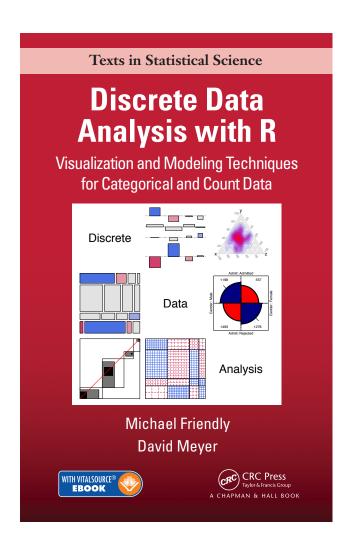
Discrete Data Analysis with R: Solutions and Hints to Exercises

January 25, 2016



This document is intended as an aid to instructors who wish to use *Discrete Data Analysis with R* in a course. It contains the text of the **Exercises** sections from all chapters, together with some solutions or hints for the various problems. Answers are indicated with the \bigstar symbol, and with text in this font.

All R code for the book, and other materials are available on the web site, http://ddar.datavis.ca.

Chapter 1

Introduction

These questions are all conceptual, or based on judgment. No solutions are provided. In general, students should come up with some interesting examples related to the questions and explain why they consider them to be good or bad graphic or tabular displays.

Exercise 1.1 A web page, "The top ten worst graphs," http://www.biostat.wisc.edu/~kbroman/topten_worstgraphs/ by Karl Broman lists his picks for the worst graphs (and a table) that have appeared in the statistical and scientific literature. Each entry links to graph(s) and a brief discussion of what is wrong and how it could be improved.

- (a) Examine a number of recent issues of a scientific or statistical journal in which you have some interest. Find one or more examples of a graph or table that is a particularly bad use of display material to summarize and communicate research findings. Write a few sentences indicating how or why the display fails and how it could be improved.
- (b) Do the same task for some popular magazine or newspaper that uses data displays to supplement the text for some story. Again, write a few sentences describing why the display is bad and how it could be improved.

Exercise 1.2 As in the previous exercise, examine the literature in recent issues of some journal of interest to you. Find one or more examples of a graph or table that you feel does a *good* job of summarizing and communicating research findings.

- (a) Write a few sentences describing why you chose these displays.
- (b) Now take the role of a tough journal reviewer. Are there any features of the display that could be modified to make them more effective?

Exercise 1.3 Infographics are another form of visual displays, quite different from the data graphics featured in this book, but often based on some data or analysis. Do a Google image search for the topic "Global warming" to see a rich collection.

- (a) Find and study one or two images that attempt some visual explanation of causes and/or effects of global warming. Describe the main message in a sentence or two.
- (b) What visual and graphic features are used in these to convey the message?

Exercise 1.4 The Wikipedia web page en.wikipedia.org/wiki/Portal:Global_warming gives a few data-based graphics on the topic of global warming. Read the text and study the graphs.

- (a) Write a short figure title for each that would announce the conclusion to be drawn in a presentation graphic.
- (b) Write a figure caption for each that would explain what is shown and the important graphical details for a reader to understand.

Exercise 1.5 The R Graph Gallery, http://rgraphgallery.blogspot.com/, contains a large collection of examples of graphs in R, tagged by type or content, together with the R code to produce them. Explore this collection for the terms (a) association plot (b) bar chart (c) categorical data (d) fluctuation diagram (e) mosaic plot Find one or two you particularly like and write a few sentences saying why you do.

Chapter 2

Working with Categorical Data

Exercise 2.1 The packages vcd (Meyer et al., 2015) and vcdExtra (Friendly, 2015) contain many data sets with some examples of analysis and graphical display. The goal of this exercise is to familiarize yourself with these resources. You can get a brief summary of these using the function datasets () from vcdExtra. Use the following to get a list of these with some characteristics and titles.

- (a) How many data sets are there altogether? How many are there in each package?
 - ★ nrow() gives the number of rows in a data frame. table() for a single variable gives the frequencies for each level.

- (b) Make a tabular display of the frequencies by Package and class.
 - ★ Use table(), but now for Package and class.

- (c) Choose one or two data sets from this list, and examine their help files (e.g., help (Arthritis) or ?Arthritis). You can use, e.g., example (Arthritis) to run the R code for a given example.
 - ★ Run the following types of commands:

```
> ?Arthritis  # Help Files
> ?Baseball  # Help Files
> example(Arthritis)  # Example Syntax/Analysis
> example(Baseball)  # Example Syntax/Analysis
```

Exercise 2.2 For each of the following data sets in the vcdExtra package, identify which are response variable(s) and which are explanatory. For factor variables, which are unordered (nominal) and which should be treated as ordered? Write a sentence or two describing substantitive questions of interest for analysis of the data. (*Hint*: use data(foo, package="vcdExtra") to load, and str(foo), help(foo) to examine data set foo.)

- (a) Abortion opinion data: Abortion
 - ★ Support_Abortion is the response, Sex and Status are binary, nominal explanatory variables. From help (Abortion), How does support for abortion depend on sex and status?

(b) Caesarian Births: Caesar

★ Infection is the response, Risk, Antibiotics and Planned are binary, nominal explanatory variables.

```
> data(Caesar, package="vcdExtra")
> str(Caesar)

table [1:3, 1:2, 1:2, 1:2] 0 1 17 0 1 1 11 17 30 4 ...
- attr(*, "dimnames")=List of 4
    ..$ Infection : chr [1:3] "Type 1" "Type 2" "None"
    ..$ Risk : chr [1:2] "Yes" "No"
    ..$ Antibiotics: chr [1:2] "Yes" "No"
    ..$ Planned : chr [1:2] "Yes" "No"
```

(c) Dayton Survey: DaytonSurvey

★ In DaytonSurvey, the variables cigarette, alcohol, and marijuana can all be treated as response variables. sex and race are potential explanatory variables. Potentially interesting questions are how each of the responses depend on sex and race, and how they vary jointly.

```
> data(DaytonSurvey, package="vcdExtra")
> str(DaytonSurvey)
```

(d) Minnesota High School Graduates: Hoyt

★ Status is the response, Rank, Occupation, and Sex are explanatory variables. Both Rank and Occupation are ordinal. How does Status vary with Rank, Occupation, and Sex?

```
> data(Hoyt, package="vcdExtra")
> str(Hoyt)
```

Exercise 2.3 The data set *UCBAdmissions* is a 3-way table of frequencies classified by Admit, Gender, and Dept.

(a) Find the total number of cases contained in this table.

★ For a table object, just use sum()

```
> data(UCBAdmissions)
> sum(UCBAdmissions)
[1] 4526
```

(b) For each department, find the total number of applicants.

★ Use margin.table(UCBAdmissions, 3) to find the marginal total for the third dimension (dept).

```
> margin.table(UCBAdmissions, 3)
Dept
A B C D E F
933 585 918 792 584 714
```

(c) For each department, find the overall proportion of applicants who were admitted.

 \star

```
> ucb.df <- as.data.frame(UCBAdmissions)
> abd <- xtabs(Freq ~ Dept + Admit, data=ucb.df)
> prop.table(abd, 1)
         Admit
Dept Admitted Rejected
        A 0.644159  0.355841
        B 0.632479  0.367521
        C 0.350763  0.649237
        D 0.339646  0.660354
        E 0.251712  0.748288
        F 0.064426  0.935574
```

(d) Construct a tabular display of department (rows) and gender (columns), showing the proportion of applicants in each cell who were admitted relative to the total applicants in that cell.

*

Exercise 2.4 The data set DanishWelfare in vcd gives a 4-way, $3 \times 4 \times 3 \times 5$ table as a data frame in frequency form, containing the variable Freq and four factors, Alcohol, Income, Status, and Urban. The variable Alcohol can be considered as the response variable, and the others as possible predictors.

- (a) Find the total number of cases represented in this table.
 - ★ This is a data set in the form of a frequency data frame, so sum the Freq variable

```
> data("DanishWelfare", package="vcd")
> sum(DanishWelfare$Freq)
[1] 5144
```

- (b) In this form, the variables Alcohol and Income should arguably be considered *ordered* factors. Change them to make them ordered.
 - ★ Use ordered() or as.ordered() on the factor variable. str() will then show them as Ord.factor.

- (c) Convert this data frame to table form, DanishWelfare.tab, a 4-way array containing the frequencies with appropriate variable names and level names.
 - ★ Use xtabs () with Freq as the response.

```
> DanishWelfare.tab <-xtabs(Freq ~ ., data = DanishWelfare)
> str(DanishWelfare.tab)

xtabs [1:3, 1:4, 1:3, 1:5] 1 3 2 8 1 3 2 5 2 42 ...
- attr(*, "dimnames")=List of 4
    ..$ Alcohol: chr [1:3] "<1" "1-2" ">2"
    ..$ Income : chr [1:4] "0-50" "50-100" "100-150" ">150"
    ..$ Status : chr [1:3] "Widow" "Married" "Unmarried"
    ..$ Urban : chr [1:5] "Copenhagen" "SubCopenhagen" "LargeCity" "City" ...
- attr(*, "class")= chr [1:2] "xtabs" "table"
- attr(*, "call")= language xtabs(formula = Freq ~ ., data = DanishWelfare)
```

- (d) The variable Urban has 5 categories. Find the total frequencies in each of these. How would you collapse the table to have only two categories, City, Non-city?
 - ★ margin.table() handles the first part; collapse.table() is designed for the second part. It is arguable whether SubCopenhagen should be considered City or NonCity.

```
> margin.table(DanishWelfare.tab, 4)
Urban
   Copenhagen SubCopenhagen
                                  LargeCity
                                                                 Country
> DW2 <- vcdExtra::collapse.table(DanishWelfare.tab,
                                   Urban=c("City", "NonCity", "City", "City", "NonCity"))
> head(ftable(DW2))
                                   "Urban" "City" "NonCity"
 "Alcohol" "Income"
                      "Status"
 "<1"
           "0-50"
                      "Widow"
                                               1.0
                      "Married"
                                              155
                                                         183
                      "Unmarried"
                                               14
                                                         10
                      "Widow"
            "50-100"
                                               2.9
                      "Married"
                                              338
                      "Unmarried"
```

(e) Use structable() or ftable() to produce a pleasing flattened display of the frequencies in the 4-way table. Choose the variables used as row and column variables to make it easier to compare levels of Alcohol across the other factors.

*

Exercise 2.5 The data set *UKSoccer* in vcd gives the distributions of number of goals scored by the 20 teams in the 1995/96 season of the Premier League of the UK Football Association.

This two-way table classifies all $20 \times 19 = 380$ games by the joint outcome (Home, Away), the number of goals scored by the Home and Away teams. The value 4 in this table actually represents 4 or more goals.

(a) Verify that the total number of games represented in this table is 380.

```
\star
```

```
> data("UKSoccer", package="vcd")
> sum(UKSoccer)
[1] 380
> margin.table(UKSoccer)
[1] 380
```

- (b) Find the marginal total of the number of goals scored by each of the home and away teams.
 - ★ Use margin.table() for each dimension:

```
> margin.table(UKSoccer, 1)
Home
    0     1     2     3     4
    76     142     90     45     27
> margin.table(UKSoccer, 2)
Away
    0     1     2     3     4
140     136     55     38     11
```

(c) Express each of the marginal totals as proportions.

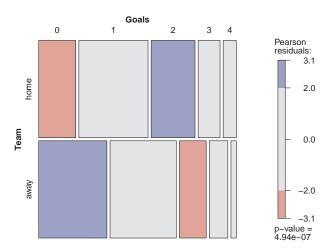
★ Use prop.table() on the result of margin.table() for each dimension:

- (d) Comment on the distribution of the numbers of home-team and away-team goals. Is there any evidence that home teams score more goals on average?
 - ★ You could find the mean number of goals, weighted by their marginal frequencies. On average, home teams score about 0.4 more goals.

```
> weighted.mean(0:4, w=margin.table(UKSoccer,1))
[1] 1.4868
> weighted.mean(0:4, w=margin.table(UKSoccer,2))
[1] 1.0632
```

Graphically, you could also compare the marginal frequencies in a mosaic plot, or use agreementplot ().

```
Goals
Team 0 1 2 3 4
home 76 142 90 45 27
away 140 136 55 38 11
> mosaic(margins, shade=TRUE)
```



Exercise 2.6 The one-way frequency table Saxony in VCd records the frequencies of families with 0, 1, 2, ... 12 male children, among 6115 families with 12 children. This data set is used extensively in Chapter 3.

```
> data("Saxony", package = "vcd")
> Saxony

nMales
0 1 2 3 4 5 6 7 8 9 10 11 12
3 24 104 286 670 1033 1343 1112 829 478 181 45 7
```

Another data set, <code>Geissler</code>, in the vcdExtra package, gives the complete tabulation of all combinations of boys and <code>girls</code> in families with a given total number of children (<code>size</code>). The task here is to create an equivalent table, <code>Saxony12</code> from the <code>Geissler</code> data.

```
> data("Geissler", package = "vcdExtra")
> str(Geissler)

'data.frame': 90 obs. of 4 variables:
    $ boys : int 0 0 0 0 0 0 0 0 0 0 0 ...
    $ girls: num 1 2 3 4 5 6 7 8 9 10 ...
    $ size : num 1 2 3 4 5 6 7 8 9 10 ...
    $ Freq : int 108719 42860 17395 7004 2839 1096 436 161 66 30 ...
```

(a) Use subset () to create a data frame, sax12 containing the Geissler observations in families with size==12.

★

```
> data("Saxony", package="vcd")
> data("Geissler", package="vcdExtra")
> sax12 <- subset(Geissler, size==12)</pre>
> sax12
     boys girls size Freq
12
         0
                  12
                          12
24
                            12
                                     24
                    11
                   10 12 104
9 12 286
8 12 670
45
                     8
54
           4
                            12 1033
```

```
69 6 6 12 1343

75 7 5 12 1112

80 8 4 12 829

84 9 3 12 478

87 10 2 12 181

89 11 1 12 45

90 12 0 12 7
```

(b) Select the columns for boys and Freq.

```
*
```

```
> sax12 <- subset(sax12, select=c("boys","Freq"))</pre>
```

(c) Use xtabs () with a formula, Freq ~ boys, to create the one-way table.



```
> Saxony12<-xtabs(Freq~boys, data=sax12)
> Saxony12
boys
0 1 2 3 4 5 6 7 8 9 10 11 12
3 24 104 286 670 1033 1343 1112 829 478 181 45 7
```

(d) Do the same steps again to create a one-way table, Saxony11, containing similar frequencies for families of size==11.

```
*
```

```
> sax11 <- subset(Geissler, size==11, select = c("boys","Freq"))
> Saxony11 <- xtabs(Freq~boys, data=sax11)
> Saxony11
boys
0  1  2  3  4  5  6  7  8  9  10  11
8  72  275  837  1540  2161  2310  1801  1077  492  93  24
```

Exercise 2.7 * Interactive coding of table factors: Some statistical and graphical methods for contingency tables are implemented only for two-way tables, but can be extended to 3+-way tables by recoding the factors to interactive combinations along the rows and/or columns, in a way similar to what ftable() and structable() do for printed displays.

