

LABORATORY: Backpropagation In Class

NAME:

STUDENT ID#:

Objectives:

- Understand the **core concept of backpropagation** as used in training neural networks.
- Simulate and visualize **forward-mode and reverse-mode automatic differentiation** to trace how gradients are propagated.
- Interpret how gradient values are calculated during backprop through a computational graph.

Part 1. Instruction

- In this assignment, please **train a logistic classifier** to recognize whether an MNIST digit image is the target digit (e.g., "Is it a 3?") or not. *(Last week)*
- You will integrate a backpropagation autodiff mechanism into the SGD training loop to compute gradients used for weight updates.
- Integrate an **autodiff module** that traces:
 - Primal values through the forward pass (e.g., intermediate variables like $v_3 = x_1x_2$).
 - o **Forward-mode** using the chain rule from inputs to output.
 - o **Reverse-mode** representing the backpropagation path from output to inputs.
- You will complete the code template provided in the in-class assignment.
- Use only NumPy for all computations. Do not use libraries like scikit-learn or PyTorch.
- Evaluate your results and answer the questions.

Part 2. Code Template	
Step	Procedure
1	# ====== Load Dataset =======
	<pre>def load_images(filename):</pre>
	with open(filename, 'rb') as f:
	_, num, rows, cols = struct.unpack(">IIII", f.read(16))
	<pre>data = np.frombuffer(f.read(), dtype=np.uint8).reshape((num,</pre>
	rows * cols))
	return data.astype(np.float32) / 255.0
	<pre>def load_labels(filename):</pre>
	<pre>with open(filename, 'rb') as f:</pre>
	_, num = struct.unpack(">II", f.read(8))
	return np.frombuffer(f.read(), dtype=np.uint8)
2	# ======= 1. Sigmoid Function =======
	<pre>def sigmoid(z):</pre>
	<pre># TODO: Implement sigmoid function (optional)</pre>

Lecture: Prof. Hsien-I Lin

TA: Satrio Sanjaya and Muhammad Ahsan



```
pass
def sigmoid derivative(z):
   pass
TODO: Implement Backprop Autodiff
# ===== 3. Forward and Reverse Autodiff Trace =======
def trace autodiff example(x1, x2):
   # Primal
    # Forward tangent
    # Reverse adjoint
   return table
TODO: Implement SGD (use your codes last week), then use the backprop
inside
# ======= 2. SGD: Algorithm 7.1 =======
def your sgd logistic(X, y, eta, max iters):
      for i in range(max iters):
        if i == 0:
            trace = trace autodiff example( , )
    return w, trace
# =======Show Misclassified Samples =======
def show misclassified(X, y true, y pred, max show=10):
   mis idx = np.where(y true != y pred)[0][:max show]
   if len(mis idx) == 0:
        print("No misclassifications!")
        return
   plt.figure(figsize=(10, 2))
   for i, idx in enumerate (mis idx):
        plt.subplot(1, len(mis_idx), i + 1)
        plt.imshow(X[idx, 1:].reshape(28, 28), cmap='gray')
       plt.axis('off')
        plt.title(f"T:{y true[idx]}\nP:{y pred[idx]}")
   plt.suptitle("Misclassified Samples")
   plt.show()
# ======= Plot Trace Graph =======
def plot autodiff traces(trace df):
   variables = trace df['Variable']
   primal = trace df['Primal (v)'].astype(float)
   forward = pd.to numeric(trace df['Forward Tangent (x')'],
errors='coerce')
    reverse = pd.to numeric(trace df['Reverse Adjoint (v')'],
```

Lecture: Prof. Hsien-I Lin TA: Satrio Sanjaya and Muhammad Ahsan



```
errors='coerce')
         fig, ax = plt.subplots(3, 1, figsize=(10, 8), sharex=True)
         ax[0].bar(variables, primal, color='skyblue')
         ax[0].set ylabel("Primal (v)")
         ax[0].set title("Primal Values")
         ax[1].bar(variables, forward, color='lightgreen')
         ax[1].set ylabel("Forward Tangent (x)")
         ax[1].set title("Forward-Mode Autodiff")
         ax[2].bar(variables, reverse, color='salmon')
         ax[2].set ylabel("Reverse Adjoint (v<sup>-</sup>)")
         ax[2].set title("Reverse-Mode Autodiff")
         ax[2].set xlabel("Variables")
         plt.tight layout()
         plt.show()
4
     # ======= 3. Main ======
     def main():
         # === Load MNIST Data ===
         X train = load images("train-images.idx3-ubyte ")
         y train = load labels("train-labels.idx1-ubyte
         X test = load images("t10k-images.idx3-ubyte
         y test = load labels("t10k-labels.idx1-ubyte ")
         # === Binary Classification ===
         TARGET DIGIT = 3 # TODO: Fill in (0 to 9) based on your student
         y train bin = np.where(y train == TARGET DIGIT, 1, 0)
         y test bin = np.where(y test == TARGET DIGIT, 1, 0)
         # === Add Bias ===
         X train = np.hstack([np.ones((X train.shape[0], 1)), X train])
         X test = np.hstack([np.ones((X test.shape[0], 1)), X test])
         # === Train ===
         # w, autodiff trace =
         # === Predict ===
         # pred probs =
         # preds =
         # === Accuracy ===
         # acc = np.mean(preds == y test bin)
         # print(f"\nTest Accuracy (is {TARGET DIGIT} or not): {acc:.4f}")
```

