* values for the levels of ordered factors in a table, e.g., to treat a factor as a quantitative variable. In such cases, you can simply re-assign the dimnames attribute of the table variables. For example, here, we assign numeric values to income as the middle of their ranges, and treat satisfaction as equally spaced with integer scores.

```
> dimnames(JobSat)$income <- c(7.5, 20, 32.5, 60)
> dimnames(JobSat)$satisfaction <- 1:4</pre>
```

A related case is when you want to preserve the character labels of table dimensions, but also allow them to be sorted in some particular order. A simple way to do this is to prefix each label with an integer index using paste().

```
> dimnames(JobSat) $income <-
+     paste(1:4, dimnames(JobSat) $income, sep = ":")
> dimnames(JobSat) $satisfaction <-
+     paste(1:4, dimnames(JobSat) $satisfaction, sep = ":")</pre>
```

A different situation arises with tables where you want to *permute* the levels of one or more variables to arrange them in a more convenient order without changing their labels. For example, in the <code>HairEyeColor</code> table, hair color and eye color are ordered arbitrarily. For visualizing the data using mosaic plots and other methods described later, it turns out to be more useful to assure that both hair color and eye color are ordered from dark to light. Hair colors are actually ordered this way already: "Black", "Brown", "Red", "Blond". But eye colors are ordered as "Brown", "Blue", "Hazel", "Green". It is easiest to re-order the eye colors by indexing the columns (dimension 2) in this array to a new order, "Brown", "Hazel", "Green", "Blue", giving the indices of the old levels in the new order (here: 1,3,4,2). Again str () is your friend, showing the structure of the result to check that the result is what you want.

```
> data(HairEyeColor, package = "datasets")
> HEC <- HairEyeColor[, c(1, 3, 4, 2), ]
> str(HEC)

num [1:4, 1:4, 1:2] 32 53 10 3 10 25 7 5 3 15 ...
- attr(*, "dimnames")=List of 3
    ..$ Hair: chr [1:4] "Black" "Brown" "Red" "Blond"
    ..$ Eye : chr [1:4] "Brown" "Hazel" "Green" "Blue"
    ..$ Sex : chr [1:2] "Male" "Female"
```

Finally, there are situations where, particularly for display purposes, you want to re-order the *dimensions* of an *n*-way table, and/or change the labels for the variables or levels. This is easy when the data are in table form: aperm() permutes the dimensions, and assigning to names and dimnames changes variable names and level labels respectively.

```
> str(UCBAdmissions)

table [1:2, 1:2, 1:6] 512 313 89 19 353 207 17 8 120 205 ...
- attr(*, "dimnames")=List of 3
    ..$ Admit : chr [1:2] "Admitted" "Rejected"
    ..$ Gender: chr [1:2] "Male" "Female"
    ..$ Dept : chr [1:6] "A" "B" "C" "D" ...

> UCB <- aperm(UCBAdmissions, c(2, 1, 3))
> dimnames(UCB) $Admit <- c("Yes", "No")
> names(dimnames(UCB)) <- c("Sex", "Admitted", "Department")
> str(UCB)
```

```
table [1:2, 1:2, 1:6] 512 89 313 19 353 17 207 8 120 202 ...

- attr(*, "dimnames")=List of 3

..$ Sex : chr [1:2] "Male" "Female"

..$ Admitted : chr [1:2] "Yes" "No"

..$ Department: chr [1:6] "A" "B" "C" "D" ...
```

2.4 Generating tables with table() and xtabs()

{sec:table}

With data in case form or frequency form, you can generate frequency tables from factor variables in data frames using the table() function; for tables of proportions, use the prop.table() function, and for marginal frequencies (summing over some variables) use margin.table(). The examples below use the same case-form data frame mydata used earlier (Section 2.1.4).

```
> set.seed(12345) # reproducibility
> n <- 100
> A <- factor(sample(c("a1", "a2"), n, replace = TRUE))
> B <- factor(sample(c("b1", "b2"), n, replace = TRUE))
> sex <- factor(sample(c("M", "F"), n, replace = TRUE))
> age <- round(rnorm(n, mean = 30, sd = 5))
> mydata <- data.frame(A, B, sex, age)</pre>
```

2.4.1 table()

{sec:table}

table (...) takes a list of variables interpreted as factors, or a data frame whose columns are so interpreted. It does not take a data= argument, so either supply the names of columns in the data frame, or select the variables using column indexes:

We can use margin.table (X, margin) to sum a table X for the indices in margin, i.e., over the dimensions not included in margin. A related function is addmargins (X, margin, FUN = sum), which extends the dimensions of a table or array with the marginal values calculated by FUN.

```
> margin.table(mytab) # sum over A & B

[1] 100
> margin.table(mytab, 1) # A frequencies (summed over B)

A
a1 a2
48 52
```

The function prop.table() expresses the table entries as a fraction of a given marginal table.

```
> prop.table(mytab)
                    # cell proportions
     b1 b2
 a1 0.18 0.30
 a2 0.22 0.30
> prop.table(mytab, 1)
                         # row proportions
    В
         b1
                 b2
  a1 0.37500 0.62500
  a2 0.42308 0.57692
> prop.table(mytab, 2)
                          # column proportions
      b1
          b2
 a1 0.45 0.50
 a2 0.55 0.50
```

 ${\tt table}$ () can also generate multidimensional tables based on 3 or more categorical variables. In this case, use the ${\tt ftable}$ () or ${\tt structable}$ () function to print the results more attractively as a "flat" (2-way) table.

