Rodriguez_Felipe_DSC680_Milestone3_Code

May 5, 2024

```
[140]: import pandas as pd
       import matplotlib.pyplot as plt
[141]: df = pd.read_csv('london_weather.csv')
[142]: df.head()
[142]:
                    cloud_cover sunshine global_radiation max_temp mean_temp \
              date
       0 19790101
                            2.0
                                      7.0
                                                        52.0
                                                                   2.3
                                                                              -4.1
       1 19790102
                            6.0
                                      1.7
                                                        27.0
                                                                   1.6
                                                                             -2.6
       2 19790103
                            5.0
                                      0.0
                                                        13.0
                                                                   1.3
                                                                             -2.8
       3 19790104
                            8.0
                                      0.0
                                                        13.0
                                                                  -0.3
                                                                             -2.6
       4 19790105
                            6.0
                                      2.0
                                                        29.0
                                                                   5.6
                                                                             -0.8
                   precipitation pressure
                                              snow_depth
          min_temp
       0
              -7.5
                              0.4 101900.0
                                                     9.0
                              0.0 102530.0
              -7.5
                                                     8.0
       1
       2
              -7.2
                              0.0 102050.0
                                                     4.0
       3
              -6.5
                              0.0 100840.0
                                                     2.0
              -1.4
                              0.0 102250.0
                                                     1.0
  [5]: df.dtypes
  [5]: date
                             int64
       cloud_cover
                           float64
                           float64
       sunshine
                           float64
       global_radiation
      max_temp
                           float64
      mean_temp
                           float64
      min_temp
                           float64
      precipitation
                           float64
       pressure
                           float64
       snow_depth
                           float64
       dtype: object
[132]: description = {
           'date': 'Date of record in YYYYMMDD Format',
```

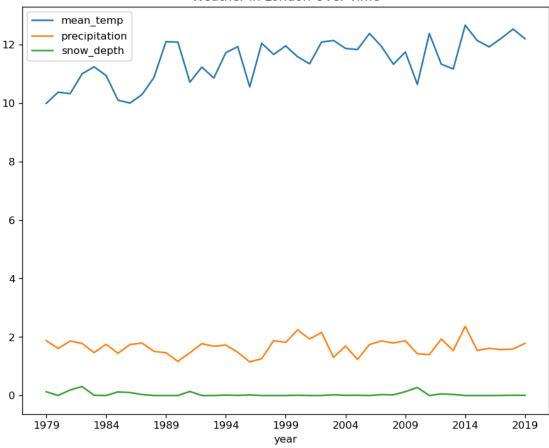
```
'cloud_cover': 'Cloud cover measurement in oktas',
    'sunshine': 'Sunshine measure in hours',
    'global_radiation': 'Irradiance measurement in Watt per square meter (W/
 \hookrightarrowm2)',
    'max_temp': 'Maximum temperature recorded in degrees Celsius (°C)',
    'mean temp': 'Mean temperature recorded in degrees Celsius (°C)',
    'min_temp': 'Min temperature recorded in degrees Celsius (°C)',
    'precipitation': 'Precipitation measurement in millimeters (mm)',
    'pressure': 'Pressure measurement in Pascals (Pa)',
    'snow_depth': 'Snow depth measurement in centimeters (cm)'
# Initialize an empty dictionary to store data types
dtype_dict = {}
# Iterate through each column and store its data type in the dictionary
for col in df.columns:
    dtype_dict[col] = str(df[col].dtype)
series1 = pd.Series(description, name='description')
series1 = series1.rename_axis('column')
series2 = pd.Series(dtype dict, name='data type')
series2 = series2.rename axis('column')
# Combining the Series into a DataFrame using pd.merge()
data_dictionary = pd.merge(series1, series2, left_index=True, right_index=True)
print('Data Dictionary\n')
print(data_dictionary.to_markdown())
```