For the *UCBAdmissions* data, produce a two-way table object, UCB.tab2, that has the combinations of Admit and Gender as the rows, and Dept as its columns, to look like the result below:

```
Dept
Admit:Gender
                    Α
                        В
                             С
                                     Ε
                                         F
  Admitted:Female 89
                       17 202 131
                                    94
                                        24
  Admitted:Male
                  512 353 120 138
                                    53
                        8 391 244 299 317
  Rejected: Female 19
                  313 207 205 279 138 351
  Rejected: Male
```

(a) Try this the long way: convert *UCBAdmissions* to a data frame (as.data.frame()), manipulate the factors (e.g., interaction()), then convert back to a table (as.data.frame()).

(b) Try this the short way: both ftable() and structable() have as.matrix() methods that convert their result to a matrix.

Exercise 2.8 The data set VisualAcuity in vcd gives a $4 \times 4 \times 2$ table as a frequency data frame.

```
> data("VisualAcuity", package = "vcd")
> str(VisualAcuity)

'data.frame': 32 obs. of 4 variables:
$ Freq : num 1520 234 117 36 266 ...
$ right : Factor w/ 4 levels "1","2","3","4": 1 2 3 4 1 2 3 4 1 2 ...
$ left : Factor w/ 4 levels "1","2","3","4": 1 1 1 1 2 2 2 2 3 3 ...
$ gender: Factor w/ 2 levels "male","female": 2 2 2 2 2 2 2 2 2 ...
```

(a) From this, use xtabs () to create two 4×4 frequency tables, one for each gender.

 \star

(b) Use structable() to create a nicely organized tabular display.

+

```
> structable(right ~ left + gender, data = va.tab)
                            3
            right 1 2
left gender
                             72
    male
                  821 116
                                   43
                 1520 234 117
112 494 151
     female
                                   36
2
     male
    female
                  266 1512
                            362
                  85 145 583
124 432 1772
    male
                                  179
    female
    male
                    35
                        27
                              87
                                  331
   female
                       78 205
               66
                                 492
```

(c) Use xtable() to create a LATEX or HTML table.

```
> library(xtable)
> va.xtab <- xtable(va.tabm)
> print(va.xtab, type="html")
```

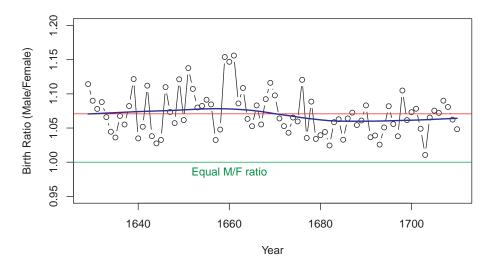
Chapter 3

Fitting and Graphing Discrete Distributions

Exercise 3.1 The Arbuthnot data in HistData (Friendly, 2014a) (Example 3.1) also contains the variable Ratio, giving the ratio of male to female births.

(a) Make a plot of Ratio over Year, similar to Figure 3.1. What features stand out? Which plot do you prefer to display the tendency for more male births?

 \star

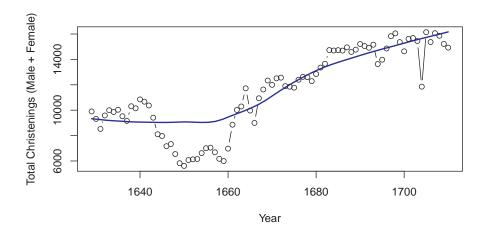


The plot is similar to Figure 3.1 in the text. If it is easier to think in terms of probability of a male birth, plotting that directly may be preferable.

(b) Plot the total number of christenings, Males + Females or Total (in 000s) over time. What unusual features do you see?

```
\star
```

```
> # total number of Christenings
> with(Arbuthnot, {
    Total= Males + Females
+ plot(Year, Total, type='b', ylab="Total Christenings (Male + Female)")
+ Arb.smooth <- loess.smooth(Year, Total)
+ lines(Arb.smooth$x, Arb.smooth$y, col="blue", lwd=2)
+ })</pre>
```



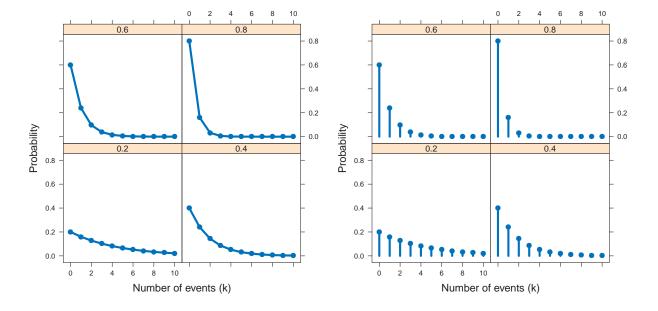
There was a large decline in births between 1640–1660, corresponding to years of plague in England.

Exercise 3.2 Use the graphical methods illustrated in Section 3.2 to plot a collection of geometric distributions for p = 0.2, 0.4, 0.6, 0.8, over a range of values of $k = 0, 1, \dots 10$.

(a) With xyplot(), try the different plot formats using points connected with lines, as in Figure 3.9, or using points and lines down to the origin, as in the panels of Figure 3.10.

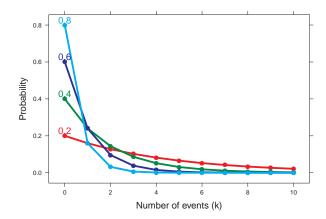
*

```
> KL <- expand.grid(k = 0 : 10, p = c(0.2, 0.4, 0.6, 0.8))
> geom_df <- data.frame(KL, prob = dgeom(KL$k, KL$p))
> geom_df$p = factor(geom_df$p)
> library(lattice)
> mycol<-palette()[2:5]
> xyplot(prob ~ k | p , data = geom_df, type = c("b"),
+ pch = 16, lwd = 4, cex = 1.25,
+ xlab = list("Number of events (k)", cex = 1.25), layout = c(2,2),
+ ylab = list("Probability", cex = 1.25))
> xyplot(prob ~ k | p , data = geom_df, type = c("h", "p"),
+ pch = 16, lwd = 4, cex = 1.25,
+ xlab = list("Number of events (k)", cex = 1.25), layout = c(2,2),
+ ylab = list("Number of events (k)", cex = 1.25), layout = c(2,2),
+ ylab = list("Probability", cex = 1.25))
```



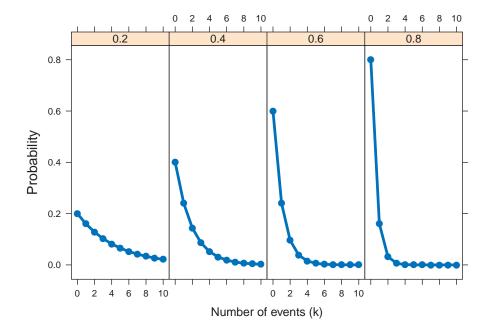
(b) Also with xyplot(), produce one version of a multi-line plot in a single panel that you think shows well how these distributions change with the probability p of success.

*



(c) Do the same in a multi-panel version, conditional on p.

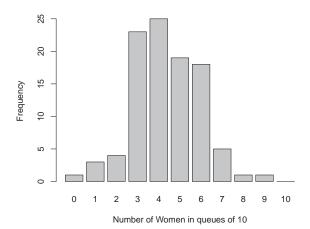
 \star



Exercise 3.3 Use the data set WomenOueue to:

(a) Produce plots analogous to those shown in Section 3.1 (some sort of bar graph of frequencies).

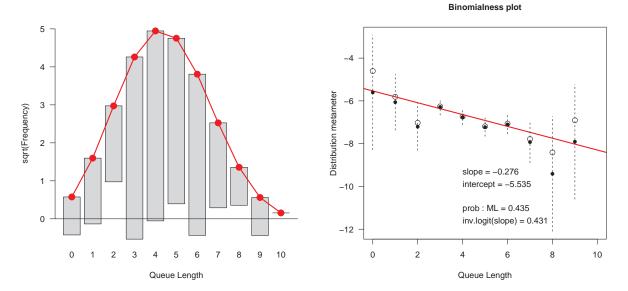
```
> data("WomenQueue", package = "vcd")
> barplot(WomenQueue, xlab="Number of Women in queues of 10", ylab= "Frequency")
```



(b) Check for goodness-of-fit to the binomial distribution using the goodfit () methods described in Section 3.3.2. \bigstar Note that with goodfit (), you should specify n=10 for the binomial distribution as the size parameter.

- (c) Make a reasonable plot showing departure from the binomial distribution.
 - ★ The simplest plot is the hanging rootogram. An alternative plot is a "binomialness" plot produced by distplot().

```
> plot(gf.women, xlab = "Queue Length")
> distplot(WomenQueue, type = "binomial", size=10, xlab = "Queue Length")
```



(d) Suggest some reasons why the number of women in queues of length 10 might depart from a binomial distribution, Bin(n = 10, p = 1/2).

*

- Perhaps women (or men) are more prevalent in these queues, so $p \neq 1/2$.
- · People often join lines in groups, so the observations are unlikely to be independent.

Exercise 3.4 Continue Example 3.13 on the distribution of male children in families in Saxony by fitting a binomial distribution, $Bin(n = 12, p = \frac{1}{2})$, specifying equal probability for boys and girls. [*Hint*: you need to specify both size and prob values for goodfit().]

(a) Carry out the GOF test for this fixed binomial distribution. What is the ratio of χ^2/df ? What do you conclude? \bigstar Note that you need to specify both n and p as fixed parameters here.

The binomial model fits very badly.

(b) Test the additional lack of fit for the model $Bin(n=12,p=\frac{1}{2})$ compared to the model $Bin(n=12,p=\hat{p})$ where \hat{p} is estimated from the data.

```
\star
```

This fits much better, but still not a good fit.

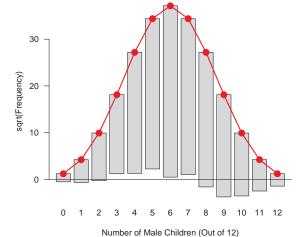
(c) Use the plot.gootfit() method to visualize these two models.

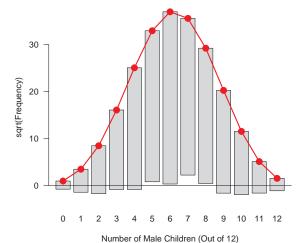


```
> plot(Saxony_gf, main = "Fit for p=0.5", xlab = "Number of Male Children (Out of 12)")
> plot(Saxony_gf2, main = "Fit for p=phat", xlab = "Number of Male Children (Out of 12)")
```

Fit for p=0.5

Fit for p=phat





Exercise 3.5 For the Federalist data, the examples in Section 3.3.1 and Section 3.3.2 showed the negative binomial to provide an acceptable fit. Compare this with the simpler special case of geometric distribution, corresponding to n = 1.

(a) Use goodfit() to fit the geometric distribution. [Hint: use type="nbinomial", but specify size=1 as a parameter.]

 \star

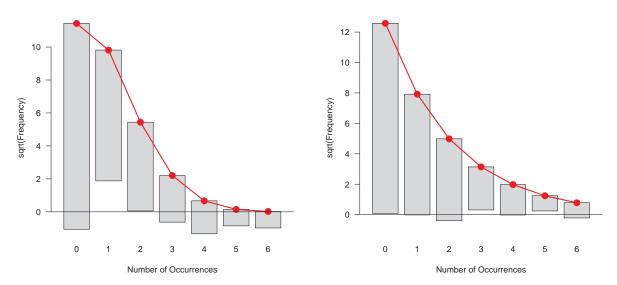
```
> fdfit1 <- goodfit(Federalist, type = "binomial", par = list(size=6))</pre>
> fdfit1
Observed and fitted values for binomial distribution
with parameters estimated by `ML'
 count observed
                    fitted pearson residual
    0 156 1.3072e+02
                             2.21074
-3.39860
             63 9.6362e+01
             29 2.9597e+01
                                    -0.10972
                                   1.43139
5.31624
              8 4.8483e+00
             8 4.8483e+00
4 4.4673e-01
1 2.1954e-02
1 4.4953e-04
                                      6.60094
                                   47.14399
> fdfit2 <- goodfit(Federalist, type = "nbinomial", par = list(size=1))</pre>
Observed and fitted values for nbinomial distribution
with parameters estimated by `ML with size fixed'
                   fitted pearson residual
 count observed
                             -0.172219
           156 158.16590
             63 62.68326
                                   0.040006
             29 24.84221
                                   0.834194
             8 9.84530
4 3.90182
                                  -0.588102
                                  0.049702
     4
                   1.54635
                                  -0.439353
                              -0.015044
                  0.61284
```

(b) Compare the negative binomial and the geometric models statistically, by a likelihood-ratio test of the difference between these two models.

 \star

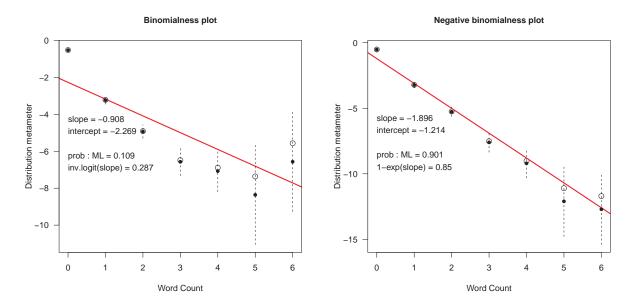
(c) Compare the negative binomial and the geometric models visually by hanging rootograms or other methods. ★ Hanging rootograms:

```
> plot(fdfit1)
> plot(fdfit2)
```



Distribution-ness plots:

```
> distplot(Federalist, type = "binomial", size=6, xlab = "Word Count")
> distplot(Federalist, type = "nbinomial", size=6, xlab = "Word Count")
```



Exercise 3.6 Mosteller and Wallace (1963, Table 2.4) give the frequencies, n_k , of counts $k = 0, 1, \ldots$ of other selected marker words in 247 blocks of text known to have been written by Alexander Hamilton. The data below show the occurrences of the word *upon*, that Hamilton used much more than did James Madison.

```
> count <- 0 : 5
> Freq <- c(129, 83, 20, 9, 5, 1)
```

- (a) Read these data into R and construct a one-way table of frequencies of counts or a matrix or data frame with frequencies in the first column and the corresponding counts in the second column, suitable for use with goodfit().
 - *\pmodfit() requires its first argument to be either a one-way table (from xtabs()), or a data.frame with frequencies in the *first* column and the corresponding counts in the second column. Both of the following forms will work.

(b) Fit and plot the Poisson model for these frequencies.

```
*
```

```
> (up0 <- goodfit(Upon, type="poisson"))</pre>
Observed and fitted values for poisson distribution
with parameters estimated by `ML'
             rved fitted pearson residual 129 121.61816 0.66937
                               0.66937
-0.34115
              83 86.16671
               20
                  30.52465
                                      -1.90494
                   7.20892
                                      0.66708
                    1.27688
                                        3.29481
                    0.18094
                                       1.75800
> summary(up0)
 Goodness-of-fit test for poisson distribution
X^2 df P(> X^2)
Likelihood Ratio 13.139 4 0.010617
> plot (up0)
```



(c) Fit and plot the negative binomial model for these frequencies.

```
*
```

```
83
                 73.89421
                                   1.059285
             20
                 28.41547
                                  -1.578705
                  9.25319
                                  -0.083233
                  2.74068
                                   1.364738
                  0.76332
                                   -0.036432
> summary (up1)
Goodness-of-fit test for nbinomial distribution
                    X^2 df P(> X^2)
Likelihood Ratio 6.0306 3 0.11013
> plot (up1)
```



(d) What do you conclude?

