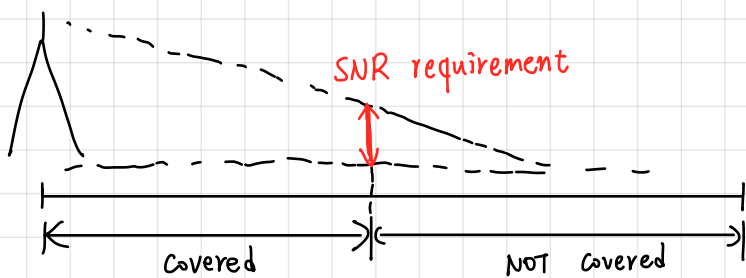


Wireless Communication Ch3

Link Budget

- Wireless system are required to provide certain minimum transmission quality at R_x
- This is usually measured by signal-to-noise ratio (SNR)
- When users move away from the BS/Tx, the SNR change and might NOT achieve the requirement
- If the case is that the interference is NOT an issue, the performance is limited by the noise power level, → called noise-limited system



- Link budget is a way to do a quick approximation of link quality and system capacity

• Key factor

T_x

- Transmission power (P_{Tx})
- Transmit antenna gain (G_{Tx})
- Radio frequency loss at T_x (L) (EIRP)

→ called equivalent isotropically radiated power

- Path loss ($PL(d)$)

R_x

- Fading margin
- Receive antenna gain (G_{Rx})
- Noise power level
 - Thermal noise
 - Receive noise

Definition of dBm and dBW

- Suppose we have P mW

⇒ equivalent to $10 \log_{10} \left(\frac{P}{1 \text{ mW}} \right)$ dBm

Ex.

$$1 \text{ mW} \longleftrightarrow 0 \text{ dBm}$$

$$10 \text{ mW} \longleftrightarrow 10 \text{ dBm}$$

$$10^3 \text{ mW} \longleftrightarrow 30 \text{ dBm}$$

- Suppose we have P W

⇒ equivalent to $10 \log_{10} \left(\frac{P}{1 \text{ W}} \right)$ dBW

Ex.

$$20 \text{ W} \longleftrightarrow 13 \text{ dBW} \longleftrightarrow 43 \text{ dBm}$$

$$40 \text{ W} \longleftrightarrow 16 \text{ dBW} \longleftrightarrow 46 \text{ dBm}$$

Pathloss model

$$P_{RX} = P_{RX}(d_{break}) \cdot \left(\frac{d}{d_{break}}\right)^{-n}$$

$$P_{RX, dB} = P_{RX, dB}(d_{break}) - 10n \log_{10}\left(\frac{d}{d_{break}}\right)$$

$$P_{RX}(d_{break}) = P_{TX} \cdot G_{TX} \cdot G_{RX} \left(\frac{\lambda_c}{4\pi d_{break}}\right)^2$$

$$P_{RX, dB}(d_{break}) = P_{TX, dB} + G_{TX, dB} + G_{RX, dB} + 20 \log_{10}\left(\frac{\lambda_c}{4\pi d_{break}}\right)$$

$$\rightarrow P_{RX, dB}(d) = P_{TX, dB} + G_{TX, dB} + G_{RX, dB} - 20 \log_{10}\frac{4\pi}{\lambda_c} - 20 \log_{10}(d_{break}) - 10n \log_{10}\left(\frac{d}{d_{break}}\right)$$

$$\text{Pathloss model: } PL(d) = 20 \log_{10}\frac{4\pi}{\lambda_c} + 20 \log_{10} d_{break} + 10n \log_{10}\frac{d}{d_{break}}$$

NOTE:

If $d_{break} = 1\text{m}$ and let $f_c = 1\text{GHz}$, then

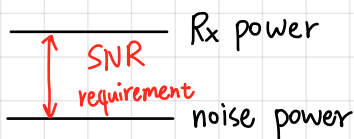
$$20 \log_{10}\left(\frac{4\pi}{\lambda_c}\right) \approx \underline{\underline{32\text{dB}}}$$