Data Dictionary

```
1
column
                 | description
data_type |
|:-----|:----|:-----|:-----|:----|:--
----|
date
                 | Date of record in YYYYMMDD Format
object
| cloud_cover
                 | Cloud cover measurement in oktas
float64
sunshine
                 | Sunshine measure in hours
float64
| global_radiation | Irradiance measurement in Watt per square meter (W/m2) |
float64
| max_temp
                 | Maximum temperature recorded in degrees Celsius (°C)
float64
                 | Mean temperature recorded in degrees Celsius (°C)
| mean_temp
```

```
float64
      | min_temp
                         | Min temperature recorded in degrees Celsius (°C)
                                                                                  1
      float64
      | precipitation
                         | Precipitation measurement in millimeters (mm)
      float64
      pressure
                         | Pressure measurement in Pascals (Pa)
      float64
                         | Snow depth measurement in centimeters (cm)
      | snow depth
                                                                                  float64
[149]: df['date'] = df['date'].astype(str)
      df['year'] = df['date'].str[0:4]
      df['month'] = df['date'].str[4:6]
      df['day'] = df['date'].str[6:]
      df.head()
[149]:
                   cloud_cover sunshine global_radiation max_temp
             date
                                                                      mean_temp \
                           2.0
                                     7.0
                                                       52.0
                                                                  2.3
                                                                            -4.1
      0 19790101
                           6.0
                                     1.7
                                                       27.0
                                                                            -2.6
      1 19790102
                                                                  1.6
      2 19790103
                           5.0
                                     0.0
                                                       13.0
                                                                  1.3
                                                                            -2.8
      3 19790104
                           8.0
                                     0.0
                                                       13.0
                                                                 -0.3
                                                                            -2.6
      4 19790105
                           6.0
                                     2.0
                                                       29.0
                                                                 5.6
                                                                            -0.8
         min_temp precipitation pressure snow_depth year month day
      0
             -7.5
                             0.4 101900.0
                                                    9.0 1979
                                                                 01 01
             -7.5
                             0.0 102530.0
      1
                                                    8.0 1979
                                                                 01 02
             -7.2
                             0.0 102050.0
                                                    4.0 1979
                                                                 01 03
      3
             -6.5
                             0.0 100840.0
                                                    2.0 1979
                                                                 01 04
             -1.4
                             0.0 102250.0
                                                    1.0 1979
                                                                 01 05
[16]: averages = df.groupby('year')[['mean_temp', 'precipitation', 'snow_depth']].
        →mean()
      averages.head()
[16]:
            mean_temp precipitation snow_depth
      year
      1979
             9.986575
                             1.875890
                                         0.128767
      1980 10.370492
                             1.606831
                                         0.000000
      1981 10.320000
                             1.861918
                                         0.189041
      1982 10.998904
                             1.780274
                                         0.306849
      1983 11.237260
                             1.465753
                                         0.008219
[133]: averages.plot()
      plt.title('Weather in London Over Time')
      plt.show()
```





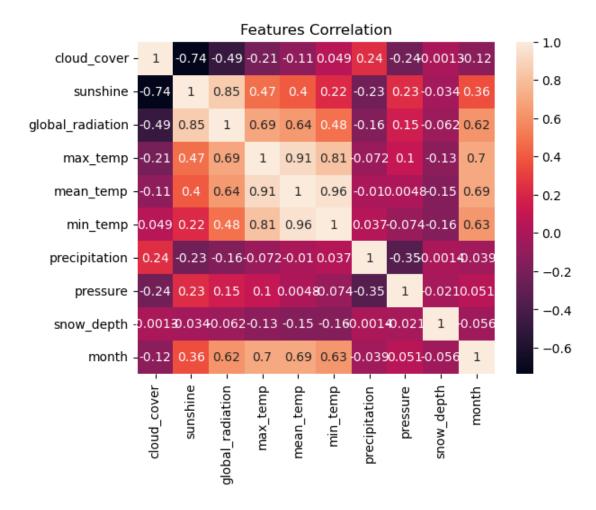
```
[28]: import seaborn as sns

[36]: df_num = df.drop(columns=['date', 'year', 'day'])

[37]: corr = df_num.corr()

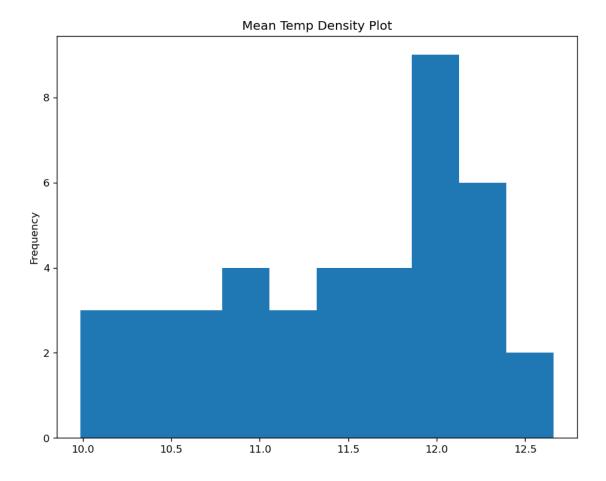
[38]: sns.heatmap(corr, annot=True)
    plt.title('Features Correlation')

[38]: Text(0.5, 1.0, 'Features Correlation')
```



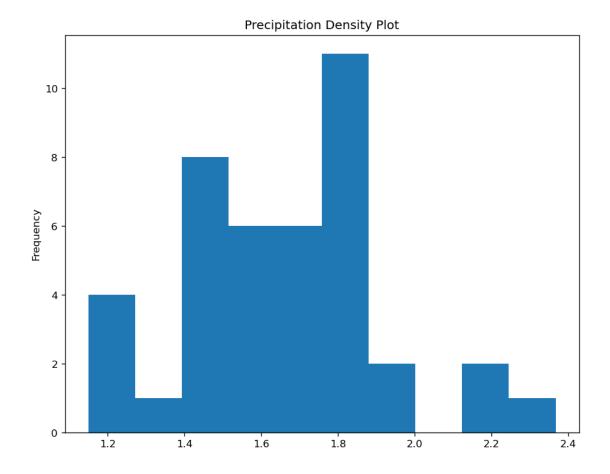
```
[134]: averages['mean_temp'].plot(kind='hist')
plt.title('Mean Temp Density Plot')
```

[134]: Text(0.5, 1.0, 'Mean Temp Density Plot')



