Chapter 1

Introduction

{ch:intro}

Categorical data consists of variables whose values comprise a set of discrete categories. Such data require different statistical and graphical methods than commonly used for quantitative data. The focus of this book is on visualization techniques and graphical methods designed to reveal patterns of relationships among categorical variables. This chapter outlines the basic orientation of the book and some key distinctions regarding the analysis and visualization of categorical data.

1.1 Data visualization and categorical data: Overview

{sec:viscat}

Beauty is truth; truth, beauty.

That is all ye know on Earth, all ye need to know.

John Keats, Ode on a Grecian urn

"Data visualization" can mean many things, from popular press infographics, to maps of voter turnout or party choice. Here we use this term in the narrower context of statistical analysis. As such, we refer to an approach to data analysis that focuses on *insightful* graphical display in the service of both *understanding* our data and *communicating* our results to others.

We may display the raw data, some summary statistics, or some indicators of the quality or adequacy of a fitted model. The word "insightful" suggests that the goal is (hopefully) to reveal some aspects of the data which might not be perceived, appreciated, or absorbed by other means. As in the quote from Keats, the overall aims include both beauty and truth, though each of these are only as perceived by the beholder.

Methods for visualizing quantitative data have a long history and are now widely used in both data analysis and in data presentation, and in both popular and scientific media. Graphical methods for categorical data, however, have only a more recent history, and are consequently not as widely used. The goal of this book is to show concretely how data visualization may be usefully applied to categorical data.

"Categorical" data means different things in different contexts. We introduce the topic in Section 1.2 with some examples illustrating (a) types of categorical variables: binary, nominal, and ordinal, (b) data in case form vs. frequency form, (c) frequency data vs. count data, (d) univariate, bivariate, and multivariate data, and (e) the distinction between explanatory and response variables.

Statistical methods for the analysis of categorical data also fall into two quite different categories, described and illustrated in Section 1.3: (a) the simple randomization-based methods typi-

fied by the classical Pearson χ^2 , Fisher's exact test, and Cochran-Mantel-Haenszel tests, and (b) the model-based methods represented by logistic regression, loglinear, and generalized linear models. In this book, Chapters 3–6 are mostly related to the randomization-based methods; Chapters 7–8 illustrate the model-based methods.

In Section 1.4 we describe some important similarities and differences between categorical data and quantitative data, and discuss the implications of these differences for visualization techniques. Section 1.4.5 outlines a strategy of data analysis focused on visualization.

In a few cases we show R code or results as illustrations here, but the fuller discussion of using R for categorical data analysis is postponed to Chapter 2.

1.2 What is categorical data?

{sec:whatis}

A *categorical variable* is one for which the possible measured or assigned values consist of a discrete set of categories, which may be *ordered* or *unordered*. Some typical examples are:

- Gender, with categories "Male", "Female".
- Marital status, with categories "Never married", "Married", "Separated", "Divorced", "Widowed".
- Fielding position (in baseball), with categories "Pitcher", "Catcher", "1st base", "2nd base", ..., "Left field".
- Side effects (in a pharmacological study), with categories "None", "Skin rash", "Sleep disorder", "Anxiety",
- Political attitude, with categories "Left", "Center", "Right".
- Party preference (in Canada), with categories "NDP", "Liberal", "Conservative", "Green".
- Treatment outcome, with categories "no improvement", "some improvement", or "marked improvement".
- Age, with categories "0-9", "10-19", "20-29", "30-39", . . .
- Number of children, with categories $0, 1, 2, \ldots$

As these examples suggest, categorical variables differ in the number of categories: we often distinguish *binary variables* such as *Gender* from those with more than two categories (called *polytomous variables*). For example, Table 1.1 gives data on 4526 applicants to graduate departments at the University of California at Berkeley in 1973, classified by two binary variables, gender and admission status.

{tab:berk220}

Table 1.1: Admissions to Berkeley graduate programs

	Admitted	Rejected	Total
Males	1198	1493	2691
Females	557	1278	1835
Total	1755	2771	4526

Some categorical variables (Political attitude, Treatment outcome) may have ordered categories (and are called *ordinal*), while other (nominal) variables like Marital status have unordered categories. For example, Table 1.2 shows a $2 \times 2 \times 3$ table of ordered outcomes ("none", "some" or "marked" improvement) to an active treatment for rheumatoid arthritis compared to a placebo for men and women.

¹An ordinal variable may be defined as one whose categories are *unambiguously* ordered along a *single* underlying dimension. Both marital status and fielding position may be weakly ordered, but not on a single dimension, and not unambiguously.

{tab:arthrit0} **Table 1.2:** Arthritis treatment data

		Iı			
Treatment	Sex	None	Some	Marked	Total
Active	Female	6	5	16	27
	Male	7	2	5	14
Placebo	Female	19	7	6	32
	Male	10	0	1	11
Total		42	14	28	84

Finally, such variables differ in the fineness or level to which some underlying observation has been categorized for a particular purpose. From one point of view, *all* data may be considered categorical because the precision of measurement is necessarily finite, or an inherently continuous variable may be recorded only to limited precision.

But this view is not helpful for the applied researcher because it neglects the phrase "for a particular purpose". Age, for example, might be treated as a quantitative variable in a study of native language vocabulary, or as an ordered categorical variable with decade groups (0-10, 11-20, 20-30, ...) in terms of the efficacy or side-effects of treatment for depression, or even as a binary variable ("child" vs. "adult") in an analysis of survival following an epidemic or natural disaster. In the analysis of data using categorical methods, continuous variables are often recoded into ordered categories with a small set of categories for some purpose.²

1.2.1 Case form vs. frequency form

{sec:case-freq}

In many circumstances, data is recorded on each individual or experimental unit. Data in this form is called case data, or data in *case form*. The data in Table 1.2, for example, were derived from the individual data listed in the data set Arthritis from the vcd package. The following lines show the first five of N=84 cases in the Arthritis data,

```
ID Treatment Sex Age Improved
       Treated Male
                             Some
                     27
2 46
       Treated Male
                      29
                             None
3 77
                      30
       Treated Male
                             None
4 17
       Treated Male
                      32
                           Marked
       Treated Male
                     46
                           Marked
```

Whether or not the data variables, and the questions we ask, call for categorical or quantitative data analysis, when the data are in case form, we can always trace any observation back to its individual identifier or data record (for example, if the case with ID==57 turns out to be unusual or noteworthy).

Data in *frequency form* has already been tabulated, by counting over the categories of the table variables. The same data shown as a table in Table 1.2 appear in frequency form as shown below.

```
Treatment Sex Improved Freq
1 Placebo Female None 19
2 Treated Female None 6
```

²This may be a waste of information available in the original variable, and should be done for substantive reasons, not mere convenience. For example, some researchers unfamiliar with regression methods often perform a "median-split" on quantitative predictors so they can use ANOVA methods. Doing this precludes the possibility of determining if those variables have non-linear relations with the outcome.

3	Placebo	Male	None	10
4	Treated	Male	None	7
5	Placebo	Female	Some	7
6	Treated	Female	Some	5
7	Placebo	Male	Some	0
8	Treated	Male	Some	2
9	Placebo	Female	Marked	6
10	Treated	Female	Marked	16
11	Placebo	Male	Marked	1
12	Treated	Male	Marked	5

Data in frequency form may be analyzed by methods for quantitative data if there is a quantitative response variable (weighting each group by the cell frequency, with a weight variable). Otherwise, such data are generally best analyzed by methods for categorical data, where statistical models are often expressed as models for the frequency variable, in the form of an R formula like Freq $\sim \ldots$

In any case, an observation in a data set in frequency form refers to all cases in the cell collectively, and these cannot be identified individually. Data in case form can always be reduced to frequency form, but the reverse is rarely possible. In Chapter 2, we identify a third format, *table form*, which is the R representation of a table like Table 1.2.

1.2.2 Frequency data vs. count data

{sec:freq-count}

In many cases the observations representing the classifications of events (or variables) are recorded from *operationally independent* experimental units or individuals, typically a sample from some population. The tabulated data may be called *frequency data*. The data in Table 1.1 and Table 1.2 are both examples of frequency data because each observation tabulated comes from a different person.

However, if several events or variables are observed for the same units or individuals, those events are not operationally independent, and it is useful to use the term *count data* in this situation. These terms (following Lindsey (1995)) are by no means standard, but the distinction is often important, particularly in statistical models for categorical data.

