RIF-regressions: tools for analyzing distributional statistics

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Introduction

Unconditional quantile regressions (UQR) via RIF (Recentered Influence functions) was introduced by Firpo, Fortin, and Lemieux (2009) as a computationally simple strategy to estimate Unconditional partial effects on quantiles.

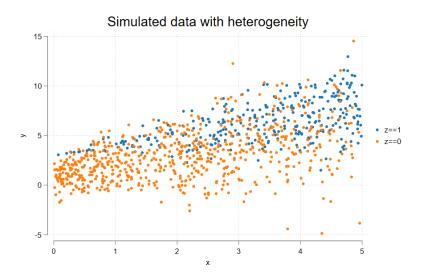
While Conditional QR, could be used to identify effects across conditional distributions (at the margin), UQR identifies effect on unconditional distributions.

These effects, however, are different from unconditional treatment effects, which compares differences in statistics, across two (or more) distributions.

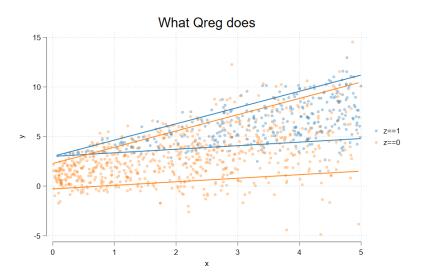
Since then, RIF-regressions have been used to analyze other statistics. See FFL(2018), Firpo and Pinto (2016), Chung and Vankerm (2018), Cowell and Flachaire (2007), Essama-Nssah and Lambert (2012) and Heckley et al (2016).

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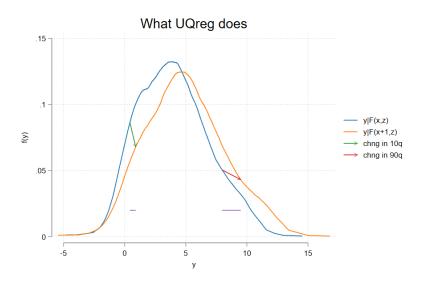
Simulated Data



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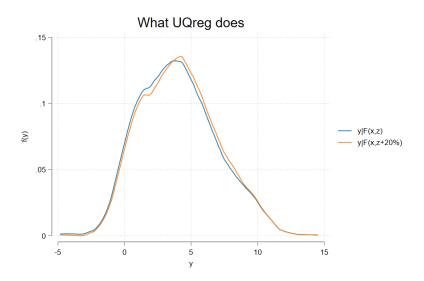


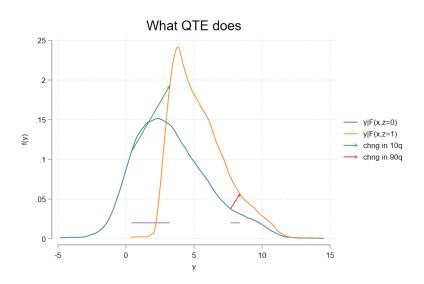
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To understand better what RIF-regressions do in general, it will be useful to set a unifying framework.

Assume that the outcome y is a function of observed x and unobserved characteristics e, such that.

$$y = g(x, e)$$

Thus, if we observe x and e, the conditional CDF is given by:

$$F(Y|X,e) = 1(Y \ge g(x,e))$$

Under the same framework, the unconditional distribution of y would be given by:

$$F(y) = \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} F(Y|X, e) f(x, e) de \ dx$$

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It is important to notice that this unconditional distribution still "conditions", but on distributions, not specific values. (F(Y) depends on f(X, e)).

Since we do not observe e, one alternative is to "integrate" over the unobserved factors e. However, to do so, we need to impose the exogeneity/independence assumption f(x,e) = f(x|e)f(e) = f(x)f(e).

This is an stronger assumption than the zero conditional mean E(e|X)=0 and Homoscedasticity assumption Var(e|X)=c combined. However under this assumption:

$$F(y) = \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} F(Y|X, e) f(x) f(e) de \ dx$$

So we can integrate over the error

$$F(y) = \int_{-\infty}^{\infty} F(Y|X) dF(x)$$

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Implicit assumption: Conditional distributions of Y are fixed F(Y|X). The only things that change are characteristics F(x).