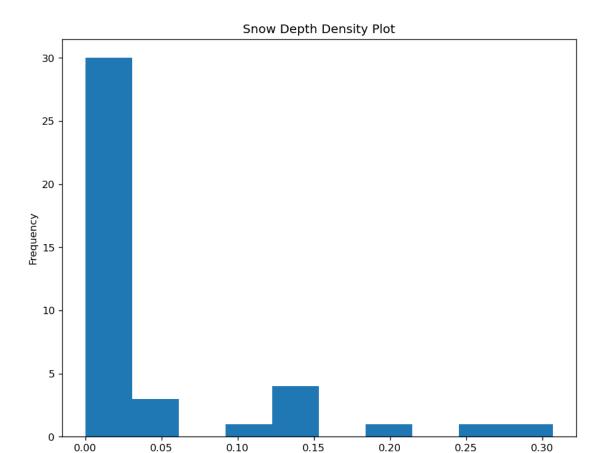
```
[135]: averages['precipitation'].plot(kind='hist')
plt.title('Precipitation Density Plot')
```

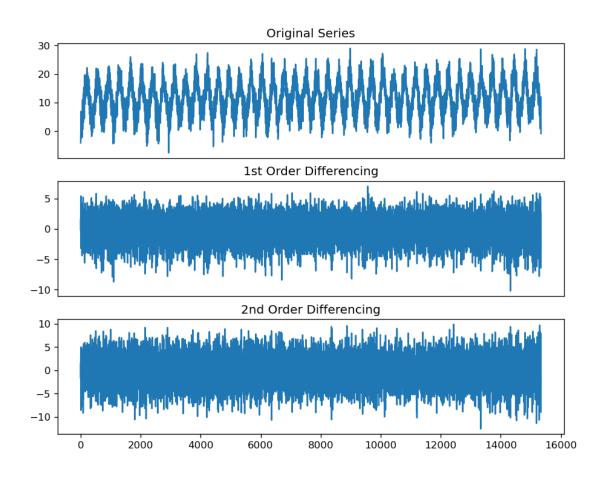
[135]: Text(0.5, 1.0, 'Precipitation Density Plot')



```
[136]: averages['snow_depth'].plot(kind='hist')
plt.title('Snow Depth Density Plot')
```

[136]: Text(0.5, 1.0, 'Snow Depth Density Plot')



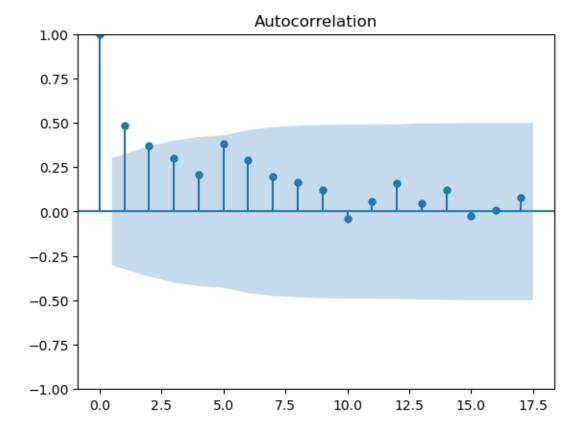


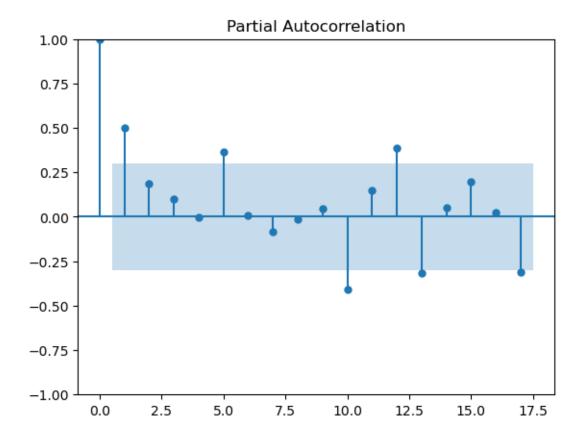
```
[66]: from statsmodels.tsa.stattools import adfuller
[68]: adf_test = adfuller(averages['mean_temp'])
    # Output the results
    print('ADF Statistic: %f' % adf_test[0])
    print('p-value: %f' % adf_test[1])

ADF Statistic: -3.584279
    p-value: 0.006069
[55]: from statsmodels.tsa.arima.model import ARIMA
    from statsmodels.graphics.tsaplots import plot_acf, plot_pacf
[65]: plot_acf(averages['mean_temp'])
    plot_pacf(averages['mean_temp'])
    plot_show()
```

/Users/feliperodriguez/opt/anaconda3/lib/python3.9/sitepackages/statsmodels/graphics/tsaplots.py:348: FutureWarning: The default method 'yw' can produce PACF values outside of the [-1,1] interval. After 0.13, the default will change to unadjusted Yule-Walker ('ywm'). You can use this method now by setting method='ywm'.

warnings.warn(





```
[75]: model = ARIMA(averages['mean_temp'], order = (1,1,1))
model_fit = model.fit()
model_fit.summary()
```

/Users/feliperodriguez/opt/anaconda3/lib/python3.9/sitepackages/statsmodels/tsa/base/tsa_model.py:471: ValueWarning: No frequency information was provided, so inferred frequency AS-JAN will be used. self. init dates(dates, freq)