For example, in a tabulation of the number of male children within families (Table 1.3, described in Section 1.2.3 below), the number of male children in a given family would be a *count* variable, taking values $0, 1, 2, \ldots$. The number of independent families with a given number of male children is a *frequency* variable. Count data also arise when we tabulate a sequence of events over time or under different circumstances in a number of individuals.

{tab:saxdata}

Table 1.3: Number of Males in 6115 Saxony Families of Size 12

Males	0	1	2	3	4	5	6	7	8	9	10	11	12
Families	3	24	104	286	670	1033	1343	1112	829	478	181	45	7

1.2.3 Univariate, bivariate, and multivariate data

{sec:uni-multi}

Another distinction concerns the number of variables: one, two or (potentially) many shown in a data set or table, or used in some analysis. Table 1.1 is an example of a bivariate (two-way) contingency table and Table 1.2 classifies the observations by three variables. Yet, we will see later that the Berkeley admissions data also recorded the department to which potential students applied (giving a three-way table), and in the arthritis data, the age of subjects was also recorded.

Any contingency table (in frequency or table form) therefore records the marginal totals, summed

over all variables not represented in the table. For data in case form, this means simply ignoring (or not recording) one or more variables; the "observations" remain the same. Data in frequency form, however, result in smaller tables when any variable is ignored; the "observations" are the cells of the contingency table. For example, in the Arthritis data, ignoring Sex gives the smaller 2×3 table for Treatment and Improved.

```
Treatment Improved Freq

1 Placebo None 29

2 Treated None 13

3 Placebo Some 7

4 Treated Some 7

5 Placebo Marked 7

6 Treated Marked 21
```

In the limiting case, only one table variable may be recorded or available, giving the categorical equivalent of univariate data. For example, Table 1.3 gives data on the distribution of the number of male children in families with 12 children (discussed further in Example 3.2). These data were part of a large tabulation of the sex distribution of families in Saxony in the 19th century, but the data in Table 1.3 have only one discrete classification variable, number of males. Without further information, the only statistical questions concern the form of the distribution. We discuss methods for fitting and graphing such discrete distributions in Chapter 3. The remaining chapters relate to bivariate and multivariate data.

1.2.4 Explanatory vs. Response variables

{sec:exp-resp}

Most statistical models make a distinction between *response variables* (or *dependent*, or *criterion* variables) and *explanatory variables* (or *independent*, or *predictor* variables).

In the standard (classical) linear models for regression and analysis of variance (ANOVA), for instance, we treat one (or more) variables as responses, to be explained by the other, explanatory variables. The explanatory variables may be quantitative or categorical (e.g., factors in R). This affects only the details of how the model is specified or how coefficients are interpreted for lm() or glm(). In these classical models, the response variable ("treatment outcome", for example), must be considered quantitative, and the model attempts to describe how the *mean* of the distribution of responses changes with the values or levels of the explanatory variables, such as age or gender.

When the response variable is categorical, however, the standard linear models do not apply, because they assume a normal (Gaussian) distribution for the model residuals. For example, in Table 1.2 the response variable is <code>Improvement</code>, and even if numerical scores were assigned to the categories "none", "some", "marked", it may be unlikely that the assumptions of the classical linear models could be met.

Hence, a categorical *response* variable generally requires analysis using methods for categorical data, but categorical *explanatory* variables may be readily handled by either method.

The distinction between response and explanatory variables also becomes important in the use of loglinear models for frequency tables (described in Chapter 8), where models can be specified in a simpler way (as equivalent logit models) by focusing on the response variable.

1.3 Strategies for categorical data analysis

{sec:strategies}

Data analysis typically begins with exploratory and graphical methods designed to expose features of the data, followed by statistical analysis designed to summarize results, answer questions and draw conclusions. Statistical methods for the analysis for categorical data can be classified into two broad categories: those concerned with *hypothesis testing* per se versus those concerned with *model building*.

Done: DM: What about explorative analysis? MF: edited above

{sec:strategies-hyp}

1.3.1 Hypothesis testing approaches

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In many studies, the questions of substantive interest translate readily into questions concerning hypotheses about *association* between variables, a more general idea than that of correlation (*linear* association) for quantitative variables. If a non-zero association exists, we may wish to characterize the strength of the association numerically and understand the pattern or nature of the association.

For example, in Table 1.1, a main question is: "Is there evidence of gender-bias in admission to graduate school?" Another way to frame this: "Are males more likely to be admitted?" These questions can be expressed in terms of an association between gender and admission status in a 2×2 contingency table of applicants classified by these two variables. If there is evidence for an association, we can assess its strength by a variety of measures, including the difference in proportions admitted for men and women or the ratio of the odds of admission for men compared to women, as described in Section 4.2.2.

Similarly, in Table 1.2, questions about the efficacy of the treatment for rheumatoid arthritis can be answered in terms of hypotheses about the associations among the table variables: Treatment, Sex, and the Improvement categories. Although the main concern might be focused on the overall association between Treatment and Improvement, one would also wish to know if this association is the same for men and women. A stratified analysis (Section 4.3) controls for the effects of background variables like Sex, and tests for homogeneity of association helping to determine if these associations are equal.

Questions involving tests of such hypotheses are answered most easily using a large variety of specific statistical tests, often based on randomization arguments. These include the familiar Pearson chi-squared test for two-way tables, the Cochran-Mantel-Haenszel test statistics, Fisher's exact test, and a wide range of measures of strength of association. These tests make minimal assumptions, principally requiring that subjects or experimental units have been randomly assigned to the categories of experimental factors. The hypothesis testing approach is illustrated in Chapter 4–6, though the emphasis is on graphical methods which help to understand the nature of association between variables.

{ex:haireye0}

EXAMPLE 1.1: Hair color and eye color

The data HairEye below records data on the relationship between hair color and eye color in a sample of nearly 600 students.

```
Brown Blue Hazel Green
Hair
  Black
            68
                  20
                        15
           119
                  84
                         54
                               29
  Brown
                  17
  Red
                         14
                               14
                        10
```

The standard analysis (with chisq.test() or assocstats()) gives a Pearson χ^2 of 138.3 with nine degrees of freedom, indicating substantial departure from independence. Among the measures of strength of association, the *phi coefficient*, $\phi = \sqrt{\chi^2/N} = 0.483$, and *Cramer's V*, $V = \sqrt{\chi^2/N} \min(r-1,c-1) = 0.279$ indicate a substantial relationship between hair and eye color.³

```
X^2 df P(> X^2)
Likelihood Ratio 146.44 9 0
Pearson 138.29 9 0

Phi-Coefficient : 0.483
Contingency Coeff.: 0.435
Cramer's V : 0.279
```

³Cramer's V varies from 0 (no association) to 1 (perfect association).

The further (and perhaps more interesting question) is how do we understand the *nature* of this association between hair and eye color? Two graphical methods related to the hypothesis testing approach are shown in Figure 1.1.

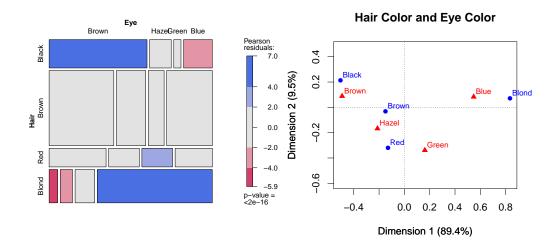


Figure 1.1: Graphical displays for the hair color and eye color data. Left: mosaic display; right: correspondence analysis plot

The left panel of Figure 1.1 is a *mosaic display* (Chapter 5), constructed so that the size of each rectangle is proportional to the observed cell frequency. The shading reflects the cell contribution to the χ^2 statistic—shades of blue when the observed frequency is substantially greater than the expected frequency under independence, shades of red when the observed frequency is substantially less, as shown in the legend.

The right panel of this figure shows the results of a correspondence analysis (Chapter 6), where the deviations of the hair color and eye color points from the origin accounts for as much of the χ^2 as possible in two dimensions.