This has parallels with standard linear regressions:

$$F(y) = \int_{-\infty}^{\infty} F(Y|X)dF(x)$$
$$y_i = b_0 + b_1 * x_i + e_i$$

This does not mean F(y|X) is constant across X, but that it is fixed to changes in X.

Side Question: How do we simulate changes in dF(x)?

- Full distribution simulations.
- Local simulations (swapping one observation at a time)
- Reweighting $dG(x) = w(x) * dF(x) \quad \forall x \in R$

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How do we analyze a the change in F(y) caused by a change in F(x)?

As stated, the change in Y can be analyzed graphically. (how the overall distribution changes).

However, this may be impractical.

- You need separate simulations for each variable in the model.
- Or different Weighting factors.
- Or local simulations (may be simplest to implement).

The alternative is to use a single statistic that summarizes the distribution of y, and focus on how that summary statistic changes when F(x) changes.

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Call this summary (or distributional) statistic v. This is a function that depends on ALL values of y or on f(y) or F(y) Simplest example:

Mean:
$$\mu_y = v(F(y)) = \int_{-\infty}^{\infty} yf(y)dy$$

This would be the unconditional mean, because it looks over the whole distribution. However, we can also write it as conditional with respect to the distribution of x

Mean:
$$\mu_y = v(F(y)) = \int_{-\infty}^{\infty} y \int_{-\infty}^{\infty} f(y|x)f(x)dxdy$$

$$\mu_y = v(F(y)) = \int_{-\infty}^{\infty} E(y|X)f(x)dx$$

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How v changes when there is a change in f(x)?

Long chain of events $\Delta f(x) o \Delta f(y) o \Delta \mu_y$

Call F(y) original distribution and G(y) the distribution after F(x) changes. The effect that this has on μ_y can be measured as

$$\Delta \mu_y = v(G(y)) - v(F(y))$$

However the "influence" of this effect should be a standardized by the change in the distribution itself.

$$\frac{\Delta \mu_y}{\Delta F(y)} = Influence(v, F(y)) = \frac{v(G(y)) - v(F(y))}{||G(y) - F(y)||}$$

And this bring us the first definition of Influence function:

$$IF(v, F(y)) = lim_{G(y) \to F(y)} \frac{v(G(y)) - v(F(y))}{||G(y) - F(y)||}$$

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$$IF(v, F(y)) = lim_{G(y) \to F(y)} \frac{v(G(y)) - v(F(y))}{||G(y) - F(y)||}$$

This expression corresponds to a directional derivative of a functional (the distributional statistic). The Rate of changes in the statistic with respect to changes in the distribution. In other words, the IF measure the "standardized" effect on the statistic v, at the "margin". Even more technical. What is G(y)

$$G(y) = \epsilon * 1(y \ge y_i) + (1 - \epsilon) * F(y)$$

where $\epsilon * 1(y \ge y_i)$ is a "contamination" error on the distribution of F(y). Thus

$$IF(y_i, F(y), v) = lim_{\epsilon \to 0} \frac{v(G(y)) - v(F(y))}{\epsilon}$$

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Consider the simplest case. The mean. How would an additional observation affect the unconditional mean?

$$\begin{aligned} & \text{if} \quad y_i > \mu_y \to \Delta \mu_y > 0 \\ & \text{if} \quad y_i < \mu_y \to \Delta \mu_y < 0 \end{aligned}$$

In fact, the impact on μ_{ν} will be:

$$\Delta\mu_{y}=(y_{i}-\mu_{y})*\frac{1}{N+1}$$

But the IF will be:

$$IF(y_i, \mu_y) = y_i - \mu_y$$

FFL (2009) introduce at this point the idea of the Re-centered IF

$$RIF(y_i, \mu_y) = \mu_y + IF(y_i, \mu_y) = y_i$$

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From the technical point of view, The RIF statistic can be thought as a first order approximation or linearization of any functional v. Or the consequence of a Taylor expansion.

