

Problem Set–5 Solutions

CS 230, Autumn 2023

$$1.a) CPI = \sum_{i=0}^3 CPI_i * p_i$$

$$MIPS = f_{CPE} / (CPI * 10^6)$$

Computer R1:

$$CPI = \sum_{i=1}^3 CPI_i * p_i = 0.16 * 6 + 0.1 * 8 + 0.08 * 10 + 0.66 * 3 = 4.54$$

Computer R1 needs an average of 4.54 clock periods for one instruction

$$MIPS = f_{CPE} / CPI * 10^6 = 400 * 10^6 / 4.54 * 10^6 = 88.1$$

Computer R1 executes an average of 88 100 000 instructions per second

Computer R2:

$$CPI = \sum CPI_i * p_i = 0.16 * 20 + 0.1 * 32 + 0.08 * 66 + 0.66 * 3 = 13.66 \text{ Computer R2}$$

needs an average of 13.66 clock periods for one instruction

$$MIPS = f_{CPE} / CPI * 10^6 = 400 * 10^6 / 13.66 * 10^6 = 29.28$$

Computer R2 executes an average of 29 280 000 instructions per second.

$$1.b) CPU_{time} = \text{Number_of_instructions} / MIPS * 10^6$$

Another form of the equation to calculate the CPU time is:

$$CPU_{time} = \text{Number_of_instructions} * CPI * t_{CPU}$$

Computer R1:

$$CPU_{time} = \text{Number_of_instructions} / MIPS * 10^6 = 12000 / 88.1 * 10^6 = 136.2 * 10^{-6} = 136.2 \mu s$$

$$\text{Computer R2: } CPU_{time} = \text{Number_of_instructions} / MIPS * 10^6 = 12000 / 29.28 * 10^6 = 410 * 10^{-6} = 410 \mu s$$

2. $\text{CPU performance}_B / \text{CPU performance}_A = \text{CPU time}_A / \text{CPU time}_B$

- $6 = 3 / \text{CPU time}_B$

User CPU Time = .5 seconds

Since the I/O time is unaffected by the performance increase, it still takes 1 second to do I/O. Therefore it takes $1 + .5 = 1.5$ seconds to run Program A on the faster CPU

Wallclock Time = 1.5 seconds

System Performance in MFLOPS = Number of Floating Point Operations * $10^6 / \text{Wallclock Time}$

Old System Performance (10) = $\#FLOP * 10^6 / 4$

- $\#FLOP = 40 * 10^6$

New System Performance = $40 * 10^6 / 1.5$

MFLOP/sec = 26.667

3. We have the instruction count: 10^9 instructions. The clock time can be computed quickly from the clock rate to be 0.5×10^{-9} seconds. So we only need to compute clocks per instruction as an effective value:

Value	Frequency	Product
3	0.5	1.5
4	0.3	1.2
5	0.2	1.0

CPI = 3.7

Then we have,

Execution Time = $1.0 * 10^9 * 3.7 * 0.5 * 10^{-9} = 1.85 \text{ sec}$

4)

If we say that there are 100 instructions, then:

30 of them will be loads and stores.

50 of them will be arithmetic instructions.

20 of them will be all others.

$(30 * 6) + (50 * 4) + (20 * 3) = 440$ cycles/100 instructions

Therefore, there are 4.4 Cycles per instruction.

5)

Given that 80% of 10^9 instructions require single cycle i.e. no conditional branching & for 20% an extra cycle required.

Time taken by 1 cycle = 10^{-9} sec

Total time = $10^{-9}(80/100 * 10^9 + 20/100 * 2 * 10^9)$

$= 10^{-9} * 10^9(4/5 + 2/5) = 6/5 = 1.2$ seconds