We observe that both the hair colors and the eye colors are ordered from dark to light in the mosaic display and along Dimension 1 in the correspondence analysis plot. The deviations between observed and expected frequencies have an opposite-corner pattern in the mosaic display, except for the combination of red hair and green eyes, which also stand out as the largest values on Dimension 2 in the Correspondence analysis plot. Displays such as these provide a means to understand *how* the variables are related. \triangle

1.3.2 Model building approaches

Model-based methods provide tests of equivalent hypotheses about associations, but offer additional advantages (at the cost of additional assumptions) not provided by the simpler hypotheses-testing approaches. Among these advantages, model-based methods provide estimates, standard errors and confidence intervals for parameters, and the ability to obtain predicted (fitted) values with associated measures of precision.

We illustrate this approach here for a dichotomous response variable, where it is often convenient to construct a model relating a function of the probability, π , of one event to a linear combination of the explanatory variables. Logistic regression uses the *logit function*,

$$logit(\pi) \equiv log_e \left(\frac{\pi}{1-\pi}\right)$$

which may be interpreted as the *log odds* of the given event. A linear logistic model can then be expressed as

$$logit(\pi) = \beta_0 + \beta_1 x_1 + \beta_2 x_2 + \dots$$

Statistical inferences from model-based methods provide tests of hypotheses for the effects of the predictors, x_1, x_2, \ldots , but they also provide estimates of parameters in the model, β_1, β_2, \ldots and associated confidence intervals. Standard modeling tools allow us to graphically display the fitted response surface (with confidence or prediction intervals) and even to extrapolate these predictions beyond the given data. A particular advantage of the logit representation in the logistic regression model is that estimates of odds ratios (Section 4.2.2.1) may be obtained directly from the parameter estimates.

{ex:nasa0}

EXAMPLE 1.2: Space shuttle disaster

To illustrate the model-based approach, the graph in Figure 1.2 is based on a logistic regression model predicting the probability of a failure in one of the O-ring seals used in the 24 NASA space shuttles prior to the disastrous launch of the *Challenger* in January, 1986. The explanatory variable is the ambient temperature at the time of the flight. The sad story behind these data, and the lessons to be learned for graphical data display are related in Example 1.10.

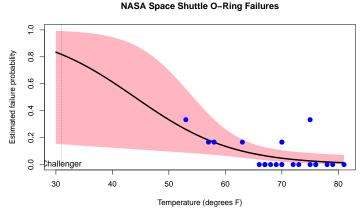


Figure 1.2: Space shuttle O-ring failure, observed and predicted probabilities. The dotted vertical

line at 31° shows the prediction for the launch of the *Challenger*.

Here, we simply note that the fitted model, shown by the solid line in Figure 1.2, corresponds to the prediction equation (with standard errors shown in parentheses),

$$logit(Failure) = \underset{(3.06)}{5.09} - \underset{(0.047)}{0.116} \text{ Temperature}$$

A hypothesis test that failure probability is unassociated with temperature is equivalent to the test that the coefficient for temperature in this model equals 0; this test has a *p*-value of 0.014, convincing evidence for rejection.

The parameter estimate for temperature, -0.116, however, gives more information. Each 1° increase in temperature decreases the log odds of failure by 0.116, with 95% confidence interval [-0.208, -0.0235]. The equivalent odds ratio is $\exp(-0.116) = 0.891$ [0.812, 0.977]. Equivalently, a 10° decrease in temperature corresponds to an odds ratio of a failure of $\exp(10 \times 0.116) = 3.18$, more than tripling the odds of a failure.

When the *Challenger* was launched, the temperature was only 31° . The shaded region in Figure 1.2 show 95% prediction intervals for failure probability. All previous shuttles (shown by the

points in the figure) had been launched at much warmer temperatures, so the prediction interval (the dashed vertical line) at 31° represents a considerable extrapolation beyond the available data. Nonetheless, the model building approach does provide such predictions along with measures of their uncertainty. Figure 1.2 is a graph that might have saved lives.

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TODO: DM: Remove Donner party example to shorten up the intro? One example for logistig regression seems enough here.

{ex:donner0}

EXAMPLE 1.3: Donner Party

In April–May of 1846 (three years before the California gold rush), the Donner and Reed families set out for California from the American mid-west in a wagon train to seek a new life and perhaps their fortune in the new American frontier. By mid July, a large group had reached a site in present-day Wyoming; George Donner was elected to lead what was to be called the "Donner Party," which eventually numbered 87 people in 23 wagons, along with their oxen, cattle, horses, and worldly possessions.

They were determined to reach California as quickly as possible. Lansford Hastings, a self-proclaimed trailblazer (retrospectively, of dubious distinction), proposed that the party follow him through a shorter path through the Wasatch Mountains. Their choice of "Hastings's Cutoff" proved disastrous: Hastings had never actually crossed that route himself, and the winter of of 1846 was to be one of the worst on record.

In October, 1846, heavy snow stranded them in the eastern Sierra Nevada, just to the east of a pass which bears their name today. The party made numerous attempts to seek rescue, most turned back by blizzard conditions. Relief parties in March–April 1847 rescued 40, but discovered grizzly evidence that those who survived had cannibalized those who died.

Here we briefly examine of how statistical models and graphical evidence can shed light on the question of who survived in the Donner party.

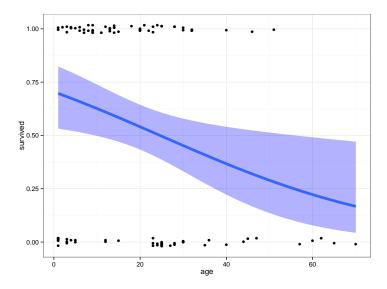


Figure 1.3: Donner party data, showing the relationship between age and survival. The blue curve and confidence band give the predicted probability of survival from a linear logistic regression model.

Figure 1.3 is an example of what we call a data-centric, model-based graph of a discrete (binary)

outcome: lived (1) versus died (0). That is, it shows both the data and a statistical summary based on a fitted statistical model. The statistical model provides a smoothing of the discrete data.

The jittered points at the top and bottom of the graph show survival in relation to age of the person. You can see that there were more people who survived among the young, and more who died among the old. The blue curve in the plot shows the fitted probability of survival from a linear logistic regression model for these data with a 95% confidence band for that predictions. The prediction equation for this model can be given as:

logit(survived) =
$$0.868 - 0.0353$$
 age $(0.372) - (0.015)$

It implies that the log odds of survival decreases by 0.0352 with each additional year of age or by $10 \times 0.0352 = 0.352$ for an additional decade. Another way to say this is that the odds of survival is multiplied by $\exp(0.353) = .702$ with each 10 years of age, a 30% decrease.

Of course, these visual and statistical summary depends on the validity of fitted model. For contrast, Figure 1.4 shows two other model-based smoothers that relax the assumption of the linear logistic regression model. The left panel shows the result of fitting a semi-parametric model with a natural cubic spline with one more degree of freedom than the linear logistic model. The right panel shows the fitted curve for a non-parametric, loess model. Both of these hint that the relationship of survival to age is more complex than what is captured in the linear logistic regression model. We return to these data in Chapter 7.

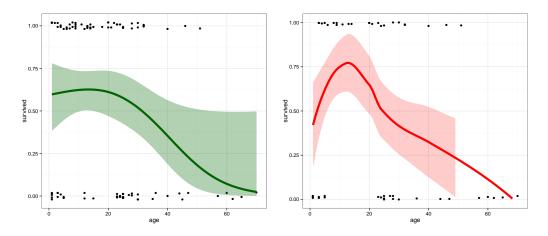


Figure 1.4: Donner party data, showing other model-based smoothers for the relationship between age and survival. Left: using a natural spline; right: using a non-parametric loss smoother.

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1.4 Graphical methods for categorical data

{sec:methods}

You can see a lot, just by looking

Yogi Berra

The graphical methods for categorical data described in this book are in some cases straightforward adaptations of more familiar visualization techniques developed for quantitative data. Graphical principles and strategies, and the relations between the visualization approach and traditional

statistical methods are described in a number of sources, including Chambers *et al.* (1983), Cleveland (1993b) and several influential books by Tufte (Tufte, 1983, 1990, 1997, 2006).

The fundamental ideas of statistical graphics as a comprehensive system of visual signs and symbols with a grammar and semantics was first proposed in Jacques Bertin's *Semiology of Graphics* (1983), These ideas were later extended to a computational theory in Wilkinson's *Grammar of Graphics* (2005), and implemented in R in Hadley Wickham's ggplot2 package (Wickham, 2009, Wickham and Chang, 2013).