$$v(F(y)) \approx v(F_0(y)) + \sum \left(\frac{\partial v(.)}{\partial F(Y)}\right) * \Delta F(Y)$$
 $v(F(y)) \approx v(F_0(y)) + \frac{1}{N} \sum IF(i_{th}, v, F(y))$
 $v(F(y)) \approx \frac{1}{N} \sum RIF(i_{th}, v, F(y))$

From here, two properties can be derived: (Deville, 1999).

$$E(RIF(i_{th}, v, F)) = v(F(y))$$

$$Var(E(RIF(i_{th}, v, F))) = Var(v(F(y)))$$

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RIF-Recentered Influence Function Regression

Reconsider the main question. We want to measure how the distribution of Y changes when the distribution of X changes:

$$F(y) = \int_{-\infty}^{\infty} F(Y|X) dF(x)$$

However, instead of focusing on the overall distribution of Y, we can concentrate on how the unconditional mean μ_Y changes when F(X) changes.

$$v(\mu_y, F(y)) = v\left(\mu_y, \int_{-\infty}^{\infty} F(Y|X)dF(x)\right)$$

On the left side of the equation, we can proxy the effects on the unconditional mean (or any other statistic) by using the RIF, which is the value itself.

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On the right side of the equation we face the same problem. However, we can capture changes in the distribution of X also using RIFs, and first order approximations. (although higher order may also be important)

$$RIF(i_{th}, v, F(y)) = a_0 + a_1 * RIF(i_{th}, \mu, F(x)) + \varepsilon_i$$

And for the unconditional mean, and a linear approximation we have:

$$y_i = a_0 + a_1 * x_i + \varepsilon_i$$

Remarks:

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- The dependent variable can be the RIF for any statistic. Including unconditional quantiles.
- For independent variables, one can use either higher order approximations (polynomial or interactions)

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 Or use RIFs for other moments of the distribution, like Variance, covariances and Kurtosis. (centered polynomials)

The most common approach is, of course, simply use polynomials or interactions of explanatory variables.

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RIF-regressions, Estimation

RIF-regressions can be estimated using any of the battery of methodologies we are already familiar with.

The estimation basically involves 3 steps.

- Define sample of interest.
- Estimate the RIF for the dependent variable and distributional Statistic of interest.
- Estimate a model using the RIF as dependent variable using flexible specification. OLS, logit, poisson.

The goal is to use a model that may best capture the linear or nonlinear relationship between the RIF of the distributional statistic, and RIF of explanatory variables.

FFL(2009), for example, proposes that RIF-UQR can be estimated via OLS, but that given the nature of the Quantile RIF, probit or logit models could also be used.

Other methods could be potentially used as well.

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RIF-regressions, Estimation

In Stata, there are many commands that allows you to implement RIF-OLS regressions. You have rifreg, riflreg, rifldreg.

My preference, is the use of rifhdreg, as it handles many RIF's, factor notation, weights, and even allows you to estimate QTE via RIF.

Syntax:

```
rifhdreg depvar [indepvar] [if in] [weight], [reg options] rif(rif options)
[over(overvar) rwlogit( indepvar)]
```

The most important option is rif(), where you indicate which statistic you are interested in analyzing.

Options over() and rwlogit() can also be used to estimate treatment effects under exogeneity. SE need correction.

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While RIF-regressions produce an output similar to the standard LR model, the interpretation requires some considerations.

Recall the model we are trying to estimate:

$$RIF_i(v, F_y) = a_0 + a_1 * x_i + e_i$$

The standard procedure for the estimation of marginal effects requires us to obtain the conditional mean, of this equation, and derive it, with respect to the variable of interest.

$$E(RIF_i|X) = a_0 + a_1 * X \rightarrow \frac{\partial E(RIF_i|X)}{\partial X} = a_1$$

With the exception of the mean (and poverty), this conditional expectation is meaningless, because:

$$E(RIF_i(v, F_y)|X = x) \neq E(RIF_i(v, F_{y|X=x})) = v(y|X = x)$$

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A better way of thinking about this is of taking unconditional expectations of the whole equation.

$$E(RIF_i) = v(y) = a_0 + a_1 * E(X) \rightarrow \frac{\partial E(RIF_i)}{\partial E(X)} = a_1$$

In this case, we are measuring how will the statistic v would change if there is a marginal change in E(X). This is, again, a location shift in the distribution in x, or simply, if everybody in the sample experiences a 1 unit increase in x.