/Users/feliperodriguez/opt/anaconda3/lib/python3.9/site-packages/statsmodels/tsa/base/tsa_model.py:471: ValueWarning: No frequency information was provided, so inferred frequency AS-JAN will be used.

self._init_dates(dates, freq)

/Users/feliperodriguez/opt/anaconda3/lib/python3.9/sitepackages/statsmodels/tsa/base/tsa_model.py:471: ValueWarning: No frequency information was provided, so inferred frequency AS-JAN will be used. self._init_dates(dates, freq)

[75]: <class 'statsmodels.iolib.summary.Summary'>

SARIMAX Results

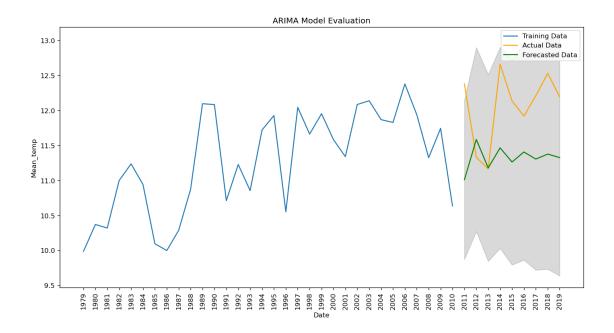
```
Dep. Variable:
                             mean_temp No. Observations:
                                                                     42
                        ARIMA(1, 1, 1) Log Likelihood
                                                                -37.917
     Model:
                     Sun, 21 Apr 2024 AIC
     Date:
                                                                  81.833
     Time:
                              11:39:51 BIC
                                                                  86.974
                           01-01-1979 HQIC
                                                                  83.705
     Sample:
                          - 01-01-2020
     Covariance Type:
     ______
                   coef std err
                                              P>|z|
                                                       Γ0.025
                                                                  0.9751
     ar.L1
                 0.0961
                         0.243
                                    0.396 0.692
                                                       -0.380
                                                                  0.573
     ma.L1
                -0.7352
                           0.204
                                    -3.598
                                             0.000
                                                       -1.136
                                                                  -0.335
                0.3664
     sigma2
                          0.090 4.077
                                              0.000
                                                        0.190
                                                                  0.543
     ______
     Ljung-Box (L1) (Q):
                                     0.31 Jarque-Bera (JB):
     0.12
     Prob(Q):
                                     0.58
                                          Prob(JB):
     0.94
     Heteroskedasticity (H):
                                     0.88
                                           Skew:
     Prob(H) (two-sided):
                            0.82
                                          Kurtosis:
     2.76
     Warnings:
     [1] Covariance matrix calculated using the outer product of gradients (complex-
     step).
     11 11 11
[104]: from sklearn.metrics import mean_squared_error
     # Split the data into train and test
     train_size = int(len(averages) * 0.8)
     train, test = averages[0:train_size], averages[train_size:len(averages)]
     # Fit the ARIMA model on the training dataset
     model_train = ARIMA(train['mean_temp'], order=(1, 1, 2))
     model_train_fit = model_train.fit()
     # Forecast on the test dataset
     test_forecast = model_train_fit.get_forecast(steps=len(test))
     test_forecast_series = pd.Series(test_forecast.predicted_mean, index=test.index)
```

mse = mean_squared_error(test['mean_temp'], test_forecast_series)

Calculate the mean squared error

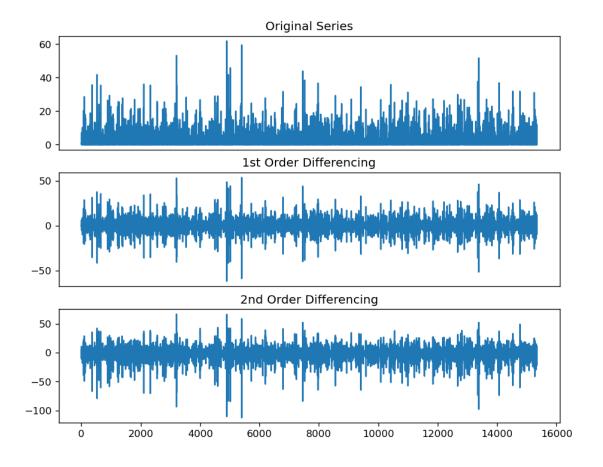
```
rmse = mse**0.5
# Create a plot to compare the forecast with the actual test data
plt.figure(figsize=(14,7))
plt.plot(train['mean_temp'], label='Training Data')
plt.plot(test['mean_temp'], label='Actual Data', color='orange')
plt.plot(test_forecast_series, label='Forecasted Data', color='green')
plt.fill_between(test.index,
                 test forecast.conf int().iloc[:, 0],
                 test_forecast.conf_int().iloc[:, 1],
                 color='k', alpha=.15)
plt.title('Mean Temp ARIMA Model Evaluation')
plt.xlabel('Date')
plt.xticks(rotation='vertical')
plt.ylabel('Mean_temp')
plt.legend()
plt.show()
print('RMSE:', rmse)
```

```
/Users/feliperodriguez/opt/anaconda3/lib/python3.9/site-
packages/statsmodels/tsa/base/tsa_model.py:471: ValueWarning: No frequency
information was provided, so inferred frequency AS-JAN will be used.
    self._init_dates(dates, freq)
/Users/feliperodriguez/opt/anaconda3/lib/python3.9/site-
packages/statsmodels/tsa/base/tsa_model.py:471: ValueWarning: No frequency
information was provided, so inferred frequency AS-JAN will be used.
    self._init_dates(dates, freq)
/Users/feliperodriguez/opt/anaconda3/lib/python3.9/site-
packages/statsmodels/tsa/base/tsa_model.py:471: ValueWarning: No frequency
information was provided, so inferred frequency AS-JAN will be used.
    self._init_dates(dates, freq)
```