Another perspective on visual data display is presented in Section 1.4.1 focusing on the communication goals of statistical graphics. However, the discrete nature of categorical data implies that some familiar graphic methods need to be adapted, while in other cases we require a new graphic metaphor for data display. These issues are illustrated in Section 1.4.2. Section 1.4.3 discusses the principle of effect ordering for categorical variables in graphs and tables.

1.4.1 Goals and design principles for visual data display

{sec:intro-goals}

Designing good graphics is surely an art, but as surely, it is one that ought to be informed by science. In constructing a graph, quantitative and qualitative information is encoded by visual features, such as position, size, texture, symbols and color. This translation is reversed when a person studies a graph. The representation of numerical magnitude and categorical grouping, and the apperception of patterns and their *meaning* must be extracted from the visual display.

There are many views of graphs, of graphical perception, and of the roles of data visualization in discovering and communicating information. On the one hand, one may regard a graphical display as a *stimulus*— a package of information to be conveyed to an idealized observer. From this perspective certain questions are of interest: which form or graphic aspect promotes greater accuracy or speed of judgment (for a particular task or question)? What aspects lead to greatest memorability or impact? Cleveland (Cleveland and McGill, 1984, 1985, Cleveland, 1993a), Spence and Lewandowsky (Lewandowsky and Spence, 1989, Spence, 1990, Spence and Lewandowsky, 1990) have made important contributions to our understanding of these aspects of graphical display.

An alternative view regards a graphical display as an act of *communication*—like a narrative, or even a poetic text or work of art. This perspective places the greatest emphasis on the desired communication goal, and judges the effectiveness of a graphical display in how well that goal is achieved (Friendly and Kwan, 2011). Kosslyn (1985, 1989) and Tufte (1983, 1990, 1997) have articulated this perspective most clearly.

In this view, an effective graphical display, like good writing, requires an understanding of its *purpose*—what aspects of the data are to be communicated to the viewer. In writing we communicate most effectively when we know our audience and tailor the message appropriately. So too, we may construct a graph in different ways to: (a) use ourselves, (b) present at a conference or meeting of our colleagues, (c) publish in a research report, or (d) communicate to a general audience (Friendly (1991, Ch. 1), Friendly and Kwan (2011)). Figure 1.5 illustrates a basic contrast between graphs for presentation purposes, designed to appeal persuasively to a large audience (one-to-many) and the use of perhaps many graphs we might make for ourselves for exploratory data analysis (many-to-one).

Figure 1.6 shows one organization of visualization methods in terms of the *primary* use or intended communication goal, the functional *presentation goal*, and suggested corresponding *design principles*.

We illustrate these ideas and distinction in the examples below, most of which are treated again in later chapters.

{ex:arrests0}

EXAMPLE 1.4: Racial profiling: Arrests for marijuana possession

In a case study that will be examined in detail in Chapter 7 (Example 7.10), the *Toronto Star* newspaper studied a huge data base of arrest records by Toronto police for indications of possible

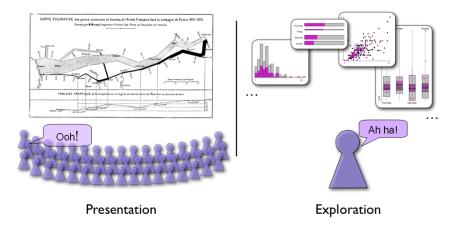


Figure 1.5: Different communication purposes require different graphs. For presentations, a single, carefully crafted graph may appeal best to a large audience; for exploratory analysis, many related images from different perspectives for a narrow audience (often you!). *Source:* Adapted from a blog entry by Martin Theus, http://www.theusrus.de/blog/presentation-vs-exploration/.

{fig:presentation-expl

racial profiling, i.e., differential treatment of those arrested on the basis of skin color. They focused on the charge of simple possession of a small amount of marijuana, for which enforcement procedures allowed police discretion. An officer could release an arrestee with a summons ("Form 9") to appear in court, or take the person to a police station for questioning ("Form 10") or booking ("Form 11.1") or order the person held in jail for a bail hearing ("Show cause").

TODO: DM: Add frequency table here? Could be easier compared with mosaic plot. MF: No, not required for this example

The statistical issue was whether the data on these arrests showed evidence of differential treatment in relation to skin color, particularly in the treatment of blacks vs. whites, controlling, of course, for other factors. Statistical tests on these data (χ^2 tests, loglinear models, logistic regression) showed overwhelming evidence of differential treatment of blacks and whites. However, tables of these results do not reveal the nature of this association.

Figure 1.7 is an example of a graph designed for *analysis*— a mosaic display (Chapter 5) showing the frequencies of those arrested on this charge by skin color and release type. The size of each rectangle shows the frequency and these are shaded in relation to the association between skin color and release— blue for positive associations (more than expected under independence) to red for negative associations.

Once you know how to read such graphs, the pattern is clear: blacks were indeed more likely to be held for more severe treatment, whites were more likely to be released with a summons. But this is hardly a graph that would be clear to a general audience, and would require a good deal of explanation.

In contrast, Figure 1.8 shows a redesign of this as a *presentation graphic* prepared by the *Star* and published on December 11, 2002 in conjunction with a meeting between the newspaper and the Toronto Police Services Board to consider the issue of racial profiling. The police vehemently denied that racial profiling was taking place. The revision makes the point immediately obvious and compelling in the following ways:

- It announces the conclusion in the figure title: "Same charge, different treatment"
- The text box at the top provides the context for this conclusion
- Skin colors "Brown" and "Other", which were of low frequency were removed, and the release categories "Form 10" and "Form 11.1" were combined as "released at station."

Exposition

Primary Use Presentation Goal Design Principles Reconnaisance Perception Exploration **Analysis** Detection Diagnosis Comparison Model building Data Display to Simulate **Aesthetics** Presentation to Persuade Rhetoric

Basic functions of data display

Figure 1.6: A taxonomy of the basic functions of data display by intended use, presentation goal and design principles.

to Inform

{fig:datadisp}

- The graphic is still a mosaic display, however, it now shows explicitly the number of charges laid against whites and blacks and the percentage of each treatment.
- The labels for Whites and Blacks were enhanced by indicating what a reader should see for each.
- The legend for color is titled non-technically as "degree of likelihood."

Clear communication is not achieved without effort. The revised graph required several iterations and emails between the graphic designer and the statistical consultant (the first author of this book) in the few hours available before the newspaper went to press. The main question was, "what are we trying to show here?" Starting with the original Figure 1.7 mosaic, we asked "what can we remove?" and "what can we add?" to make the message clearer.

 \triangle

1.4.2 Categorical data require different graphical methods

{sec:intro-catdata}

We mentioned earlier, and will see in greater detail in Chapter 7 and Chapter 8 that statistical models for discrete response data and for frequency data are close analogs of the linear regression and ANOVA models used for quantitative data. These analogies suggest that the graphical methods commonly used for quantitative data may be adapted directly to categorical data.

Happily, it turns out that many of the analysis graphs and diagnostic displays (e.g., effect plots, influence plots, added variable and partial residual plots, etc.) that have become common adjuncts in the analysis of quantitative data have been extended to generalized linear models including logistic regression (Section 7.5) and loglinear models (Section 9.6)

Unhappily, the familiar techniques for displaying raw data are often disappointing when applied to categorical data. The simple scatterplot, for example, widely used to show the relation between quantitative response and predictors, when applied to discrete variables, gives a display of the category combinations, with all identical values overplotted, and no representation of their frequency.

Instead, frequencies of categorical variables are often best represented graphically using *areas* rather than as position along a scale. Friendly (1995) describes conceptual and statistical models that give a rationale for this graphic representation. Figure 1.7 does this in the form of a modified bar chart (mosaic plot), where the widths of the horizontal bars show the proportions of whites

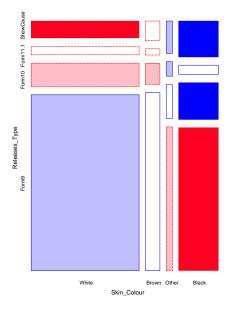


Figure 1.7: Mosaic display showing the relationship between skin color and release type for those arrested on a charge of simple possession of marijuana in Toronto, 1996-2002.

and blacks in the data, and the divisions of each group give the percents of each release type. Consequently, the areas of each bar are proportional to the frequency in the cells of this 2×3 table. As we describe later in this book, using the visual attribute

area \sim frequency

also allows creating novel graphical displays of frequency data for special circumstances.