Fading margin

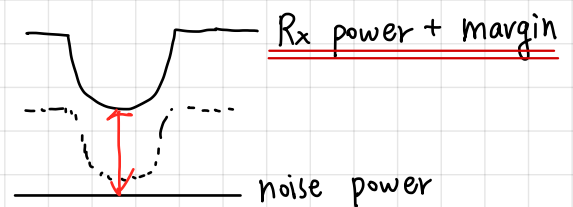
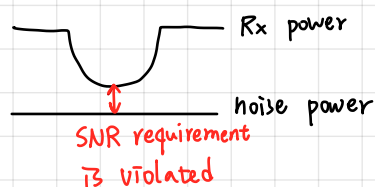
- 在傳播時可能受到 fading 影響, 為了確保在 fading 下仍可接收信號

→ 會在 RX 處加上 fading margin

• No fading



• With fading



Thermal Noise

$$P_n = k_B T_e \cdot B$$

- B : Bandwidth at Rx (in Hz)
- k_B : 1.38×10^{-23} J/K (Boltzmann's constant)
- T_e : environment temperature (in K)
- $N_0 = k_B T_e$: noise power density (W/Hz)

Ex.

if $T_e = 300\text{K}$. then

$$N_0 = -174 \text{ dBm/Hz}$$

$$\Rightarrow P_{n, \text{dB}} = \underline{-174 + 10 \log_{10}(B)}$$

Receive noise

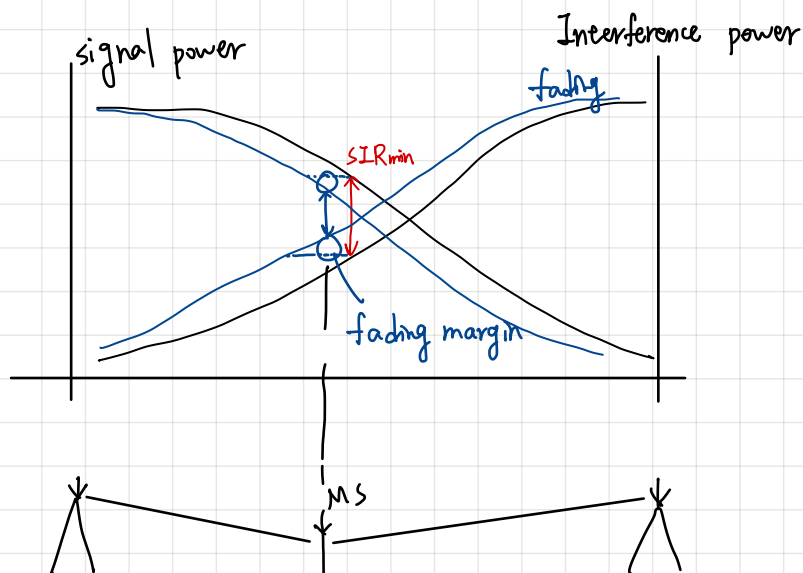
→ 會放大雜訊, 因此須要先把 input SNR 乘 F 倍

$$F = \frac{\text{SNR at Rx input}}{\text{SNR at Rx output}}$$

- The amplifier and mixer at Rx are noisy
- This increase the noise power. such effect is in general described by noise figure F

Interference - limited system

- The major issue is the interference
- We look at the signal-to-interference ratio (SIR)
- We can do the SIR link budget calculation based on our previous approach.
- If we consider fading effect on both signal and interference, we need to increase fading margin
- In this case, fading margin can be set to be twice of the margin of the noise-limited system



Example 3.1 Link budget

Consider the downlink of a GSM system (see also Chapter 24). The carrier frequency is 950 MHz and the **RX sensitivity is (according to GSM specifications) -102 dBm** . The output power of the TX amplifier is 30 W. The antenna gain of the TX antenna is 10 dB and the aggregate attenuation of connectors, combiners, etc. is 5 dB. The fading margin is 12 dB and the breakpoint d_{break} is at a distance of 100 m. What distance can be covered?