TODO: DM: is there any advantage of ftable() over structable()? I think not, so just use structable()?

table() ignores missing values by default, but has optional arguments useNA and exclude that can be used to control this. See help(table) for the details.

2.4.2 xtabs()

{sec:xtabs}

The xtabs() function allows you to create cross tabulations of data using formula style input. This typically works with case-form or frequency-form data supplied in a data frame or a matrix.

The result is a contingency table in array format, whose dimensions are determined by the terms on the right side of the formula. As shown below, the summary method for tables produces a simple χ^2 test of independence of all factors, and indicates the number of cases and dimensions.

```
> # 3-Way Frequency Table
> mytable <- xtabs(~ A + B + sex, data = mydata)
> ftable(mytable) # print table
      sex F M
  В
a1 b1
           9
             9
          15 15
   b2
         12 10
a2 b1
   b2
         19 11
                     # chi-squared test of independence
> summary (mytable)
Call: xtabs(formula = ~A + B + sex, data = mydata)
Number of cases in table: 100
Number of factors: 3
Test for independence of all factors:
Chisq = 1.54, df = 4, p-value = 0.82
```

When the data have already been tabulated in frequency form, include the frequency variable (usually count or Freq) on the left side of the formula, as shown in the example below for the GSS data.

For "table" objects, the plot method produces basic mosaic plots using the mosaicplot () function.

2.5 Printing tables with structable() and ftable()

{sec:structable}

2.5.1 Text output

For 3-way and larger tables, the functions ftable () (in the stats package) and structable () (in VCd) provide a convenient and flexible tabular display in a "flat" (2-way) format.

With ftable (X, row.vars=, col.vars=), variables assigned to the rows and/or columns of the result can be specified as the integer numbers or character names of the variables in the array X. By default, the last variable is used for the columns. The formula method, in the form ftable (colvars ~ rowvars, data) allows a formula, where the left and right hand side of formula specify the column and row variables respectively.

```
ftable (UCB)
                                     # default
                                                      F
                                    В
                                         C
                                             D
                                                 \mathbf{E}
                 Department
Sex
       Admitted
                              512 353 120 138
                                                53
Male
       Yes
                              313 207 205 279 138 351
       No
                                               94
                                   17 202 131
Female Yes
                               89
                                    8 391 244 299 317
       No
> #ftable(UCB, row.vars = 1:2)
                                       # same result
   ftable(Admitted + Sex ~ Department, data = UCB)
                                                          # formula method
            Admitted Yes
                     Male Female Male Female
Department
                       512
                                    313
                                             19
В
                       353
                                17
                                    207
                                              8
С
                       120
                               202
                                    205
                                            391
D
                               131
                                    279
                                            244
                       138
Ε
                        53
                                94
                                    138
                                            299
                                            317
F
                        22
                                24
                                    351
```

The structable() function is similar, but more general, and uses recursive splits in the vertical or horizontal directions (similar to the construction of mosaic displays). It works with both data frames and table objects.

```
> structable(HairEyeColor)
                                                 # show the table: default
              Eye Brown Blue Hazel Green
Hair
     Sex
Black Male
                           11
                                  10
      Female
                      36
                                         2
                           50
Brown Male
                      53
                                  25
                                        15
                      66
                           34
                                  29
      Female
                                        14
      Male
                      10
                           10
                            7
                                   7
                                         7
      Female
                      16
Blond Male
                           30
                                   5
                                         8
                                   5
                                         8
      Female
                      4
                           64
> structable(Hair + Sex ~ Eye, HairEyeColor)
                                                   # specify col ~ row variables
      Hair Black
                          Brown
                                         Red
      Sex
            Male Female
                          Male Female Male Female Male Female
Eye
                             53
Brown
               32
                                     66
                                          10
                                                                  4
Blue
               11
                        9
                             50
                                     34
                                          10
                                                         30
                                                                64
                        5
Hazel
               10
                             25
                                     29
                                           7
                                                          5
                                                                 5
                                                                  8
                             15
                                     14
```

It also returns an object of class "structable" for which there are a variety of special methods. For example, the transpose function t() interchanges rows and columns, so that a call like t(structable(HairEyeColor)) produces the second result shown just above; "structable" objects can be subset using the [and [[operators, using either level indices or names. There are also plot methods: for example, plot() produces mosaic plots.

```
# save structable object
> HSE <- structable (Hair + Sex ~ Eye, HairEyeColor)
> HSE[1:2,]
                                                         # subset rows
      Hair Black
                         Brown
                                        Red
                                                   Blond
                         Male Female Male Female
            Male Female
                                                    Male Female
Eye
Brown
                                    66
Blue
              11
                            50
                                    34
                                         10
                                                       30
                                                              64
```

2.6 Collapsing tables

{sec:collapsetables}

{sec:collapse}

It sometimes happens that we have a data set with more variables or factors than we want to analyse, or else, having done some initial analyses, we decide that certain factors are not important, and so should be excluded from graphic displays by collapsing (summing) over them. For example, mosaic plots and fourfold displays are often simpler to construct from versions of the data collapsed over the factors which are not shown in the plots.

