LaTeX Equations with symbolicMatrix, Eqn and matrix2latex

Phil Chalmers, Michael Friendly

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The `matlib` package provides a collection of functions that simplify using LaTeX notation for matrices, vectors and equations in documentation and in writing.

- `symbolicMatrix()`: Constructs the LaTeX code for a symbolic matrix, whose elements are a symbol, with row and column subscripts.
- `matrix2latex()`: Constructs the LaTeX code for a symbolic matrix, whose elements are a symbol, with row and column subscripts
- `showEqn()`: Shows what matrices $\mathbf{A}, \mathbf{b}$ look like as the system of linear equations, $\mathbf{A x} = \mathbf{b}$, but written out as a set of equations.
- `Eqn()`: A wrapper to produce LaTeX expressions that can be copied/pasted into documents or used directly in `.Rmd` or `.qmd` documents to compile to equations.

When used directly in R, they produce their output to the console (using `cat()`). In a `.Rmd` or `.qmd` document, use the chunk options: `results='asis', echo=FALSE` so that `knitr` just outputs the text of the equations to the document. The rendering of the equations is handled by `pandoc`.

Using `symbolicMatrix()` and `Eqn()`

`symbolicMatrix()` constructs the LaTeX code for a symbolic matrix, whose elements are a symbol, with row and column subscripts. For example, by default (with no arguments) it produces the expression for a matrix whose elements are $x_{ij}, i = 1, 2, \cdots, n; j = 1, 2, \cdots, m$ in a LaTeX `\begin{pmatrix} ... \end{pmatrix}` environment.

```
\begin{pmatrix}
  x_{11} & x_{12} & \cdots & x_{1m} \\
  x_{21} & x_{22} & \cdots & x_{2m} \\
  \vdots & \vdots &        & \vdots \\
  x_{n1} & x_{n2} & \cdots & x_{nm} \\
\end{pmatrix}
```

The code above appears in the console. To render this as a matrix in a document, this must be wrapped in a display math environment, which is provided by `Eqn()`.

```
symbolicMatrix() |> Eqn(number = FALSE)
```

$$\begin{pmatrix}
  x_{11} & x_{12} & \cdots & x_{1m} \\
  x_{21} & x_{22} & \cdots & x_{2m} \\
  \vdots & \vdots &   & \vdots \\
  x_{n1} & x_{n2} & \cdots & x_{nm} \\
\end{pmatrix}$$

Some other examples:

- A 3×3 identity matrix with square brackets, specified as an equation with a left-hand side $\mathbf{I}_3$

```
symbolicMatrix(diag(3), lhs = "\\mathbf{I}_3", matrix="bmatrix") |>
  Eqn(number = FALSE)
```

$$\mathbf{I}_3 = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

- A row or column vector; the first argument to `symbolicMatrix()` must be a **matrix**, so wrap an R vector in `matrix()`, supplying `nrow=1` (or `ncol = 1`).

```
symbolicMatrix(matrix(LETTERS[1:4], nrow=1)) |> Eqn(number = FALSE)
```

$$\begin{pmatrix} A & B & C & D \end{pmatrix}$$

As a more complicated example, here we write out the LaTeX equation for the singular value decomposition (SVD) of a general $n \times p$ matrix $\mathbf{X}$ using `Eqn()` and `symbolicMatrix()`. In Rmd markup, `Eqn()` can be given an equation label. Two calls to `Eqn()` produce separate equations in the output.