RMSE: 0.9002148303139442

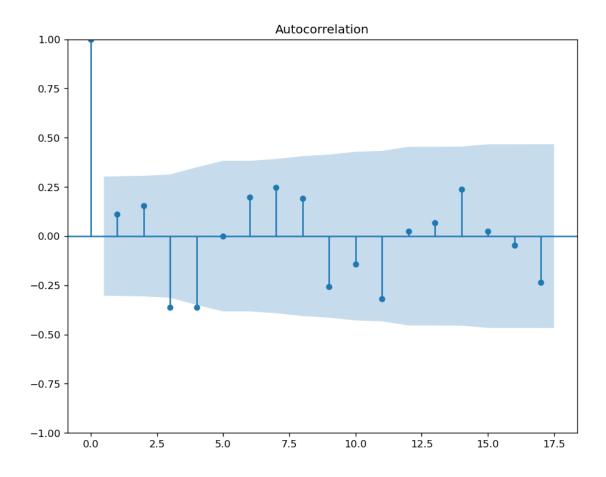
Precipitation

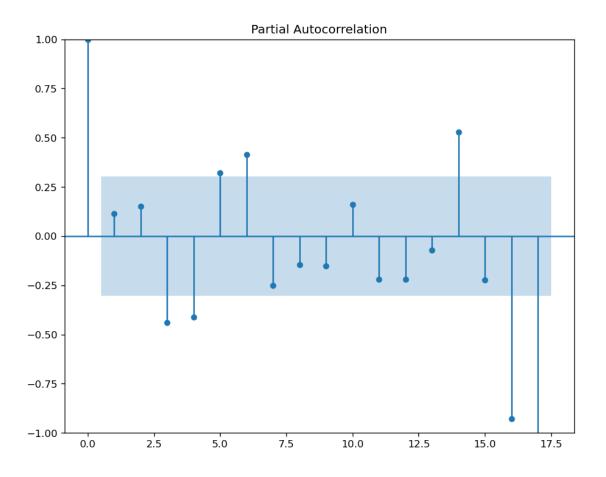


```
[86]: plot_acf(averages['precipitation'])
    plot_pacf(averages['precipitation'])
    plt.show()
```

/Users/feliperodriguez/opt/anaconda3/lib/python3.9/site-packages/statsmodels/graphics/tsaplots.py:348: FutureWarning: The default method 'yw' can produce PACF values outside of the [-1,1] interval. After 0.13, the default will change tounadjusted Yule-Walker ('ywm'). You can use this method now by setting method='ywm'.