The appropriate tools to use again depend on the form in which the data are represented—a case-form data frame, a frequency-form data frame (aggregate()), or a table-form array or table object (margin.table() or apply()).

When the data are in frequency form, and we want to produce another frequency data frame, aggregate() is a handy tool, using the argument FUN = sum to sum the frequency variable over the factors *not* mentioned in the formula.

{ex:dayton1}

EXAMPLE 2.6: Dayton survey

The data frame DaytonSurvey in the vcdExtra package represents a 2^5 table giving the frequencies of reported use ("ever used?") of alcohol, cigarettes and marijuana in a sample of 2276 high school seniors, also classified by sex and race.

```
> data(DaytonSurvey, package = "vcdExtra")
> str(DaytonSurvey)
'data.frame': 32 obs. of 6 variables:
 $ cigarette: Factor w/ 2 levels "Yes", "No": 1 2 1 2 1 2 1 2 1 2
 $ alcohol : Factor w/ 2 levels "Yes", "No": 1 1 2 2 1 1 2 2 1 1
 $ marijuana: Factor w/ 2 levels "Yes", "No": 1 1 1 1 2 2 2 2 1 1 ...
           : Factor w/ 2 levels "female", "male": 1 1 1 1 1 1 1 2 2 : Factor w/ 2 levels "white", "other": 1 1 1 1 1 1 1 1 1 1
             : num 405 13 1 1 268 218 17 117 453 28 ...
 $ Freq
> head (DaytonSurvey)
  cigarette alcohol marijuana
                                    sex race Freq
                            Yes female white
        Yes
                 Yes
                                                405
         No
                            Yes female white
                  Yes
         Yes
                  No
                            Yes female white
         No
                  No
                             Yes female white
         Yes
                  Yes
                              No female white
                                                 268
6
         No
                             No female white
```

To focus on the associations among the substances, we want to collapse over sex and race. The right-hand side of the formula used in the call to aggregate() gives the factors to be retained in the new frequency data frame, Dayton_ACM_df. The left-hand side is the frequency variable (Freq), and we aggregate using the FUN = sum.

```
> # data in frequency form: collapse over sex and race
> Dayton_ACM_df <- aggregate (Freq ~ cigarette + alcohol + marijuana,
                             data = DaytonSurvey, FUN = sum)
> Dayton_ACM_df
  cigarette alcohol marijuana Freq
                           Yes
                                911
        Yes
                Yes
         No
                Yes
                           Yes
        Yes
                 No
                           Yes
                                  3
                 No
```

| _ | | | | |
|---|-----|-----|----|-----|
| 5 | Yes | Yes | No | 538 |
| 6 | No | Yes | No | 456 |
| 7 | Yes | No | No | 43 |
| 8 | No | No | No | 279 |

 \triangle

When the data are in table form, and we want to produce another table, apply() with FUN = sum can be used in a similar way to sum the table over dimensions not mentioned in the MARGIN argument. margin.table() is just a wrapper for apply() using the sum() function.

{ex:davton2}

EXAMPLE 2.7: Dayton survey

To illustrate, we first convert the <code>DaytonSurvey</code> to a 5-way table using <code>xtabs()</code>, <code>giving Dayton_tab</code>.

```
> # convert to table form
> Dayton_tab <- xtabs(Freq ~ cigarette + alcohol + marijuana + sex + race,
                     data = DaytonSurvey)
> structable(cigarette + alcohol + marijuana ~ sex + race, data = Dayton_tab)
            cigarette Yes
                                       No
            alcohol Yes
                               No
                                      Yes
                                               No
            marijuana Yes No Yes No Yes
                                          No Yes
                                                   No
      race
                      405 268
                                   17
                                       13 218
female white
                                1
                                                1 117
      other
                       23 23
                                0
                                    1
                                          19
                                                0
male
      whit.e
                       453 228
                                1 17 28 201
                                                1 133
      other
                       30 19
                               1 8 1 18
```

Then, use <code>apply()</code> on <code>Dayton_tab</code> to give the 3-way table <code>Dayton_ACM_tab</code> summed over sex and race. The elements in this new table are the column sums for <code>Dayton.tab</code> shown by <code>structable()</code> just above.

Δ

(Note that structable () would do the collapsing job for us anyway.)

TODO: DM: plyr seems too much here -> remove?

