

Problem 1.

(a) 求 transmit power.

- 已知 $BER_{BPSK} = Q(\sqrt{2\gamma_b}) = 5 \times 10^{-6} \rightarrow \gamma_s = SNR = 9.755 \text{ dB}$
- $SNR = P_{RX} - P_N$

$$\left\{ \begin{aligned} \text{(i)} \quad P_{RX} &= P_{TX} + G_{BS} + G_{MS} - PL(d) \\ PL(d) &= 20 \log_{10}\left(\frac{4\pi}{\lambda_c}\right) + 20 \log_{10}(d_{break}) + n \cdot 10 \log_{10}\left(\frac{d}{d_{break}}\right) \\ &= 32 + 2.7 + 45 \log_{10}(110) = 137.86 \\ \Rightarrow P_{RX} &= P_{TX} - 117.86 \\ \text{(ii)} \quad N_0 B &= K T_e B = (1.38 \times 10^{-23}) \times 290(7-1) \times 2 \times 10^7 \\ &= 4.8 \times 10^{-13} = -123 \text{ dBW} = -93 \text{ dBm} \\ P_N &= -93 + 7 = -86 \text{ dBm} \end{aligned} \right.$$

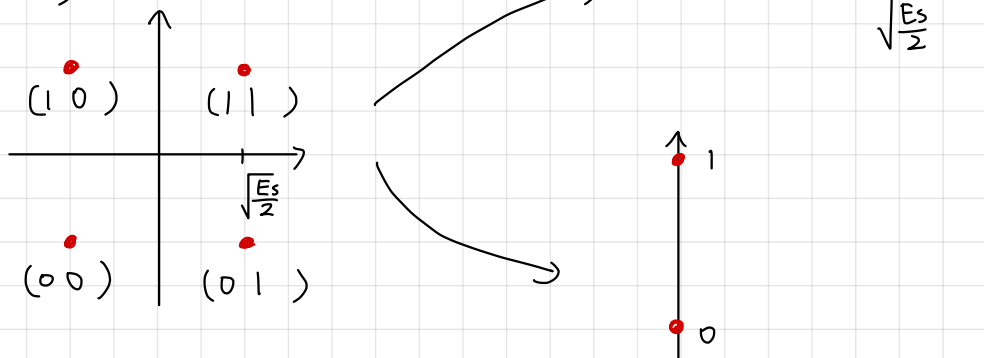
$$\rightarrow SNR = 9.755 = P_{TX} - 117.86 - (-86)$$

$$\Rightarrow P_{TX} = 41.615 \text{ dBm}$$

$$\underline{\text{Ans: } P_{TX} = 41.615 \text{ dBm}}$$

(b)

Gray-code QPSK



$$\bullet BER = Q\left(\sqrt{\frac{2E_s}{2N_0}}\right) = Q(\sqrt{\gamma_s}) = \underline{Q(\sqrt{2\gamma_b})}$$

$$\bullet SER = 1 - (1 - P_e)^2 = 2P_e - P_e^2 = \underline{2Q(\sqrt{2\gamma_b}) - Q^2(\sqrt{2\gamma_b})}$$

Problem 1.

(c)

If use gray code. QPSK. $\gamma_s = 2\gamma_b$

$$\text{BER} = Q(\sqrt{2\gamma_b}) = Q(\sqrt{\gamma_s}) = 5 \times 10^{-6} \Rightarrow \gamma_s = 9.755 + \underline{\underline{3}} = 12.755 \text{ dB}$$

$$\Rightarrow P_{\text{Tx}} = 41.615 + 3 = 44.615 \text{ dBm}$$

Ans: 44.615 dBm ✱

(d)

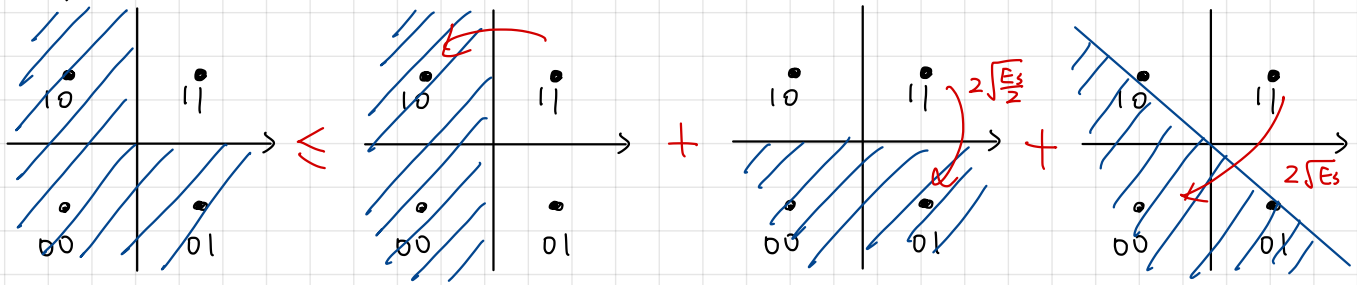
$$Q(\sqrt{\gamma_s}) = 10^{-7}, \quad \gamma_s = (Q^{-1}(10^{-7}))^2 = 14.32 \text{ dB}$$