Figure 1.9 shows two examples. The left panel gives a *fourfold display* of the frequencies of admission and gender in the Berkeley data shown in Table 1.1. What should be seen at a glance is that males are more often admitted and females more often rejected (shaded blue); see Section 4.4 for details.

The right panel shows another specialized display, an *agreement chart* designed to show the strength of agreement in a square table for two raters (see Section 4.7.2). The example here (Example 4.17) concerns agreement of ratings of breast cancer from mammograms by two raters. The dark squares along the diagonal show exact agreement; the lighter diagonal rectangles allow 1-off agreement, and both are shown in relation to chance agreement (diagonal enclosing rectangles). What should be seen at a glance is that exact agreement is moderately strong and extremely strong if you allow the raters to differ by one rating category.

1.4.3 Effect ordering and rendering for data display

{sec:effect-order}

In plots of quantitative variables, standard methods (histograms, scatterplots) automatically position values along ordered scales, facilitating comparison ("which is less/more?") and detection of patterns, trends and anomalies. However, by its nature, categorical data involves discrete variables such as education level, hair color, geographic region (state or province) or preference for a political party. With alphabetic labels for ordered categories (e.g., education: Low, Medium, High), it

ig:arrests0-mosaic}

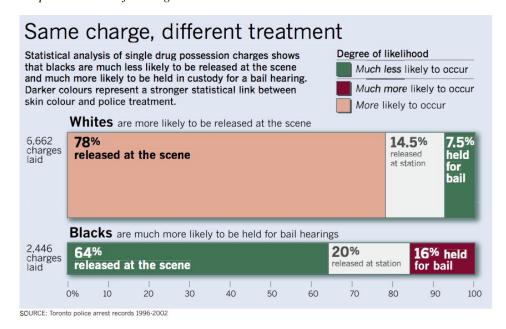


Figure 1.8: Redesign of Figure 1.7 as a presentation graphic. *Source*: Graphics department, *The Toronto Star*, December 11, 2002. Used by permission.

{fig:arrests0-star}

is unfortunately all to easy to end up with a nonsensical display with the categories ordered High, Low, Medium. Geographic regions (U.S. states) are often ordered alphabetically by default as are the names of political parties and other categorical variables. This may be useful for lookup, but for the purposes of comparison and detection, this is almost always a bad idea.

Instead, Friendly and Kwan (2003), proposed the principle of *effect-order sorting* for visual displays (tables as well as graphs):

sort the data by the effects to be seen to facilitate comparison

For quantitative data, this is often achieved by sorting the data according to means or medians of row and column factors, called *main-effect ordering*. For categorical data, graphs and tables are often most effective when the categories are arranged in an order reflecting their association, called *association ordering*.

Another important principle concerns the *rendering* of visual attributes of elements in graphical displays (Friendly, 2002). For example, categorical variables in plots (and tables) can be distinguished by any one or more of color, size, shape, or font. The examples below show the use of color to illustrate the precept:

render the data by the effects to be seen to facilitate detection

{ex:glass}

EXAMPLE 1.5: British social mobility

Bishop *et al.* (1975, p. 100) analyzed data on the occupations of 3500 British fathers and their sons from a study by Glass (1954), with five occupational categories: Professional, Managerial, Supervisory, Skilled manual and Unskilled manual.

One would expect, of course, a strong association between a son's occupation and that of his father— the apple doesn't fall very far from the tree. Mosaic plots (detailed in Chapter 5) provide a natural way to show such relationships. Figure 1.10 shows two such plots. The left panel shows the result obtained when the table variables father and son are read as factors, and therefore ordered

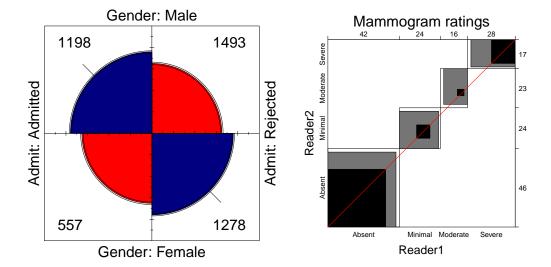


Figure 1.9: Frequencies of categorical variables shown as areas. Left: fourfold display of the relation between gender and admission in the Berkeley data; right: agreement plot for two raters assessing mammograms.

{fig:area-diagrams}

alphabetically by default. It is difficult to see any overall pattern, except for the large values in the diagonal cells (shaded blue) corresponding to equal occupational status.

In the right panel, the categories have been arranged in decreasing order of occupational status to show the association according to status. Now you can see a global pattern of shading color, where the tiles become increasingly red as one moves away from the main diagonal, reflecting a greater difference between the occupation of the father and son. The interpretation here is that most sons remain in their father's occupational class, but when they differ, there is little mobility across large steps.

In this example, father and son are clearly ordinal variables and should be treated as such in both graphs and statistical models. Correspondence analysis (Chapter 6) provides a natural way to depict association by assigning scores to the categories to optimally represent their relationships. Loglinear models provide special methods for ordinal variables (Section 8.6) and square frequency tables (Section 8.7).

 \triangle

The ideas of effect ordering and rendering with color shading to enhance perception can also be used in tabular displays, as illustrated in the next example.

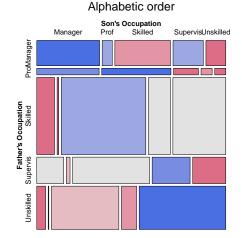
{ex:barley}

EXAMPLE 1.6: Barley data

The classic barley dataset (in lattice) from Immer *et al.* (1934) gives a $10 \times 2 \times 6$ table of yields of 10 varieties of barley in two years (1931, 1932) planted at 6 different sites in Minnesota. Cleveland (1993b) and many others have used this data to illustrate graphical methods, and one surprising finding not revealed in standard tabular displays is that the data for one site (Morris) may have had the values for 1931 and 1932 switched.⁴

To focus attention on this suspicious effect in a tabular display, you can calculate the yield

⁴This canonical story, like many others in statistics and graphics lore turns out to be apocryphal on closer examination. Wright (2013) recently took a closer look at the original data and gives an expanded data set as minnesota.barley.yield in the agridat package. With a wider range of years (1927–1936), other local effects like weather had a greater impact than the overall year effects seen in 1931–1932, and the results for the Morris site no longer stand out as surprising.



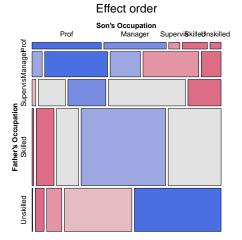


Figure 1.10: Mosaic plots for Glass' mobility table of occupational status. In these displays the area of each tile is proportional to frequency and shading color shows the departure from independence, using blue for positive, red for negative association. Left: default alphabetic ordering of categories; right: occupational categories ordered by status.

{fiq:glass-mosaic}

difference $\Delta y_{ij} = y_{ij,1931} - y_{ij,1932}$. Table 1.4 shows these values in a 10×6 table with the rows and columns sorted by their means (main-effect ordering). In addition, the table cells have been colored according to the sign and magnitude of the year difference. The shading scheme uses blue for large positive values and red for large positive values, with a white background for intermediate values. The shading intensity values were determined as $|\Delta y_{ij}| > \{2,3\} \times \widehat{\sigma}(\Delta y_{ij})$.

Effect ordering and color rendering have the result of revealing a new effect, shown as a regular progression in the body of the table. The negative values for Morris now immediately stand out. In addition, the largely positive other values show a lower-triangular pattern, with the size of the yield difference increasing with both row and column means. Against this background, one other cell, for Velvet grown at Grand Rapids stands out with an anomalous negative value.

Although the use of color for graphs is now more common in some journals, color and other rendering details in tables are still difficult. The published version of Table 1.4 (Friendly and Kwan, 2003, Table 3) was forced to use only font shape (normal, italics) to distinguish positive and negative values.

Δ

Finally, effect ordering is also usefully applied to the variables in multivariate data sets, which by default, are often ordered in data displays according to their position in a data frame or alphabetically. **TODO**: DM: Remove this section if parallel coordinates plots are removed from Sec. 5.7. MF: I'd like to keep this example

 $\{ex:1.7\}$

EXAMPLE 1.7: Iris data

The classic iris data set (Anderson, 1935, Fisher, 1936) gives the measurements in centimeters of the variables sepal length and width and petal length and width, respectively, for 50 flowers from each of 3 species of iris, *Iris setosa*, *versicolor*, and *virginica*. Such multivariate data are often displayed in *parallel coordinate plot*s, using a separate vertical axis for each variable, scaled from its minimum to maximum.