$$\begin{aligned} T_x & \cdot P_{Tx} = 30\text{W} = 45\text{ dBm} \\ & \cdot G_{Tx} = 10\text{ dB} \\ & \cdot \text{Losses} = 5\text{ dB (非 PL)} \\ \Rightarrow \text{EIRP} &= 45 + 10 - 5 = 50\text{ dB} \end{aligned}$$

$$\begin{aligned} R_x & \cdot R_x \text{ sensing} = -102\text{ dB} \\ & \cdot \text{Fading margin} = 12\text{ dB} \\ \Rightarrow \text{minimum RX power} &= -90\text{ dB} \end{aligned}$$

考慮 Pathloss suppose $n=3.5$

$$50 - PL(d) \geq -90$$

$$\begin{aligned} \cdot PL(d) &= 20 \log_{10}\left(\frac{4\pi}{\lambda_c}\right) + 20 \log_{10}(d_{\text{break}}) + 10n \log_{10}\left(\frac{d}{d_{\text{break}}}\right) \leq 140\text{ dB} \\ &= 32 + 20 \log_{10}(100) + 3.5 \cdot 10 \log_{10}\left(\frac{d}{100}\right) \leq 140 \\ \text{則 } d &\approx 8.8\text{ km} \end{aligned}$$

Example 3.2 Link budget

Consider a mobile radio system at 900-MHz carrier frequency, and with 25-kHz bandwidth, that is affected only by thermal noise (temperature of the environment $T_e = 300\text{ K}$). Antenna gains at the TX and RX sides are 8 dB and 2 dB ,⁴ respectively. Losses in cables, combiners, etc. at the TX are 2 dB . The **noise figure of the RX is 7 dB** and the 3-dB bandwidth of the signal is 25 kHz . The **required operating SNR is 18 dB** and the desired range of coverage is 2 km . The **breakpoint is at 10-m distance**; beyond that point, the **path loss exponent is 3.8** , and the fading margin is 10 dB . What is the minimum TX power?

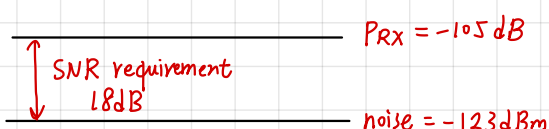
The way this problem is formulated makes working our way backward from the RX to the TX advantageous.

① Noise:

$$\begin{aligned} \cdot N_0 &= -174\text{ dBm/Hz} \\ \cdot B &= 25\text{ kHz} = 44\text{ dBHz} \\ \Rightarrow P_n &= -174 + 44 = -130\text{ dBm} \\ \text{RX noise} &= P_n + F \\ &= -130 + 7 = -123\text{ dBm} \end{aligned}$$

② SNR:

$$\begin{aligned} \cdot \text{require SNR} &= 18\text{ dB} \\ \rightarrow \text{require } P_{Rx} &= -123 + 18 = -105\text{ dBm} \end{aligned}$$



③ 考慮 Pathloss

$$\begin{aligned} \cdot P_{Tx} - PL(d) &\geq P_{Rx} \\ \cdot PL(d) &= 20 \log_{10}\left(\frac{4\pi}{\lambda_c}\right) + 20 \log_{10}(d_{\text{break}}) + 10n \log_{10}\left(\frac{d}{d_{\text{break}}}\right) \\ &= 32 + 2 \cdot 10 \log_{10} 10 + 3.8 \cdot 10 \log_{10}\left(\frac{2000}{10}\right) \\ &= 32 + 20 + 87 = 139\text{ dB} \end{aligned}$$

$$\text{故 } P_{Tx} + G_{Tx} + G_{Rx} - PL(d) - \text{Loss} \geq P_{Rx} + \text{fading margin}$$

$$\Rightarrow P_{Tx} + 8 - 2 - 139 - 2 \geq -105 + 10$$

$$\begin{aligned} P_{Tx} &\geq 40\text{ dBm} = 10\text{ W} \\ \rightarrow 10^4\text{ mW} &= 10\text{ W} \end{aligned}$$