$$14.32 - 12.755 = 1.565$$

Ans: increase 1.565 dB ✱

Problem 2.

(a)



• By union bound,

$$SER \leq Q\left(\sqrt{\frac{2E_s}{2N_0}}\right) \times 2 + Q\left(\sqrt{\frac{4E_s}{2N_0}}\right) = 2Q(\sqrt{\gamma_s}) + Q(\sqrt{2\gamma_s}) ; \gamma_s = 2\gamma_b$$

← 錯 2 個 bit

$$BER \leq \frac{2Q(\sqrt{\gamma_s}) + Q(\sqrt{2\gamma_s}) \times 2}{\log_2 4} = Q(\sqrt{2\gamma_b}) + Q(\sqrt{4\gamma_b}) = 5 \times 10^{-5}$$

$$\Rightarrow \gamma_b \approx 7.566 \text{ \#}$$

• 1(b) 的 $BER = Q(\sqrt{2\gamma_b}) = 5 \times 10^{-5}$, $\gamma_b = (Q^{-1}(5 \times 10^{-5}))^2 / 2$

$$\Rightarrow \gamma_b = (3.89)^2 / 2 = 7.566 \text{ \#}$$

→ They are almost same, the union bound is a good approximate. \#

(b)

100	101	111	110
•	•	•	•
		← 2d	
•	•	•	•
000	001	011	010

$$E_s = \frac{1}{2} (d^2 + d^2 + 9d^2 + d^2) = 6d^2 \quad d = \sqrt{\frac{E_s}{6}}$$

Ans: 距離為 $2d = 2\sqrt{\frac{E_s}{6}} = \sqrt{\frac{2E_s}{3}} \text{ \#}$

(c)

100	101	111	110
•	•	•	•
		← 2d	
•	•	•	•
000	001	011	010

$$SER_1 = Q\left(\sqrt{\frac{E_s/6}{N_0/2}}\right) \times 2 = 2Q\left(\sqrt{\frac{E_s}{3N_0}}\right)$$

$$SER_2 = Q\left(\sqrt{\frac{E_s/6}{N_0/2}}\right) \times 3 = 3Q\left(\sqrt{\frac{E_s}{3N_0}}\right)$$

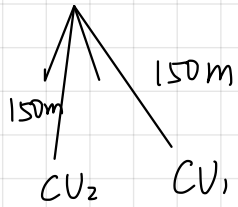
$$SER = \frac{5}{2} Q\left(\sqrt{\frac{E_s}{3N_0}}\right) = \frac{5}{2} Q\left(\sqrt{\frac{E_b}{N_0}}\right)$$

$$\Rightarrow BER = \frac{SER}{\log_2 8} = \frac{5}{6} Q(\sqrt{\gamma_b})$$

Ans: $BER = \frac{5}{6} Q(\sqrt{\gamma_b}) \text{ \#}$

Problem 3 (a). $P_{ms} = 0.1W = 20 \text{ dBm}$

$$N_0B = -174 + 10 \log_{10}(1.7 \times 10^5) = -121.7 \text{ dBm}$$



$$PL(d) = 20 \log_{10}\left(\frac{4\pi}{\lambda}\right) + 20 \log_{10}(d_{break}) + 10 \log_{10}\left(\frac{d}{d_{break}}\right)$$

$$= 32 + 20 \log_{10}(0.9) + 20 + 45 \log_{10}(15)$$

$$= 32 - 0.915 + 20 + 52.92 = 104 \text{ dB}$$

$$\Rightarrow SNR = (20 + 3 + 3 - 104) - (-121.7) = 43.7 \text{ dB}$$

$$G_{No}(f, \alpha, T) = \begin{cases} 1 & ; 0 \leq |f| \leq \frac{1-\alpha}{2T} \\ \frac{1}{2} \left(1 - \sin\left(\frac{T}{2\alpha} |2\pi f - \frac{\pi}{T}|\right)\right) & ; \frac{1-\alpha}{2T} \leq |f| \leq \frac{1+\alpha}{2T} \end{cases}$$