Both of these equations are numbered (by default). (`Eqn()` uses the LaTeX `equation` environment, `\begin{equation} ... \end{equation}`, or `equation*` if the equation is not numbered (`number = FALSE`)). The two calls to `Eqn()` are rendered as separate equations, center aligned.

```
Eqn("\\mathbf{X} = \\mathbf{U} \\mathbf{\\Lambda} \\mathbf{V}^\\top", label='eqn:svd')
Eqn(symbolicMatrix("u", "n", "k", lhs = ''),
    symbolicMatrix("\\lambda", "k", "k", diag=TRUE),
    symbolicMatrix("v", "k", "p", transpose = TRUE))
```

This produces the two numbered equations:

$$\mathbf{X} = \mathbf{U} \mathbf{\Lambda} \mathbf{V}^\top \tag{1}$$

$$= \begin{pmatrix} u_{11} & u_{12} & \cdots & u_{1k} \\ u_{21} & u_{22} & \cdots & u_{2k} \\ \vdots & \vdots & & \vdots \\ u_{n1} & u_{n2} & \cdots & u_{nk} \end{pmatrix} \begin{pmatrix} \lambda_1 & 0 & \cdots & 0 \\ 0 & \lambda_2 & \cdots & 0 \\ \vdots & \vdots & \ddots & \vdots \\ 0 & 0 & \cdots & \lambda_k \end{pmatrix} \begin{pmatrix} v_{11} & v_{12} & \cdots & v_{1p} \\ v_{21} & v_{22} & \cdots & v_{2p} \\ \vdots & \vdots & & \vdots \\ v_{k1} & v_{k2} & \cdots & v_{kp} \end{pmatrix}^\top \tag{2}$$

The matrix names in the 1 are printed in a **boldface** math font, typically used for matrices and vectors. Note that when using LaTeX code in R expressions each backslash (\) must be doubled (\\) in R because \ is the escape character.

Note that the first equation can be referenced because it was labeled: "As seen in Equation 1 . . . ". (In Quarto, equation labels must be of the form `#eq-label` and equation references are of the form `@eq-label`)

As another example, the chunk below shows a system of equations $\mathbf{A}\mathbf{x} = \mathbf{b}$ written out using symbolic matrices. Note the use of `cat()` to insert arbitrary LaTeX into the stream

```
Eqn(symbolicMatrix("a", nrow = "m", ncol="n", matrix="bmatrix"),
    symbolicMatrix("x", nrow = "n", ncol=1),
    cat("\\quad=\\quad"),
    symbolicMatrix("b", nrow = "m", ncol=1))
```

$$
\begin{bmatrix}
a_{11} & a_{12} & \cdots & a_{1n} \\
a_{21} & a_{22} & \cdots & a_{2n} \\
\vdots & \vdots & & \vdots \\
a_{m1} & a_{m2} & \cdots & a_{mn}
\end{bmatrix}
\begin{pmatrix}
x_{1} \\
x_{2} \\
\vdots \\
x_{n}
\end{pmatrix}
=
\begin{pmatrix}
b_{1} \\
b_{2} \\
\vdots \\
b_{m}
\end{pmatrix}
\tag{3}
$$

aligned environment

You can also align separate equations relative to some symbol like an `=` sign to show separate steps of re-expression, using the option `Eqn(..., align=TRUE)`.

Show the singular value decomposition again, but now as two separate equations aligned after the `=` sign. Note the locations of the `&` for alignment, specified as the left-hand side (`lhs`) of the second equation.

```
Eqn("\\mathbf{X} & = \\mathbf{U} \\mathbf{\\Lambda} \\mathbf{V}\\top",
    Eqn_newline(),
    symbolicMatrix("u", "n", "k", lhs = '&'),
    symbolicMatrix("\\lambda", "k", "k", diag=TRUE),
    symbolicMatrix("v", "k", "p", transpose = TRUE),
    align=TRUE)
```

$$
\begin{aligned}
\mathbf{X} & = \mathbf{U} \mathbf{\Lambda} \mathbf{V}\top \qquad (4) \\
& = \begin{pmatrix}
u_{11} & u_{12} & \cdots & u_{1k} \\
u_{21} & u_{22} & \cdots & u_{2k} \\
\vdots & \vdots & & \vdots \\
u_{n1} & u_{n2} & \cdots & u_{nk}
\end{pmatrix}
\begin{pmatrix}
\lambda_{1} & 0 & \cdots & 0 \\
0 & \lambda_{2} & \cdots & 0 \\
\vdots & \vdots & \ddots & \vdots \\
0 & 0 & \cdots & \lambda_{k}
\end{pmatrix}
\begin{pmatrix}
v_{11} & v_{12} & \cdots & v_{1p} \\
v_{21} & v_{22} & \cdots & v_{2p} \\
\vdots & \vdots & & \vdots \\
v_{k1} & v_{k2} & \cdots & v_{kp}
\end{pmatrix}^\top \qquad (5)
\end{aligned}
$$