Many of these operations can be performed using the $\star\star ply()$ functions in the plyr package. For example, with the data in a frequency form data frame, use ddply() to collapse over unmentioned factors, and summarise() as the function to be applied to each piece.

```
> Dayton_ACM_df <- ddply(DaytonSurvey, .(cigarette, alcohol, marijuana),
+ summarise, Freq = sum(Freq))</pre>
```

2.6.2 Collapsing table levels: collapse.table()

A related problem arises when we have a table or array and for some purpose we want to reduce the number of levels of some factors by summing subsets of the frequencies. For example, we may have initially coded Age in 10-year intervals, and decide that, either for analysis or display purposes, we want to reduce Age to 20-year intervals. The collapse.table() function in vcdExtra was designed for this purpose.

{ex:collapse-cat}

EXAMPLE 2.8: Collapsing categories

Create a 3-way table, and collapse Age from 10-year to 20-year intervals and Education from three levels to two. To illustrate, we first generate a $2 \times 6 \times 3$ table of random counts from a Poisson distribution with mean of 100, with factors sex, age and education.

```
> # create some sample data in frequency form
> set.seed(12345)
                     # reproducibility
                   "Female")
 sex <- c("Male",
 age <- c("10-19", "20-29",
                                "30-39", "40-49", "50-59", "60-69")
> education <- c("low", "med", "high")</pre>
> dat <- expand.grid(sex = sex, age = age, education = education)
> counts <- rpois(36, 100)
                               # random Poisson cell frequencies
> dat <- cbind(dat, counts)</pre>
> # make it into a 3-way table
> tab1 <- xtabs (counts ~ sex + age + education, data = dat)
> structable(tab1)
                  age 10-19 20-29 30-39 40-49 50-59 60-69
sex
       education
Male
                        105
                               98
                                     123
                                            97
                                                        105
                         74
                               113
                                     114
                                            82
                                                   95
                                                         85
       med
                        121
                               116
                                     104
                                            103
                                                   89
                                                        100
       high
Female low
                        107
                               95
                                     105
                                           116
                                                  103
                                                         92
                         96
                               88
                                      93
                                           118
                                                   99
                                                        108
       med
                        120
                               102
                                      96
                                           103
                                                  127
       high
```

Now collapse age to 20-year intervals, and education to 2 levels. In the arguments to collapse.table(), levels of age and education given the same label are summed in the resulting smaller table.

```
> # collapse age to 3 levels, education to 2 levels
> tab2 <- collapse.table(tab1,
           age=c("10-29", "10-29", "30-49", "30-49", "50-69", "50-69"),
           education=c("<high", "<high", "high"))
  structable (tab2)
                 age 10-29 30-49 50-69
       education
                        390
       <high
                              416
                                    380
Male
                        237
                              207
                                    189
                        386
                              432
                                    402
Female <high
       high
                              199
```

Δ

TODO: DM: Add section on subsetting tables using subset(), and the [and [[methods for tables and structables. These skills are required in some examples.

2.7 Converting among frequency tables and data frames

{sec:convert}

As we've seen, a given contingency table can be represented equivalently in case form, frequency form and table form. However, some R functions were designed for one particular representation.

Table 2.1 gives an overview on some handy tools (with sketched usage) for converting from one form to another, discussed below.

{tab:convert}

Table 2.1: Tools for converting among different forms for categorical data

| | To this | | | | | |
|---------------------------|-----------------------------|--|----------------------|--|--|--|
| From this | Case form | Frequency form | Table form | | | |
| Case form | | <pre>Z <- xtabs(~ A + B) as.data.frame(Z)</pre> | table(A, B) | | | |
| Frequency form Table form | expand.dft(X) expand.dft(X) | as.data.frame(X) | xtabs(count ~ A + B) | | | |

2.7.1 Table form to frequency form

A contingency table in table form (an object of class "table") can be converted to a data frame in frequency form with as.data.frame(). The resulting data frame contains columns representing the classifying factors and the table entries (as a column named by the responseName argument, defaulting to Freq. The function as.data.frame() is the inverse of xtabs(), which converts a data frame to a table.

{ex:GSS-convert}

EXAMPLE 2.9: General social survey

Convert the GSStab in table form to a data frame in frequency form. By default, the frequency variable is named Freq, and the variables sex and party are made factors.

```
> as.data.frame(GSStab)

    sex party Freq
1 female dem 279
2 male dem 165
3 female indep 73
4 male indep 47
5 female rep 225
6 male rep 191
```

Δ

In addition, there are situations where numeric table variables are represented as factors, but you need to convert them to numerics for calculation purposes.

{ex:horse.df}

EXAMPLE 2.10: Death by horse kick

For example, We might want to calculate the weighted mean of nDeaths in the HorseKicks data. Using as.data.frame() won't work here, because the variable nDeaths becomes a factor.

```
> str(as.data.frame(HorseKicks))
'data.frame': 5 obs. of 2 variables:
$ nDeaths: Factor w/ 5 levels "0","1","2","3",..: 1 2 3 4 5
$ Freq : int 109 65 22 3 1
```

 $^{^5}$ Because R is object-oriented, this is actually a short-hand for the function as.data.frame.table().