$$S = \int_{-\frac{0.85}{T}}^{\frac{0.85}{T}} |G_{No}(f, \alpha, T) G_{No}^*(f, \alpha, T)|^2 df = 6.8281 \times 10^4$$

$$I = \int_{\frac{0.15}{T}}^{\frac{0.85}{T}} |G_{No}(f, \alpha, T) \cdot G_{No}^*\left(f - \frac{1.4}{T}, \alpha, T\right)|^2 df = 1.7023$$

$$\Rightarrow SIR = \frac{6.828 \times 10^4}{1.7023} = 40110 = 46.03 \text{ dB}$$

$$\Rightarrow SINR = \frac{S}{P_N + I} = \frac{1}{\frac{1}{SINR} + \frac{1}{SIR}} = \frac{1}{\frac{1}{23442.5} + \frac{1}{40110}} = 14795.22 = 41.7 \text{ dB}$$

Ans: $\begin{matrix} SNR = 43.7 \text{ dB} \\ SIR = 46.03 \text{ dB} \\ SINR = 41.7 \text{ dB} \end{matrix}$ #

(b)

$$BER = Q(\sqrt{2\gamma_b}) = Q(\sqrt{\gamma_s}) = Q(\sqrt{41.7}) \approx 0 \neq$$

$$SER = 2Q(\sqrt{\gamma_s}) + Q(\sqrt{\gamma_s}) \approx 0 \neq$$

$$c) P_1 = X, P_2 = X + 45 \log_{10}(15) - 45 \log_{10}(10) = X + 7.92$$

$$SIR_1' = SIR - 7.92 = 38.11 \text{ dB} = 6471.42$$

$$\rightarrow SINR_{u1} = \frac{1}{\frac{1}{6471} + \frac{1}{23442}} = 5071.42 = 37 \text{ dB}, Q(\sqrt{37}) \approx 0 \begin{cases} BER_1 \approx 0 \\ SER_1 \approx 0 \end{cases} \neq$$

$$SIR_2' = SIR + 7.92 = 53.95 \text{ dB} = 248313.$$

$$\rightarrow SINR_{u2} = \frac{1}{\frac{1}{248313} + \frac{1}{23442}} = 21420 = 43.3 \text{ dB}, Q(\sqrt{43.3}) \approx 0 \begin{cases} BER_2 \approx 0 \\ SER_2 \approx 0 \end{cases} \neq$$

Problem 4.

(a)

$$\gamma_{\text{req}} = 20 \text{ dB} = 100, P_{\text{out, req}} = 0.03$$

$$\begin{aligned} \circ P_{\text{out}} &= 1 - \exp\left(-\frac{100}{\bar{\gamma}_s}\right) \Rightarrow \bar{\gamma}_s = -\frac{100}{\ln(0.97)} = 3283.08 = 35.16 \text{ dB} \\ \circ N_0 B &= 10 \log_{10}[(1.38 \times 10^{-23}) \cdot 290(7-1) \cdot 10 \times 10^6] = -96.2 \\ &\rightarrow P_N = -96.2 + 7 = -89.2 \text{ dBm} \\ \circ PL(d) &= 20 \log_{10}\left(\frac{4\pi d f_{\text{break}}}{\lambda_c}\right) + 10 \log_{10}\left(\frac{d}{d_{\text{break}}}\right) = 32 + 20 + 41 \cdot \log_{10}(12) = 96.246 \\ &\Rightarrow P_{\text{Tx}} + 5 + 0 - 96.246 - (-89.2) = 35.16 \quad \text{Ans: } P_{\text{Tx}} = 37.2 \text{ dBm} \end{aligned}$$

