Example Project Ideas DATA 37200: Learning, Decisions, and Limits (Winter'25)

Note: it is likely we will update this document with additional references and example topics, in which case we will update the copy on the website.

Suggested Project Topics (biased due to the instructor's knowledge, experience, etc)

Importantly, we would like to reiterate that we strongly encourage you to identify your own topics for the project. The suggested topics below is supposed to serve as examples to stimulate your thinking and also as your second resort, if you were not able to find your own project topics. Moreover, please feel free to discuss with the instructors/TA for suggestions/comments on your ideas and for additional sources of references.

NOTE: papers below are arbitrarily chosen and given to give EXAMPLES of recent research efforts in a theoretical direction and hopefully serve as helpful jumping off points into the broader literature. The examples given are not at all intended to be fully "representative" of all the work in each area, and we are unfortunately not aware of all important works in the massive literature related to these topics. For whatever specific direction you choose to work on, you need to search and try to understand the literature yourself. (Some basic tips: try looking at papers cited or cited by other papers using tools like google scholar, etc.)

- 1. Reinforcement learning, computational complexity, and computational-statistical gaps. See for example the recent paper https://arxiv.org/pdf/2404.03774 and several previous works discussed in related work.
- 2. Partially Observable MDPs. See for example the recent papers https://arxiv.org/abs/2206.03446, https://arxiv.org/abs/2307.02884, and lots of previous work, for example as discussed there.
- 3. Various types of robustness questions in RL, Control Theory, etc. As phrased this includes a extremely massive literature. See https://skoge.folk.ntnu.no/puublications_others/1978_doyle_margins-lqg-there-are-none.pdf for an interesting classic paper in control theory. (See also H^{∞} control, etc.)
- 4. RL theory with function approximation: statistical and computational considerations. Another massive literature. See e.g. https://arxiv.org/pdf/2406.11640, https://proceedings.mlr.press/v162/zhang22aa/zhang22aa.pdf, https://www.jmlr.org/papers/volume25/22-0687/22-0687.pdf, https://arxiv.org/pdf/2112.14195, https://arxiv.org/abs/2102.02049, for a few recent papers with some pointers to some subset of the literature...

- 5. Multiagent RL, another massive literature... https://arxiv.org/pdf/2006.12007, ...
- 6. Pessimism and Offline RL... https://arxiv.org/abs/2205.10671, https://arxiv.org/abs/2012.15085, https://yuxinchen2020.github.io/publications/Pessimistic_Qlearning_ICML.pdf, https://arxiv.org/abs/2106.06926, ...
- 7. Imitation learning, learning from demonstrations, etc. Some arbitrarily chosen recent works: https://arxiv.org/pdf/2307.14619, https://arxiv.org/abs/2407.15007v1, https://arxiv.org/abs/2312.00054,...
- 8. Thompson sampling for bandits and related ideas in RL. See e.g. https://arxiv.org/abs/1611.06534, https://arxiv.org/pdf/1906.02870, https://arxiv.org/pdf/2308.07843.
- 9. *ϵ*-Greedy strategies in bandits and RL. E.g. https://arxiv.org/pdf/2206.09421, lecture notes https://arxiv.org/pdf/2312.16730, ...
- 10. Decision-Estimation coefficient, information-theoretic ideas in RL theory. Relevant lecture notes https://arxiv.org/pdf/2312.16730, an example recent work https://arxiv.org/abs/2209.11745,...
- 11. Connections between martingales and online learning. E.g. https://arxiv.org/pdf/1803.07617,...
- 12. Actor-critic, policy gradient, etc related theory... https://epubs.siam.org/doi/full/10. 1137/23M1560215, https://arxiv.org/pdf/2110.11280, ...
- 13. RL algorithms for fine-tuning LLMs, with RLHF [OWJ⁺22] and DPO [RSM⁺24] as main representatives, and numerous papers citing these two.
- 14. Adversarial bandits [ACBFS02], which has an extensive literature as well easiest way will be look at highly-cited follow-up papers that cited [ACBFS02].
- 15. Multi-agent bandit learning, and convergence to equilibrium.
 - There is an extensive literature on this frontier for zero-sum games [PP16, MJS19], congestion games [CXFD22], dominance-elimination solvable games [WXY22, WKBJ22], monotone games [COZ22]. However, many problems remain open. For example, the regret bound of [CXFD22] leaves significant room for improvement. An interesting open problem from [WXY22] is whether there exists a no-regret learning algorithm that provably converges to rationalizable equilibrium in two-player games.
- 16. Decisions + Languages, with applications to solving real games such as *Diplomacy* [FBB⁺22], or by letting language agents to debate in order to arrive at better reasoning capabilities [DVJ⁺24]

References

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 - [COZ22] Yang Cai, Argyris Oikonomou, and Weiqiang Zheng. Finite-time last-iterate convergence for learning in multi-player games. *Advances in Neural Information Processing Systems*, 35:33904–33919, 2022.

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- [DVJ⁺24] Tim R Davidson, Veniamin Veselovsky, Martin Josifoski, Maxime Peyrard, Antoine Bosselut, Michal Kosinski, and Robert West. Evaluating language model agency through negotiations. arXiv preprint arXiv:2401.04536, 2024.
- [FBB⁺22] Meta Fundamental AI Research Diplomacy Team (FAIR)†, Anton Bakhtin, Noam Brown, Emily Dinan, Gabriele Farina, Colin Flaherty, Daniel Fried, Andrew Goff, Jonathan Gray, Hengyuan Hu, et al. Human-level play in the game of diplomacy by combining language models with strategic reasoning. *Science*, 378(6624):1067–1074, 2022.
 - [MJS19] Eric V Mazumdar, Michael I Jordan, and S Shankar Sastry. On finding local nash equilibria (and only local nash equilibria) in zero-sum games. *arXiv preprint arXiv:1901.00838*, 2019.
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