FFL(2009) call this the Unconditional partial effect. An effect, at the margin, of how a general increase in x would affect the distributional statistic v.

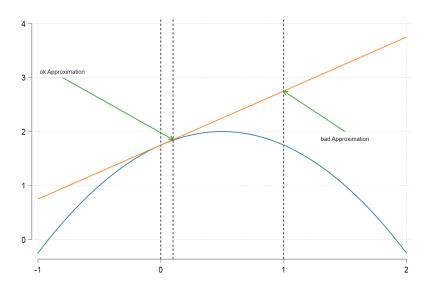
IE. If X is correlated with an increase in the RIF of an observation, then We should expect the overall statistic to increase as well.

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When your dependent variable is binary or with a limited range (0-5), particular care is needed.

- RIF-reg are useful for obtaining effects at the margin (good approximations for small local changes).
- a 1 unit change for dummies, or for dependent variables with limited ranges may be too large.
- This means, the approximation may not be appropriate.
- Similar to making linear extrapolations in nonlinear models, or non linear explanatory variables.

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```
. rifmean income_pcp , rif(q(10), q(50), q(90), gini, lor(40), ucs(90))
Mean estimation
                                           Number of obs = 88,906
                                             [95% conf. interval]
                               Std. err.
                        Mean
rif_income_pcp_1 |
                    3204.528
                                20.5559
                                             3164.239
                                                         3244.818
rif_income_pcp_2 |
                    11382.28
                               53.54245
                                             11277.34
                                                         11487,23
rif_income_pcp_3 |
                    72454.33
                               602.472
                                                         73635.17
                                             71273.49
rif_income_pcp_4 |
                     .6537654
                               .0016039
                                             .6506218
                                                         .6569091
rif_income_pcp_5 |
                     .0639714
                               .0004294
                                             .0631298
                                                         .0648129
rif_income_pcp_6 |
                    .5341139
                               .0022211
                                             .5297606
                                                         .5384672
```

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```
. rifmean expenditure_pcp , rif(q(10), q(50), q(90) , gini, lor(40), ucs(90))

Mean estimation

Number of obs = 88,906
```

	Mean	Std. err.	[95% conf. interval]
rif_expenditure_pcp_1	3275.501	17.1785	3241.831 3309.171
rif_expenditure_pcp_2	9907.519	40.46346	9828.211 9986.827
rif_expenditure_pcp_3	51069.12	413.4056	50258.85 51879.39
<pre>rif_expenditure_pcp_4 rif_expenditure_pcp_5 rif_expenditure_pcp_6 </pre>	.6165029	.0017325	.6131073 .6198985
	.0814099	.0005105	.0804094 .0824104
	.5079673	.0022486	.50356 .5123745

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Income	(1) q(10)		(2) q(90)		(3) gini		(4) m4	
Female	-0.060	(0.001)	-0.131	(0.000)	-0.274	(0.620)	0.411	(0.000)
Secondary S in~e	0.241	(0.000)	0.315	(0.000)	-5.119	(0.000)	0.318	(0.000)
Secondary S Co~e	0.429	(0.000)	1.725	(0.000)	-0.467	(0.381)	0.177	(0.000)
College+	0.262	(0.000)	4.988	(0.000)	54.652	(0.000)	0.053	(0.000)
age_hh	0.027	(0.000)	0.021	(0.000)	-0.075	(0.000)	53.255	(0.000)
Household size	-0.026	(0.000)	-0.041	(0.000)	0.020	(0.765)	6.002	(0.000)
couple=1	0.053	(0.003)	0.256	(0.000)	0.582	(0.292)	0.554	(0.000)
sh_nchild05	-0.005	(0.000)	-0.017	(0.000)	0.011	(0.422)	12.820	(0.000)
sh_nchild615	-0.005	(0.000)	-0.011	(0.000)	0.010	(0.384)	17.998	(0.000)
sh_wrk_wmen	0.005	(0.000)	0.009	(0.000)	-0.020	(0.000)	34.069	(0.000)
sh_wrk_men	0.008	(0.000)	0.007	(0.000)	-0.081	(0.000)	41.933	(0.000)
Constant	6.331	(0.000)	9.390	(0.000)	71.035	(0.000)		
Observations	68548		68548		68579		68579	
rifmean	8.079		11.192		65.377			