One solution is to use data.frame() directly and as.numeric() to coerce the table names to numbers.

```
> horse.df <- data.frame(nDeaths = as.numeric(names(HorseKicks)),
                        Freq = as.vector(HorseKicks))
> str(horse.df)
'data.frame': 5 obs. of 2 variables:
$ nDeaths: num 0 1 2 3 4
 $ Freq : int 109 65 22 3 1
> horse.df
 nDeaths Freq
      0 109
2
           65
       1
           22
3
       2
       3
            3
```

Then, weighted.mean() works as we would like:

```
> weighted.mean(horse.df$nDeaths, weights=horse.df$Freq)
[1] 2
```

Δ

2.7.2 Case form to table form

{ex:Arth-convert}

Going the other way, we use table () to convert from case form to table form.

EXAMPLE 2.11: Arthritis treatment

Convert the Arthritis data in case form to a 3-way table of Treatment \times Sex \times Improved. We select the desired columns with their names, but could also use column numbers, e.g., table (Arthritis [, c(2, 3, 5)])

```
> Art.tab <- table(Arthritis[,c("Treatment", "Sex", "Improved")])</pre>
> str(Art.tab)
 'table' int [1:2, 1:2, 1:3] 19 6 10 7 7 5 0 2 6 16 ...
 - attr(*, "dimnames") = List of 3
  ..$ Treatment: chr [1:2] "Placebo" "Treated"
..$ Sex : chr [1:2] "Female" "Male"
  ..$ Improved : chr [1:3] "None" "Some" "Marked"
> ftable(Art.tab)
                   Improved None Some Marked
Treatment Sex
                                19
                                       7
Placebo Female
                                               6
           Male
                                10
                                       0
                                               1
                                       5
                                             16
Treated
           Female
                                 6
           Male
```

2.7.3 Table form to case form

There may also be times that you will need an equivalent case form data frame with factors representing the table variables rather than the frequency table. For example, the mca() function in package MASS (for multiple correspondence analysis) only operates on data in this format. The function expand.dft() ⁶ in vcdExtra does this, converting a table into a case form.

{ex:Arth-convert2}

EXAMPLE 2.12: Arthritis treatment

Convert the Arthritis data in table form (Art.tab) back to a data.frame in case form, with factors Treatment, Sex and Improved.

```
> Art.df <- expand.dft(Art.tab)
> str(Art.df)

'data.frame': 84 obs. of 3 variables:
$ Treatment: Factor w/ 2 levels "Placebo", "Treated": 1 1 1 1 1 1 1 1 1 1 1 ...
$ Sex : Factor w/ 2 levels "Female", "Male": 1 1 1 1 1 1 1 1 1 1 ...
$ Improved : Factor w/ 3 levels "Marked", "None",...: 2 2 2 2 2 2 2 2 2 2 ...
```

 \triangle

2.7.4 Publishing tables to LATEX or HTML

OK, you've read your data into R, done some analysis, and now want to include some tables in a LATEX document or in a web page in HTML format. Formatting tables for these purposes is often tedious and error-prone.

There are a great many packages in R that provide for nicely formatted, publishable tables for a wide variety of purposes; indeed, most of the tables in this book are generated using these tools. See Leifeld (2013) for description of the texreg package and a comparison with some of the other packages.

Here, we simply illustrate the xtable package, which, along with capabilities for statistical model summaries, time-series data, and so forth, has a xtable.table method for one-way and two-way table objects.

The HorseKicks data is a small one-way frequency table described in Example ?? and containing the frequencies of 0, 1, 2, 3, 4 deaths per corps-year by horse-kick among soldiers in 20 corps in the Prussian army.

```
> data(HorseKicks, package = "vcd")
> HorseKicks

nDeaths
    0     1     2     3     4
109     65     22     3     1
```

By default, xtable() formats this in LaTeXas a vertical table, and prints the LaTeX markup to the R console. This output is shown below (without the usual ## comment used to indicate R output).

```
> library(xtable)
> xtable(HorseKicks)
% latex table generated in R 3.1.1 by xtable 1.8-0 package
% Thu Jan 01 15:48:31 2015
\begin{table}[ht]
\centering
\begin{tabular}{rr}
```

⁶The original code for this function was provided by Marc Schwarz on the R-Help mailing list.

```
\hline
& nDeaths \\
\hline
0 & 109 \\
1 & 65 \\
2 & 22 \\
3 & 3 \\
4 & 1 \\
\hline
\end{tabular}
\end{table}
```

When this is rendered in a LATEX document, the result of xtable() appears as shown in the table below.

```
> xtable(HorseKicks)
```

| | nDeaths |
|---|---------|
| 0 | 109 |
| 1 | 65 |
| 2 | 22 |
| 3 | 3 |
| 4 | 1 |

The table above isn't quite right, because the column label "nDeaths" belongs to the first column, and the second column should be labeled "Freq". To correct that, we convert the <code>HorseKicks</code> table to a data frame (see Section 2.7 for details), add the appropriate <code>colnames</code>, and use the <code>xtable.print</code> method to supply some other options.

```
> tab <- as.data.frame(HorseKicks)
> colnames(tab) <- c("nDeaths", "Freq")
> print(xtable(tab), include.rownames = FALSE, include.colnames = TRUE)
```

| nDeaths | Freq |
|---------|------|
| 0 | 109 |
| 1 | 65 |
| 2 | 22 |
| 3 | 3 |
| 4 | 1 |

TODO: DM: The code looks quite complicated and the result is not satisfying (no separator between header and table) - maybe too confusing?