warnings.warn(

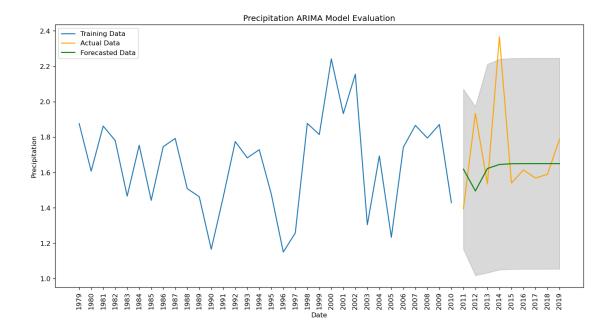




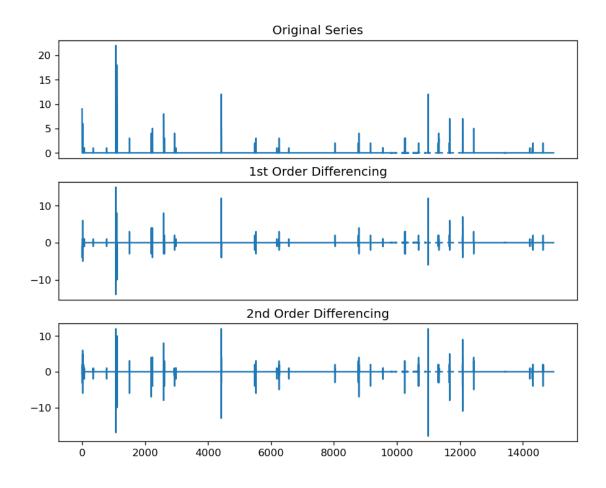
```
[138]: # Split the data into train and test
       train_size = int(len(averages) * 0.8)
       train, test = averages[0:train_size], averages[train_size:len(averages)]
       # Fit the ARIMA model on the training dataset
       model_train = ARIMA(train['precipitation'], order=(1, 1, 3))
       model_train_fit = model_train.fit()
       # Forecast on the test dataset
       test_forecast = model_train_fit.get_forecast(steps=len(test))
       test_forecast_series = pd.Series(test_forecast.predicted_mean, index=test.index)
       # Calculate the mean squared error
       mse = mean_squared_error(test['precipitation'], test_forecast_series)
       rmse = mse**0.5
       # Create a plot to compare the forecast with the actual test data
       plt.figure(figsize=(14,7))
       plt.plot(train['precipitation'], label='Training Data')
       plt.plot(test['precipitation'], label='Actual Data', color='orange')
```

```
plt.plot(test_forecast_series, label='Forecasted Data', color='green')
plt.fill_between(test.index,
                 test_forecast.conf_int().iloc[:, 0],
                 test_forecast.conf_int().iloc[:, 1],
                 color='k', alpha=.15)
plt.title('Precipitation ARIMA Model Evaluation')
plt.xlabel('Date')
plt.xticks(rotation='vertical')
plt.ylabel('Precipitation')
plt.legend()
plt.show()
print('RMSE:', rmse)
/Users/feliperodriguez/opt/anaconda3/lib/python3.9/site-
packages/statsmodels/tsa/base/tsa_model.py:471: ValueWarning: No frequency
information was provided, so inferred frequency AS-JAN will be used.
  self._init_dates(dates, freq)
/Users/feliperodriguez/opt/anaconda3/lib/python3.9/site-
packages/statsmodels/tsa/base/tsa model.py:471: ValueWarning: No frequency
information was provided, so inferred frequency AS-JAN will be used.
  self._init_dates(dates, freq)
/Users/feliperodriguez/opt/anaconda3/lib/python3.9/site-
packages/statsmodels/tsa/base/tsa_model.py:471: ValueWarning: No frequency
information was provided, so inferred frequency AS-JAN will be used.
  self. init dates(dates, freq)
/Users/feliperodriguez/opt/anaconda3/lib/python3.9/site-
packages/statsmodels/tsa/statespace/sarimax.py:978: UserWarning: Non-invertible
starting MA parameters found. Using zeros as starting parameters.
  warn('Non-invertible starting MA parameters found.'
/Users/feliperodriguez/opt/anaconda3/lib/python3.9/site-
packages/statsmodels/base/model.py:604: ConvergenceWarning: Maximum Likelihood
optimization failed to converge. Check mle_retvals
```

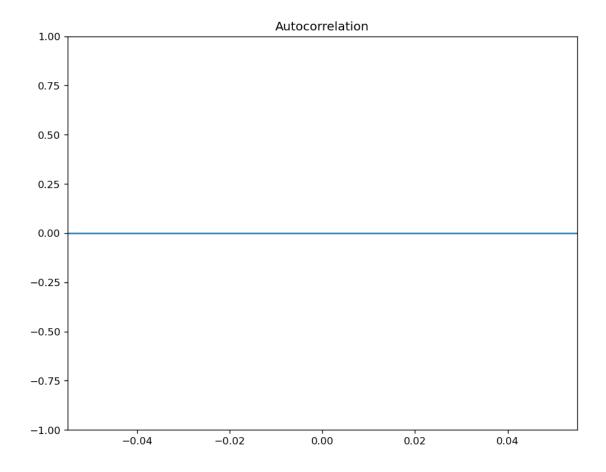
warnings.warn("Maximum Likelihood optimization failed to "

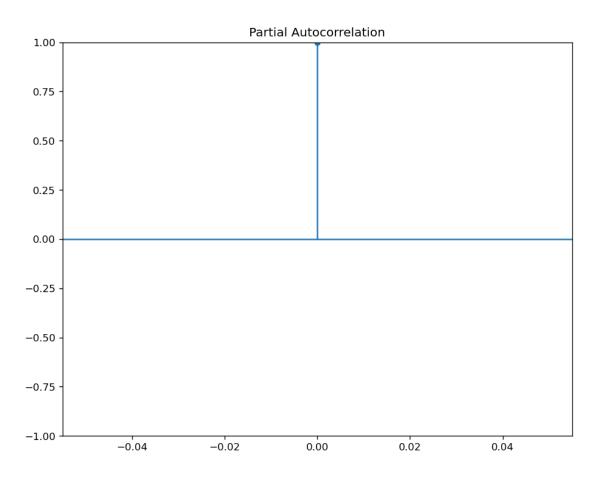


RMSE: 0.300663266736998



```
[95]: plot_acf(averages['snow_depth'])
  plot_pacf(averages['snow_depth'])
  plt.show()
```





```
[97]: averages = averages.dropna()

[139]: # Split the data into train and test
    train_size = int(len(averages) * 0.8)
    train, test = averages[0:train_size], averages[train_size:len(averages)]

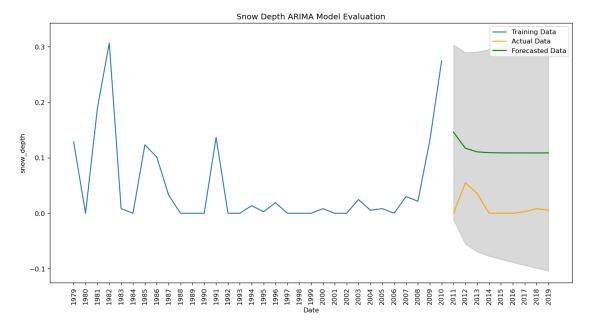
# Fit the ARIMA model on the training dataset
    model_train = ARIMA(train['snow_depth'], order=(1, 1, 1))
    model_train_fit = model_train.fit()

# Forecast on the test dataset
    test_forecast = model_train_fit.get_forecast(steps=len(test))
    test_forecast_series = pd.Series(test_forecast.predicted_mean, index=test.index)

# Calculate the mean squared error
    mse = mean_squared_error(test['snow_depth'], test_forecast_series)
    rmse = mse**0.5

# Create a plot to compare the forecast with the actual test data
    plt.figure(figsize=(14,7))
```