p-values in parentheses

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	(1)		(2)		(3)		(4)	
Expenditure	q(10)		q(90)		gini		m4	
Female	-0.081	(0.000)	-0.133	(0.000)	-0.571	(0.339)	0.411	(0.000)
Secondary S in~e	0.411	(0.000)	0.334	(0.000)	-5.479	(0.000)	0.318	(0.000)
Secondary S Co~e	0.484	(0.000)	1.633	(0.000)	1.775	(0.002)	0.177	(0.000)
College+	0.409	(0.000)	4.576	(0.000)	57.754	(0.000)	0.053	(0.000)
age_hh	0.010	(0.000)	0.019	(0.000)	0.094	(0.000)	53.255	(0.000)
Household size	-0.096	(0.000)	-0.071	(0.000)	0.524	(0.000)	6.002	(0.000)
couple=1	-0.002	(0.902)	0.310	(0.000)	2.667	(0.000)	0.554	(0.000)
sh_nchild05	-0.005	(0.000)	-0.012	(0.000)	-0.080	(0.000)	12.820	(0.000)
sh_nchild615	-0.003	(0.000)	-0.010	(0.000)	-0.065	(0.000)	17.998	(0.000)
sh_wrk_wmen	0.003	(0.000)	0.006	(0.000)	0.003	(0.516)	34.069	(0.000)
sh_wrk_men	0.003	(0.000)	0.003	(0.000)	-0.016	(0.001)	41.933	(0.000)
Constant	7.824	(0.000)	9.501	(0.000)	53.635	(0.000)		
Observations	68579		68579		68579		68579	
rifmean	8.094		10.841		61.650			

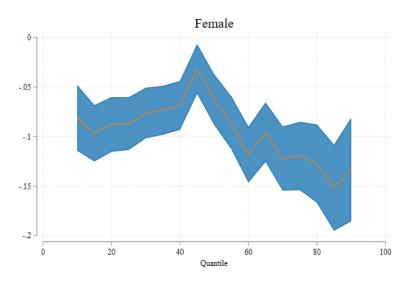
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	(1)		(2)		(3)		(4)	
	q(10)		q(90)		gini		m4	
Female hh	-0.069	(0.000)	-0.210	(0.000)	-1.907	(0.024)	0.411	(0.000)
Secondary S in~e	0.404	(0.000)	0.257	(0.000)	-6.561	(0.000)	0.318	(0.000)
Secondary S Co~e	0.445	(0.000)	1.992	(0.000)	6.615	(0.000)	0.177	(0.000)
College+	0.435	(0.000)	3.996	(0.000)	59.089	(0.000)	0.053	(0.000)
age_hh	0.008	(0.000)	0.019	(0.000)	0.043	(0.148)	53.255	(0.000)
Household size	-0.069	(0.000)	-0.063	(0.000)	0.468	(0.000)	6.002	(0.000)
couple=1	0.031	(0.049)	0.313	(0.000)	2.824	(0.000)	0.554	(0.000)
sh_nchild05	-0.005	(0.000)	-0.017	(0.000)	-0.149	(0.000)	12.820	(0.000)
sh_nchild615	-0.003	(0.000)	-0.014	(0.000)	-0.118	(0.000)	17.998	(0.000)
sh_wrk_wmen	0.002	(0.000)	0.005	(0.000)	0.015	(0.215)	34.069	(0.000)
sh_wrk_men	0.002	(0.000)	0.004	(0.000)	-0.003	(0.717)	41.933	(0.000)
Constant	7.851	(0.000)	9.550	(0.000)	56.645	(0.000)		
Observations	68579		68579		68579		68579	
rifmean	8.125		10.756		60.452			