★ The negative binomial model fits better than the Poisson.

Exercise 3.7 The data frame *Geissler* in the vcdExtra package contains the complete data from Geissler's (1889) tabulation of family sex composition in Saxony. The table below gives the number of boys in families of size 11.

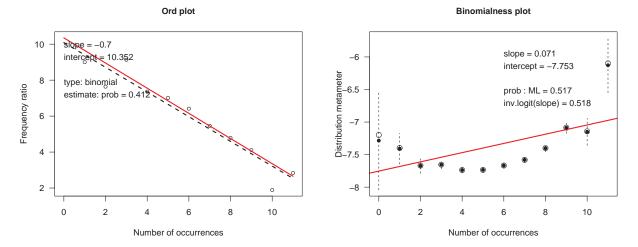
boys	0	1	2	3	4	5	6	7	8	9	10	11
Freq	8	72	275	837	1,540	2,161	2,310	1,801	1,077	492	93	24

- (a) Read these data into R.
 - ★ See Exercise 2.6, which calculates sax11 in the form of a data frame.
- (b) Following Example 3.13, use goodfit () to fit the binomial model and plot the results. Is there an indication that the binomial does not fit these data?
 ★ The binomial distribution fits badly, where the extremes are under-fitted, and the middle values are over-fitted.

```
> sax11.tab <- xtabs(Freq ~ boys, data=sax11)
> goodfit(sax11.tab, type="binomial", par=list(size=11))
Observed and fitted values for binomial distribution
with parameters estimated by `ML'
 count observed
                       fitted pearson residual
                       3.5616
                8
                                           2.3518
                    41.9479 224.5724
                                            4.6400
              275
                                           3.3650
             837 721.3629
1540 1544.7559
                                           4.3055
                                           -0.1210
             2161 2315.6023
2310 2479.3627
                                           -3.2128
                                           -3.4013
             1801 1896.2173
                                           -2.1866
      8
              1077 1015.1593
                                            1.9409
              492
                    362.3173
                                            6.8130
     10
               93
                      77.5881
                                            1.7497
                       7.5523
                                            5.9850
> summary(goodfit(sax11.tab, type="binomial", par=list(size=11)))
```

- (c) Diagnose the form of the distribution using the methods described in Section 3.4.
 - ★ The Ord plot indicates that the closest distribution according to its heuristics is the binomial; the binomialness distribution plot, however, shows this is not an acceptable model, as was also seen in the text for families of size 12.

```
> Ord_plot(sax11.tab)
> distplot(sax11.tab, type="binomial", size=11)
```



(d) Try fitting the negative binomial distribution, and use distplot () to diagnose whether the negative binomial is a reasonable fit. **TODO**: Something wrong here.

```
> goodfit(sax11.tab, type="nbinomial", par=list(size=11))
Observed and fitted values for nbinomial distribution with parameters estimated by `ML with size fixed' \,
 count observed
                    fitted pearson residual
                8
                   109.12
                                       -9.6801
               72
                    409.11
                                      -16.6667
              275 836.63
                                      -19.4171
              837 1235.67
                                      -11.3414
                                        1.7171
             1540 1474.07
             2161 1507.26
                                       16.8389
             2310 1369.95
                                       25.3981
             1801 1133.97
                                       19.8082
             1077
                   869.62
                                        7.0323
                   625.73
              492
                                       -5.3462
                   426.55
               93
                                      -16.1500
                                       -25.3999
```

Exercise 3.8 The data frame *Bundesliga* gives a similar data set to that for UK soccer scores (*UKSoccer*) examined in Example 3.9, but over a wide range of years. The following lines calculate a two-way table, BL1995, of home-team and away-team goals for the 306 games in the year 1995.

```
4 3 5 3 0 0 0 0
5 4 1 0 1 0 0 0
```

- (a) As in , find the one-way distributions of HomeGoals, AwayGoals, and TotalGoals = HomeGoals +
 - ★ There are several ways to do this, but as illustrated in the text for Example 3.9, create the one-way variables in a data.frame, and then use xtabs () to get their marginal distributions.

```
> BL.df <- as.data.frame(BL1995, stringsASFactors=FALSE)
> BL.df <- as.data.rrame(BL1995, strings)
BL.df <- within(BL.df, {
+ HomeGoals <- as.numeric(HomeGoals)
+ AwayGoals <- as.numeric(AwayGoals)
+ TotalGoals <- HomeGoals + AwayGoals
      # marginal distributions
> (BL.home <- xtabs(Freq ~ HomeGoals, data=BL.df))
HomeGoals

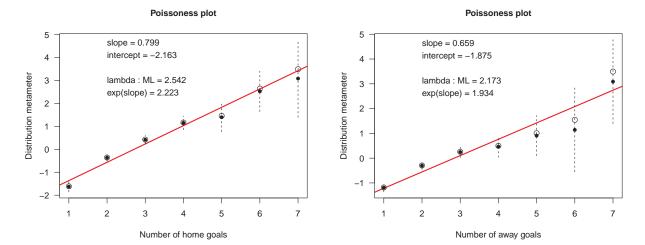
1 2 3 4 5 6 7
61 107 78 41 11 6 2
> (BL.away <- xtabs(Freq ~ AwayGoals, data=BL.df))</pre>
       2 3 4
 1 2 3 4 5 6 7
94 114 66 21 7 2 2
> (BL.total <- xtabs(Freq ~ TotalGoals, data=BL.df))
TotalGoals
2 3 4 5 6 7 8 9 10 11 12 13 14 26 35 98 62 39 29 10 4 2 1 0 0 0
```

- (b) Use goodfit () to fit and plot the Poisson distribution to each of these. Does the Poisson seem to provide a reasonable fit?
 ★ The Poisson distribution has a bad fit for all of these.

```
> summary(goodfit(BL.home))
Goodness-of-fit test for poisson distribution
                   X^2 df P(> X^2)
Likelihood Ratio 70.722 5 7.2516e-14
> summary(goodfit(BL.away))
Goodness-of-fit test for poisson distribution
                   X^2 df P(> X^2)
Likelihood Ratio 97.973 5 1.4131e-19
> summary(goodfit(BL.total))
Goodness-of-fit test for poisson distribution
                   X^2 df P(> X^2)
Likelihood Ratio 72.558 8 1.5185e-12
```

- (c) Use distplot () to assess fit of the Poisson distribution.
 - ★ The distribution plots for home goals looks better than that for away goals, which shows a systematic departure from the red line.

```
> distplot(BL.home, xlab="Number of home goals")
> distplot(BL.away, xlab="Number of away goals")
```



- (d) What circumstances of scoring goals in soccer might cause these distributions to deviate from Poisson distributions?
 - ★ The Poisson distribution relies on (a) independent events with (b) constant probabilities. The probability of scoring a goal is almost certainly not constant over all pairs of teams.

Exercise 3.9 * Repeat the exercise above, this time using the data for all years in which there was the standard number (306) of games, that is for Year>1965, tabulated as shown below.

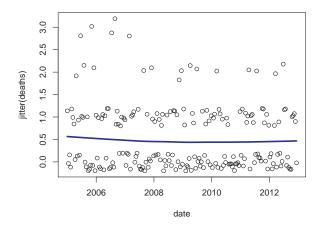
```
> BL <- xtabs(~ HomeGoals + AwayGoals, data = Bundesliga,
                subset = (Year > 1965))
> BL
          AwayGoals
HomeGoals
                                                                   9
                  590
            868
                        458
                              206
                                     88
                                           22
                                                       2
                                                                   0
                                                 12
           1049 1550
                        589
                              360
                                    121
                                           34
                                                 8
                                                       6
           1039
                        810
                                     95
                                           26
                                                                   0
             712
                  793
                        392
                              187
                                     43
                                           8
                                                                   0
                  388
                        245
                                                                   0
             128
                  164
                        106
                               34
                                                             0
                                                                   0
                   63
                         38
                               10
        8
                                                             0
                                                                   0
                     0
        10
        11
                     2
                          0
                                0
                                      0
                                                                   0
```

★ The steps are similar to those in the previous problem, but now there are more years, and the range of both home goals and away goals is larger.

Exercise 3.10 Using the data CyclingDeaths introduced in Example 3.6 and the one-way frequency table CyclingDeaths.tab = table (CyclingDeaths\$deaths),

- (a) Make a sensible plot of the number of deaths over time. For extra credit, add a smoothed curve (e.g., using lines(lowess(...))).
 - ★ The number of deaths in a given fortnight are discrete, taking values 0:3. A barplot, using plot (deaths ~ date, type="h", data=CyclingDeaths) is one option. Perhaps slightly better is to jitter the number of deaths.

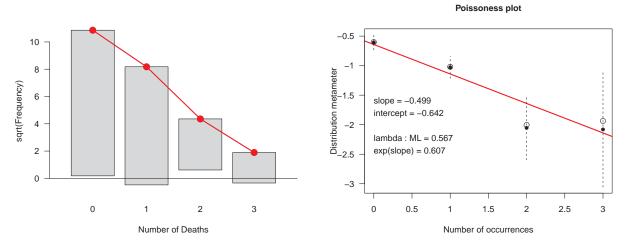
```
> data("CyclingDeaths", package="vcdExtra")
> CyclingDeaths.tab <- table(CyclingDeaths$deaths)
> plot(jitter(deaths) ~ date, data=CyclingDeaths)
> with(CyclingDeaths, {lines(lowess(date, deaths), lwd=3, col="blue")})
```



 $(b) \ \ Test \ the \ goodness \ of \ fit \ of \ the \ table \ \texttt{CyclingDeaths.tab} \ to \ a \ Poisson \ distribution \ statistically \ using \ \texttt{goodfit} \ () \ .$

(c) Continue this analysis using a ${\tt rootogram}$ () and ${\tt distplot}$ ().

```
> plot(gf, xlab="Number of Deaths")
> distplot(CyclingDeaths.tab)
```



(d) Write a one-paragraph summary of the results of these analyses and your conclusions.

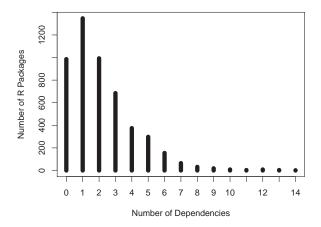
Exercise 3.11 * The one-way table, *Depends*, in vcdExtra and shown below gives the frequency distribution of the number of dependencies declared in 4,983 R packages maintained on the CRAN distribution network on January 17, 2014. That is, there were 986 packages that had no dependencies, 1,347 packages that depended on one other package, . . . up to 2 packages that depended on 14 other packages.

Depends	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14
# Pkgs	986	1,347	993	685	375	298	155	65	32	19	9	4	9	4	2

(a) Make a bar plot of this distribution.

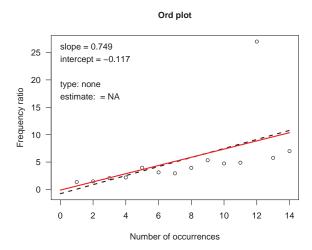
*

```
> data("Depends", package="vcdExtra")
> plot(Depends, xlab="Number of Dependencies", ylab="Number of R Packages", lwd=8)
```

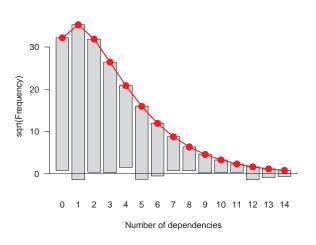


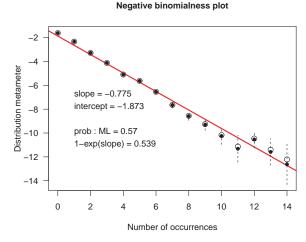
- (b) Use Ord_plot () to see if this method can diagnose the form of the distribution.
 - ★ This turns out to be a case where the Ord plot method, as implemented in Ord_plot() does not determine the form of the distribution. According to Table 3.11, the log series distribution is the only one with positive slope b and negative intercept a, but this requires a = -b.

> Ord_plot (Depends)



- (c) Try to fit a reasonable distribution to describe dependencies among R packages.
 - ★ Among the distributions described in Chapter 3 and implemented in the vcd package the negative binomial may be the best to try.





So, this does not fit well, particularly for the packages with many dependencies, but it is not altogether terrible. The remaining differences come from further heterogeneity for which we haven't got any covariates in the data set. For example, the age of the package would seem like a natural candidate: older packages probably have fewer dependencies.

Exercise 3.12 * How many years does it take to get into the baseball Hall of Fame? The Lahman (Friendly, 2014b) package provides a complete record of historical baseball statistics from 1871 to the present. One table, HallOfFame, records the history of players nominated to the Baseball Hall of Fame, and those eventually inducted. The table below, calculated in help (HallOfFame, package="Lahman"), records the distribution of the number of years taken (from first nomination) for the 109 players in the Hall of Fame to be inducted (1936–present). Note that years==0 does not, and cannot, occur in this table, so the distribution is restricted to positive counts. Such distributions are called *zero-truncated distributions*. Such distributions are like the ordinary ones, but with the probability of zero being zero. Thus the other probabilities are scaled up (i.e., divided by 1 - Pr(Y = 0)) so they sum to 1.

years	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
inducted	46	10	8	7	8	4	2	4	6	3	3	1	4	1	2

(a) For the Poisson distribution, show that the zero-truncated probability function can be expressed in the form

$$\Pr\{X = k \mid k > 0\} = \frac{1}{1 - e^{-\lambda}} \times \frac{e^{-\lambda} \lambda^k}{k!} \qquad k = 1, 2, \dots$$

★ The standard Poisson distribution has the probability mass function

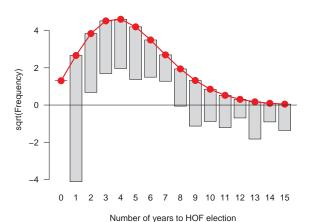
$$\Pr\{X = k\} = \frac{e^{-\lambda} \lambda^k}{k!} \quad k = 1, 2, \dots.$$

For this, $\Pr\{X=0\}=e^{-\lambda}$. The formula given in the problem scales the standard probability to account for zero-truncation, i.e., by the factor $\frac{1}{1-\Pr\{X=0\}}$.

(b) Show that the mean is $\lambda/(1 - \exp(-\lambda))$.

- (c) Enter these data into R as a one-way table, and use goodfit () to fit the standard Poisson distribution, as if you hadn't encountered the problem of zero truncation.
 - ★ The rootogram below shows why zero truncation needs to be taken into account.