Finally, in Chapter 3, we display a number of similar one-way frequency tables in a transposed form to save display space. Table 3.3 is the finished version we show there. The code below uses the following techniques: (a) addmargins () is used to show the sum of all the frequency values; (b) t () transposes the data frame to have 2 rows; (c) rownames () assigns the labels we want for the rows; (d) using the caption argument provides a table caption, and a numbered table in LATEX; (d) column alignment ("r" or "l") for the table columns is computed as a character string used for the align argument.

```
> horsetab <- t(as.data.frame(addmargins(HorseKicks)))
> rownames(horsetab) <- c( "Number of deaths", "Frequency" )
> horsetab <- xtable(horsetab, digits = 0,
+ caption = "von Bortkiewicz's data on deaths by horse kicks",
+ align = paste0("l|", paste(rep("r", ncol(horsetab)), collapse = ""))
+ )
> print(horsetab, include.colnames = FALSE)
```

| Number of deaths | 0 | 1 | 2 | 3 | 4 | Sum |
|------------------|-----|----|----|---|---|-----|
| Frequency | 109 | 65 | 22 | 3 | 1 | 200 |

Table 2.2: von Bortkiewicz's data on deaths by horse kicks

TODO: DM: also show HTML version? – I think this is unnecessary

2.8 A complex example: TV viewing data

{sec:working-complex}

If you have followed so far, congratulations! You are ready for a more complicated example that puts together a variety of the skills developed in this chapter: (a) reading raw data, (b) creating tables, (c) assigning level names to factors and (d) collapsing levels or variables for use in analysis.

For an illustration of these steps, we use the dataset tv.dat, supplied with the initial implementation of mosaic displays in R by Jay Emerson. In turn, they were derived from an early, compelling example of mosaic displays (Hartigan and Kleiner, 1984), that illustrated the method with data on a large sample of TV viewers whose behavior had been recorded for the Neilsen ratings. This data set contains sample television audience data from Neilsen Media Research for the week starting November 6, 1995.

The data file, tv.dat is stored in frequency form as a file with 825 rows and 5 columns. There is no header line in the file, so when we use read.table() below, the variables will be named V1-V5. This data represents a 4-way table of size $5\times11\times5\times3=825$ where the table variables are V1-V4, and the cell frequency is read as V5.

The table variables are:

```
V1- values 1:5 correspond to the days Monday-Friday;
```

V2-values 1:11 correspond to the quarter hour times 8:00PM through 10:30PM;

V3- values 1:5 correspond to ABC, CBS, NBC, Fox, and non-network choices;

V4- values 1:3 correspond to transition states: turn the television Off, Switch channels, or Persist in viewing the current channel.

2.8.1 Creating data frames and arrays

The file tv.dat is stored in the doc/extdata directory of vcdExtra; it can be read as follows:

```
> tv_data <- read.table(system.file("doc", "extdata", "tv.dat", package = "vcdExtra"))
> str(tv_data)

'data.frame': 825 obs. of 5 variables:
$ V1: int 1 2 3 4 5 1 2 3 4 5 ...
$ V2: int 1 1 1 1 1 2 2 2 2 2 2 ...
$ V3: int 1 1 1 1 1 1 1 1 1 1 ...
$ V4: int 1 1 1 1 1 1 1 1 1 ...
$ V5: int 6 18 6 2 11 6 29 25 17 29 ...
```

To read such data from a local file, just use read.table() in this form:

```
> tv_data <- read.table("C:/R/data/tv.dat")

or
> tv_data <- file.choose()</pre>
```

to select the path using the file chooser tool.

We could use this data in frequency form for analysis by renaming the variables, and converting the integer-coded factors V1 - V4 to R factors. The lines below use the function within() to avoid having to use TV.dat\$Day <- factor(TV.dat\$Day) etc., and only supplies labels for the first variable.

Alternatively, we could just reshape the frequency column (V5 or $tv_data[,5]$) into a 4-way array. In the lines below, we rely on the facts that the (a) the table is complete—there are no missing cells, so $nrow(tv_data)=825$; (b) the observations are ordered so that V1 varies most rapidly and V4 most slowly. From this, we can just extract the frequency column and reshape it into an array using the dim argument. The level names are assigned to dimnames (TV) and the variable names to names (dimnames (TV)).

More generally (even if there are missing cells), we can use xtabs() to do the cross-tabulation, using V5 as the frequency variable. Here's how to do this same operation with xtabs():

Note that in the lines above, the variable names are assigned directly as the names of the elements in the dimnames list.