The default plot, with variables shown in their data frame order is shown in the left panel of Figure 1.11, and gives rise to the epithet *spaghetti plot* for such displays because of the large number

Table 1.4: Barley data, yield differences, 1931-1932, sorted by mean difference, and shaded by value

{tab:barley2c}

	Site							
Variety	Morris	Duluth	University Farm	Grand Rapids	Waseca	Crookston	Mean	
No. 475	-22	6	-5	4	6	12	0.1	
Wisconsin No. 38	-18	2	1	14	1	14	2.4	
Velvet	-13	4	13	-9	13	9	2.9	
Peatland	-13	1	5	8	13	16	4.8	
Manchuria	-7	6	0	11	15	7	5.5	
Trebi	-3	3	7	9	15	5	6.1	
Svansota	-9	3	8	13	9	20	7.3	
No. 462	-17	6	11	5	21	18	7.4	
Glabron	-6	4	6	15	17	12	8.0	
No. 457	-15	11	17	13	16	11	8.8	
Mean	-12.2	4.6	6.3	8.2	12.5	12.5	5.3	

of line crossings. This feature arises because one variable, sepal width, has negative relations in the species means with the other variables. Simple rearrangement of the variables to put sepal width last (or first) makes the relations among the species and the variables more apparent, as shown in the right panel of Figure 1.11. This plot has also been enhanced by using *alpha-blending* (partial transparency) of thicker lines, so that the density of lines is more apparent.

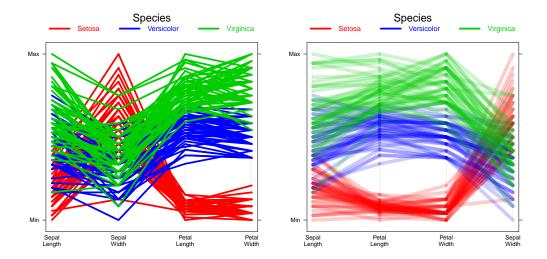


Figure 1.11: Parallel coordinates plots of the Iris data. Left: Default variable order; right: Variables ordered to make the pattern of correlations more coherent.

Parallel coordinate plots for categorical data are discussed in an online supplement on the web site for the book. A general method for reordering variables in multivariate data visualizations based on cluster analysis was proposed by Hurley (2004).

:intro-interactive}

19

1.4.4 Interactive and dynamic graphics

Graphics displayed in print form, such as this book, are necessarily static and fixed at the time they are designed and rendered as an image. Yet, recent developments in software, web technology and media alternative to print have created the possibility to extend graphics in far more useful and interesting ways, for both presentation and analysis purposes.

Interactive graphics allow the viewer to directly manipulate the statistical and visual components of graphical display. These range from

- graphical controls (sliders, selection boxes and other widgets) to control details of an analysis (e.g., a smoothing parameter) or graph (colors and other graphic details), to
- higher-level interaction including zooming in or out, drilling down to a data subset, linking multiple displays, selecting terms in a model and so forth.

The important effect is that the analysis and/or display is immediately re-computed and updated visually.

In addition, *dynamic graphics* use animation to show a series of views, as frames in a movie. Adding time as an additional dimension allows far more possibilities, for example showing a rotating view of a 3D graph or showing smooth transitions or interpolations from one view to another.

There are now many packages in R providing interactive and dynamic plots (e.g., rggobi, iplots) as well as capabilities to incorporate these into interactive documents, presentations and web pages (e.g., rCharts, googleVis). The animate package facilitates creating animated graphics and movies in a variety of formats. The RStudio editor and development environment⁵ provides its own manipulate package, as well as the shiny framework for developing interactive R web applications.

{ex:512paths}

EXAMPLE 1.8: 512 paths to the White House

Shortly before the 2012 U.S. presidential election (November 2, 2012) the *New York Times* published an interactive graphic⁶, designed by Mike Bostock And Shan Carter.⁷ showing the effect that a win for Barack Obama or Mitt Romney in the nine most highly contested states would have on the chances that either candidate would win the presidency.

With these nine states most in play there are $2^9 = 512$ possible outcomes but with different number of votes in the Electorial College. In Figure 1.12, a win for Obama in Florida and Virginia was selected, with wins for Romney in Ohio and North Carolina. Most other selections also lead to a win by Obama, but those with the most votes are made most visible at the top. An R version of this chart was created using the rCharts package. The design of this graphic as a *binary tree* was chosen here, but another possibility would be a *treemap* graphic (Shneiderman, 1992) or a mosaic plot.

Δ

1.4.5 Visualization = Graphing + Fitting + Graphing ...

{sec:vis}

Look here, upon this picture, and on this.

Shakespeare, Hamlet

Statistical summaries, hypothesis tests, and the numerical parameters derived in fitted models are

⁵http://www.rstudio.com

⁶http://www.nytimes.com/interactive/2012/11/02/us/politics/paths-to-the-white-house.html

 $^{^{7}}see$: https://source.opennews.org/en-US/articles/nyts-512-paths-white-house/ for a description of their design process.

 $^{^8}$ http://timelyportfolio.github.io/rCharts_512paths/

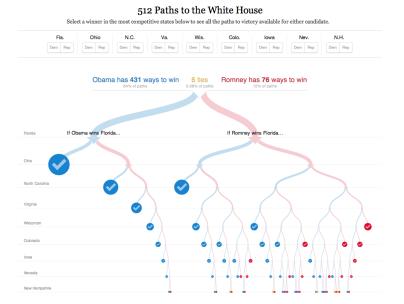


Figure 1.12: 512 paths to the White House. This interactive graphic allows the viewer to select a winner in any one or more of the nine most highly contested U.S. states and highlights the number of paths leading to a win by Obama or Romney, sorted and weighted by the number of Electoral College votes.

{fig:nyt_512paths}

designed to capture a particular feature of the data. A quick analysis of the data from Table 1.1, for example, shows that 1198/2691 = 44.5% of male applicants were admitted, compared to 557/1835 = 30.4% of female applicants.

Statistical tests give a Pearson χ^2 of 92.2 with 1 degree of freedom for association between admission and gender (p < 0.001), and various measures for the strength of association. Expressed in terms of the *odds ratio*, males were apparently 1.84 times as likely to be admitted as females, with 99% confidence bounds (1.56, 2.17). Each of these numbers expresses some part of the relationship between gender and admission in the Berkeley data. Numerical summaries such as these are each designed to compress the information in the data, focusing on some particular feature. **TODO**: Use this for a lab exercise in Ch 2.

In contrast, the visualization approach to data analysis is designed to (a) expose information and structure in the data, (b) supplement the information available from numerical summaries, and (c) suggest more adequate models. In general, the visualization approach seeks to serve the needs of both summarization and exposure.

This approach recognizes that both data analysis and graphing are *iterative* processes. You should not expect that any one model captures all features of the data, any more than we should expect that a single graph shows all that may be seen. In most cases, your initial steps should include some graphical display guided by understanding of the subject matter of the data. What you learn from a graph may then help suggest features of the data to be incorporated into a fitted model. Your desire to ensure that the fitted model is an adequate summary may then lead to additional graphs.

The precept here is that

Visualization = Graphing + Fitting + Graphing . . .

where the ellipsis indicates the often iterative nature of this process. Even for descriptive purposes,

an initial fit of salient features can be removed from the data, giving residuals (departures from a model). Displaying the residuals may then suggest additional features to account for.

Simple examples of this idea include detrending time series graphs to remove overall and seasonal effects and plots of residuals from main-effect models for ANOVA designs. For categorical data, mosaic plots (Chapter 5) display the unaccounted-for association between variables by shading, as in Figure 1.10. Additional models and plots considered in Section 8.7 can reveal additional structure in square tables beyond the obvious effect that sons tend most often to follow in their fathers' footsteps.