/Users/feliperodriguez/opt/anaconda3/lib/python3.9/sitepackages/statsmodels/tsa/base/tsa_model.py:471: ValueWarning: No frequency
information was provided, so inferred frequency AS-JAN will be used.
 self._init_dates(dates, freq)
/Users/feliperodriguez/opt/anaconda3/lib/python3.9/sitepackages/statsmodels/tsa/base/tsa_model.py:471: ValueWarning: No frequency
information was provided, so inferred frequency AS-JAN will be used.
 self._init_dates(dates, freq)
/Users/feliperodriguez/opt/anaconda3/lib/python3.9/sitepackages/statsmodels/tsa/base/tsa_model.py:471: ValueWarning: No frequency
information was provided, so inferred frequency AS-JAN will be used.
 self._init_dates(dates, freq)



RMSE: 0.10456593039572244

SARIMA Model

```
[137]: from statsmodels.tsa.statespace.sarimax import SARIMAX
       # Split the data into train and test
       train_size = int(len(averages) * 0.8)
       train, test = averages[0:train_size], averages[train_size:len(averages)]
       # Fit the SARIMA model on the training dataset
       model_train = SARIMAX(train['precipitation'], order=(1, 1, 2),
        \Rightarrowseasonal_order=(1, 1, 2, 12))
       model_train_fit = model_train.fit()
       # Forecast on the test dataset
       test forecast = model train fit.get forecast(steps=len(test))
       test_forecast_series = pd.Series(test_forecast.predicted_mean, index=test.index)
       # Calculate the mean squared error
       mse = mean_squared_error(test['precipitation'], test_forecast_series)
       rmse = mse**0.5
       # Create a plot to compare the forecast with the actual test data
       plt.figure(figsize=(14,7))
       plt.plot(train['precipitation'], label='Training Data')
       plt.plot(test['precipitation'], label='Actual Data', color='orange')
       plt.plot(test_forecast_series, label='Forecasted Data', color='green')
       plt.fill_between(test.index,
                        test_forecast.conf_int().iloc[:, 0],
                        test_forecast.conf_int().iloc[:, 1],
                        color='k', alpha=.15)
       plt.title('Precipitation SARIMA Model Evaluation')
       plt.xlabel('Date')
       plt.xticks(rotation='vertical')
       plt.ylabel('Precipitation')
       plt.legend()
       plt.show()
       print('RMSE:', rmse)
```

```
/Users/feliperodriguez/opt/anaconda3/lib/python3.9/site-
packages/statsmodels/tsa/base/tsa_model.py:471: ValueWarning: No frequency
information was provided, so inferred frequency AS-JAN will be used.
self._init_dates(dates, freq)
/Users/feliperodriguez/opt/anaconda3/lib/python3.9/site-
packages/statsmodels/tsa/base/tsa_model.py:471: ValueWarning: No frequency
```

information was provided, so inferred frequency AS-JAN will be used.
 self._init_dates(dates, freq)

/Users/feliperodriguez/opt/anaconda3/lib/python3.9/site-packages/statsmodels/tsa/statespace/sarimax.py:866: UserWarning: Too few

observations to estimate starting parameters for seasonal ARMA. All parameters except for variances will be set to zeros.

warn('Too few observations to estimate starting parameters%s.' This problem is unconstrained.

RUNNING THE L-BFGS-B CODE

* * *

Machine precision = 2.220D-16N = 7 M = 10

At XO 0 variables are exactly at the bounds

At iterate f= 4.19743D-01 |proj g|= 2.56820D-01 At iterate |proj g|= 6.07192D-02 5 f= 3.80875D-01 At iterate 10 f= 3.75655D-01 |proj g| = 2.63465D-02f= 3.68063D-01 |proj g|= 2.14258D-02 At iterate 15 |proj g|= 1.76635D-03 At iterate f= 3.62500D-01 20 |proj g|= 3.86149D-03 At iterate 25 f= 3.62407D-01 |proj g|= 1.27176D-03 At iterate 30 f= 3.62359D-01 At iterate f= 3.62347D-01 |proj g|= 8.71139D-04 35 At iterate f= 3.62346D-01 |proj g| = 3.71540D-0440