(b) For Rayleigh fading, $\text{BER}_{\text{req}} = 1 \times 10^{-5}$

$$\overline{\text{BER}}_{\text{DBPSK}} \simeq \frac{1}{2\bar{\gamma}_s} = 1 \times 10^{-5}, \quad \bar{\gamma}_s = 5 \times 10^4 = 47 \text{ dB}$$

$$P_{\text{Tx}} = 37.2 + (47 - 35.16) = 49.04 \text{ dBm} \quad \#$$

(c) For Rician fading, $\text{BER}_{\text{req}} = 1 \times 10^{-5}$

$$\circ \text{With } K_r = 10, \quad \overline{\text{BER}}_{\text{DBPSK}} = \frac{11}{2(11 + \bar{\gamma}_s)} \exp\left(-\frac{10\bar{\gamma}_s}{11 + \bar{\gamma}_s}\right) = 1 \times 10^{-5} \quad \bar{\gamma}_s = 18.8 \text{ dB}$$

$$P_{\text{Tx}} = 37.2 + (18.8 - 35.16) = 20.8 \text{ dBm} \quad \#$$

$$\circ \text{With } K_r = 0, \quad \overline{\text{BER}}_{\text{DBPSK}} = \frac{1}{2(1 + \bar{\gamma}_s)} = 1 \times 10^{-5}, \quad \bar{\gamma}_s = 47 \text{ dB}$$

$$P_{\text{Tx}} = 37.2 + (47 - 35.16) = 49.04 \text{ dBm} \quad \#$$

When $K_r \rightarrow 0$, Rician fading turn into Rayleigh fading

s.t. the answer equal to 4.(b) $\#$

Problem 5.

(a)

16QAM gray coding.

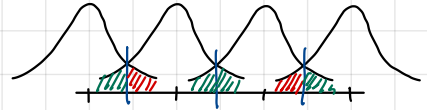
$\overset{x}{1000}$	$\overset{x}{1001}$	$\overset{x}{1011}$	$\overset{x}{1010}$
$\overset{x}{1100}$	$\overset{x}{1101}$	$\overset{x}{1111}$	$\overset{x}{1110}$
$\overset{x}{0100}$	$\overset{x}{0101}$	$\overset{x}{0111}$	$\overset{x}{0110}$
$\overset{x}{0000}$	$\overset{x}{0001}$	$\overset{x}{0011}$	$\overset{x}{0010}$

$E_s = \text{Average Symbol Energy.}$

$$= \frac{1}{4} d^2 (1+1+1+9+1+9+9+9) = 10d^2$$

$$\rightarrow d = \sqrt{\frac{E_s}{10}}$$

Consider I- channel



$$SER_I = \frac{1}{4} \left[2Q\left(\sqrt{\frac{4d^2}{2N_0}}\right) + 2 \cdot 2Q\left(\sqrt{\frac{4d^2}{2N_0}}\right) \right] = \frac{3}{2} Q\left(\sqrt{\frac{E_s}{5N_0}}\right)$$

$$SER_Q = SER_I = \frac{3}{2} Q\left(\sqrt{\frac{E_s}{5N_0}}\right)$$

可忽略

$$\rightarrow SER = 1 - (1 - SER_I)(1 - SER_Q) = 3Q\left(\sqrt{\frac{E_s}{5N_0}}\right) - \frac{9}{4} Q^2\left(\sqrt{\frac{E_s}{5N_0}}\right) \quad ; E_s = 4E_b$$

$$BER = \frac{SER}{\log_2 16} = \frac{3}{4} Q\left(\sqrt{\frac{4}{5} \frac{E_b}{N_0}}\right) = \frac{3}{4} Q(\sqrt{0.8 \gamma_b})$$

(b) Formula: $2 \int_0^\infty Q(\sqrt{2x}) \cdot a \exp(-ax) dx = 1 - \sqrt{\frac{1}{1+a}}$

$$BER_{QAM} = \int_0^\infty \frac{1}{\gamma_b} \exp\left(-\frac{\gamma_b}{\gamma_b}\right) \cdot \frac{3}{4} Q(\sqrt{0.8 \gamma_b}) d\gamma_b, \quad \begin{matrix} \hat{=} x = \frac{2}{5} \gamma_b \\ dx = \frac{2}{5} d\gamma_b \end{matrix}$$

$$= 2 \int_0^\infty Q(\sqrt{2x}) \cdot \exp\left(-\frac{5x}{2\gamma_b}\right) \cdot \frac{5}{2\gamma_b} dx \cdot \frac{3}{4} \cdot \frac{5}{2} \cdot \frac{1}{5} \cdot \frac{1}{2}$$

$$= \frac{3}{8} \left[1 - \sqrt{\frac{1}{1 + \frac{5}{2\gamma_b}}} \right]$$

$$Ans: \frac{3}{8} \left(1 - \sqrt{\frac{0.4 \gamma_b}{1 + 0.4 \gamma_b}} \right)$$