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2.8.2 Subsetting and collapsing

For many purposes, the 4-way table TV is too large and awkward to work with. Among the networks, Fox and Other occur infrequently, so we will remove them. We can also cut it down to a 3-way table by considering only viewers who persist with the current station.⁷

```
TV <- TV[,,1:3,]
TV <- TV[,,,3]
                          # keep only ABC, CBS, NBC
                           # keep only Persist -- now a 3 way table
> structable(TV)
             Time 8:00 8:15 8:30 8:45 9:00 9:15 9:30 9:45 10:00 10:15 10:30
Day Network
Mon ABC
                     146
    CBS
                     337
                          293
                                304
                                      233
                                           311
                                                 251
                                                       241
                                                             164
                                                                           265
    NBC
                     263
                          219
                                236
                                      140
                                                       239
                                                                           263
                                                                                  283
Tue ABC
                     244
                          181
                                231
                                      205
                                            385
                                                 283
                                                       345
                                                                           351
                                                                                  364
    CBS
                          180
                                184
                                      109
                                            218
                                                 235
                                                       256
    NBC
                     315
                          254
                                280
                                      241
                                            370
                                                 214
                                                       195
                                                                           190
                                194
                                            339
    ABC
                          126
                                                 103
Thu ABC
                          183
                                            187
                                                       211
                                                                    110
    CBS
                     196
                          185
                                195
                                      104
                                            106
                                                       116
    NBC
                     515
                          463
                                            590
                                                 473
                                                       446
                                                             349
                                                                    649
                                                                           705
                                                                                  747
                          281
                                305
                                      239
                                           278
                                                 246
                                                       245
                                                             138
                                                                           232
                                                                                  233
Fri ABC
                                                                    246
                                154
                                       81
                                           129
                                                 153
                                                       136
                                                                    138
                                                                           136
                                                                                  152
    CBS
                     130
                          144
                                2.48
                                     160
                                           172
                                                 164
                                                       169
```

Finally, for some purposes, we might also want to collapse the 11 times into a smaller number. Here, we use collapse.table(), which was designed for this purpose. **Done:** DM: Why not using collapse.table() as introduced before?

```
> TV2 <- collapse.table(TV,
                         Time=c(rep("8:00-8:59", 4),
                           rep("9:00-9:59", 4), rep("10:00-10:44", 3)))
 structable(Day ~ Time + Network, TV2)
                    Day Mon Tue
                                    Wed
                                          Thu Fri
Time
            Network
8:00-8:59
            ABC
                          536
                               861
                                    744
                                          735 1119
            CBS
                         1167 646
                                    550
                                         680
                                               509
                          858 1090
                                    512 1927
            NBC.
                                               823
9:00-9:59
            ABC
                         1401 1205
                                   1022
                               959
            CBS
                          967
                                    409
                                          385
                                               544
                          946
                               890
                                     831 1858
                                               590
10:00-10:44 ABC
                          910 1044
                                     668
                                          349
                                               711
                          789
                               798
                                     324
                                          270
            CBS
                          825
            NBC
                               588
                                    869 2101
```

Congratulations! If you followed the operations described above, you are ready for the material described in the rest of the book. If not, try working through some of exercises below.

2.9 Lab exercises

{lab:21} {sec:ch02-exercises}

Exercise 2.1 The packages vcd and vcdExtra contain many data sets with some examples of analysis and graphical display. The goal of this exercise is to familiarize yourself with these resources. You can get a brief summary of these using the function datasets(). Use the following to get a list of these with some characteristics and titles.

⁷This relies on the fact that indexing an array drops dimensions of length 1 by default, using the argument drop = TRUE; the result is coerced to the lowest possible dimension.

- (a) How many data sets are there altogether? How many are there in each package?
- (b) Make a tabular display of the frequencies by Package and class.
- (c) Choose one or two data sets from this list, and examine their help files (e.g., help (Arthritis) or ?Arthritis). You can use, e.g., example (Arthritis) to run the R code for a given example.

{lab:2.2}

Exercise 2.2 The data set UCBADdmissions is a 3-way table of frequencies classified by Admit, Gender and Dept.

- (a) Find the total number of cases contained in this table.
- (b) For each department, find the total number of applicants.
- (c) For each department, find the overall proportion of applicants who were admitted.
- (d) Construct a tabular display of department (rows) and gender (columns), showing the proportion of applicants in each cell who were admitted.

{lab:2.3}

Exercise 2.3 The data set DanishWelfare in vcd gives a 4-way, $3 \times 4 \times 3 \times 5$ table as a data frame in frequency form, containing the variable Freq and four factors, Alcohol, Income, Status and Urban. The variable Alcohol can be considered as the response variable, and the others as possible predictors.

- (a) Find the total number of cases represented in this table.
- (b) In this form, the variables Alcohol and Income should arguably be considered ordered factors. Change them to make them ordered.
- (c) Convert this data frame to table form, DanishWelfare.tab, a 4-way array containing the frequencies with appropriate variable names and level names.
- (d) The variable *Urban* has 5 categories. Find the total frequencies in each of these. How would you collapse the table to have only two categories, City, Non-city?
- (e) Use structable() or ftable() to produce a pleasing flattened display of the frequencies in the 4-way table. Choose the variables used as row and column variables to make it easier to compare levels of Alcohol across the other factors.