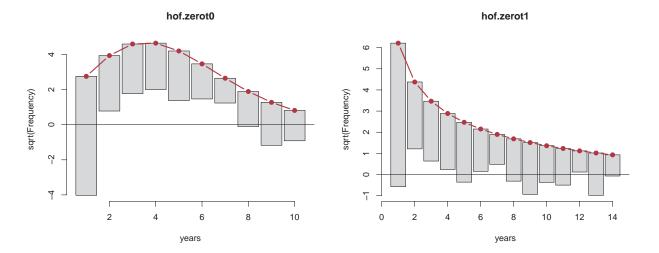
```
> years <- 1:15
> inducted <- c(46, 10, 8, 7, 8, 4, 2, 4, 6, 3, 3, 1, 4, 1, 2)
> HOF.df <- data.frame(years, inducted)
> HOF.tab <- xtabs(inducted ~ years, data=HOF.df)
> goodfit(HOF.tab)
Observed and fitted values for poisson distribution with parameters estimated by `ML' \,
                           fitted pearson residual
                      1.7081050
                  0
                                                -1.30694
                  46 7.0988218
                                               14.60056
                  10 14.7512214
                                                -1.23706
                  8 20.4351783
                                               -2.75082
                   7 21.2319627
                                                -3.08866
                  8 17.6478516
                                                -2.29660
                   4 12.2239706
                                               -2.35221
                  2 7.2574819
4 3.7702285
6 1.7409924
                                               -1.95157
       8
                                                0.11833
                                                3.22782
       9
                   3 0.7235500
     1.0
                                                2.67623
                   3 0.2733679
     11
                                                5.21498
                  1 0.0946756
4 0.0302668
                                                 2.94229
                                                22.81803
      14
                   1 0.0089848
                                                10.45503
     15
                   2 0.0024894
                                                34.54549
> summary(HOF.tab)
Number of cases in table: 109
Number of factors: 1
> plot(goodfit(HOF.tab), xlab='Number of years to HOF election')
```



Though not asked in the problem, the zero-truncated Poisson distribution can be fit using vglm() in the VGAM (Yee, 2015) package.

Models for count data, taking account of excess zeros or zero truncation are examined in more detail in Chapter 11. There, we use the countreg (Zeileis and Kleiber, 2014) package, that provides a zerotrunc() function for these problems. The zero truncated negative binomial provides a better fit than the zero truncated Poisson, but that is not great either.

```
> library(countreg)
> hof.zerot0 <- zerotrunc(years ~ 1, weights = inducted, data=HOF.df)
> hof.zerot1 <- zerotrunc(years ~ 1, weights = inducted, dist="negbin")
> countreg::rootogram(hof.zerot0)
> countreg::rootogram(hof.zerot1)
```



Chapter 4

Two-Way Contingency Tables

Exercise 4.1 The data set fat, created below, gives a 2×2 table recording the level of cholesterol in diet and the presence of symptoms of heart disease for a sample of 23 people.

(a) Use chisq.test (fat) to test for association between diet and disease. Is there any indication that this test may not be appropriate here?



(b) Use a fourfold display to test this association visually. Experiment with the different options for standardizing the margins, using the margin argument to fourfold(). What evidence is shown in different displays regarding whether the odds ratio differs significantly from 1?



(c) oddsratio(fat, log = FALSE) will give you a numerical answer. How does this compare to your visual impression from fourfold displays?



(d) With such a small sample, Fisher's exact test may be more reliable for statistical inference. Use fisher.test (fat), and compare these results to what you have observed before.

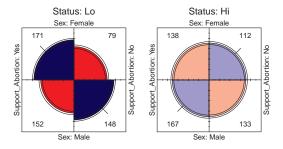


(e) Write a one-paragraph summary of your findings and conclusions for this data set.

Exercise 4.2 The data set Abortion in vcdExtra gives a $2 \times 2 \times 2$ table of opinions regarding abortion in relation to sex and status of the respondent. This table has the following structure:

(a) Taking support for abortion as the outcome variable, produce fourfold displays showing the association with sex, stratified by status.

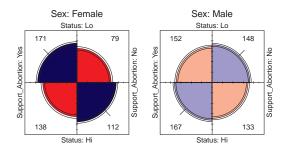
```
\star
```



(b) Do the same for the association of support for abortion with status, stratified by sex.



```
> Abortion3<-aperm(Abortion, c(2,3,1))
> fourfold(Abortion3)
```



(c) For each of the problems above, use oddsratio() to calculate the numerical values of the odds ratio, as stratified in the question.

 \star

```
# Sex by support for abortion, stratified by status
> summary (oddsratio (Abortion2))
z test of coefficients:
                       Estimate Std. Error z value Pr(>|z|)
Female:Male/Yes:No|Lo 0.7455 0.1784 4.18 2.9e-05
Female:Male/Yes:No|Hi -0.0189 0.1723 -0.11 0.91
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
>  # Status by support for abortion, stratified by sex
> summary(oddsratio(Abortion3))
z test of coefficients:
                      Estimate Std. Error z value Pr(>|z|)
                       0.563
                                            3.03
-1.23
Lo:Hi/Yes:No|Female
                                     0.186
                                                        0.0025
Lo:Hi/Yes:No|Male
                                      0.164
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

- (d) Write a brief summary of how support for abortion depends on sex and status.
 - ★ Regardless of status, more women say no to abortion and more men say yes. Regardless of gender, more low status say no and more high status say yes.

Exercise 4.3 The *JobSat* table on income and job satisfaction created in Example 2.5 is contained in the vcdExtra package.

(a) Carry out a standard χ^2 test for association between income and job satisfaction. Is there any indication that this test might not be appropriate? Repeat this test using simulate.p.value = TRUE to obtain a Monte Carlo test that does not depend on large sample size. Does this change your conclusion?



(b) Both variables are ordinal, so CMH tests may be more powerful here. Carry out that analysis. What do you conclude?



Exercise 4.4 The Hospital data in vcd gives a 3×3 table relating the length of stay (in years) of 132 long-term schizophrenic patients in two London mental hospitals with the frequency of visits by family and friends.

(a) Carry out a χ^2 test for association between the two variables.

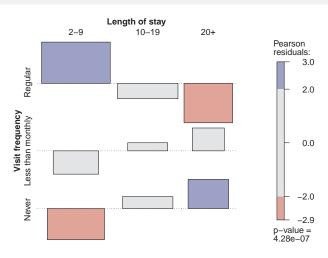


```
> data("Hospital", package="vcd")
> chisq.test(Hospital)
Pearson's Chi-squared test
data: Hospital
X-squared = 35.2, df = 4, p-value = 4.3e-07
```

(b) Use association () to compute association statistics. How would you describe the strength of association here?

By the contingency coefficient, there is moderately strong association between the length of stay long-term schizophrenic patients and the frequency of visits by family and friends.

(c) Produce an association plot for these data, with visit frequency as the vertical variable. Describe the pattern of the relation you see here.



(d) Both variables can be considered ordinal, so CMHtest () may be useful here. Carry out that analysis. Do any of the tests lead to different conclusions?

```
> CMHtest (Hospital)

Cochran-Mantel-Haenszel Statistics for Visit frequency by Length of stay

AltHypothesis Chisq Df Prob

cor Nonzero correlation 29.1 1 6.74e-08

rmeans Row mean scores differ 34.4 2 3.40e-08

cmeans Col mean scores differ 29.6 2 3.72e-07

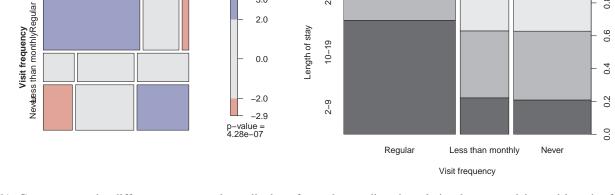
general General association 34.9 4 4.86e-07
```

The results of all four tests lead to the same conclusion that there is a significant association between the visit frequency and the length of stay. The test for non-zero correlation, trteating both variables as ordinal, has the largest ratio of χ^2/df .

Exercise 4.5 Continuing with the *Hospital* data:

(a) Try one or more of the following other functions for visualizing two-way contingency tables with this data: plot(), tile(), mosaic(), and spineplot(). [For all except spineplot(), it is useful to include the argument shade=TRUE].





(b) Comment on the differences among these displays for understanding the relation between visits and length of stay.

 \star

Exercise 4.6 The two-way table *Mammograms* in vcdExtra gives ratings on the severity of diagnosis of 110 mammograms by two raters.

(a) Assess the strength of agreement between the raters using Cohen's κ , both unweighted and weighted.

```
★
> Kappa (Mammograms)

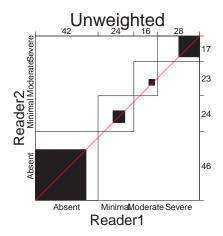
value ASE z Pr(>|z|)
Unweighted 0.371 0.0603 6.15 7.56e-10
Weighted 0.596 0.0492 12.11 8.90e-34
```

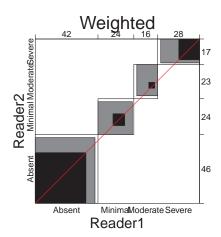
```
> Kappa (Mammograms, weights= "Fleiss-Cohen")

value ASE z Pr(>|z|)
Unweighted 0.371 0.0603 6.15 7.56e-10
Weighted 0.764 0.0400 19.12 1.67e-81
```

(b) Use agreementplot() for a graphical display of agreement here.

```
> agreementplot (Mammograms, main="Unweighted", weights=1)
> agreementplot (Mammograms, main="Weighted")
```





(c) Compare the Kappa measures with the results from assocstats(). What is a reasonable interpretation of each of these measures?

Exercise 4.7 Agresti and Winner (1997) gave the data in Table 4.1 on the ratings of 160 movies by the reviewers Gene Siskel and Roger Ebert for the period from April 1995 through September 1996. The rating categories were Con ("thumbs down"), Mixed, and Pro ("thumbs up").

Table 4.1: Movie ratings by Siskel & Ebert, April 1995-September 1996. Source: Agresti and Winner (1997)

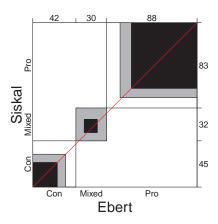
	, 1		Ebert		
		Con	Mixed	Pro	Total
	Con	24	8	13	45
Siskel	Mixed	8	13	11	32
	Pro	10	9	64	83
	Total	42	30	88	160

(a) Assess the strength of agreement between the raters using Cohen's κ , both unweighted and weighted.

(b) Use agreementplot() for a graphical display of agreement here.



```
> agreementplot(ratings)
```



(c) Assess the hypothesis that the ratings are *symmetric* around the main diagonal, using an appropriate χ^2 test. *Hint*: Symmetry for a square table T means that $t_{ij} = t_{ji}$ for $i \neq j$. The expected frequencies under the hypothesis of symmetry are the average of the off-diagonal cells, $E = (T + T^{\mathsf{T}})/2$.

```
\star
```

```
> T <- (ratings + t(ratings))/2
> (Chisq <- sum((ratings - T)^2 / T))
[1] 0.5913
> df <- nrow(T) * (nrow(T)-1) /2
> pchisq(Chisq,df, lower.tail = FALSE)
[1] 0.89842
```

(d) Compare the results with the output of mcnemar.test().

\star

```
> mcnemar.test(ratings)
McNemar's Chi-squared test
data: ratings
McNemar's chi-squared = 0.591, df = 3, p-value = 0.9
```

Exercise 4.8 For the *VisualAcuity* data set:

(a) Use the code shown in the text to create the table form, VA.tab.

```
\star
```

```
> data("VisualAcuity", package = "vcd")
> VA <- xtabs(Freq ~ right + left + gender, data = VisualAcuity)
> dimnames(VA)[1:2] <- list(c("high", 2, 3, "low"))
> names(dimnames(VA))[1:2] <- paste(c("Right", "Left"), "eye grade")</pre>
```

(b) Perform the CMH tests for this table.

```
> CMHtest (VA)
$`gender:male
Cochran-Mantel-Haenszel Statistics for Right eye grade by Left eye grade
in stratum gender:male
                 AltHypothesis Chisq Df Prob
         Nonzero correlation 1555
cor
rmeans Row mean scores differ cmeans Col mean scores differ
                                 1556
                                 1557
general
         General association 3303
$`gender:female`
Cochran-Mantel-Haenszel Statistics for Right eye grade by Left eye grade
in stratum gender: female
                 AltHypothesis Chisq Df Prob
          Nonzero correlation 3691
rmeans Row mean scores differ
                                 3709
                                 3724
cmeans Col mean scores differ
                                             0
general General association 8096
```

(c) Use the woolf_test() described in Section 4.3.2 to test whether the association between left and right eye acuity can be considered the same for men and women.

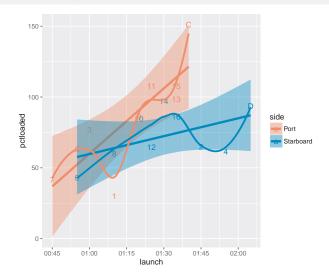
```
> woolf_test(VA)
Woolf-test on Homogeneity of Odds Ratios (no 3-Way assoc.)
data: VA
X-squared = 0.0892, df = 1, p-value = 0.77
```

Exercise 4.9 The graph in Figure 4.23 may be misleading, in that it doesn't take into account of the differing capacities of the 18 life boats on the *Titanic*, given in the variable cap in the *Lifeboats* data.

(a) Calculate a new variable, pctloaded, as the percentage loaded relative to the boat capacity.

```
★
> Lifeboats$pctloaded <- with(Lifeboats, 100*total/cap)
```

(b) Produce a plot similar to Figure 4.23, showing the changes over time in this measure.



Test a model allowing different slopes and intercepts for port and starboard sides:

Chapter 5

Mosaic Displays for n-Way Tables

Exercise 5.1 The data set criminal in the package logmult (Bouchet-Valat, 2015) gives the 4×5 table below of the number of men aged 15–19 charged with a criminal case for whom charges were dropped in Denmark from 1955–1958.

```
> data("criminal", package = "logmult")
> criminal

Age
Year    15    16    17    18    19
    1955    141    285    320    441    427
    1956    144    292    342    441    396
    1957    196    380    424    462    427
    1958    212    424    399    442    430
```

(a) Use loglm() to test whether there is an association between Year and Age. Is there evidence that dropping of charges in relation to age changed over the years recorded here?



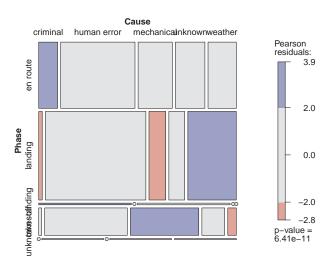
(b) Use mosaic() with the option shade=TRUE to display the pattern of signs and magnitudes of the residuals. Compare this with the result of mosaic() using "Friendly shading," from the option gp=shading_Friendly. Describe verbally what you see in each regarding the pattern of association in this table.



Exercise 5.2 The data set AirCrash in vcdExtra gives a database of all crashes of commercial airplanes between 1993–2015, classified by Phase of the flight and Cause of the crash. How can you best show is the nature of the association between these variables in a mosaic plot? Start by making a frequency table, aircrash.tab:

```
> data("AirCrash", package = "vcdExtra")
> aircrash.tab <- xtabs(~ Phase + Cause, data = AirCrash)</pre>
```

(a) Make a default mosaic display of the data with shade=TRUE and interpret the pattern of the high-frequency cells.



Four cells stand out as having greater than expected frequencies, if Phase and Cause were independent. Both take-off and en-route are positively associated with criminal activities. Crashes in landing are more associated with weather. It is difficult to interpret the unknown cells.

(b) The default plot has overlapping labels due to the uneven marginal frequencies relative to the lengths of the category labels. Experiment with some of the labeling_args options (abbreviate, rot_labels, etc.) to see if you can make the plot more readable. *Hint*: a variety of these are illustrated in Section 4.1 of vignette ("strucplot")



(c) The levels of Phase and Cause are ordered alphabetically (because they are factors). Experiment with other orderings of the rows/columns to make interpretation clearer, e.g., ordering Phase temporally or ordering both factors by their marginal frequency.



Exercise 5.3 The Lahman package contains comprehensive data on baseball statistics for Major League Baseball from 1871 through 2012. For all players, the *Master* table records the handedness of players, in terms of throwing (L, R) and batting (B, L, R), where B indicates "both." The table below was generated using the following code:

```
> library(Lahman)
> data("Master", package = "Lahman")
> basehands <- with(Master, table(throws, bats))</pre>
```

	Bats						
Throws	В	L	R				
L	177	2640	527				
R	924	1962	10442				

• Use the code above, or else enter these data into a frequency table in R.



• Construct mosaic displays showing the relation of batting and throwing handedness, split first by batting and then by throwing.



• From these displays, what can be said about players who throw with their left or right hands in terms of their batting handedness?



Exercise 5.4 * A related analysis concerns differences in throwing handedness among baseball players according to the fielding position they play. The following code calculates such a frequency table.