* * *

Tit = total number of iterations

Tnf = total number of function evaluations

Tnint = total number of segments explored during Cauchy searches

Skip = number of BFGS updates skipped

Nact = number of active bounds at final generalized Cauchy point

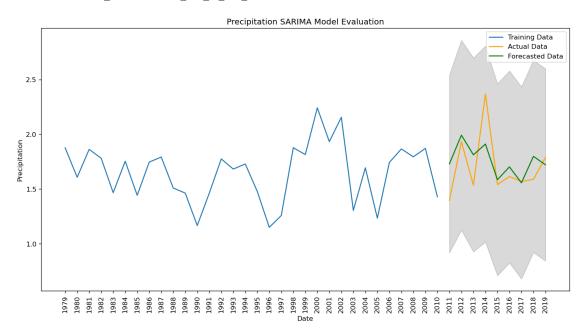
Projg = norm of the final projected gradient

F = final function value

* * *

```
N Tit Tnf Tnint Skip Nact Projg F
7 44 59 1 0 0 4.092D-05 3.623D-01
F = 0.36234568679425577
```

CONVERGENCE: REL_REDUCTION_OF_F_<=_FACTR*EPSMCH



RMSE: 0.22582083286525856

```
[128]: # Split the data into train and test
    train_size = int(len(averages) * 0.8)
    train, test = averages[0:train_size], averages[train_size:len(averages)]

# Fit the SARIMA model on the training dataset
    model_train = SARIMAX(train['snow_depth'], order=(1, 1, 1), seasonal_order=(1, 1, 1, 12))
    model_train_fit = model_train.fit()

# Forecast on the test dataset
    test_forecast = model_train_fit.get_forecast(steps=len(test))
    test_forecast_series = pd.Series(test_forecast.predicted_mean, index=test.index)

# Calculate the mean squared error
    mse = mean_squared_error(test['snow_depth'], test_forecast_series)
    rmse = mse**0.5

# Create a plot to compare the forecast with the actual test data
    plt.figure(figsize=(14,7))
```

```
plt.plot(train['snow_depth'], label='Training Data')
plt.plot(test['snow_depth'], label='Actual Data', color='orange')
plt.plot(test_forecast_series, label='Forecasted Data', color='green')
plt.fill_between(test.index,
                 test_forecast.conf_int().iloc[:, 0],
                 test_forecast.conf_int().iloc[:, 1],
                 color='k', alpha=.15)
plt.title('Snow Depth SARIMA Model Evaluation')
plt.xlabel('Date')
plt.xticks(rotation='vertical')
plt.ylabel('Snow Depth')
plt.legend()
plt.show()
print('RMSE:', rmse)
/Users/feliperodriguez/opt/anaconda3/lib/python3.9/site-
packages/statsmodels/tsa/base/tsa_model.py:471: ValueWarning: No frequency
information was provided, so inferred frequency AS-JAN will be used.
  self._init_dates(dates, freq)
/Users/feliperodriguez/opt/anaconda3/lib/python3.9/site-
packages/statsmodels/tsa/base/tsa model.py:471: ValueWarning: No frequency
information was provided, so inferred frequency AS-JAN will be used.
  self._init_dates(dates, freq)
/Users/feliperodriguez/opt/anaconda3/lib/python3.9/site-
packages/statsmodels/tsa/statespace/sarimax.py:866: UserWarning: Too few
observations to estimate starting parameters for seasonal ARMA. All parameters
except for variances will be set to zeros.
  warn('Too few observations to estimate starting parameters%s.'
This problem is unconstrained.
RUNNING THE L-BFGS-B CODE
Machine precision = 2.220D-16
N =
                5
                      M =
                                    10
At XO
              O variables are exactly at the bounds
At iterate
                   f = -4.34994D - 01
                                      |proj g| = 4.65547D+00
At iterate
             5
                   f = -4.80322D - 01
                                      |proj g|= 4.85228D-02
At iterate
                   f= -4.85501D-01
             10
                                     |proj g|= 1.62895D-01
```

|proj g| = 6.74680D-02

f = -5.04503D - 01

At iterate 15

At iterate 20 f= -5.04561D-01 |proj g|= 3.95180D-03At iterate 25 f= -5.04564D-01 |proj g|= 2.54990D-03

* * *

Tit = total number of iterations

Tnf = total number of function evaluations

Tnint = total number of segments explored during Cauchy searches

Skip = number of BFGS updates skipped

Nact = number of active bounds at final generalized Cauchy point

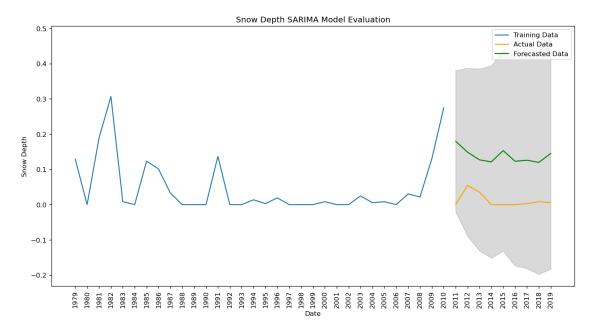
Projg = norm of the final projected gradient

F = final function value

* * *

N Tit Tnf Tnint Skip Nact Projg F 5 28 37 1 0 0 6.758D-04 -5.046D-01 F = -0.50456421413981323

CONVERGENCE: REL_REDUCTION_OF_F_<=_FACTR*EPSMCH



RMSE: 0.12910089674446118