{ex:donner0a}

EXAMPLE 1.9: Donner party

The graphs in Figure 1.3 and Figure 1.4 suggest three different initial descriptions for survival in the Donner party. Yet they ignore all other influences, of which gender and family structure might also be important. A more complete understanding of this data can be achieved by taking these effects into account, both in fitted models and graphs. See Example 7.9 for a continuation of this story. \triangle

{ex:nasa}

EXAMPLE 1.10: Space shuttle disaster

The space shuttle *Challenger* mentioned in Example 1.2 exploded 73 seconds after take-off on January 28, 1986. Subsequent investigation presented to the presidential commission headed by William Rogers determined that the cause was failure of the O-ring seals used to isolate the fuel supply from burning gases. The story behind the *Challenger* disaster is perhaps the most poignant missed opportunity in the history of statistical graphics. See Tufte (1997) for a complete exposition. It may be heartbreaking to find out that some important information was there, but the graph maker missed it.

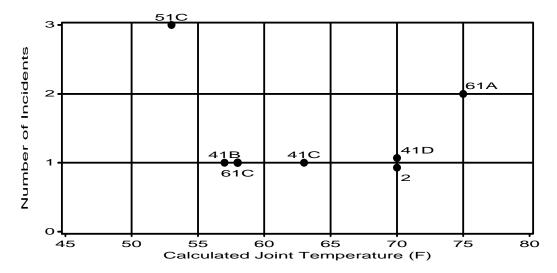


Figure 1.13: NASA Space Shuttle pre-launch graph prepared by the engineers at Morton Thiokol

{fig:nasa0}

Engineers from Morton Thiokol, manufacturers of the rocket motors, had been worried about the effects of unseasonably cold weather on the O-ring seals and recommended aborting the flight. NASA staff analysed the data, tables and charts submitted by the engineers and concluded that there was insufficient evidence to cancel the flight.

The data relating O-ring failures to temperature were depicted as in Figure 1.13, our candidate for the most misleading graph in history. There had been 23 previous launches of these rockets giving data on the number of O-rings (out of 6) that were seen to have suffered some damage or

failure. However, the engineers omitted the observations where no O-rings failed or showed signs of damage, believing that they were uninformative.

Examination of this graph seemed to indicate that there was no relation between ambient temperature and failure. Thus, the decision to launch the *Challenger* was made, in spite of the initial concerns of the Morton Thiokol engineers. Unfortunately, those observations had occurred when the launch temperature was relatively warm $(65-80^{\circ}\text{F})$ and were indeed informative. The coldest temperature at any previous launch was 53° ; when *Challenger* was launched on January 28, the temperature was a frigid 31° .

These data have been analyzed extensively (Dalal *et al.*, 1989, Lavine, 1991). Tufte (1997) gives a thorough and convincing visual analysis of the evidence available prior to the launch. We consider statistical analysis of these data in Chapter 7, Example 7.4.

But, what if the engineers had simply made a better graph? At the very least, that would entail (a) drawing a smoothed curve to fit the points (to show the trend) (b) removing the background grid lines (which obscure the data). Figure 1.14 shows a revised version of the same graph, highlighting the the non-zero observations and adding a simple quadratic curve to allow for a possible non-linear relationship. For comparison, the excluded zero observations are also shown in grey. This plot, even showing only the non-zero points should have caused any engineer to conclude that either: (a) the data were wrong, or (b) there were excessive risks associated with both high and low temperatures. But it is well-known that brittleness of the rubber used in the O-rings is inversely proportional to Temperature cubed, so prudent interest might have focussed on the first possibility.⁹

Done: DM: Maybe remove coda: example is quite long already. MF: Made a footnote

Δ

1.4.6 The 80-20 rule

The Italian economist Vilfredo Pareto observed in 1906 that 80% of the land in Italy was owned by 20% of the population and this ratio also applied in other countries. It also applied to the yield of peas from peapods in his garden (Pareto, 1971). This idea became known as the *Pareto principle* or the *80–20 rule*. The particular 80/20 ratio is not as important as the more general idea of the uneven distribution of results and causes in a variety of areas.

Common applications are the rules of thumb that: (a) in business 80% of sales come from 20% of clients; (b) in criminology 80% of crimes are said to be committed by 20% of the population. (c) In software development, it is said that 80% of errors and (d) crashes can be eliminated by fixing the top 20% most reported bugs or that 80% of errors reside in 20% of the code.

The *Pareto chart* was designed to display the frequency distribution of a variable with a histogram or bar chart together with a cumulative line graph to highlight the most frequent category, and the *Pareto distribution* gives a mathematical form to such distributions with a parameter α (the *Pareto index*) reflecting the degree of inequality.

Applied to statistical graphics, the precept is that

20% of your effort can generate 80% of your desired result in producing a given plot.

This is good news for exploratory graphs you produce for yourself. Very often, the default settings will give a reasonable result, or you will see immediately something simple to add or change to make the plot easier to understand.

The bad news is the corollary of this rule:

⁹A coda to this story shows the role of visual explanation in practice as well (Tufte, 1997, p. 50–53). The Rogers Commission contracted the reknown theoretical physicist Richard Feynman to contribute to their investigation. He determined that the most probable cause of the shuttle failure was the lack of resiliancy of the rubber O-rings at low temperature. But how could he make this point convincingly? At a televised public hearing, he took a piece of the O-ring material, squeezed it in C-clamp and plunged it into a glass of ice water. After a few minutes, he released the clamp, and the rubber did not spring back to shape. He mildly said, "... there is no resilience in this particular material when it is at a temperature of 32 degress. I believe this has some significance for our problem" (Feynman, 1988).

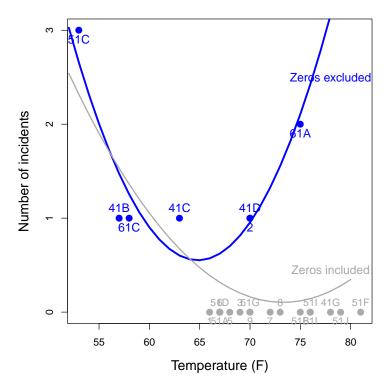


Figure 1.14: Re-drawn version of the NASA pre-launch graph, showing the locations of the excluded observations and with fitted quadratics for both sets of observations

80% of your effort may be required to produce the remaining 20% of a finished graph.

This is particularly important for presentation graphs, where several iterations may be necessary to get it right (or right enough) for your communication purposes. Some important details are:

graph title A presentation graphic can be more effective when it announces the main point or conclusion in the graphic title, as in Figure 1.8.

axis and value labels Axes should be labelled with meaningful variable descriptions (and perhaps the data units) rather than just plot defaults (e.g., "Temperature (degrees F)" in Figure 1.2, not temp). Axis values are often more of a challenge for categorical variables, where their text labels often overlap, requiring abbreviation, a smaller font or text rotation.

grouping attributes Meaningfully different subsets of the data should be rendered with distinct visual attributes such as color, shape, and line style, and sometimes with more than one.

legends and direct labels Different data groups in a graphic display shown by color, shape, etc. usually need at least a graphic legend defining the symbols and group labels. Sometimes you can do better by applying the labels directly to the graphical elements, ¹⁰ as was done in Figure 1.14.

legibility A common failure in presentation graphs in journals and lectures is the use of text fonts

{fig:nasa}

¹⁰ For example, the identify() function allows points in a plot to be labeled interactively with a mouse. The directlabels package provides a general method for a variety of plots.

too small to be read easily. One rule of thumb is to hold the graph at arms length for a journal and put it on the floor for a lecture slide. If you can't read the labels, the font is too small.

plot annotations Beyond the basic graphic data display, additional annotations can add considerable information to interpret the context or uncertainty, as in the use of plot envelopes to show confidence bands or regions (see Figure 1.3 and Figure 1.4).

aspect ratio Line graphs (such as Figure 3.1) are often easiest to understand when the ratio of height to width is such that line segments have an average slope near 1.0 (Cleveland *et al.*, 1988). In R, you can easily manipulate a graph window manually with a mouse to observe this effect and find an aspect ratio that looks right.

Moreover, in graphs for biplots and correspondence analysis (Chapter 6), interpretation involves distances between points and angles between line segments. This requires an aspect ratio that equates the units on the axes. Careful software will do this for you, ¹¹ and you should resist the temptation to re-shape the plot.

Nearly all of the graphs in this book were produced using R code in scripts saved as files. This has the advantages of reproducibility and enhancement: just re-run the code, or tweak it to improve a graph. If this is too hard, you can always use an external graphics editor (Gimp, Inkscape, Adobe Illustrator, etc.) to make improvements manually.