{lab:2.4}

Exercise 2.4 The data set UKSoccer in vcd gives the distributions of number of goals scored by the 20 teams in the 1995/96 season of the Premier League of the UK Football Association.

This two-way table classifies all $20 \times 19 = 380$ games by the joint outcome (Home, Away), the

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number of goals scored by the Home and Away teams. The value 4 in this table actually represents 4 or more goals.

- (a) Verify that the total number of games represented in this table is 380.
- (b) Find the marginal total of the number of goals scored by each of the home and away teams.
- (c) Express each of the marginal totals as proportions.
- (d) Comment on the distribution of the numbers of home-team and away-team goals. Is there any evidence that home teams score more goals on average?

{lab:2.5}

Exercise 2.5 The one-way frequency table, Saxony in VCd records the frequencies of families with 0, 1, 2, ... 12 male children, among 6115 families with 12 children. This data set is used extensively in Chapter 3.

```
> data(Saxony, package="vcd")
> Saxony
nMales
                         4
              2.
                   3
                                    6
                                               8
                                                    9
                                                         10
                                                                    12
   0
                                                              11
   3
           104 286 670 1033 1343 1112
                                            829
                                                  478
```

Another data set, Geissler in the vcdExtra package, gives the complete tabulation of all combinations of boys and girls in families with a given total number of children size. The task here is to create an equivalent table, Saxony12 from the Geissler data.

```
> data(Geissler, package="vcdExtra")
> str(Geissler)

'data.frame': 90 obs. of 4 variables:
$ boys : int 0 0 0 0 0 0 0 0 0 ...
$ girls: num 1 2 3 4 5 6 7 8 9 10 ...
$ size : num 1 2 3 4 5 6 7 8 9 10 ...
$ Freq : int 108719 42860 17395 7004 2839 1096 436 161 66 30 ...
```

- (a) Use subset () to create a data frame, sax12 containing the Geissler observations in families with size==12.
- (b) Select the columns for boys and Freq.
- (c) Use xtabs () with a formula, Freq ~ boys, to create the one-way table.
- (d) Do the same steps again, to create a one-way table, Saxony11 containing similar frequencies for families of size==11.

{lab:2.6}

Exercise 2.6 Interactive coding of table factors: Some statistical and graphical * methods for contingency tables are implemented only for two-way tables, but can be extended to 3+ way tables by recoding the factors to interactive combinations along the rows and/or columns, in a way similar to what ftable() and structable() do for printed displays.

For the UCBAdmissions data, produce a two-way table object, UCB.tab2 that has the combinations of Admit and Gender as the rows, and Dept as its columns, to look like the result below:

```
Dept
Admit:Gender
                     Α
                          В
                              С
                                  D
                                       Ε
                                           F
                    89
                        17 202 131
                                      94
                                          24
  Admitted: Female
                   512 353 120 138
  Admitted: Male
  Rejected: Female 19
                          8 391 244 299 317
  Rejected: Male
                   313 207 205 279 138 351
```

Hint: convert to a data frame, manipulate the factors, then convert back to a table.

{lab:2.7}

Exercise 2.7 The data set VisualAcuity in VCd gives $4 \times 4 \times 2$ table as a frequency data frame.

```
> data("VisualAcuity", package="vcd")
> str(VisualAcuity)

'data.frame': 32 obs. of 4 variables:
   $ Freq : num 1520 234 117 36 266 ...
   $ right : Factor w/ 4 levels "1","2","3","4": 1 2 3 4 1 2 3 4 1 2 ...
   $ left : Factor w/ 4 levels "1","2","3","4": 1 1 1 1 2 2 2 2 2 3 3 ...
   $ gender: Factor w/ 2 levels "male","female": 2 2 2 2 2 2 2 2 2 ...
```

- (a) From this, use xtabs () to create two 4×4 frequency tables, one for each gender.
- (b) Use structable() to create a nicely organized tabular display.
- (c) Use ${\tt xtable}$ () to create a LATEX or HTML table.

References

- Agresti, A. (2002). *Categorical Data Analysis*. Wiley Series in Probability and Statistics. New York: Wiley-Interscience [John Wiley & Sons], 2nd edn.
- Fox, J. and Weisberg, S. (2011). *An R Companion to Applied Regression*. Thousand Oaks CA: Sage, 2nd edn.
- Hartigan, J. A. and Kleiner, B. (1984). A mosaic of television ratings. *The American Statistician*, 38, 32–35.
- Koch, G. and Edwards, S. (1988). Clinical efficiency trials with categorical data. In K. E. Peace, ed., *Biopharmaceutical Statistics for Drug Development*, (pp. 403–451). New York: Marcel Dekker.
- Leifeld, P. (2013). texreg: Conversion of statistical model output in r to latex and html tables. *Journal of Statistical Software*, 55(8), 1–24.