Note that in this example, there are three calls to `symbolicMatrix()`, wrapped inside `Eqn()`. `Eqn_newline()` emits a newline (`\\`) between equations.

matrix2latex

The `matrix2latex()` function can also generate symbolic equations from numeric or character matrices.

Create character matrix and vector:

```
A <- matrix(paste0('a_', 1:9), 3, 3, byrow = TRUE) |> print()
```

```
##      [,1]  [,2]  [,3] 
## [1,] "a_1" "a_2" "a_3"
## [2,] "a_4" "a_5" "a_6"
## [3,] "a_7" "a_8" "a_9"
```

```
b <- paste0("\\beta_", 1:3) |> print()
```

```
## [1] "\\beta_1" "\\beta_2" "\\beta_3"
```

Using `matrix2latex()` we can show the matrix $[\mathbf{A}|\mathbf{b}]$. Note that you can pipe the result of `matrix2latex()` to `Eqn()`:

```
matrix2latex(cbind(A,b)) |> Eqn(number=FALSE)
```

$$
\begin{bmatrix}
a_{1} & a_{2} & a_{3} & \beta_{1} \\
a_{4} & a_{5} & a_{6} & \beta_{2} \\
a_{7} & a_{8} & a_{9} & \beta_{3}
\end{bmatrix}
$$

showEqn

`showEqn()` is designed to show a system of linear equations, $\mathbf{A}\mathbf{x} = \mathbf{b}$, but written out as a set of equations individually. With the option `latex = TRUE` it writes these out in LaTeX form.

Here, we create a character matrix containing the elements of a 3×3 matrix `A`, whose elements are of the form `a_{ij}` and two character vectors, `b_i` and `x_i`.

```
A <- matrix(paste0("a_{", outer(1:3, 1:3, FUN  = paste0), "}"),
            nrow=3) |> print()
```

```
##      [,1]     [,2]     [,3]
## [1,] "a_{11}" "a_{12}" "a_{13}"
## [2,] "a_{21}" "a_{22}" "a_{23}"
## [3,] "a_{31}" "a_{32}" "a_{33}"
```

```
b <- paste0("b_", 1:3)
x <- paste0("x", 1:3)
```

`showEqn(..., latex = TRUE)` produces the three equations in a single `\begin{array} ... \begin{array}` environment.

```
showEqn(A, b, vars = x, latex=TRUE)
```

If this line was run in an R console, it would produce:

```
\begin{array}{lllllll}
a_{11} \cdot x_1 &+& a_{12} \cdot x_2 &+& a_{13} \cdot x_3  &=&  b_1 \\
a_{21} \cdot x_1 &+& a_{22} \cdot x_2 &+& a_{23} \cdot x_3  &=&  b_2 \\
a_{31} \cdot x_1 &+& a_{32} \cdot x_2 &+& a_{33} \cdot x_3  &=&  b_3 \\
\end{array}
```

Evaluating the above code in an unnumbered LaTeX math environment via `Eqn()` gives the desired result:

```
showEqn(A, b, vars = x, latex=TRUE) |> Eqn(number=FALSE)
```

$$
\begin{array}{lllllll}
a_{11} \cdot x_1 &+& a_{12} \cdot x_2 &+& a_{13} \cdot x_3 &=& b_1 \\
a_{21} \cdot x_1 &+& a_{22} \cdot x_2 &+& a_{23} \cdot x_3 &=& b_2 \\
a_{31} \cdot x_1 &+& a_{32} \cdot x_2 &+& a_{33} \cdot x_3 &=& b_3
\end{array}
$$