```
> library(Lahman)
> MasterFielding <- data.frame(merge(Master, Fielding, by = "playerID"))
> throwPOS <- with(MasterFielding, table(POS, throws))</pre>
```

(a) Make a mosaic display of throwing hand vs. fielding position.



(b) Calculate the percentage of players throwing left-handed by position. Make a sensible graph of this data.



(c) Re-do the mosaic display with the positions sorted by percentage of left-handers.



(d) Is there anything you can say about positions that have very few left-handed players?



Exercise 5.5 For the Bartlett data described in Example 5.12, fit the model of no three-way association, H_4 in Table 5.2.

(a) Summarize the goodness of fit for this model, and compare to simpler models that omit one or more of the two-way terms.



(b) Use a mosaic-like display to show the lack of fit for this model.



Exercise 5.6 Red core disease, caused by a fungus, is not something you want if you are a strawberry. The data set jansen.strawberry from the agridat (Wright, 2015) package gives a frequency data frame of counts of damage from this fungus from a field experiment reported by Jansen (1990). See the help file for details. The following lines create a $3 \times 4 \times 3$ table of crossings of 3 male parents with 4 (different) female parents, recording the number of plants in four blocks of 9 or 10 plants each showing red core disease in three ordered categories, C1, C2, or C3.

(a) Use pairs (jansen.tab, shade=TRUE) to display the pairwise associations among the three variables. Describe how disease category appears to vary with male and female parent. Why is there no apparent association between male and female parent?



(b) As illustrated in Figure 5.6, use mosaic() to prepare a 3-way mosaic plot with the tiles colored in increasing shades of some color according to disease category. Describe the pattern of category C3 in relation to male and female parent. (Hint: the highlighting arguments are useful here.)



(c) With category as the response variable, the minimal model for association is [MF][C], or $\sim 1 * 2 + 3$. Fit this model using loglm() and display the residuals from this model with mosaic(). Describe the pattern of lack of fit of this model.

Exercise 5.7 The data set caith in MASS (Ripley, 2015) gives another classic 4×5 table tabulating hair color and eye color, this for people in Caithness, Scotland, originally from Fisher (1940). The data is stored as a data frame of cell frequencies, whose rows are eye colors and whose columns are hair colors.

```
> data("caith", package = "MASS")
> caith
       fair red medium dark black
blue
       326 38
                   241 110
light
        688 116
                   584
                        188
                                4
       343 84
                   909
                        412
                               26
medium
            48
                   403 681
```

(a) The loglm() and mosaic() functions don't understand data in this format, so use Caith <- as.matrix(caith) to convert to array form. Examine the result, and use names (dimnames (Caith)) <-c() to assign appropriate names to the row and column dimensions.

*

(b) Fit the model of independence to the resulting matrix using loglm().

*

(c) Calculate and display the residuals for this model.

 \star

(d) Create a mosaic display for this data.



Exercise 5.8 The HairEyePlace data in vcdExtra gives similar data on hair color and eye color, for both Caithness and Aberdeen as a $4 \times 5 \times 2$ table.

(a) Prepare separate mosaic displays, one for each of Caithness and Aberdeen. Comment on any difference in the pattern of residuals.

*

(b) Construct conditional mosaic plots, using the formula ~ Hair + Eye | Place and both mosaic() and cotabplot(). It is probably more useful here to suppress the legend in these plots. Comment on the difference in what is shown in the two displays.



Exercise 5.9 Bertin (1983, pp. 30–31) used a 4-way table of frequencies of traffic accident victims in France in 1958 to illustrate his scheme for classifying data sets by numerous variables, each of which could have various types and could be assigned to various visual attributes. His data are contained in Accident in vcdExtra, a frequency data frame representing his $5 \times 2 \times 4 \times 2$ table of the variables age, result (died or injured), mode of transportation, and gender.

```
> data("Accident", package = "vcdExtra")
> str(Accident, vec.len=2)

'data.frame': 80 obs. of 5 variables:
$ age : Ord.factor w/ 5 levels "0-9"<"10-19"<...: 5 5 5 5 5 ...
$ result: Factor w/ 2 levels "Died", "Injured": 1 1 1 1 1 1 ...
$ mode : Factor w/ 4 levels "4-Wheeled", "Bicycle", ...: 4 4 2 2 3 ...
$ gender: Factor w/ 2 levels "Female", "Male": 2 1 2 1 2 ...
$ Freq : int 704 378 396 56 742 ...</pre>
```

(a) Use loglm() to fit the model of mutual independence, Freq ~ age+mode+gender+result to this data set.

 \star

(b) Use mosaic() to produce an interpretable mosaic plot of the associations among all variables under the model of mutual independence. Try different orders of the variables in the mosaic. (*Hint*: the abbreviate component of the labeling_args argument to mosaic() will be useful to avoid some overlap of the category labels.)

```
*
```

(c) Treat result ("Died" vs. "Injured") as the response variable, and fit the model

Freq ~ age*mode*gender + result that asserts independence of result from all others jointly.

 \star

(d) Construct a mosaic display for the residual associations in this model. Which combinations of the predictor factors are more likely to result in death?



Exercise 5.10 The data set Vietnam in vcdExtra gives a $2 \times 5 \times 4$ contingency table in frequency form reflecting a survey of student opinion on the Vietnam War at the University of North Carolina in May 1967. The table variables are sex, year in school, and response, which has categories: (A) Defeat North Vietnam by widespread bombing and land invasion; (B) Maintain the present policy; (C) De-escalate military activity, stop bombing and begin negotiations; (D) Withdraw military forces immediately. How does the chosen response vary with sex and year?

```
> data("Vietnam", package = "vcdExtra")
> str(Vietnam)

'data.frame': 40 obs. of 4 variables:
$ sex : Factor w/ 2 levels "Female", "Male": 1 1 1 1 1 1 1 1 1 1 1 1 ...
$ year : int 1 1 1 1 2 2 2 2 3 3 ...
$ response: Factor w/ 4 levels "A", "B", "C", "D": 1 2 3 4 1 2 3 4 1 2 ...
$ Freq : int 13 19 40 5 5 9 33 3 22 29 ...
```

(a) With response (R) as the outcome variable and year (Y) and sex (S) as predictors, the minimal baseline loglinear model is the model of joint independence, [R][YS]. Fit this model, and display it in a mosaic plot.



(b) Construct conditional mosaic plots of the response versus year separately for males and females. Describe the associations seen here.



(c) Follow the methods shown in Example 5.10 to fit separate models of independence for the levels of sex, and the model of conditional independence, $R \perp Y \mid S$. Verify that the decomposition of G^2 in Eqn. (5.6) holds for these models.



(d) Construct a useful 3-way mosaic plot of the data for the model of conditional independence.



Exercise 5.11 Consider the models for 4-way tables shown in Table 5.3.

(a) For each model, give an independence interpretation. For example, the model of mutual independence corresponds to $A \perp B \perp C \perp D$.



(b) Use the functions shown in the table together with loglin2formula() to print the corresponding model formulas for each.



Exercise 5.12 The dataset *Titanic* classifies the 2,201 pasengers and crew of the *Titanic* by Class (1st, 2nd, 3rd, Crew), Sex, Age, and Survived. Treating Survived as the response variable,

(a) Fit and display a mosaic plot for the baseline model of joint independence, [CGA][S]. Describe the remaining pattern of associations.



(b) Do the same for a "main effects" model that allows two-way associations between each of C, G, and A with S.



(c) What three-way association term should be added to this model to allow for greater survival among women and children? Does this give an acceptable fit?



(d) Test and display models that allow additional three-way associations until you obtain a reasonable fit.

*

Chapter 6

Correspondence Analysis

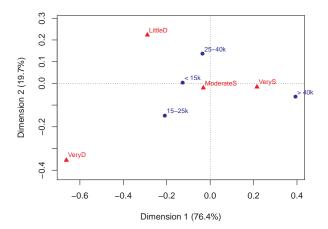
These solutions use an updated version of the ca package, v. 0.64 or greater.

Exercise 6.1 The JobSat data in vcdExtra gives a 4×4 table recording job satisfaction in relation to income.

- (a) Carry out a simple correspondence analysis on this table. How much of the inertia is accounted for by a one-dimensional solution? How much by a two-dimensional solution?
 - ★ The 1D solution accounts for 76.4

(b) Plot the 2D CA solution. To what extent can you consider the association between job satisfaction and income "explained" by the ordinal nature of these variables?

```
> plot(jobsat.ca)
```



Job satisfaction is ordered as expected by its ordinal levels along Dimension 1. The levels of income in this plot do not appear to be ordered according to the quantitative levels they represent.

Exercise 6.2 Refer to Exercise 5.1 in Chapter 5. Carry out a simple correspondence analysis on the 4×5 table criminal from the logmult package.

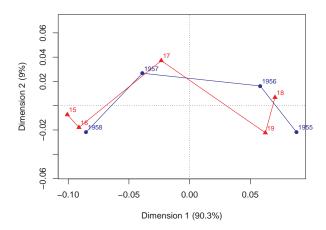
(a) What percentages of the Pearson χ^2 for association are explained by the various dimensions?

```
> data("criminal", package = "logmult")
> criminal.ca <- ca(criminal)
>  # just show the scree plot
> summary(criminal.ca, rows=FALSE, columns=FALSE)
```

(b) Plot the 2D correspondence analysis solution. Describe the pattern of association between year and age.

```
*
```

```
> plot(criminal.ca, lines=TRUE)
```



The category points for both year and age vary systematically over Dimension 1. There were more younger men in later years, and more older in earlier years.

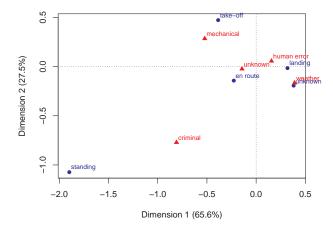
Exercise 6.3 Refer to Exercise 5.2 for a description of the AirCrash data from the vcdExtra package. Carry out a simple correspondence analysis on the 5×5 table of Phase of the flight and Cause of the crash.

(a) What percentages of the Pearson χ^2 for association are explained by the various dimensions? \bigstar aircrash.tab was calculated in Exercise 5.2.

```
> aircrash.tab
       Cause
Phase
         criminal human error mechanical unknown weather
                             29
 en route 16 63
                                         2.5
                                                 2.4
 landing
                                                 55
                        114
                                   19
                                          18
 standing
                         29
                                   2.4
                                           8
 take-off
 unknown
> aircrash.ca <- ca(aircrash.tab)</pre>
> summary(aircrash.ca, rows=FALSE, columns=FALSE)
Principal inertias (eigenvalues):
                   cum%
dim
       value
                          scree plot
      2
                0.3 100.0
      0.000562
Total: 0.187452 100.0
```

(b) Plot the 2D correspondence analysis solution. Describe the pattern of association between phase and cause. How would you interpret the dimensions?

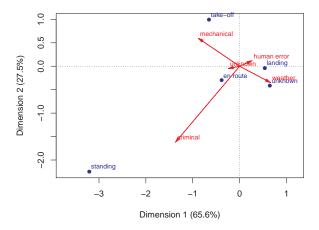
*



Dimension 1 largely distinguishes standing from landing, where the main causes are human error and weather problems. Dimension 2 largely distinguishes standing from take-off, where mechanical problems are more prevalent.

(c) The default plot method uses map="symmetric" with points for both rows and columns. Try using map="symbiplot" with vectors (arrows=) for either rows or columns. (Read help(plot.ca) for a description of these options.)

```
> plot(aircrash.ca, map="symbiplot", arrows=c(FALSE, TRUE))
```



Exercise 6.4 The data set *caith* in MASS gives a classic table tabulating hair color and eye color of people in Caithness, Scotland, originally from Fisher (1940).

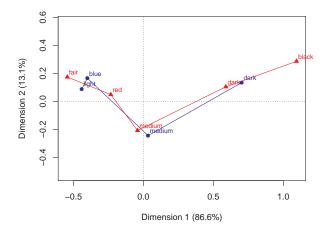
(a) Carry out a simple correspondence analysis on this table. How many dimensions seem necessary to account for most of the association in the table?

```
> data("caith", package="MASS")
> caith.ca <- ca(caith)
> summary(caith.ca, rows=FALSE, columns=FALSE)
Principal inertias (eigenvalues):
```

One could argue that a 1D solution is adequate here. The 2D solution is essentially complete.

(b) Plot the 2D solution. The interpretation of the first dimension should be obvious; is there any interpretation for the second dimension?

```
> plot(caith.ca, lines=TRUE)
```



Dimension 1 is the obvious light–dark dimension for hair color and eye color (but not that blue and light eyes have quite similar positions). Dimension 2 could be called "extremes vs. middle", but in CA results with largely 1D association, this effect is common, often called the "horseshoe" or "arch" effect.

Exercise 6.5 The same data, plus a similar table for Aberdeen, are given as a three-way table as <code>HairEyePlace</code> in <code>vcdExtra</code>.

(a) Carry out a similar correspondence analysis to the last exercise for the data from Aberdeen. Comment on any differences in the placement of the category points.



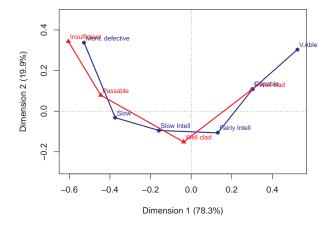
(b) Analyze the three-way table, stacked to code hair color and place interactively, i.e., for the loglinear model [Hair Place] [Eye]. What does this show?



Exercise 6.6 The data set Gilby in vcdExtra gives a classic (but now politically incorrect) 6×4 table of English schoolboys classified according to their clothing and their teacher's rating of "dullness" (lack of intelligence).

(a) Compute and plot a correspondence analysis for this data. Write a brief description and interpretation of these results.