1.5 Chapter summary

- Categorical data differs from quantitative data because the variables take on discrete values (ordered or unordered, character or numeric) rather than continuous numerical values. Consequently, such data often appear in aggregated form representing category frequencies or in tables.
- Data analysis methods for categorical data are comprised of those concerned mainly with testing
 particular hypotheses versus those that fit statistical models. Model building methods have the
 advantages of providing parameter estimates and model-predicted values, along with measures
 of uncertainty (standard errors).
- Graphical methods can serve different purposes for different goals (data analysis versus presentation), and these suggest different design principles that a graphic should respect to achieve a given communication goal.
- For categorical data, some graphic forms (bar charts, line graphs, scatterplots) used for quantitative data can be readily adapted to discrete variables. However, frequency data often requires novel graphics using area and other visual attributes.
- Graphics can be far more effective when categorical variables are ordered to facilitate comparison of the effects to be seen and rendered to facilitate detection of patterns, trends or anomalies.
- The visualization approach to data analysis often entails a sequence of intertwined steps involving graphing and model fitting.
- Producing effective graphs for presentation is often hard work, requiring attention to details that support or detract from your communication goal.

¹¹For example using the graphics parameter asp=1, eqsplot() in MASS, or the equivalents in lattice (aspect="iso") and ggplot2 (coord_equal).

1.6: Further reading 25

1.6 Further reading

{sec:ch01-reading}

sec:ch01-exercises

1.7 Lab exercises

Exercise 1.1 A web page, "The top ten worst graphs," http://www.biostat.wisc.edu/~kbroman/topten_worstgraphs/ by Karl Broman lists his picks for the worst graphs (and a table) that have appeared in the statistical and scientific literature. Each entry links to graph(s) and a brief discussion of what is wrong and how it could be improved.

- (a) Examine a number of recent issues of a scientific or statistical journal in which you have some interest. Find one or more examples of a graph or table that is a particularly bad use of display material to summarize and communicate research findings. Write a few sentences indicating how or why the display fails and how it could be improved.
- (b) Do the same task for some popular magazine or newspaper that uses data displays to supplement the text for some story. Again, write a few sentences describing why the display is bad and how it could be improved.

{lab:1.2}

Exercise 1.2 As in the previous exercise, examine the recent literature in recent issues of some journal of interest to you. Find one or more examples of a graph or table that you feel does a *good* of summarizing and communicating research findings.

- (a) Write a few sentences describing why you chose these displays.
- (b) Now take the role of a tough journal reviewer. Are there any features of the display that could be modified to make them more effective?

{lab:1.3}

Exercise 1.3 Infographics are another form of visual displays, quite different from the data graphics featured in this book, but often based on some data or analysis. Do a Google image search for the topic "Global warming" to see a rich collection.

- (a) Find and study one or two that attempt some visual explanation of causes and/or effects of global warming. Describe the main message in a sentence or two.
- (b) What visual and graphic features are used in these to convey the message?

{lab:1.4}

Exercise 1.4 The Wikipedia web page en.wikipedia.org/wiki/Portal:Global_warming gives a few data-based graphics on the topic of global warming. Read the text and study the graphs.

- (a) Write a short figure title for each that would announce the conclusion to be drawn in a presentation graphic.
- (b) Write a figure caption for each that would explain what is shown and the important graphical details for a reader to understand.

References

- Anderson, E. (1935). The irises of the Gaspé peninsula. *Bulletin of the American Iris Society*, 35, 2–5.
- Bertin, J. (1983). *Semiology of Graphics*. Madison, WI: University of Wisconsin Press. (trans. W. Berg).
- Bishop, Y. M. M., Fienberg, S. E., and Holland, P. W. (1975). *Discrete Multivariate Analysis: Theory and Practice*. Cambridge, MA: MIT Press.
- Chambers, J. M., Cleveland, W. S., Kleiner, B., and Tukey, P. A. (1983). *Graphical Methods for Data Analysis*. Belmont, CA: Wadsworth.
- Cleveland, W. S. (1993a). A model for studying display methods of statistical graphics. *Journal of Computational and Graphical Statistics*, 2, 323–343.
- Cleveland, W. S. (1993b). Visualizing Data. Summit, NJ: Hobart Press.
- Cleveland, W. S., McGill, M. E., and McGill, R. (1988). The shape parameter of a two-variable graph. *Journal of the American Statistical Association*, 83, 289–300.
- Cleveland, W. S. and McGill, R. (1984). Graphical perception: Theory, experimentation and application to the development of graphical methods. *Journal of the American Statistical Association*, 79, 531–554.
- Cleveland, W. S. and McGill, R. (1985). Graphical perception and graphical methods for analyzing scientific data. *Science*, 229, 828–833.
- Dalal, S., Fowlkes, E. B., and Hoadley, B. (1989). Risk analysis of the space shuttle: Pre-Challenger prediction of failure. *Journal of the American Statistical Association*, 84(408), 945–957.
- Feynman, R. P. (1988). What Do You Care What Other People Think? Further Adventures of a Curious Character. New York: W. W. Norton.
- Fisher, R. A. (1936). The use of multiple measurements in taxonomic problems. *Annals of Eugenics*, 8, 379–388.
- Friendly, M. (1991). SAS System for Statistical Graphics. Cary, NC: SAS Institute, 1st edn.
- Friendly, M. (1995). Conceptual and visual models for categorical data. *The American Statistician*, 49, 153–160.
- Friendly, M. (2002). Corrgrams: Exploratory displays for correlation matrices. *The American Statistician*, 56(4), 316–324.
- Friendly, M. and Kwan, E. (2003). Effect ordering for data displays. *Computational Statistics and Data Analysis*, 43(4), 509–539.

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Friendly, M. and Kwan, E. (2011). Comment (graph people versus table people). *Journal of Computational and Graphical Statistics*, 20(1), 18–27.

- Glass, D. V. (1954). Social Mobility in Britain. Glencoe, IL: The Free Press.
- Hurley, C. B. (2004). Clustering visualizations of multidimensional data. *Journal of Computational and Graphical Statistics*, 13, 788–Ű806.
- Immer, F. R., Hayes, H., and Powers, L. R. (1934). Statistical determination of barley varietial adaptation. *Journal of the American Society of Agronomy*, 26, 403–419.
- Kosslyn, S. M. (1985). Graphics and human information processing: A review of five books. *Journal of the American Statistical Association*, 80, 499–512.
- Kosslyn, S. M. (1989). Understanding charts and graphs. Applied Cognitive Psychology, 3, 185–225.
- Lavine, M. (1991). Problems in extrapolation illustrated with space shuttle O-ring data. *Journal of the American Statistical Association*, 86, 912–922.
- Lewandowsky, S. and Spence, I. (1989). The perception of statistical graphs. *Sociological Methods & Research*, 18, 200–242.
- Lindsey, J. K. (1995). Modelling Frequency and Count Data. Oxford, UK: Oxford University Press.
- Pareto, V. (1971). *Manuale di economia politica ("Manual of political economy")*. New York: A.M. Kelley. Translated by Ann S. Schwier. Edited by Ann S. Schwier and Alfred N. Page.
- Shneiderman, B. (1992). Tree visualization with treemaps: A 2-D space-filling approach. *ACM Transactions on Graphics*, 11(1), 92–99.
- Spence, I. (1990). Visual psychophysics of simple graphical elements. *Journal of Experimental Psychology: Human Perception and Performance*, 16, 683–692.
- Spence, I. and Lewandowsky, S. (1990). Graphical perception. In J. Fox and J. S. Long, eds., *Modern Methods of Data Analysis*, chap. 1, (pp. 13–57). Sage Publications, Inc.
- Tufte, E. (2006). Beautiful Evidence. Cheshire, CT: Graphics Press.
- Tufte, E. R. (1983). The Visual Display of Quantitative Information. Cheshire, CT: Graphics Press.
- Tufte, E. R. (1990). *Envisioning Information*. Cheshire, CT: Graphics Press.
- Tufte, E. R. (1997). Visual Explanations: Images and Quantities, Evidence and Narrative. Cheshire, CT: Graphics Press.
- Wickham, H. (2009). ggplot2: Elegant Graphics for Data Analysis. Springer New York.
- Wickham, H. and Chang, W. (2013). ggplot2: An implementation of the Grammar of Graphics. R package version 0.9.3.1.
- Wilkinson, L. (2005). The Grammar of Graphics. New York: Springer, 2nd edn.
- Wright, K. (2013). Revisiting immer's barley data. *The American Statistician*, 67(3), 129–133.