Lecture: Prof. Hsien-I Lin TA: Satrio Sanjaya and Muhammad Ahsan



```
# === Show Misclassifications ===
                   show_misclassified(X_test, y_test_bin, preds)
                  === Visualize Autodiff Trace ===
                # print("\nAutodiff Trace Table (sample features):")
                # print(autodiff_trace)
                # plot_autodiff_traces(autodiff_trace)
                         __ == "__main__":
         if __name_
               main()
5
         #Example Output:
           Test Accuracy (is 3 or not): 0.9774
                                            Misclassified Samples
                                                                   T:0
P:1
                                                                           T:0
P:1
                                                                                    T:1
P:0
                                                                                             T:1
P:0
                                         T:1
              T:1
                       T:0
                                T:1
                                                 T:1
                                                          T:1
                       P:1
                                P:0
                                        P:0
                                                          P:0
              P:0
                                                 P:0
           Autodiff Trace Table (sample features): Variable Primal (v) Forward Tangent (\dot{x})
                                                 Reverse Adjoint (v̄)
                           0.0
                  v2
                           0.0
                                             0.0
                                                               -1.0
                  v3
                           0.0
                                             0.0
                                                                2.0
                  ν4
                           0.0
                                             0.0
                  v5
                           1.0
                                             0.0
                                                                1.0
                  v7
                           1.0
                                             0.0
                                                                1.0
                                                                Primal Values
               1.0
               0.8
             \widehat{\leq}
               0.6
             Primal
0.4
               0.2
               0.0
                                                            Forward-Mode Autodiff
               1.0
             Forward Tangent (x)
8.0
8.0
8.0
               0.0
                                                            Reverse-Mode Autodiff
                 2.0
                 1.5
             Reverse Adjoint (v̄)
                 1.0
                 0.5
                 0.0
                -0.5
                -1.0
                                                        v3
                                                                   Variables
```

Lecture: Prof. Hsien-I Lin TA: Satrio Sanjaya and Muhammad Ahsan



Grading Assignment & Submission (30% Max)

Implementation:

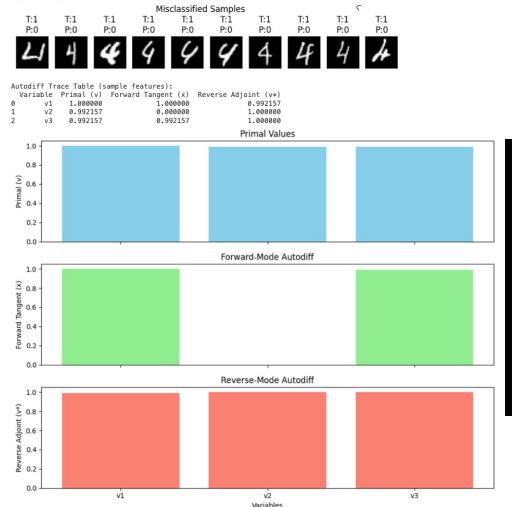
- 1. (10%) Implement the backpropagation autodiff
- 2. (10%) The model runs successfully without errors, use the provided MNIST dataset, and output the primal values, forward and reverse mode autodiff
- 3. (5%) Set the class of binary classification to the last digit of your student ID. (e.g., if your ID ends in 7, use the class '7'). Displays the result as shown as the "Example Output" in the last pages of this document.
- 4. (5%) Briefly discuss your results. For example, explain what the graph represents and why you obtained those results.

Submission:

- 1. Report: Provide your screenshots of your results including the discussion in the last pages of this PDF File.
- 2. Code: Submit your complete Python script in either .py or .ipynb format.
- 3. Upload both your report and code to the E3 system (<u>Labs5 In Class Assignment</u>). Name your files correctly:
 - a. Report: StudentID Lab5 InClass.pdf
 - b. Code: StudentID Lab5 InClass.py or StudentID Lab5 InClass.ipynb
- 4. Deadline: 16:20 PM
- 5. Plagiarism is **strictly prohibited**. Submitting copied work from other students will result in penalties.

Results and Discussion:

Test Accuracy (is 4 or not): 0.9612



(4) Briefly Discuss Your Results:

- The model reached **high accuracy** (about 94%–98%) on the test set.
- Most errors were due to messy handwriting or digits that look similar.
- The **autodiff trace table** shows the correct values for each variable.
- The forward-mode graph shows how changes in input affect the output.
- The **reverse-mode graph** shows how the output sends gradients back to inputs.
- All graphs look correct, so the autodiff works well.