```
Rows:
                            inr
292
                                                        k=2
337
              mass
75
                                    k=1
-527
     name
                     qlt
996
                                          cor
707
                                               ctr
264
                                                             cor ctr
289 426
     Mntd
                                               223
2
                      943
                            187
                                                        -32
               127
                                          936
     Slow
               236
                      938
                             85
                                    -159
                                                        -95
                                                             247
                                                                  106
     SlwI
                                          691
4 5
               310
217
                            88
223
                                          601 67
885 253
                                                       -107
109
                                                             398 176
115 129
                      999
                                     131
304
     FrlI
                    1000
     Cpbl
6
     VAbl
                            125
                                     524
                                          740 118
                                                        304
                                                             250 157
                34
                      990
Columns:
                                                        k=2 cor ctr
107 113 208
     name
              mass
                            inr
                                          cor ctr
                                     299 886 414
                    1000
     VWll
              369
                            366
2
                                                       -151 934
79 30
     Wllc
               435
                      989
                            106
                                           56
                                                                  496
                                    -445 946 383
                      976
                                                                   47
     Pssb
               154
                            317
                                                             30
4
     Insf
                42
                     955
                            212
                                   -605
                                          722 195
                                                        344 233 248
> plot(gilby.ca, lines="TRUE", lwd=2)
```

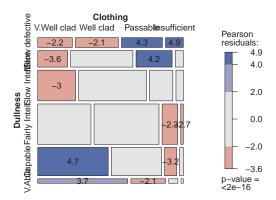


The association between clothing and dullness is largely one dimensional, but there is a moderately large horseshoe effect. On Dimension 1, the categories of both variables are approximately equally spaced.

(b) Make an analogous mosaic plot of this table. Interpret this in relation to the correspondence analysis plot.

 \star

```
> mosaic(Gilby, shade=TRUE, labeling=labeling_residuals)
```



The mosaic nearly shows the opposite corner pattern associated with a unidimensional association

of two ordered variables, but the largest residuals are not systematically confined to the diagonally opposite cells. The mosaic shows the marginal frequencies of dullness and the cell frequencies by the area of the tiles, while this information is not available in the CA plot.

Exercise 6.7 For the mental health data analyzed in Example 6.2, construct a shaded sieve diagram and mosaic plot. Compare these with the correspondence analysis plot shown in Figure 6.2. What features of the data and the association between SES and mental health status are shown in each?



Exercise 6.8 Simulated data are often useful to help understand the connections between data, analysis methods, and associated graphic displays. Section 6.3.1 illustrated interactive coding in R, using a simulated 4-way table of counts of pets, classified by age, color, and sex, but with no associations because the counts had a constant Poisson mean, $\lambda = 15$.

- (a) Re-do this example, but in the call to rpois(), specify a non-negative vector of Poisson means to create some associations among the table factors.
 - ★ First, create a data.frame of the factor levels. Then you can use these variables to create the Poisson means in a way that varies across some of the category combinations to create associations. Here we try to creates associations between Pet and Color (more black dogs than other combinations) and between Age and Sex (more young male pets). These cell means are then used in the call to rpois().

(b) Use CA methods to determine if and how the structure you created in the data appears in the results.



Exercise 6.9 The TV data was analyzed using CA in Example 6.4, ignoring the variable Time. Carry out analyses of the 3-way table, reducing the number of levels of Time to three hourly intervals as shown below.

```
> data("TV", package="vcdExtra")
> # reduce number of levels of Time

> TV.df <- as.data.frame.table(TV)

> levels(TV.df$Time) <- rep(c("8", "9", "10"), c(4, 4, 3))
> TV3 <- xtabs(Freq ~ Day + Time + Network, TV.df) > structable(Day ~ Network + Time, TV3)
                 Day Monday Tuesday Wednesday Thursday Friday
Network Time
                           536
                          1401
                                     1205
                                                   1022
                                                                 682
                                                                          907
           10
                                                    668
                                                                 349
CBS
                          1167
                                      646
                                                    550
                                                                 680
                                                                          509
                           967
                                       959
                                                    409
                                                                 385
                                                                          544
                                       798
           10
                            789
                                                    324
                                                                 270
                                                                          426
NBC
                                     1090
                                                               1927
           8
                           858
                                                    512
                                                                          823
           9
                                                               1858
                                                                          590
                           946
                                       890
                                                    831
           10
                           825
                                       588
                                                                           585
```

(a) Use the stacking approach (Section 6.3) to perform a CA of the table with Network and Time coded interactively. You can create this using the as.matrix() method for a "structable" object.

```
> TV3S <- as.matrix(structable(Day ~ Network + Time, TV3), sep=":")
```

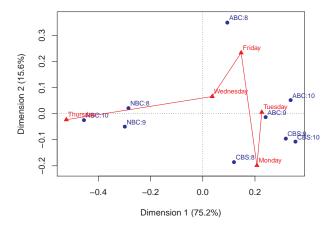
```
*
```

```
> TV3S.ca <-ca(TV3S)
> TV3S
              Day
Network: Time Monday Tuesday Wednesday Thursday Friday
       ABC:8
                            861
                                        744
                   536
                                                          1119
       ABC:9
                                                   682
       ABC:10
                   910
                                        668
       CBS:8
                  1167
                            646
                                                   680
                                                           509
                            959
                                                           544
       CBS:9
                   967
                                        409
                                                   385
       CBS:10
                   789
                            798
                                        324
                                                           426
       NBC:8
                   858
                           1090
                                        512
                                                  1927
                                                           823
                                        831
                                                 1858
       NBC: 9
                   946
                            890
                                                           590
       NBC:10
                            588
                                                 2101
                                                           585
                   825
                                        869
```

- (b) What loglinear model is analyzed by this approach?
 - ★ The model is the joint independence model, [Day][Network Time], asserting that the frequencies of watching the combinations of networks in different time slots do not vary with day of the week.
- (c) Plot the 2D solution. Compare this to the CA plot of the two-way table in Figure 6.4.

*

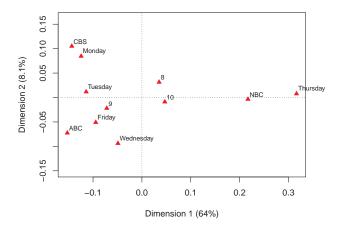
```
> plot(TV3S.ca, lines=c(FALSE, TRUE))
```



Overall, the plot is somewhat similar to that of Figure 6.4 except for the (arbitrary) reversal of Dimension 1. The category points for NBC cluster near Thursday, while those for ABC and CBS are at the other end of that dimension and Dimension 2 is related to the difference in viewership to those channels.

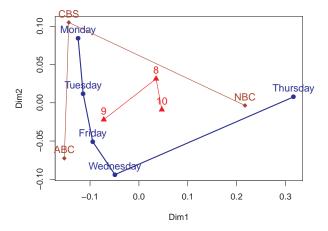
- (d) Carry out an MCA analysis using mjca() of the three-way table TV3. Plot the 2D solution, and compare this with both the CA plot and the solution for the stacked three-way table.
 - ★ The MCA analysis differs in that it includes all pairwise associations of Day, Time and Network rather than just the joint independence model analyzed by the stacking approach.

```
> TV3.mca <- mjca(TV3)
> plot(TV3.mca, collabels="level")
```



The default plot is somewhat difficult to read because the factor points s aren't distinguished by color or shape. A customized plot can be constructed as follows (as illustrated in the text, e.g., for Figure 6.10). (The multilines() function is new in the ca (Greenacre and Nenadic, 2014) package, v. 0.64.)

```
> res <- plot(TV3.mca, labels=0, pch='.', cex.lab=1.2)
> coords <- data.frame(res$cols, TV3.mca$factors)
> nlev <- rle(as.character(coords$factor))$lengths
> fact <- unique(as.character(coords$factor))
>
> cols <- c("blue", "red", "brown")
> lwd <- 2
> plot(Dim2 ~ Dim1, type='n', data=coords)
> points(coords[,1:2], pch=rep(16:18, nlev), col=rep(cols, nlev), cex=1.2)
> text(coords[,1:2], labels=coords$level, col=rep(cols, nlev), pos=3, cex=1.2, xpd=TRUE)
> multilines(coords[, c("Dim1", "Dim2")], group=coords$factor, col=cols, lwd=lwd)
```



Exercise 6.10 Refer to the MCA analysis of the PreSex data in Example 6.8. Use the stacking approach to analyze the stacked table with the combinations of premarital and extramarital sex in the rows and the combinations of gender and marital status in the columns. As suggested in the exercise above, you can use as .matrix (structable()) to create the stacked table.

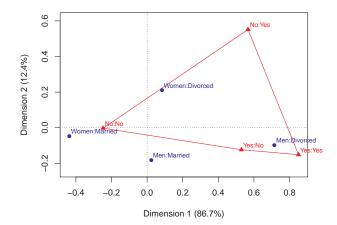
```
Women:Married 4 25 4 322
Men:Divorced 28 60 17 68
Men:Married 11 42 4 130
```

- (a) What loglinear model is analyzed by this approach? Which associations are included and which are excluded in this analysis?
 - ★ The model is that of independence between the combinations of the row variables and the column variables, i.e., [Pre Extra][Gender Marital]. The associations that remain indicate how the combinations of pre- and extra-marital sex are related to the the combinations of gender and marital status. The association between pre-marital sex and extra-marital sex is excluded, as is the association between gender and marital status.
- (b) Plot the 2D CA solution for this analysis. You might want to draw lines connecting some of the row points or column points to aid in interpretation.
 - ★ The 2D solution accounts for 99.1% of association between these sets of variables.

```
> presexS.ca <- ca(presexS)</pre>
> summary (presexS.ca)
Principal inertias (eigenvalues):
        value % cum% scree
0.153126 86.7 86.7 *****
0.021929 12.4 99.1 ***
                               scree plot
        0.001552
                  0.9 100.0
Total: 0.176606 100.0
Rows:
                 qlt
995
    name
                              k=1 cor ctr
           mass
                       inr
           310
343
                        90 |
                               84 138 14
                                              210 857 622
    WmnD
                      376 |
                                              -46 11 34
2
 | WmnM |
                 995
                             -437 984 427
   MnDv
            167
                 996
                      494
                              715 978 558
                                              -97
                                                    18
4 | MnMr |
           181
Columns:
                                   name
           mass
                       inr
            58
                       250 |
                              850
    YsYs |
2 |
            175 989
                      296
                             530
   YesN |
             59 1000
3 i
                      209
                              567
   NoYs I
           708 1000
                            -247 1000 283 |
4 | NoNo |
                      245 |
```

Here is one version of a plot, drawing lines connecting the pairs of Gender and Marital status.

```
> res <- plot (presexS.ca)
> # join pairs of column points
> lines(res$cols[1:2,], col="red")
> lines(res$cols[3:4,], col="red")
> lines(res$cols[c(1,3),], col="red")
> lines(res$cols[c(2,4),], col="red")
```



- (c) How does this analysis differ from the MCA analysis shown in Figure 6.10?
 - ★ The MCA analysis treats all four factors individually, analyzing all bivariate associations. The stacked approach here treats them in two sets, analyzing only the associations *between* sets.

Exercise 6.11 Refer to Exercise 5.10 for a description of the Vietnam data set in vcdExtra.

(a) Using the stacking approach, carry out a correspondence analysis corresponding to the loglinear model [R][YS], which asserts that the response is independent of the combinations of year an sex.



(b) Construct an informative 2D plot of the solution, and interpret in terms of how the response varies with year for males and females.



(c) Use mjca() to carry out an MCA on the three-way table. Make a useful plot of the solution and interpret in terms of the relationship of the response to year and sex.



Exercise 6.12 Refer to Exercise 5.9 for a description of the Accident data set in vcdExtra. The data set is in the form of a frequency data frame, so first convert to table form.

```
> accident.tab <- xtabs(Freq ~ age + result + mode + gender, data=Accident)
```

(a) Use mjca() to carry out an MCA on the four-way table accident.tab.

```
\star
```

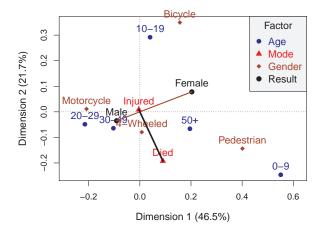
```
> accident.mca <- mjca(accident.tab)</pre>
> summary (accident.mca)
Principal inertias (eigenvalues):
 dim
        value
                         cum%
                                scree plot
        0.025429
                   46.5
                        46.5
                                *****
                   21.7
                         68.1
71.6
        0.011848
        0.001889
                    3.5
        0.000491
                    0.9
                          72.5
 Total: 0.054700
Columns:
                               qlt
                                     inr
                                            k=1 cor ctr
                                                            k=2 cor ctr
             age:0-9
                               672
                                     107
                                            551
                                                561
                                                            -246
           age:10-19
                           49
                               678
                                     91
                                             40
                                                 13
                                                            292 665
                                                                     354
3
           age:20-29
                           56
                               784
                                     85
                                                            -48
                                                                      11
4
            age:30-49
                           76
                              546
                                     75
                                           -103 396
                                                            -63 149
              age:50+
                           56
                               687
                                            196 616
                                                            -67
         result:Died
                               515
                                     100
                                             90
```

```
result: Injured |
                          239
                               515
8
                                      73
                                               8
                                                       0
                                                              -80 228
                                                                       43
      mode: 4-Wheeled
                               230
                           81
9
                                762
                                            156 127
        mode:Bicycle
                                      98
                                                      30
                                                             349 635 320
                           31
     mode:Motorcycle
                               686
                                      70
                                            -209 684 170
10
                           99
                                                              11
                               677
                                            401 600 241
                                                                       66
11
     mode:Pedestrian
                           38
                                                             -144
       gender:Female
                               788
                                      77
                                            203 686 126
                                                              78 101
12
                                                                       4.0
                               788
                                      35
                                                             -35
                                                                 101
1.3
         gender: Male
                                            -91 686
                                                      56
                                                                       18
```

The adjusted inertias indicate that a 2D solution accounts for only 68.1% of the pairwise associations. The qualities (qlt) of the factor levels indicate that the categories are only moderately well-represented in a 2D plot.

(b) Construct an informative 2D plot of the solution, and interpret in terms of how the variable result varies in relation to the other factors.

★ Here, the plot becomes too messy to if we connect all factor levels with lines.



In the figure above, one interpretation of the dimensions is in terms of the age categories: Dimension 1 for young adults vs. old and young, Dimension 2 for teenage vs. the rest. In these terms, Dimension 1 shows associations among males, aged 20–49, riding a motorcycle or 4-wheeled vehicle and more likely to be injured, vs. females, either old or very young, as pedestrians and more likely to have died. Dimension 2 contrasts bicycle accidents involving youth aged 10–19 who are more likely to be just injured against the other categories.

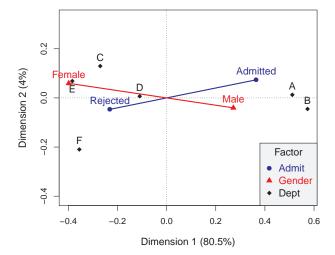
Exercise 6.13 The *UCBAdmissions* data was featured in numerous examples in Chapter 4 (e.g., Example 4.11, Example 4.15) and Chapter 5 (e.g., Example 5.14, Example 5.18).

(a) Use mjca() to carry out an MCA on the three-way table UCBAdmissions.