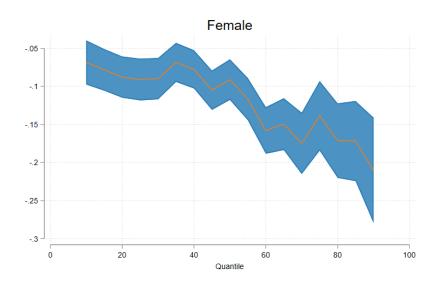
p-values in parentheses

Example, UPE of Female HH



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Example, QTE of Female HH



Example: Analyzing Education, health and Life SF in South Africa

```
Population 15-40: Erreygers's and Wagstaff Indices
                     Mean Std. err. [95% conf. interval]
rif_educ_status_1 | .207547 .0028534 .2019543 .2131398
rif_educ_status_2 | .2125617 .0028988 .20688 .2182434
                 Mean Std. err. [95% conf. interval]
rif_health_1 | .0662624 .0029254 .0605286 .0719962
rif_health_2 | .071507 .003162 .0653095 .0777045
              Mean Std. err. [95% conf. interval]
rif_life_satis_1 | .1883218 .0031558 .1821364 .1945073
rif_life_satis_2 | .2020434 .003374 .1954302 .2086566
```

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Example: Analyzing Education, health and Life SF in South Africa

	(1)	(2)	(3)	(4)
	EDUC	Health	Life_Sa~s	m4
Male	0.000	0.000	0.000	0.489*
Female	-1.276*	0.846	0.200	0.511*
Age of each ho~r	0.675*	0.204*	0.072	28.297*
Female hh	-1.783	0.309	1.045	0.411*
Secondary S in~e	-10.140*	-1.752*	0.110	0.318*
Secondary S Co~e	2.204*	4.549*	9.663*	0.177*
College+	51.266*	11.328*	43.398*	0.053*
age_hh	-0.090*	0.021	0.037	53.255*
Household size	-0.219	-0.556*	-0.083	6.002*
couple=1	0.876	1.109	4.481*	0.554*
sh_nchild05	0.101*	-0.055*	-0.014	12.820*
sh_nchild615	0.016	0.030	-0.004	17.998*
sh_wrk_wmen	0.062*	0.018*	0.042*	34.069*
sh_wrk_men	0.032*	0.009	0.029*	41.933*
Constant	4.991*	0.507	6.574*	
Observations	28311	28329	27624	68579
rifmean	20.755	6.626	18.832	

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* p<0.05

Rios-Avila (Levy) RIF-regressions

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Example: Analyzing Education, health and Life SF in South Africa

	(1)	(2)	(3)	(4)	
TE	EDUC	Health 1	Life_Sa~s	m4	
Male	0.000	0.000	0.000	0.489*	
Female	-0.658	0.713	0.213	0.511*	
Age of each ho~r	0.726*	0.156*	0.030	28.297*	
Female hh	-2.223*	-0.146	0.962	0.411*	
Secondary S in~e	-9.550*	-1.674*	0.057	0.318*	
Secondary S Co~e	5.219*	4.966*	8.880*	0.177*	
College+	58.526*	11.731*	41.566*	0.053*	
age_hh	-0.052	0.021	0.043	53.255*	
Household size	-0.158	-0.575*	0.060	6.002*	
couple=1	0.263	1.025	4.353*	0.554*	
sh_nchild05	0.100*	-0.052	-0.004	12.820*	
sh_nchild615	0.002	0.029	0.007	17.998*	
sh_wrk_wmen	0.073*	0.017	0.044*	34.069*	
sh_wrk_men	0.022*	0.015	0.035*	41.933*	
Constant	0.956	1.737	6.416*		
Observations	28311	28329	27624	68579	
rifmean	20.601	6.210	19.407		



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Conclusions

- In this presentation, I provided a general review of RIF regressions theory and estimation.
- RIF, by default estimates effects at the margin (UPE). But can be used to estimate distributional Effects
- IPW can be combined with RIF to estimate Distributional TE. But Standard errors need correction
- Their application is straight forward with the commands rifhdreg and oaxaca_rif

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Thank you

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Material: https://tinyurl.com/rifsa21

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