```
> ucb.mca <- mjca(UCBAdmissions)
> summary(ucb.mca)
Principal inertias (eigenvalues):
```

```
dim
        value
                         cum%
                                scree plot
        0.114945
                          80.5
        0.005694
                    4.0
                         84.5
                    0.0
                          84.5
                    0.0
                          84.5
        00000000
                    0.0
                          84.5
 Total: 0.142840
Columns:
                                           k=1 cor ctr
                                                            k=2 cor ctr
                name
                       mass
                              qlt
                                   inr
                                           365 875 150
                                                                36 123
     Admit:Admitted
                        129
                              911
                                    93
2
                                                    95
     Admit:Rejected
                         204
                              911
                                     59
                                          -231 875
                                                            -47
                                                                 36
                                                                     78
                                    95
      Gender:Female
                              863
                                          -399845
                                                    187
                                                            59
                                                                 19
4 5
        Gender:Male
                         198
                              863
                                     65
                                           272 845
                                                    127
                                                            -40
                                                                19
              Dept:A
                         69
                              838
                                    117
                                           512 837
                                                    156
                                                            13
6
7
              Dept:B
                          43
                              829
                                   124
                                           573 824
                                                    123
                                                            -45
              Dept:C
                          68
                              731
                                    108
                                          -270
                                               594
                                                     43
                                                            130 137
                                                                    199
8
              Dept:D
                          58
                              832
                                   106
                                          -110 828
                                                      6
                                                                      0
9
              Dept:E
                          43
                              812
                                   117
                                          -384
                                               787
                                                             69
                              737
                                   116
                                          -355 547
              Dept:F
```

(b) Plot the 2D MCA solution in a style similar to that shown in Figure 6.10 and Figure 6.11



- (c) Interpret the plot. Is there some interpretation for the first dimension? What does the plot show about the relation of admission to the other factors?
 - ★ The first dimension largely corresponds to Admission, showing the overall association of Males more likely to be admitted, Females more likely to be rejected. Note that the departments, labeled A–F, were actually ordered by overall rate of admission, but this ordering does not appear along Dimension 1 in the plot

Chapter 7

Logistic Regression Models

Exercise 7.1 Arbuthnot's data on the sex ratio of births in London was examined in Example 3.1. Use a binomial logistic regression model to assess whether the proportion of male births varied with the variables Year, Plague, and Mortality in the Arbuthnot data set. Produce effect plots for the terms in this model. What do you conclude?

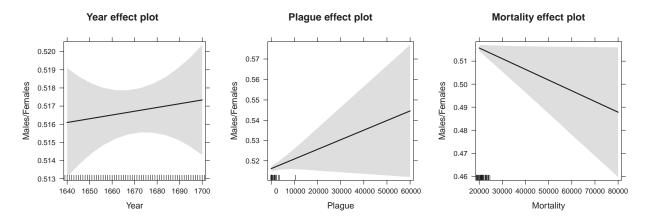
* For the binomial logistic model, use cbind (Males, Females) for the response variable in the model.

```
> data(Arbuthnot, package="HistData")
> arbuth.mod <- glm(cbind(Males, Females) ~ Year + Plague + Mortality,
                         data=Arbuthnot, family=binomial)
> summary(arbuth.mod)
Call:
qlm(formula = cbind(Males, Females) ~ Year + Plaque + Mortality,
     family = binomial, data = Arbuthnot)
Deviance Residuals:
Min 1Q Median 3Q -3.184 -0.996 -0.005 0.850
Coefficients:
Estimate Std. Error z value Pr(>|z|) (Intercept) -4.07e-02 3.09e-01 -0.13 0.895 Year 8.28e-05 1.93e-04 0.43 0.668 Plague 1.91e-06 1.13e-06 1.68 0.093 . Mortality -1.86e-06 9.26e-07 -2.01 0.045 *
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
(Dispersion parameter for binomial family taken to be 1)
Null deviance: 169.74 on 81 degrees of freedom Residual deviance: 156.31 on 78 degrees of freedom
Number of Fisher Scoring iterations: 3
> LRstats (arbuth.mod)
Likelihood summary table:

AIC BIC LR Chisq Df Pr(>Chisq)
                             156 78 3.6e-07 ***
arbuth.mod 964 973
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

The effects of Year and Plague are small and non-significant. The Male/Female proportion appears to decrease with increasing Mortality.

```
> library(effects)
> arbuth.eff <- allEffects(arbuth.mod)
> plot(arbuth.eff, ylab="Males/Females", rows=1, cols=3)
```



In the plots for Plague and Mortality, it is apparent that both are extremely skewed. One alternative is to represent these as log(Plague+1) and log(Mortality) in the model. Overall, these effects are quite small, but the main effects model arbuth.mod is better than the null model.

Exercise 7.2 For the Donner Party data in *Donner*, examine Grayson's 1990 claim that survival in the Donner Party was also mediated by the size of the family unit. This takes some care, because the family variable in the *Donner* data is a simplified grouping based on the person's name and known alliances among families from the historical record. Use the following code to compute a family.size variable from each individual's last name:

```
> data("Donner", package="vcdExtra")
> Donner$survived <-factor(Donner$survived, labels=c("no", "yes"))
> # use last name for family
> lname <-strsplit(rownames(Donner), ",")
> lname <-sapply(lname, function(x) x[[1]])
> Donner$family.size <-as.vector(table(lname)[lname])</pre>
```

(a) Choose one of the models (donner.mod4, donner.mod6) from Example 7.9 that include the interaction of age and sex and nonlinear terms in age. Fit a new model that adds a main effect of family.size. What do you conclude about Grayson's claim?

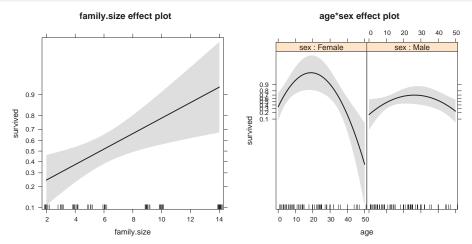
```
> library(car)
> donner.mod4a <- glm(survived ~ poly(age,2) * sex + family.size, data=Donner, family=binomial)
> Anova(donner.mod4a)
Analysis of Deviance Table (Type II tests)
Response: survived
                  LR Chisq Df Pr(>Chisq)
                      14.94
                                  0.00057
poly(age, 2)
                       4.24
                                   0.03944 *
sex
family.size
                      11.54
                                   0.00068 ***
poly(age, 2):sex
                     12.24
                                  0.00220 **
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

Family size seems to have an effect on survival.

(b) Produce an effect plot for this model.

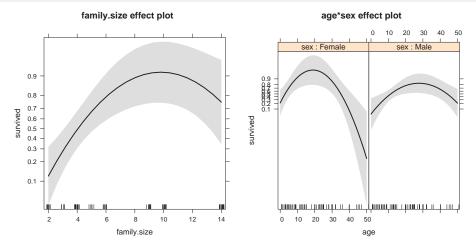
*

```
> library(effects)
> donner.eff4a <- allEffects(donner.mod4a, xlevels=list(age=seq(0,50,5)))
> plot(donner.eff4a, ticks=list(n=8))
```



(c) Continue, by examining whether the effect of family size can be taken as linear, or whether a nonlinear term should be added.

> donner.mod4b <- glm(survived ~ poly(age,2) * sex + poly(family.size, 2), data=Donner, family=binomial) > Anova (donner.mod4b) Analysis of Deviance Table (Type II tests) Response: survived LR Chisq Df Pr(>Chisq) 17.64 2 0.00015 0.00015 poly(age, 2) 0.12688 2.33 sex 24.81 poly(family.size, 2) 4.1e-06 ***0.00219 ** poly(age, 2):sex 12.25 Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1 > donner.eff4b <- allEffects(donner.mod4b, xlevels=list(age=seq(0,50,5)))</pre> > plot(donner.eff4b, ticks=list(n=8))



Exercise 7.3 Use component+residual plots (Section 7.5.3) to examine the additive model for the ICU data given by

```
> icu.glm2 <- glm(died ~ age + cancer + admit + uncons,
+ data=ICU, family=binomial)</pre>
```

(a) What do you conclude about the linearity of the (partial) relationship between age and death in this model?



(b) An alternative strategy is to allow some nonlinear relation for age in the model using a quadratic (or cubic) term like poly(age, 2) (or poly(age, 3)) in the model formula. Do these models provide evidence for a nonlinear effect of age on death in the ICU?



Exercise 7.4 Explore the use of other marginal and conditional plots to display the relationships among the variables predicting death in the ICU in the model icu.glm2. For example, you might begin with a marginal gpairs () plot showing all bivariate marginal relations, something like this:

```
> library(gpairs)
> gpairs(ICU[,c("died", "age", "cancer", "admit", "uncons")],
+ diag.pars=list(fontsize=16, hist.color="lightgray"),
+ mosaic.pars=list(gp=shading_Friendly,
+ gp_args=list(interpolate=1:4)))
```



Exercise 7.5 The data set Caesar in VCdExtra gives a 3×2^3 frequency table classifying 251 women who gave birth by Caesarian section by Infection (three levels: none, Type 1, Type2) and Risk, whether Antibiotics were used, and whether the Caesarian section was Planned or not. Infection is a natural response variable. In this exercise, consider only the binary outcome of infection vs. no infection.

```
> data("Caesar", package="vcdExtra")
> Caesar.df <- as.data.frame(Caesar)
> Caesar.df$Infect <- as.numeric(Caesar.df$Infection %in%
+ c("Type 1", "Type 2"))</pre>
```

(a) Fit the main-effects logit model for the binary response Infect. Note that with the data in the form of a frequency data frame you will need to use weights=Freq in the call to glm(). (It might also be convenient to reorder the levels of the factors so that "No" is the baseline level for each.)



(b) Use summary() or car(Fox and Weisberg, 2015)::Anova() to test the terms in this model.



(c) Interpret the coefficients in the fitted model in terms of their effect on the odds of infection.



(d) Make one or more effects plots for this model, showing separate terms, or their combinations.



Exercise 7.6 The data set birthwt in the MASS package gives data on 189 babies born at Baystate Medical Center, Springfield, MA during 1986. The quantitative response is bwt (birth weight in grams), and this is also recorded as low, a binary variable corresponding to bwt < 2500 (2.5 Kg). The goal is to study how this varies with the available predictor variables. The variables are all recorded as numeric, so in R it may be helpful to convert some of these into factors and possibly collapse some low frequency categories. The code below is just an example of how you might do this for some variables.

(a) Make some exploratory plots showing how low birth weight varies with each of the available predictors. In some cases, it will probably be helpful to add some sort of smoothed summary curves or lines.



(b) Fit several logistic regression models predicting low birth weight from these predictors, with the goal of explaining this phenomenon adequately, yet simply.



(c) Use some graphical displays to convey your findings.



Exercise 7.7 Refer to Exercise 5.9 for a description of the Accident data. The interest here is to model the probability that an accident resulted in death rather than injury from the predictors age, mode, and gender. With glm(), and the data in the form of a frequency table, you can use the argument weight=Freq to take cell frequency into account.

(a) Fit the main effects model, result == "Died" ~ age + mode + gender. Use Car::Anova() to assess the model terms.



(b) Fit the model that allows all two-way interactions. Use anova() to test whether this model is significantly better than the main effects model.



(c) Fit the model that also allows the three-way interaction of all factors. Does this offer any improvement over the two-way model?



(d) Interpret the results of the analysis using effect plots for the two-way model, separately for each of the model terms. Describe verbally the nature of the age*gender effect. Which mode of transportation leads to greatest risk of death?



Chapter 8

Models for Polytomous Responses

Exercise 8.1 For the women's labor force participation data (Womenlf), the response variable, partic, can be treated as ordinal by using

Use the methods in Section 8.1 to test whether the proportional odds model holds for these data.



Exercise 8.2 The data set housing in the MASS package gives a $3 \times 3 \times 4 \times 2$ table in frequency form relating (a) satisfaction (Sat) of residents with their housing (High, Medium, Low), (b) perceived degree of influence (Infl) they have on the management of the property (High, Medium, Low), (c) Type of rental (Tower, Atrium, Apartment, Terrace), and (d) contact (Cont) residents have with other residents (Low, High). Consider satisfaction as the ordinal response variable.

(a) Fit the proportional odds model with additive (main) effects of housing type, influence in management, and contact with neighbors to this data. (Hint: Using polr(), with the data in frequency form, you need to use the weights argument to supply the Freq variable.)



(b) Investigate whether any of the two-factor interactions among Infl, Type, and Cont add substantially to goodness of fit of this model. (Hint: use stepAIC(), with the scope formula ~ .^2 and direction="forward".)

(c) For your chosen model from the previous step, use the methods of Section 8.1.5 to plot the probabilities of the categories of satisfaction.



(d) Write a brief summary of these analyses, interpreting *how* satisfaction with housing depends on the predictor variables.



Exercise 8.3 The data TV on television viewing was analyzed using correspondence analysis in Example 6.4, ignoring the variable Time, and extended in Exercise 6.9. Treating Network as a three-level response variable, fit a generalized logit model (Section 8.3) to explain the variation in viewing in relation to Day and Time. The TV data is a three-way table, so you will need to convert it to a frequency data frame first.

```
> data("TV", package="vcdExtra")
> TV.df <- as.data.frame.table(TV)</pre>
```

(a) Fit the main-effects model, Network ~ Day + Time, with multinom(). Note that you will have to supply the weights argument because each row of TV.df represents the number of viewers in the Freq variable.



(b) Prepare an effects plot for the fitted probabilities in this model.

*

(c) Interpret these results in comparison to the correspondence analysis in Example 6.4.



Exercise 8.4 * Refer to Exercise 5.10 for a description of the *Vietnam* data set in vcdExtra. The goal here is to fit models for the polytomous response variable in relation to year and sex.

(a) Fit the proportional odds model to these data, allowing an interaction of year and sex.

*

(b) Is there evidence that the proportional odds assumption does not hold for this data set? Use the methods described in Section 8.1 to assess this.

*

(c) Fit the multinomial logistic model, also allowing an interaction. Use car::Anova() to assess the model terms.



(d) Produce an effect plot for this model and describe the nature of the interaction.

*

(e) Fit the simpler multinomial model in which there is no effect of year for females and the effect of year is linear for males (on the logit scale). Test whether this model is significantly worse than the general multinomial model with interaction.



Chapter 9

Loglinear and Logit Models for Contingency Tables

Exercise 9.1 Consider the data set DaytonSurvey (described in Example 2.6), giving results of a survey of use of alcohol (A), cigarettes (C), and marijuana (M) among high school seniors. For this exercise, ignore the variables sex and race, by working with the marginal table Dayton. ACM, a $2 \times 2 \times 2$ table in frequency data frame form.

(a) Use loglm() to fit the model of mutual independence, [A][C][M].



(b) Prepare mosaic display(s) for associations among these variables. Give a verbal description of the association between cigarette and alcohol use.



(c) Use fourfold() to produce fourfold plots for each pair of variables, AC, AM, and CM, stratified by the remaining one. Describe these associations verbally.



Exercise 9.2 Continue the analysis of the *DaytonSurvey* data by fitting the following models:

(a) Joint independence, [AC][M]



(b) Conditional independence, [AM][CM]



(c) Homogeneous association, [AC][AM][CM]



(d) Prepare a table giving the goodness-of-fit tests for these models, as well as the model of mutual independence, [A][C][M], and the saturated model, [ACM]. *Hint*: anova() and LRstats() are useful here. Which model appears to give the most reasonable fit?



Exercise 9.3 The data set Caesar in VCdExtra gives a 3×2^3 frequency table classifying 251 women who gave birth by Caesarian section by Infection (three levels: none, Type 1, Type2) and Risk, whether Antibiotics were used, and whether the Caesarian section was Planned or not. Infection is a natural response variable, but the table has quite a few zeros.

(a) Use structable() and mosaic() to see the locations of the zero cells in this table.



(b) Use loglm() to fit the baseline model [I][RAP]. Is there any problem due to zero cells indicated in the output?



(c) For the purpose of this excercise, treat all the zero cells as *sampling zeros* by adding 0.5 to all cells, e.g., Caesar1 <- Caesar + 0.5. Refit the baseline model.



(d) Now fit a "main effects" model [IR][IA][IP][RAP] that allows associations of Infection with each of the predictors.



Exercise 9.4 The <code>Detergent</code> in vcdExtra gives a $2^3 \times 3$ table classifying a sample of 1,008 consumers according to their preference for (a) expressed <code>Preference</code> for Brand "X" or Brand "M" in a blind trial, (b) <code>Temperature</code> of laundry water used, (c) previous use (<code>M_user</code>) of detergent Brand "M," and (d) the softness (<code>Water_softness</code>) of the laundry water used.

(a) Make some mosaic displays to visualize the associations among the table variables. Try using different orderings of the table variables to make associations related to Preference more apparent.



(b) Use a doubledecker () plot to visualize how Preference relates to the other factors.



(c) Use loglm() to fit the baseline model [P][TMW] for Preference as the response variable. Use a mosaic display to visualize the lack of fit for this model.



Chapter 10

Extending Loglinear Models

Exercise 10.1 Example 10.5 presented an analysis of the data on visual acuity for the subset of women in the *VisualAcuity* data. Carry out a parallel analysis of the models fit there for the men in this data set, given by:

```
> data("VisualAcuity", package="vcd")
> men <- subset(VisualAcuity, gender=="male", select=-gender)</pre>
```



Exercise 10.2 Table 10.1 gives a 4×4 table of opinions about premarital sex and whether methods of birth control should be made available to teenagers aged 14–16, from the 1991 General Social Survey (Agresti, 2013, Table 10.3). Both variables are ordinal, and their grades are represented by the case of the row and column labels.

Table 10.1: Opinions about premarital sex and availability of teenage birth control. Source: Agresti (2013, Table 10.3).

Premarital sex	Birth control			
	DISAGREE	disagree	agree	AGREE
WRONG	81	68	60	38
Wrong	24	26	29	14
wrong	18	41	74	42
OK	36	57	161	157

- (a) Fit the independence model to these data using loglm() or glm().
 - \star
- (b) Make a mosaic display showing departure from independence and describe verbally the pattern of association.
 - *
- (c) Treating the categories as equally spaced, fit the $L \times L$ model of uniform association, as in Section 10.1. Test the difference against the independence model with a likelihood-ratio test.
 - \star
- (d) Fit the RC(1) model with gnm (), and test the difference of this against the model of uniform association.
 - \star
- (e) Write a brief summary of these results, including plots useful for explaining the relationships in this data set.



Exercise 10.3 For the data on attitudes toward birth control in Table 10.1,

- (a) Calculate and plot the observed local log odds ratios.
 - \star
- (b) Also fit the R, C, and R+C models.
 - *
- (c) Use the method described in Section 10.1.2 to visualize the structure of fitted local log odds ratios implied by each of these models, together with the RC(1) model.
 - \star

Exercise 10.4 The data set gss8590 in logmult gives a $4\times5\times4$ table of education levels and occupational categories for the four combinations of gender and race from the General Social Surveys, 1985–1990, as reported by Wong (2001, Table 2). Wong (2010, Table 2.3B) later used the subset pertaining to women to illustrate RC(2) models. This data is created below as Women.tab, correcting an inconsistency to conform with the 2010 table.



```
> data("gss8590", package="logmult")
> Women.tab <- margin.table(gss8590[,,c("White Women", "Black Women")], 1:2)
> Women.tab[2,4] <- 49
> colnames(Women.tab)[5] <- "Farm"</pre>
```

(a) Fit the independence model, and also the RC(1) and RC(2) models using rc() with marginal weights, as illustrated in Example 10.4. Summarize these statistical tests in a table.

 \star

(b) Plot the solution for the RC(2) model with 68% confidence ellipses. What verbal labels would you use for the two dimensions?

 \star

(c) Is there any indication that a simpler model, using integer scores for the row (Education) or column (Occupation) categories, or both, might suffice? If so, fit the analogous column effects, row effects, or $L \times L$ model, and compare with the models fit in part (a).

 \star

Chapter 11

Generalized Linear Models for Count Data

Exercise 11.1 Poole (1989) studied the mating behavior of elephants over 8 years in Amboseli National Park, Kenya. A focal aspect of the study concerned the mating success of males in relation to age, since larger males tend to be more successful in mating. Her data were used by Ramsey and Schafer (2002, Chapter 22) as a case study, and are contained in the Sleuth2 (Ramsey et al., 2012) package (Ramsey et al., 2012) as case 2201.

For convenience, rename this to elephants, and study the relation between Age (at the beginning of the study) and number of successful Matings for the 41 adult male elephants observed over the course of this study, ranging in age from 27–52.

(a) Create some exploratory plots of Matings against Age in the styles illustrated in this chapter. To do this successfully, you will have to account for the fact that Matings has a range of only 0–9, and use some smoothing methods to show the trend.



(b) Repeat (a) above, but now plotting log (Matings+1) against Age to approximate a Poisson regression with a log link and avoid problems with the zero counts.

*

(c) Fit a linear Poisson regression model for Matings against Age. Interpret the fitted model *verbally* from a graph of predicted number of matings and/or from the model coefficients. (*Hint*: Using Age-27 will make the intercept directly interpretable.)

 \star

(d) Check for nonlinearity in the relationship by using the term poly (Age, 2) in a new model. What do you conclude?

*

(e) Assess whether there is any evidence of overdispersion in these data by fitting analogous quasi-Poisson and negative-binomial models.

 \star

Exercise 11.2 The data set *quine* in MASS gives data on absenteeism from schools in rural New South Wales, Australia. 146 children were classified by ethnic background (Eth), age (Age, a factor), Sex, and Learner status (Lrn), and the number of days absent (Days) from school in a particular school year was recorded.

(a) Fit the all main-effects model in the Poisson family and examine the tests of these effects using summary () and car::Anova(). Are there any terms that should be dropped according to these tests?

*

(b) Re-fit this model as a quasi-Poisson model. Is there evidence of overdispersion? Test for overdispersion formally, using dispersiontest() from AER (Kleiber and Zeileis, 2015).

 \star

(c) Carry out the same significance tests and explain why the results differ from those for the Poisson model.

 \star

Exercise 11.3 The data set *AirCrash* in vcdExtra was analyzed in Exercise 5.2 and Exercise 6.3 in relation to the Phase of the flight and Cause of the crash. Additional variables include the number of Fatalities and Year. How does Fatalities depend on the other variables?

(a) Use the methods of this chapter to make some exploratory plots relating fatalities to each of the predictors.

*

(b) Fit a main effects poisson regression model for Fatalities, and make effects plots to visualize the model. Which phases and causes result in the largest number of fatalities?

 \star

(c) A linear effect of Year might not be appropriate for these data. Try using a natural spline term, ns (Year, df) to achieve a better, more adequate model.

 \star

(d) Use a model-building tool like add1 () or MASS::stepAIC() to investigate whether there are important two-way interactions among the factors and your chosen effect for Year.

 \star

(e) Visualize and interpret your final model and write a brief summary to answer the question posed.



Exercise 11.4 Male double-crested cormorants use advertising behavior to attract females for breeding. The *Cormorants* data set in vcdExtra gives some results from a study by Meagan Mc Rae (2015) on counts of advertising males observed two or three times a week at six stations in a tree-nesting colony for an entire breeding season. The number of advertising birds was counted and these observations were classified by characteristics of the trees and nests. The goal was to determine how this behavior varies temporally over the season and spatially over observation stations, as well as with characteristics of nesting sites. The response variable is count and other predictors are shown below. See help (Cormorants, package="vcdExtra") for further details.

```
> data("Cormorants", package = "vcdExtra")
> car::some (Cormorants)
      category week station
                                 nest height
                                              density tree_health count
44
                          В2
                                  no
                                                           healthy
                                        high
84
           Pre
                          С4
                                                   few
                                                              dead
                                  no
                                                           healthy
98
           Pre
                          В1
                                 full
                                         mid
                                                   few
                          В1
                                  no
                                         mid
                                                   few
                                                              dead
159 Incubation
                          C2 partial
                                         low
                                                               dead
176 Incubation
                          C4
                                 full
                                        high
                                                   few
                                                              dead
243 Incubation
                   6
                                 full
                                         mid
                                                   few
                                                               dead
248 Incubation
                   6
                          СЗ
                                                               dead
                                        high
                                                  high
                                  no
                                                               dead
315 Incubation
                          В2
                                         mid moderate
                                   no
317 Incubation
                                        high moderate
                                                               dead
                                   no
```

(a) Using the methods illustrated in this chapter, make some exploratory plots of the number of advertising birds against week in the breeding season, perhaps stratified by another predictor, like tree height, nest condition, or observation station. To see anything reasonable, you should plot count on a log (or square root) scale, jitter the points, and add smoothed curves. The variable category breaks the weeks into portions of the breeding season, so adding vertical lines separating those will be helpful for interpretation.

*

(b) Fit a main-effects Poisson GLM to these data and test the terms using Anova () from the car package.



(c) Interpret this model using an effects plot.



(d) Investigate whether the effect of week should be treated as linear in the model. You could try using a polynomial term like poly (week, degree) or perhaps better, using a natural spline term like ns (week, df) from the splines package.



(e) Test this model for overdispersion, using either a quasipoisson family or dispersiontest () in AER.



Exercise 11.5 For the *CodParasites* data, recode the area variable as an ordered factor as suggested in footnote 13. Test the hypotheses that prevalence and intensity of cod parasites is linearly related to area.



Exercise 11.6 In Example 11.10, we ignored other potential predictors in the *CodParasites* data: depth, weight, length, sex, stage, and age. Use some of the graphical methods shown in this case study to assess whether any of these are related to prevalence and intensity.



Exercise 11.7 The analysis of the *PhdPubs* data in the examples in this chapter were purposely left incomplete, going only as far as the negative binomial model.

(a) Fit the zero-inflated and hurdle models to this data set, considering whether the count component should be Poisson or negative-binomial, and whether the zero model should use all predictors or only a subset. Describe your conclusions from this analysis in a few sentences.



(b) Using the methods illustrated in this chapter, create some graphs summarizing the predicted counts and probabilities of zero counts for one of these models.



(c) For your chosen model, use some of the diagnostic plots of residuals and other measures shown in Section 11.6 to determine if your model solves any of the problems noted in Example 11.17 and Example 11.18, and whether there are any problems that remain.



Exercise 11.8 In Example 11.19 we used a simple analysis of $\log(y+1)$ for the multivariate responses in the *NMES1988* data using a classical MLM (Eqn. (11.16)) as a rough approximation of a multivariate Poisson model. The HE plot in Figure 11.40 was given as a visual summary, but did not show the data. Examine why the MLM is not appropriate statistically for these data, as follows:

(a) Calculate residuals for the model nmes.mlm using

```
> resids <- residuals(nmes.mlm, type="deviance")</pre>
```

(b) Make univariate density plots of these residuals to show their univariate distributions. These should be approximately normal under the MLM. What do you conclude?



(c) Make some bivariate plots of these residuals. Under the MLM, each should be bivariate normal with elliptical contours and linear regressions. Add 2D density contours (kde2d(), or geom_density2d() in ggpplot2 (Wickham and Chang, 2015)) and some smoothed curve. What do you conclude?



References

- Agresti, A. (2013). *Categorical Data Analysis*. Wiley Series in Probability and Statistics. New York: Wiley-Interscience [John Wiley & Sons], 3rd edn.
- Agresti, A. and Winner, L. (1997). Evaluating agreement and disagreement among movie reviewers. *Chance*, 10(2), 10–14.
- Bertin, J. (1983). Semiology of Graphics. Madison, WI: University of Wisconsin Press. (trans. W. Berg).
- Bouchet-Valat, M. (2015). *lognult: Log-Multiplicative Models, Including Association Models*. R package version 0.6.1.
- Fisher, R. A. (1940). The precision of discriminant functions. Annals of Eugenics, 10, 422-429.
- Fox, J. and Weisberg, S. (2015). car: Companion to Applied Regression. R package version 2.0-25/r421.
- Friendly, M. (2014a). *HistData: Data sets from the history of statistics and data visualization*. R package version 0.7-5.
- Friendly, M. (2014b). Lahman: Sean Lahman's Baseball Database. R package version 3.0-1.
- Friendly, M. (2015). vcdExtra: vcd Extensions and Additions. R package version 0.6-7.
- Geissler, A. (1889). Beitrage zur frage des geschlechts verhaltnisses der geborenen. Z. K. Sachsischen Statistischen Bureaus, 35(1), n.p.
- Grayson, D. K. (1990). Donner party deaths: A demographic assessment. *Journal of Anthropological Research*, 46(3), 223–242.
- Greenacre, M. and Nenadic, O. (2014). ca: Simple, Multiple and Joint Correspondence Analysis. R package version 0.58.
- Jansen, J. (1990). On the statistical analysis of ordinal data when extravariation is present. *Journal of the Royal Statistical Society. Series C (Applied Statistics)*, 39(1), 75–84.
- Kleiber, C. and Zeileis, A. (2015). AER: Applied Econometrics with R. R package version 1.2-3.
- Mc Rae, M. (2015). Spatial, Habitat and Frequency Changes in Double-crested Cormorant Advertising Display in a *Tree-nesting Colony*. Masters project, environmental studies, York University.
- Meyer, D., Zeileis, A., and Hornik, K. (2015). vcd: Visualizing Categorical Data. R package version 1.3-3.
- Mosteller, F. and Wallace, D. L. (1963). Inference in an authorship problem. *Journal of the American Statistical Association*, 58(302), 275–309.
- Poole, J. H. (1989). Mate guarding, reproductive success and female choice in African elephants. *Animal Behavior*, 37, 842–849.
- Ramsey, F. L. and Schafer, D. W. (2002). *The Statistical Sleuth: A Course in Methods of Data Analysis*. Belmont, CA: Duxbury, 2nd edn.
- Ramsey, F. L., Schafer, D. W., Sifneos, J., and Turlach, B. A. (2012). *Sleuth2: Data sets from Ramsey and Schafer's* Statistical Sleuth (2nd ed). R package version 1.0-7.
- Ripley, B. (2015). MASS: Support Functions and Datasets for Venables and Ripley's MASS. R package version 7.3-40.
- Wickham, H. and Chang, W. (2015). ggplot2: An Implementation of the Grammar of Graphics. R package version 1.0.1.

- Wong, R. S.-K. (2001). Multidimensional association models: A multilinear approach. *Sociological Methods and Research*, 30(2), 197–240.
- Wong, R. S.-K. (2010). *Association Models*. Quantitative Applications in the Social Sciences. Los Angeles: SAGE Publications.
- Wright, K. (2015). agridat: Agricultural Datasets. R package version 1.11.
- Yee, T. W. (2015). VGAM: Vector Generalized Linear and Additive Models. R package version 0.9-7.
- Zeileis, A. and Kleiber, C. (2014). countreg: Count Data Regression. R package version 0.1-2/r88.